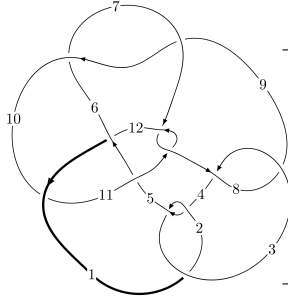
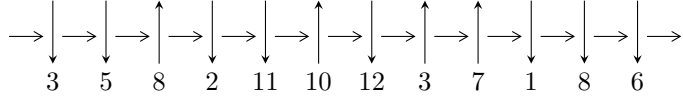


$12n_{0255}$ ($K12n_{0255}$)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7,12 \xrightarrow{c_7} 3,8 \xrightarrow{c_3} 4 \xrightarrow{c_8} 9 \xrightarrow{c_9} 10 \xrightarrow{c_6} 6 \xrightarrow{c_{12}} 1 \xrightarrow{c_1} 2 \xrightarrow{c_{11}} 11 \xrightarrow{c_5} 5 \rightsquigarrow c_2, c_4, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 1.59660 \times 10^{327} u^{87} - 4.52798 \times 10^{327} u^{86} + \dots + 9.40594 \times 10^{329} b + 8.06817 \times 10^{330}, \\ - 1.52962 \times 10^{329} u^{87} + 3.20986 \times 10^{329} u^{86} + \dots + 4.75941 \times 10^{331} a - 3.66335 \times 10^{331}, \\ u^{88} - 2u^{87} + \dots - 4968u - 1771 \rangle$$

$$I_2^u = \langle 4u^8 + u^6 - 4u^5 + 2u^4 - 5u^3 - u^2 + 7b + u + 3, 4u^8 + 7u^7 + 15u^6 + 10u^5 + 16u^4 + 9u^3 + 13u^2 + 7a + u + 3, \\ u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

$$I_3^u = \langle -4u^{15} - 30u^{13} + \dots + b + 8, 2u^{15} + 14u^{13} + \dots + a - 7, u^{16} + 8u^{14} + \dots - 3u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 113 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 1.60 \times 10^{327} u^{87} - 4.53 \times 10^{327} u^{86} + \dots + 9.41 \times 10^{329} b + 8.07 \times 10^{330}, -1.53 \times 10^{329} u^{87} + 3.21 \times 10^{329} u^{86} + \dots + 4.76 \times 10^{331} a - 3.66 \times 10^{331}, u^{88} - 2u^{87} + \dots - 4968u - 1771 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.00321388u^{87} - 0.00674424u^{86} + \dots - 11.3051u + 0.769708 \\ -0.00169744u^{87} + 0.00481396u^{86} + \dots - 12.5593u - 8.57774 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.00233250u^{87} - 0.00315963u^{86} + \dots - 27.9840u - 7.24757 \\ -0.00137179u^{87} + 0.00300797u^{86} + \dots - 5.06937u - 5.35127 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.00153178u^{87} - 0.00266896u^{86} + \dots - 23.2890u - 2.25667 \\ -0.00185920u^{87} + 0.00347861u^{86} + \dots + 19.0323u + 2.82726 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.000327420u^{87} + 0.000809657u^{86} + \dots - 4.25669u + 0.570591 \\ -0.00185920u^{87} + 0.00347861u^{86} + \dots + 19.0323u + 2.82726 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.000561869u^{87} - 0.00155079u^{86} + \dots - 8.50672u - 1.66797 \\ -0.000861961u^{87} + 0.00450290u^{86} + \dots - 41.5986u - 14.7883 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.000151726u^{87} + 0.00147337u^{86} + \dots + 0.554564u - 2.10313 \\ -0.00150768u^{87} + 0.00204381u^{86} + \dots + 20.3844u + 3.14401 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.00467421u^{87} + 0.0109893u^{86} + \dots + 15.1651u - 4.16426 \\ 0.00197314u^{87} - 0.00700781u^{86} + \dots + 30.3390u + 12.6165 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.000632418u^{87} - 0.00298532u^{86} + \dots + 1.50043u + 2.65355 \\ -1.09936 \times 10^{-6} u^{87} + 0.00267945u^{86} + \dots - 37.8923u - 12.7574 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $0.0135860u^{87} - 0.0234158u^{86} + \dots - 148.906u - 31.3158$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{88} + 36u^{87} + \dots + 9016u + 2401$
