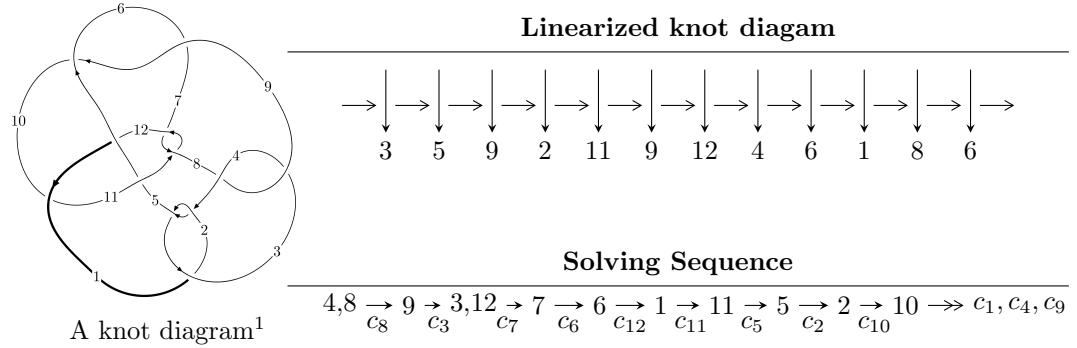


## $12n_{0259}$ ( $K12n_{0259}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 8.06424 \times 10^{33}u^{29} - 3.08706 \times 10^{34}u^{28} + \dots + 2.02678 \times 10^{35}b + 8.88012 \times 10^{34}, \\ - 1.10182 \times 10^{35}u^{29} + 5.35345 \times 10^{35}u^{28} + \dots + 2.02678 \times 10^{36}a - 5.52972 \times 10^{36}, \\ u^{30} - 5u^{29} + \dots + 208u - 64 \rangle$$

$$I_2^u = \langle -50322u^{16} + 60651u^{15} + \dots + 148714b + 159141, \\ - 2740465u^{16} + 777157u^{15} + \dots + 297428a + 8444609,$$

$$u^{17} + 3u^{15} - 2u^{14} + 5u^{13} - 9u^{12} + 2u^{11} - 20u^{10} - 2u^9 - 25u^8 + u^7 - 17u^6 + 6u^5 + 3u^3 + 2u^2 - 3u - 1 \rangle$$

$$I_3^u = \langle -158244u^8a^3 - 40800u^8a^2 + \dots + 813522a - 91963, 2u^8a^3 - u^8a^2 + \dots + 94a + 520, \\ u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

$$I_1^v = \langle a, b + 2v + 2, 4v^2 + 6v + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 85 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 8.06 \times 10^{33}u^{29} - 3.09 \times 10^{34}u^{28} + \dots + 2.03 \times 10^{35}b + 8.88 \times 10^{34}, -1.10 \times 10^{35}u^{29} + 5.35 \times 10^{35}u^{28} + \dots + 2.03 \times 10^{36}a - 5.53 \times 10^{36}, u^{30} - 5u^{29} + \dots + 208u - 64 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0543630u^{29} - 0.264136u^{28} + \dots - 10.6974u + 2.72833 \\ -0.0397885u^{29} + 0.152314u^{28} + \dots - 0.205764u - 0.438140 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0394700u^{29} - 0.200918u^{28} + \dots - 9.53676u + 4.27030 \\ -0.0378177u^{29} + 0.199367u^{28} + \dots + 10.9483u - 5.71363 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0249093u^{29} - 0.112539u^{28} + \dots - 1.85669u - 1.21498 \\ -0.0341130u^{29} + 0.167188u^{28} + \dots + 6.77674u - 4.71681 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0984923u^{29} - 0.480645u^{28} + \dots - 18.1702u + 6.77214 \\ 0.0129199u^{29} - 0.117465u^{28} + \dots - 13.8793u + 11.1867 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0145745u^{29} - 0.111822u^{28} + \dots - 10.9032u + 2.29019 \\ -0.0397885u^{29} + 0.152314u^{28} + \dots - 0.205764u - 0.438140 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0265616u^{29} - 0.114090u^{28} + \dots - 0.445179u - 3.65831 \\ -0.0719307u^{29} + 0.366555u^{28} + \dots + 17.7250u - 10.4304 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0766915u^{29} + 0.396957u^{28} + \dots + 20.3635u - 7.97007 \\ -0.00269807u^{29} + 0.0505818u^{28} + \dots + 12.2023u - 10.7644 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0441293u^{29} - 0.216509u^{28} + \dots - 7.47278u + 5.04380 \\ 0.0527084u^{29} - 0.269779u^{28} + \dots - 13.6736u + 11.6248 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $-0.171902u^{29} + 0.740462u^{28} + \dots + 32.2278u - 42.5665$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{30} + 17u^{29} + \cdots + 6768u + 256$
$c_2, c_4$	$u^{30} - 3u^{29} + \cdots - 44u - 16$
$c_3, c_8$	$u^{30} - 5u^{29} + \cdots + 208u - 64$
$c_5, c_7, c_{11}$	$u^{30} - u^{29} + \cdots + 2u^2 - 1$
$c_6, c_9, c_{12}$	$u^{30} - 30u^{28} + \cdots - u + 1$
$c_{10}$	$u^{30} - 19u^{29} + \cdots + 2048u - 512$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{30} - 5y^{29} + \cdots - 31895296y + 65536$
$c_2, c_4$	$y^{30} - 17y^{29} + \cdots - 6768y + 256$
$c_3, c_8$	$y^{30} + 9y^{29} + \cdots - 21248y + 4096$
$c_5, c_7, c_{11}$	$y^{30} + y^{29} + \cdots - 4y + 1$
$c_6, c_9, c_{12}$	$y^{30} - 60y^{29} + \cdots - 63y + 1$
$c_{10}$	$y^{30} - 23y^{29} + \cdots - 3145728y + 262144$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.920671 + 0.215050I$		
$a = 0.474770 + 0.236439I$	$-0.678358 - 0.594987I$	$-11.14828 - 1.26949I$
$b = 0.185709 - 0.495074I$		
$u = -0.920671 - 0.215050I$		
$a = 0.474770 - 0.236439I$	$-0.678358 + 0.594987I$	$-11.14828 + 1.26949I$
$b = 0.185709 + 0.495074I$		
$u = 0.997695 + 0.376702I$		
$a = 0.437212 + 0.126971I$	$-1.30376 + 3.43482I$	$-13.9978 - 7.1058I$
$b = 0.612963 - 0.562757I$		
$u = 0.997695 - 0.376702I$		
$a = 0.437212 - 0.126971I$	$-1.30376 - 3.43482I$	$-13.9978 + 7.1058I$
$b = 0.612963 + 0.562757I$		
$u = 0.316298 + 0.849109I$		
$a = 0.425852 + 0.030660I$	$-2.07471 - 1.64401I$	$-10.99207 + 2.69705I$
$b = 0.918017 - 0.164528I$		
$u = 0.316298 - 0.849109I$		
$a = 0.425852 - 0.030660I$	$-2.07471 + 1.64401I$	$-10.99207 - 2.69705I$
$b = 0.918017 + 0.164528I$		
$u = 0.250072 + 0.795467I$		
$a = 0.08474 + 1.97666I$	$-2.30189 - 1.11843I$	$-12.20818 + 6.54898I$
$b = -0.528572 - 0.417784I$		
$u = 0.250072 - 0.795467I$		
$a = 0.08474 - 1.97666I$	$-2.30189 + 1.11843I$	$-12.20818 - 6.54898I$
$b = -0.528572 + 0.417784I$		
$u = -0.439076 + 1.238770I$		
$a = -0.341907 - 1.274950I$	$3.50589 + 3.81678I$	$-10.18184 - 5.51966I$
$b = -0.664768 + 0.726793I$		
$u = -0.439076 - 1.238770I$		
$a = -0.341907 + 1.274950I$	$3.50589 - 3.81678I$	$-10.18184 + 5.51966I$
$b = -0.664768 - 0.726793I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.672305 + 0.131504I$		