c_2, c_4	$u^{88} - 16u^{87} + \dots + 504u - 49$
c_3, c_8	$u^{88} + u^{87} + \dots + 14336u + 25088$
c_5	$u^{88} - u^{87} + \dots + 8558243u - 2435537$
c_6, c_9	$u^{88} + 3u^{87} + \dots - 1497u - 181$
c_7, c_{11}	$u^{88} + 2u^{87} + \dots + 4968u - 1771$
c_{10}	$u^{88} - 14u^{87} + \dots - 5848u + 1043$
c_{12}	$u^{88} - 4u^{87} + \dots + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{88} + 48y^{87} + \dots - 1539089020y + 5764801$
c_2, c_4	$y^{88} - 36y^{87} + \dots - 9016y + 2401$
c_3, c_8	$y^{88} - 63y^{87} + \dots - 10096214016y + 629407744$
c_5	$y^{88} + 33y^{87} + \dots + 85934090519941y + 5931840478369$
c_6, c_9	$y^{88} + 49y^{87} + \dots - 883509y + 32761$
c_7, c_{11}	$y^{88} + 70y^{87} + \dots + 39623986y + 3136441$
c_{10}	$y^{88} + 2y^{87} + \dots + 12594048y + 1087849$
c_{12}	$y^{88} - 16y^{87} + \dots + 6y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.805310 + 0.589984I$	$-0.95191 - 5.34222I$	0
$a = 0.054018 - 0.595613I$		
$b = -0.564062 + 0.307745I$		
$u = 0.805310 - 0.589984I$	$-0.95191 + 5.34222I$	0
$a = 0.054018 + 0.595613I$		
$b = -0.564062 - 0.307745I$		
$u = -0.992163 + 0.083390I$	$-3.57000 + 4.86222I$	0
$a = 0.98711 + 1.32599I$		
$b = 1.43776 + 0.20661I$		
$u = -0.992163 - 0.083390I$	$-3.57000 - 4.86222I$	0
$a = 0.98711 - 1.32599I$		
$b = 1.43776 - 0.20661I$		
$u = -0.948677 + 0.240901I$	$4.48132 - 0.68778I$	0
$a = 0.003868 - 0.312365I$		
$b = 1.265110 - 0.356204I$		
$u = -0.948677 - 0.240901I$	$4.48132 + 0.68778I$	0
$a = 0.003868 + 0.312365I$		
$b = 1.265110 + 0.356204I$		
$u = -0.139706 + 0.952235I$	$-8.88186 + 0.52240I$	0
$a = -0.096405 + 1.302030I$		
$b = 0.428123 + 0.474722I$		
$u = -0.139706 - 0.952235I$	$-8.88186 - 0.52240I$	0
$a = -0.096405 - 1.302030I$		
$b = 0.428123 - 0.474722I$		
$u = -0.517483 + 0.776305I$	$-2.86090 + 2.57918I$	0
$a = 2.48790 - 5.29655I$		
$b = -4.92316 + 0.17599I$		
$u = -0.517483 - 0.776305I$	$-2.86090 - 2.57918I$	0
$a = 2.48790 + 5.29655I$		
$b = -4.92316 - 0.17599I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.919116 + 0.059965I$ $a = 0.276517 - 0.504859I$ $b = -1.240560 - 0.144966I$	$4.06052 - 5.39830I$	0
$u = -0.919116 - 0.059965I$ $a = 0.276517 + 0.504859I$ $b = -1.240560 + 0.144966I$	$4.06052 + 5.39830I$	0
$u = 0.740792 + 0.830928I$ $a = 0.330688 + 0.146176I$ $b = -0.648519 + 0.066233I$	$-0.52740 - 2.78156I$	0
$u = 0.740792 - 0.830928I$ $a = 0.330688 - 0.146176I$ $b = -0.648519 - 0.066233I$	$-0.52740 + 2.78156I$	0
$u = 0.248018 + 0.848575I$ $a = 0.59296 + 1.67847I$ $b = -1.039260 - 0.222833I$	$-2.35191 - 3.21223I$	$-7.96555 + 6.35540I$
$u = 0.248018 - 0.848575I$ $a = 0.59296 - 1.67847I$ $b = -1.039260 + 0.222833I$	$-2.35191 + 3.21223I$	$-7.96555 - 6.35540I$
$u = 0.079212 + 1.132010I$ $a = -2.23389 - 0.84898I$ $b = 1.65660 + 0.78050I$	$2.28913 + 1.10084I$	0
$u = 0.079212 - 1.132010I$ $a = -2.23389 + 0.84898I$ $b = 1.65660 - 0.78050I$	$2.28913 - 1.10084I$	0
$u = -0.319029 + 1.102470I$ $a = -1.74887 + 0.76112I$ $b = 0.788989 - 0.262436I$	$6.66068 + 5.31014I$	0
$u = -0.319029 - 1.102470I$ $a = -1.74887 - 0.76112I$ $b = 0.788989 + 0.262436I$	$6.66068 - 5.31014I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.174859 + 0.815548I$ $a = -0.149816 + 0.368917I$ $b = 0.641340 - 0.280050I$	$1.08551 - 1.92358I$	$4.64840 + 3.23156I$
$u = 0.174859 - 0.815548I$ $a = -0.149816 - 0.368917I$ $b = 0.641340 + 0.280050I$	$1.08551 + 1.92358I$	$4.64840 - 3.23156I$
$u = 0.767240 + 0.896651I$ $a = -0.055340 + 0.668537I$ $b = 0.212608 - 0.126711I$	$-0.156171 - 0.447897I$	0
$u = 0.767240 - 0.896651I$ $a = -0.055340 - 0.668537I$ $b = 0.212608 + 0.126711I$	$-0.156171 + 0.447897I$	0
$u = -0.237078 + 0.779145I$ $a = -0.81168 - 1.26283I$ $b = -0.67193 + 1.62533I$	$-2.63864 + 1.15581I$	$-8.11133 + 0.I$
$u = -0.237078 - 0.779145I$ $a = -0.81168 + 1.26283I$ $b = -0.67193 - 1.62533I$	$-2.63864 - 1.15581I$	$-8.11133 + 0.I$
$u = 0.451795 + 1.101000I$ $a = 0.358681 + 0.343345I$ $b = -0.360929 - 0.818141I$	$0.22772 - 2.36626I$	0
$u = 0.451795 - 1.101000I$ $a = 0.358681 - 0.343345I$ $b = -0.360929 + 0.818141I$	$0.22772 + 2.36626I$	0
$u = -0.938892 + 0.789370I$ $a = 0.273538 - 0.331883I$ $b = 0.201529 - 0.414522I$	$-5.45148 - 0.98119I$	0
$u = -0.938892 - 0.789370I$ $a = 0.273538 + 0.331883I$ $b = 0.201529 + 0.414522I$	$-5.45148 + 0.98119I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.785869 + 0.950757I$ $a = -0.138404 + 0.139505I$ $b = -0.271984 + 0.082732I$	$-4.90136 + 7.25149I$	0
$u = -0.785869 - 0.950757I$ $a = -0.138404 - 0.139505I$ $b = -0.271984 - 0.082732I$	$-4.90136 - 7.25149I$	0
$u = -0.135066 + 1.254400I$ $a = 2.22121 + 0.15503I$ $b = -2.05694 - 0.67244I$	$1.84545 + 6.92325I$	0
$u = -0.135066 - 1.254400I$ $a = 2.22121 - 0.15503I$ $b = -2.05694 + 0.67244I$	$1.84545 - 6.92325I$	0
$u = -0.166697 + 1.254150I$ $a = -0.034446 - 0.623225I$ $b = -0.319789 - 0.663059I$	$1.34449 + 3.11057I$	0
$u = -0.166697 - 1.254150I$ $a = -0.034446 + 0.623225I$ $b = -0.319789 + 0.663059I$	$1.34449 - 3.11057I$	0
$u = -0.128440 + 1.272930I$ $a = 1.93796 - 0.20251I$ $b = -2.15691 - 0.51379I$	$1.74481 + 1.77274I$	0
$u = -0.128440 - 1.272930I$ $a = 1.93796 + 0.20251I$ $b = -2.15691 + 0.51379I$	$1.74481 - 1.77274I$	0
$u = 0.696650 + 0.064826I$ $a = 1.51721 + 1.08264I$ $b = 1.40952 + 0.93931I$	$-4.59376 + 2.75184I$	$-8.12364 - 4.75878I$
$u = 0.696650 - 0.064826I$ $a = 1.51721 - 1.08264I$ $b = 1.40952 - 0.93931I$	$-4.59376 - 2.75184I$	$-8.12364 + 4.75878I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.112427 + 1.300630I$ $a = 1.68962 - 0.37026I$ $b = -1.092740 + 0.486491I$	$8.28391 - 2.17535I$	0
$u = -0.112427 - 1.300630I$ $a = 1.68962 + 0.37026I$ $b = -1.092740 - 0.486491I$	$8.28391 + 2.17535I$	0