$a = 0.465097 - 0.014978I$	$-10.75090 - 0.00550I$	$-26.5001 + 2.7456I$
$b = -1.333120 + 0.111490I$		
$u = 0.672305 - 0.131504I$		
$a = 0.465097 + 0.014978I$	$-10.75090 + 0.00550I$	$-26.5001 - 2.7456I$
$b = -1.333120 - 0.111490I$		
$u = 0.673336 + 1.153840I$		
$a = -0.01039 - 1.60109I$	$-8.26944 - 5.68185I$	$-13.8804 + 4.5637I$
$b = 0.938705 + 0.985912I$		
$u = 0.673336 - 1.153840I$		
$a = -0.01039 + 1.60109I$	$-8.26944 + 5.68185I$	$-13.8804 - 4.5637I$
$b = 0.938705 - 0.985912I$		
$u = -1.195980 + 0.596147I$		
$a = 0.433700 + 0.140568I$	$-5.01474 - 3.34334I$	$-11.59669 + 2.94079I$
$b = -0.804031 - 0.882885I$		
$u = -1.195980 - 0.596147I$		
$a = 0.433700 - 0.140568I$	$-5.01474 + 3.34334I$	$-11.59669 - 2.94079I$
$b = -0.804031 + 0.882885I$		
$u = 1.165670 + 0.733627I$		
$a = 0.464934 - 0.150862I$	$-7.65940 + 8.88821I$	$-13.8511 - 5.5347I$
$b = -0.96952 + 1.09583I$		
$u = 1.165670 - 0.733627I$		
$a = 0.464934 + 0.150862I$	$-7.65940 - 8.88821I$	$-13.8511 + 5.5347I$
$b = -0.96952 - 1.09583I$		
$u = 0.221400 + 1.363400I$		
$a = 0.015740 - 1.022660I$	$4.53000 - 0.32057I$	$-7.71560 - 1.10595I$
$b = -0.132717 + 0.871865I$		
$u = 0.221400 - 1.363400I$		
$a = 0.015740 + 1.022660I$	$4.53000 + 0.32057I$	$-7.71560 + 1.10595I$
$b = -0.132717 - 0.871865I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.647790 + 1.222820I$		
$a = -0.535702 + 1.224120I$	$1.35480 - 9.44263I$	$-13.2001 + 10.5014I$
$b = -0.802016 - 0.702401I$		
$u = 0.647790 - 1.222820I$		
$a = -0.535702 - 1.224120I$	$1.35480 + 9.44263I$	$-13.2001 - 10.5014I$
$b = -0.802016 + 0.702401I$		
$u = 1.40325$		
$a = 0.323081$	$-10.9270$	$-40.4210$
$b = -0.580884$		
$u = -0.79217 + 1.21119I$		
$a = 0.24417 + 1.46527I$	$-2.95388 + 10.39440I$	$-10.10326 - 5.62687I$
$b = 0.94680 - 1.23179I$		
$u = -0.79217 - 1.21119I$		
$a = 0.24417 - 1.46527I$	$-2.95388 - 10.39440I$	$-10.10326 + 5.62687I$
$b = 0.94680 + 1.23179I$		
$u = 0.86453 + 1.17030I$		
$a = 0.39716 - 1.50383I$	$-6.1786 - 16.1705I$	$-12.9056 + 8.4851I$
$b = 1.07853 + 1.31263I$		
$u = 0.86453 - 1.17030I$		
$a = 0.39716 + 1.50383I$	$-6.1786 + 16.1705I$	$-12.9056 - 8.4851I$
$b = 1.07853 - 1.31263I$		
$u = -0.43744 + 1.41584I$		
$a = -0.014032 + 1.010380I$	$3.27546 + 6.39941I$	$-8.60195 - 5.42628I$
$b = 0.154110 - 0.976877I$		
$u = -0.43744 - 1.41584I$		
$a = -0.014032 - 1.010380I$	$3.27546 - 6.39941I$	$-8.60195 + 5.42628I$
$b = 0.154110 + 0.976877I$		
$u = -0.450762$		
$a = 0.594234$	$-0.635586$	$-15.5630$
$b = 0.380692$		