$u = 0.313929 + 1.278860I$ $a = -1.83698 - 0.13210I$ $b = 1.40992 - 1.21165I$	$-0.73301 - 6.46230I$	0
$u = 0.313929 - 1.278860I$ $a = -1.83698 + 0.13210I$ $b = 1.40992 + 1.21165I$	$-0.73301 + 6.46230I$	0
$u = 0.266726 + 1.305550I$ $a = -0.493116 + 0.134447I$ $b = 0.801100 + 0.630667I$	$3.68905 - 4.17717I$	0
$u = 0.266726 - 1.305550I$ $a = -0.493116 - 0.134447I$ $b = 0.801100 - 0.630667I$	$3.68905 + 4.17717I$	0
$u = 0.021756 + 1.350550I$ $a = 0.747687 - 0.219765I$ $b = -0.820694 - 0.756021I$	$2.82569 + 0.98099I$	0
$u = 0.021756 - 1.350550I$ $a = 0.747687 + 0.219765I$ $b = -0.820694 + 0.756021I$	$2.82569 - 0.98099I$	0
$u = -0.018865 + 0.638570I$ $a = 0.079600 + 0.747971I$ $b = 0.756230 - 0.701359I$	$0.93570 - 1.73737I$	$2.01048 + 1.71572I$
$u = -0.018865 - 0.638570I$ $a = 0.079600 - 0.747971I$ $b = 0.756230 + 0.701359I$	$0.93570 + 1.73737I$	$2.01048 - 1.71572I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.588985$ $a = 0.818540$ $b = -0.302376$	-1.64409	-5.83610
$u = 0.094002 + 0.577464I$ $a = -0.249160 - 1.294160I$ $b = -0.365512 + 1.099090I$	$-2.55730 + 1.15360I$	$-7.35870 + 0.72400I$
$u = 0.094002 - 0.577464I$ $a = -0.249160 + 1.294160I$ $b = -0.365512 - 1.099090I$	$-2.55730 - 1.15360I$	$-7.35870 - 0.72400I$
$u = -0.54155 + 1.31866I$ $a = 1.35023 - 0.95631I$ $b = -1.88027 + 0.08346I$	$7.90999 + 10.78390I$	0
$u = -0.54155 - 1.31866I$ $a = 1.35023 + 0.95631I$ $b = -1.88027 - 0.08346I$	$7.90999 - 10.78390I$	0
$u = -0.41333 + 1.36783I$ $a = 0.044748 + 0.458558I$ $b = 0.159156 + 0.689302I$	$1.05954 + 9.78750I$	0
$u = -0.41333 - 1.36783I$ $a = 0.044748 - 0.458558I$ $b = 0.159156 - 0.689302I$	$1.05954 - 9.78750I$	0
$u = 1.40756 + 0.26250I$ $a = -0.226308 + 0.033161I$ $b = -1.81552 + 0.07911I$	$1.45716 - 4.42701I$	0
$u = 1.40756 - 0.26250I$ $a = -0.226308 - 0.033161I$ $b = -1.81552 - 0.07911I$	$1.45716 + 4.42701I$	0
$u = -0.42686 + 1.41707I$ $a = -1.42953 + 0.73379I$ $b = 1.96059 + 0.05533I$	$9.65161 + 4.27098I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.42686 - 1.41707I$ $a = -1.42953 - 0.73379I$ $b = 1.96059 - 0.05533I$	$9.65161 - 4.27098I$	0
$u = 0.26866 + 1.45831I$ $a = 1.54716 + 0.09889I$ $b = -1.83374 + 0.14991I$	$5.43825 - 8.83857I$	0
$u = 0.26866 - 1.45831I$ $a = 1.54716 - 0.09889I$ $b = -1.83374 - 0.14991I$	$5.43825 + 8.83857I$	0
$u = 0.478957 + 0.175114I$ $a = 0.62555 + 1.48896I$ $b = -0.128706 - 0.360441I$	$-0.78467 - 1.23926I$	$-5.32242 + 5.47295I$
$u = 0.478957 - 0.175114I$ $a = 0.62555 - 1.48896I$ $b = -0.128706 + 0.360441I$	$-0.78467 + 1.23926I$	$-5.32242 - 5.47295I$
$u = 0.07800 + 1.49272I$ $a = -1.50386 + 0.09747I$ $b = 1.82804 + 0.09407I$	$8.16387 - 2.18472I$	0
$u = 0.07800 - 1.49272I$ $a = -1.50386 - 0.09747I$ $b = 1.82804 - 0.09407I$	$8.16387 + 2.18472I$	0
$u = 1.51183 + 0.01086I$ $a = 0.317761 - 0.182920I$ $b = 2.09380 + 0.13018I$	$0.06365 + 10.42840I$	0
$u = 1.51183 - 0.01086I$ $a = 0.317761 + 0.182920I$ $b = 2.09380 - 0.13018I$	$0.06365 - 10.42840I$	0
$u = -0.13980 + 1.52059I$ $a = -0.39445 + 1.40951I$ $b = 1.54870 - 3.66586I$	$1.66607 + 0.20314I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.13980 - 1.52059I$ $a = -0.39445 - 1.40951I$ $b = 1.54870 + 3.66586I$	$1.66607 - 0.20314I$	0
$u = 0.030492 + 0.449001I$ $a = 0.296509 - 1.156240I$ $b = -1.046570 + 0.812879I$	$-1.21942 - 6.06914I$	$-0.76059 - 2.63784I$
$u = 0.030492 - 0.449001I$ $a = 0.296509 + 1.156240I$ $b = -1.046570 - 0.812879I$	$-1.21942 + 6.06914I$	$-0.76059 + 2.63784I$
$u = 0.50465 + 1.51967I$ $a = 1.50482 + 0.37400I$ $b = -2.01643 + 0.96407I$	$7.20481 - 10.90700I$	0
$u = 0.50465 - 1.51967I$ $a = 1.50482 - 0.37400I$ $b = -2.01643 - 0.96407I$	$7.20481 + 10.90700I$	0
$u = -0.378884$ $a = -2.36935$ $b = -0.867969$	-2.22317	-0.252670
$u = 0.64911 + 1.49897I$ $a = -1.44538 - 0.56337I$ $b = 2.26266 - 0.99181I$	$4.8344 - 17.8080I$	0
$u = 0.64911 - 1.49897I$ $a = -1.44538 + 0.56337I$ $b = 2.26266 + 0.99181I$	$4.8344 + 17.8080I$	0
$u = -0.71431 + 1.53469I$ $a = 1.114620 - 0.373137I$ $b = -1.21769 - 1.82144I$	$7.13913 + 0.48203I$	0
$u = -0.71431 - 1.53469I$ $a = 1.114620 + 0.373137I$ $b = -1.21769 + 1.82144I$	$7.13913 - 0.48203I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.92191 + 1.43934I$ $a = -1.111690 + 0.636225I$ $b = 1.44949 + 1.78433I$	$6.56818 + 7.36505I$	0
$u = -0.92191 - 1.43934I$ $a = -1.111690 - 0.636225I$ $b = 1.44949 - 1.78433I$	$6.56818 - 7.36505I$	0
$u = -0.237720 + 0.158364I$ $a = -3.64518 - 2.93335I$ $b = -0.681565 - 0.621880I$	$-2.23495 - 1.29247I$	$-6.68617 - 1.38636I$
$u = -0.237720 - 0.158364I$ $a = -3.64518 + 2.93335I$ $b = -0.681565 + 0.621880I$	$-2.23495 + 1.29247I$	$-6.68617 + 1.38636I$
$u = 0.62041 + 1.63980I$ $a = 0.998177 + 0.582876I$ $b = -2.10790 + 0.42331I$	$6.07321 - 3.61773I$	0
$u = 0.62041 - 1.63980I$ $a = 0.998177 - 0.582876I$ $b = -2.10790 - 0.42331I$	$6.07321 + 3.61773I$	0
$u = 0.43998 + 1.83287I$ $a = -1.036670 - 0.340691I$ $b = 2.46384 - 0.76211I$	$6.26435 + 2.30308I$	0
$u = 0.43998 - 1.83287I$ $a = -1.036670 + 0.340691I$ $b = 2.46384 + 0.76211I$	$6.26435 - 2.30308I$	0

$$\text{II. } I_2^u = \langle 4u^8 + u^6 - 4u^5 + 2u^4 - 5u^3 - u^2 + 7b + u + 3, 4u^8 + 7u^7 + \dots + 7a + 3, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{4}{7}u^8 - u^7 + \dots - \frac{1}{7}u - \frac{3}{7} \\ -\frac{4}{7}u^8 - \frac{1}{7}u^6 + \dots - \frac{1}{7}u - \frac{3}{7} \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{4}{7}u^8 - u^7 + \dots - \frac{1}{7}u - \frac{3}{7} \\ -\frac{4}{7}u^8 - \frac{1}{7}u^6 + \dots - \frac{1}{7}u - \frac{3}{7} \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^8 + u^6 + u^4 - 1 \\ u^8 + u^7 + u^6 + 2u^5 + u^4 + 2u^3 + 2u - 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{3}{7}u^8 - u^7 + \dots - \frac{1}{7}u - \frac{10}{7} \\ \frac{3}{7}u^8 + u^7 + \dots + \frac{13}{7}u - \frac{10}{7} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ -u^8 - u^7 - u^6 - 2u^5 - u^4 - 2u^3 - 2u + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -\frac{5}{49}u^8 - \frac{16}{7}u^7 - \frac{241}{49}u^6 - \frac{184}{49}u^5 - \frac{307}{49}u^4 - \frac{342}{49}u^3 - \frac{361}{49}u^2 + \frac{95}{49}u - \frac{618}{49}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^9$