## II.

$$I_2^u = \langle -5.03 \times 10^4 u^{16} + 6.07 \times 10^4 u^{15} + \dots + 1.49 \times 10^5 b + 1.59 \times 10^5, -2.74 \times 10^6 u^{16} + 7.77 \times 10^5 u^{15} + \dots + 2.97 \times 10^5 a + 8.44 \times 10^6, u^{17} + 3u^{15} + \dots - 3u - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 9.21388u^{16} - 2.61292u^{15} + \dots + 9.55963u - 28.3921 \\ 0.338381u^{16} - 0.407837u^{15} + \dots + 0.429865u - 1.07011 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 8.05673u^{16} - 2.39322u^{15} + \dots + 5.18074u - 23.8643 \\ 0.240774u^{16} + 0.356863u^{15} + \dots + 0.945237u - 0.542810 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 7.15244u^{16} - 2.00192u^{15} + \dots + 5.24891u - 22.0139 \\ 0.161686u^{16} + 0.219011u^{15} + \dots + 1.21485u - 0.151512 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1.06597u^{16} - 0.172287u^{15} + \dots + 1.14668u - 3.00192 \\ -0.00475409u^{16} - 0.200035u^{15} + \dots + 0.818719u + 0.219011 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 9.55226u^{16} - 3.02076u^{15} + \dots + 9.98950u - 29.4622 \\ 0.338381u^{16} - 0.407837u^{15} + \dots + 0.429865u - 1.07011 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.14506u^{16} + 0.0344352u^{15} + \dots - 0.877073u + 3.39322 \\ -0.0790880u^{16} - 0.137852u^{15} + \dots + 0.269611u + 0.391298 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.11352u^{16} - 0.409703u^{15} + \dots + 2.18844u - 3.03636 \\ 0.179102u^{16} - 0.186802u^{15} + \dots + 1.19578u - 0.0528397 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 8.14791u^{16} - 2.44064u^{15} + \dots + 8.41295u - 24.3902 \\ 0.343135u^{16} - 0.207802u^{15} + \dots - 0.388854u - 1.28913 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $\frac{6794471}{297428}u^{16} - \frac{1681861}{297428}u^{15} + \dots + \frac{571348}{74357}u - \frac{25623465}{297428}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{17} - 10u^{16} + \cdots + 17u - 1$
$c_2$	$u^{17} + 4u^{16} + \cdots - u + 1$
$c_3$	$u^{17} + 3u^{15} + \cdots - 3u + 1$
$c_4$	$u^{17} - 4u^{16} + \cdots - u - 1$
$c_5, c_{11}$	$u^{17} + 6u^{15} + \cdots - 3u - 1$
$c_6, c_{12}$	$u^{17} - 3u^{16} + \cdots + 6u^2 + 1$
$c_7$	$u^{17} + 6u^{15} + \cdots - 3u + 1$
$c_8$	$u^{17} + 3u^{15} + \cdots - 3u - 1$
$c_9$	$u^{17} + 3u^{16} + \cdots - 6u^2 - 1$
$c_{10}$	$u^{17} - 5u^{16} + \cdots + 5u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{17} - 2y^{16} + \cdots + 157y - 1$
$c_2, c_4$	$y^{17} - 10y^{16} + \cdots + 17y - 1$
$c_3, c_8$	$y^{17} + 6y^{16} + \cdots + 13y - 1$
$c_5, c_7, c_{11}$	$y^{17} + 12y^{16} + \cdots + 5y - 1$
$c_6, c_9, c_{12}$	$y^{17} - 5y^{16} + \cdots - 12y - 1$
$c_{10}$	$y^{17} - 17y^{16} + \cdots + 11y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.222868 + 0.957169I$		
$a = 0.937935 - 0.366003I$	$-3.24280 + 2.04185I$	$-17.4447 - 3.6628I$
$b = 0.975905 + 0.087227I$		
$u = -0.222868 - 0.957169I$		
$a = 0.937935 + 0.366003I$	$-3.24280 - 2.04185I$	$-17.4447 + 3.6628I$
$b = 0.975905 - 0.087227I$		
$u = -0.143073 + 1.125680I$		
$a = -0.06490 + 1.65937I$	$6.60440 - 0.23148I$	$-4.66739 - 0.18271I$
$b = -0.240226 - 1.383230I$		
$u = -0.143073 - 1.125680I$		
$a = -0.06490 - 1.65937I$	$6.60440 + 0.23148I$	$-4.66739 + 0.18271I$
$b = -0.240226 + 1.383230I$		
$u = -0.934717 + 0.786177I$		
$a = -0.460802 - 0.068107I$	$0.49138 - 1.47201I$	$-4.39198 + 2.32537I$
$b = 0.102794 + 0.830593I$		
$u = -0.934717 - 0.786177I$		