c_3, c_8	u^9
c_4	$(u + 1)^9$
c_5, c_{10}	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
c_6	$u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$
c_7	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$
c_9	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$
c_{11}	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
c_{12}	$u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^9$
c_3, c_8	y^9
c_5, c_{10}	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
c_6, c_9	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$
c_7, c_{11}	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
c_{12}	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$ $a = 0.903964 + 0.094390I$ $b = -0.852846 + 0.158943I$	$0.13850 - 2.09337I$	$-5.47770 + 4.24226I$
$u = 0.140343 - 0.966856I$ $a = 0.903964 - 0.094390I$ $b = -0.852846 - 0.158943I$	$0.13850 + 2.09337I$	$-5.47770 - 4.24226I$
$u = 0.628449 + 0.875112I$ $a = -0.53175 + 1.59553I$ $b = -1.55776 - 1.17662I$	$-2.26187 - 2.45442I$	$-3.78210 + 4.39771I$
$u = 0.628449 - 0.875112I$ $a = -0.53175 - 1.59553I$ $b = -1.55776 + 1.17662I$	$-2.26187 + 2.45442I$	$-3.78210 - 4.39771I$
$u = -0.796005 + 0.733148I$ $a = 0.476406 + 0.294981I$ $b = 0.390088 - 0.527698I$	$-6.01628 - 1.33617I$	$-12.84367 + 3.27176I$
$u = -0.796005 - 0.733148I$ $a = 0.476406 - 0.294981I$ $b = 0.390088 + 0.527698I$	$-6.01628 + 1.33617I$	$-12.84367 - 3.27176I$
$u = -0.728966 + 0.986295I$ $a = -0.352455 - 0.113243I$ $b = -0.007269 + 0.556797I$	$-5.24306 + 7.08493I$	$-15.6193 - 1.7431I$
$u = -0.728966 - 0.986295I$ $a = -0.352455 + 0.113243I$ $b = -0.007269 - 0.556797I$	$-5.24306 - 7.08493I$	$-15.6193 + 1.7431I$
$u = 0.512358$ $a = -1.42091$ $b = -0.373004$	-2.84338	-15.1670

$$\text{III. } I_3^u = \langle -4u^{15} - 30u^{13} + \dots + b + 8, 2u^{15} + 14u^{13} + \dots + a - 7, u^{16} + 8u^{14} + \dots - 3u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^{15} - 14u^{13} + \dots - 13u + 7 \\ 4u^{15} + 30u^{13} + \dots + 18u - 8 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^{14} - 14u^{12} + \dots + 3u - 1 \\ 2u^{15} + 15u^{13} + \dots + 10u - 6 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{15} - u^{14} + \dots - 5u + 2 \\ u^{15} + 8u^{13} + \dots + 10u - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{14} - 7u^{12} + \dots + 5u - 1 \\ u^{15} + 8u^{13} + \dots + 10u - 3 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{15} - 7u^{13} + \dots - u - 1 \\ -3u^{15} - u^{14} + \dots - 14u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3u^{15} + 2u^{14} + \dots - 13u + 3 \\ -u^{15} + u^{14} + \dots - 13u + 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{15} + u^{14} + \dots - 8u + 4 \\ -2u^{15} - u^{14} + \dots - 11u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{15} - 7u^{13} + \dots + 5u^2 - u \\ -3u^{15} - u^{14} + \dots + 17u^2 - 14u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = 35u^{15} + 12u^{14} + 275u^{13} - 18u^{12} + 898u^{11} - 348u^{10} + 1661u^9 - 964u^8 + 1955u^7 - 1160u^6 + 1383u^5 - 706u^4 + 579u^3 - 256u^2 + 146u - 39$$

(iv) u -Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{16} - 10u^{15} + \dots - 7u + 1$
c_2	$u^{16} + 6u^{15} + \dots - u + 1$
c_3	$u^{16} - 3u^{14} + \dots - u + 1$
c_4	$u^{16} - 6u^{15} + \dots + u + 1$
c_5	$u^{16} + 3u^{15} + \dots + 6u + 1$
c_6	$u^{16} + 3u^{15} + \dots + 8u^2 + 1$
c_7	$u^{16} + 8u^{14} + \dots - 3u + 1$
c_8	$u^{16} - 3u^{14} + \dots + u + 1$
c_9	$u^{16} - 3u^{15} + \dots + 8u^2 + 1$
c_{10}	$u^{16} - 5u^{13} + \dots - 5u + 1$
c_{11}	$u^{16} + 8u^{14} + \dots + 3u + 1$
c_{12}	$u^{16} - 6u^{15} + \dots - 3u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{16} - 2y^{15} + \dots + 61y + 1$
c_2, c_4	$y^{16} - 10y^{15} + \dots - 7y + 1$
c_3, c_8	$y^{16} - 6y^{15} + \dots + 9y + 1$
c_5	$y^{16} - 5y^{15} + \dots - 14y + 1$
c_6, c_9	$y^{16} + 11y^{15} + \dots + 16y + 1$
c_7, c_{11}	$y^{16} + 16y^{15} + \dots + 11y + 1$
c_{10}	$y^{16} + 10y^{14} + \dots + 9y + 1$
c_{12}	$y^{16} - 14y^{15} + \dots - 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.192282 + 1.004160I$ $a = -0.054945 - 1.233160I$ $b = 0.391316 - 0.450641I$	$-8.83850 - 0.76161I$	$-4.2680 + 18.7238I$
$u = 0.192282 - 1.004160I$ $a = -0.054945 + 1.233160I$ $b = 0.391316 + 0.450641I$	$-8.83850 + 0.76161I$	$-4.2680 - 18.7238I$
$u = 0.405160 + 0.782797I$ $a = -0.41658 + 1.39011I$ $b = -0.522604 - 0.259087I$	$-1.72004 - 2.39298I$	$-3.94028 + 2.30129I$
$u = 0.405160 - 0.782797I$ $a = -0.41658 - 1.39011I$ $b = -0.522604 + 0.259087I$	$-1.72004 + 2.39298I$	$-3.94028 - 2.30129I$
$u = -0.380479 + 0.681918I$ $a = -3.58192 - 6.22555I$ $b = -2.28948 + 4.19034I$	$-2.96721 + 2.98693I$	$-21.6572 + 12.8409I$
$u = -0.380479 - 0.681918I$ $a = -3.58192 + 6.22555I$ $b = -2.28948 - 4.19034I$	$-2.96721 - 2.98693I$	$-21.6572 - 12.8409I$
$u = 0.445295 + 0.521652I$ $a = -1.043710 + 0.252877I$ $b = 0.938529 - 0.582515I$	$0.00207 - 2.08322I$	$-6.76763 + 3.46484I$
$u = 0.445295 - 0.521652I$ $a = -1.043710 - 0.252877I$ $b = 0.938529 + 0.582515I$	$0.00207 + 2.08322I$	$-6.76763 - 3.46484I$
$u = 0.279505 + 0.496867I$ $a = 0.739008 - 0.233492I$ $b = -1.056140 + 0.735456I$	$-1.36164 - 6.43556I$	$-8.1558 + 16.1878I$
$u = 0.279505 - 0.496867I$ $a = 0.739008 + 0.233492I$ $b = -1.056140 - 0.735456I$	$-1.36164 + 6.43556I$	$-8.1558 - 16.1878I$

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.08961 + 1.47734I$		
$a = 0.703553 - 0.688380I$	$1.50817 - 0.70603I$	$-8.36846 + 5.87842I$
$b = -1.15108 + 2.45886I$		
$u = 0.08961 - 1.47734I$		
$a = 0.703553 + 0.688380I$	$1.50817 + 0.70603I$	$-8.36846 - 5.87842I$
$b = -1.15108 - 2.45886I$		
$u = -0.60082 + 1.36455I$		
$a = 1.40109 - 0.55373I$	$6.18219 + 6.62853I$	$-4.79477 - 3.23115I$
$b = -1.40464 - 0.96198I$		
$u = -0.60082 - 1.36455I$		
$a = 1.40109 + 0.55373I$	$6.18219 - 6.62853I$	$-4.79477 + 3.23115I$
$b = -1.40464 + 0.96198I$		
$u = -0.43055 + 1.58967I$		
$a = -1.246490 + 0.210919I$	$7.19496 - 0.24679I$	$-1.04785 + 3.22477I$
$b = 1.59410 + 1.15005I$		
$u = -0.43055 - 1.58967I$		
$a = -1.246490 - 0.210919I$	$7.19496 + 0.24679I$	$-1.04785 - 3.22477I$
$b = 1.59410 - 1.15005I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^9)(u^{16} - 10u^{15} + \dots - 7u + 1)$ $\cdot (u^{88} + 36u^{87} + \dots + 9016u + 2401)$
c_2	$((u-1)^9)(u^{16} + 6u^{15} + \dots - u + 1)(u^{88} - 16u^{87} + \dots + 504u - 49)$
c_3	$u^9(u^{16} - 3u^{14} + \dots - u + 1)(u^{88} + u^{87} + \dots + 14336u + 25088)$
c_4	$((u+1)^9)(u^{16} - 6u^{15} + \dots + u + 1)(u^{88} - 16u^{87} + \dots + 504u - 49)$
c_5	$(u^9 + u^8 + \dots - u - 1)(u^{16} + 3u^{15} + \dots + 6u + 1)$ $\cdot (u^{88} - u^{87} + \dots + 8558243u - 2435537)$
c_6	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{16} + 3u^{15} + \dots + 8u^2 + 1)(u^{88} + 3u^{87} + \dots - 1497u - 181)$
c_7	$(u^9 + u^8 + \dots + u - 1)(u^{16} + 8u^{14} + \dots - 3u + 1)$ $\cdot (u^{88} + 2u^{87} + \dots + 4968u - 1771)$
c_8	$u^9(u^{16} - 3u^{14} + \dots + u + 1)(u^{88} + u^{87} + \dots + 14336u + 25088)$
c_9	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)$ $\cdot (u^{16} - 3u^{15} + \dots + 8u^2 + 1)(u^{88} + 3u^{87} + \dots - 1497u - 181)$
c_{10}	$(u^9 + u^8 + \dots - u - 1)(u^{16} - 5u^{13} + \dots - 5u + 1)$ $\cdot (u^{88} - 14u^{87} + \dots - 5848u + 1043)$
c_{11}	$(u^9 - u^8 + \dots + u + 1)(u^{16} + 8u^{14} + \dots + 3u + 1)$ $\cdot (u^{88} + 2u^{87} + \dots + 4968u - 1771)$
c_{12}	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)$ $\cdot (u^{16} - 6u^{15} + \dots - 3u + 1)(u^{88} - 4u^{87} + \dots + 2u - 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y-1)^9)(y^{16} - 2y^{15} + \dots + 61y + 1)$ $\cdot (y^{88} + 48y^{87} + \dots - 1539089020y + 5764801)$
c_2, c_4	$((y-1)^9)(y^{16} - 10y^{15} + \dots - 7y + 1)$ $\cdot (y^{88} - 36y^{87} + \dots - 9016y + 2401)$
c_3, c_8	$y^9(y^{16} - 6y^{15} + \dots + 9y + 1)$ $\cdot (y^{88} - 63y^{87} + \dots - 10096214016y + 629407744)$
c_5	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{16} - 5y^{15} + \dots - 14y + 1)$ $\cdot (y^{88} + 33y^{87} + \dots + 85934090519941y + 5931840478369)$
c_6, c_9	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{16} + 11y^{15} + \dots + 16y + 1)(y^{88} + 49y^{87} + \dots - 883509y + 32761)$
c_7, c_{11}	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (y^{16} + 16y^{15} + \dots + 11y + 1)$ $\cdot (y^{88} + 70y^{87} + \dots + 39623986y + 3136441)$
c_{10}	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{16} + 10y^{14} + \dots + 9y + 1)$ $\cdot (y^{88} + 2y^{87} + \dots + 12594048y + 1087849)$
c_{12}	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (y^{16} - 14y^{15} + \dots - 5y + 1)(y^{88} - 16y^{87} + \dots + 6y + 1)$