$a = -0.460802 + 0.068107I$	$0.49138 + 1.47201I$	$-4.39198 - 2.32537I$
$b = 0.102794 - 0.830593I$		
$u = 0.463922 + 1.145870I$		
$a = 0.43983 - 1.42671I$	$5.30175 - 4.82160I$	$-8.88387 + 5.04151I$
$b = -0.17875 + 1.49824I$		
$u = 0.463922 - 1.145870I$		
$a = 0.43983 + 1.42671I$	$5.30175 + 4.82160I$	$-8.88387 - 5.04151I$
$b = -0.17875 - 1.49824I$		
$u = 0.622575 + 1.114960I$		
$a = -0.632046 + 0.809570I$	$4.76952 - 2.66666I$	$-3.51429 + 3.01636I$
$b = -0.340268 - 0.934275I$		
$u = 0.622575 - 1.114960I$		
$a = -0.632046 - 0.809570I$	$4.76952 + 2.66666I$	$-3.51429 - 3.01636I$
$b = -0.340268 + 0.934275I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.621513 + 0.226133I$		
$a = 3.17814 + 0.77491I$	$2.59448 + 0.58189I$	$-16.1225 - 5.9646I$
$b = 0.068320 + 1.335540I$		
$u = 0.621513 - 0.226133I$		
$a = 3.17814 - 0.77491I$	$2.59448 - 0.58189I$	$-16.1225 + 5.9646I$
$b = 0.068320 - 1.335540I$		
$u = -0.76282 + 1.20700I$		
$a = -0.450462 - 0.871861I$	$1.99341 + 8.23287I$	$-9.38259 - 6.87786I$
$b = -0.529361 + 0.773457I$		
$u = -0.76282 - 1.20700I$		
$a = -0.450462 + 0.871861I$	$1.99341 - 8.23287I$	$-9.38259 + 6.87786I$
$b = -0.529361 - 0.773457I$		
$u = -0.509710$		
$a = -3.08687$	$-4.29378$	$-7.87230$
$b = 0.727999$		
$u = 1.53136$		
$a = -0.327837$	$-10.7956$	$20.7800$
$b = 0.362879$		
$u = -0.310720$		
$a = -25.4807$	$-5.48556$	$-72.0930$
$b = -0.807701$		

$$\text{III. } I_3^u = \langle -1.58 \times 10^5 a^3 u^8 - 4.08 \times 10^4 a^2 u^8 + \dots + 8.14 \times 10^5 a - 9.20 \times 10^4, 2u^8 a^3 - u^8 a^2 + \dots + 94a + 520, u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} a \\ 0.250587a^3 u^8 + 0.0646088a^2 u^8 + \dots - 1.28825a + 0.145628 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.0695431a^3 u^8 - 0.0718551a^2 u^8 + \dots - 0.741380a + 2.26000 \\ -0.0275854a^3 u^8 + 0.352029a^2 u^8 + \dots + 1.67727a + 0.105629 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.0695431a^3 u^8 + 0.0718551a^2 u^8 + \dots + 0.741380a + 1.74000 \\ -0.250587a^3 u^8 - 0.0646088a^2 u^8 + \dots + 1.28825a + 0.854372 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 - 1 \\ -u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.250587a^3 u^8 + 0.0646088a^2 u^8 + \dots - 0.288252a + 0.145628 \\ 0.250587a^3 u^8 + 0.0646088a^2 u^8 + \dots - 1.28825a + 0.145628 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^4 - u^2 - 1 \\ -u^4 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^6 + u^4 + 2u^2 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.324754a^3 u^8 + 0.342471a^2 u^8 + \dots - 0.326854a + 0.340849 \\ 0.0741671a^3 u^8 + 0.277862a^2 u^8 + \dots - 0.0386022a + 0.195221 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^7 - 4u^6 - 4u^5 - 4u^4 - 8u^3 - 4u^2 - 14$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^4$
$c_2, c_4$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^4$
$c_3, c_8$	$(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^4$
$c_5, c_7, c_{11}$	$u^{36} + 3u^{35} + \dots - 136u - 31$
$c_6, c_9, c_{12}$	$u^{36} - 3u^{35} + \dots + 18264u - 3559$
$c_{10}$	$(u^2 + u - 1)^{18}$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^4$
$c_2, c_4$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^4$
$c_3, c_8$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^4$
$c_5, c_7, c_{11}$	$y^{36} + 11y^{35} + \dots + 16224y + 961$
$c_6, c_9, c_{12}$	$y^{36} - 25y^{35} + \dots + 545224y + 12666481$
$c_{10}$	$(y^2 - 3y + 1)^{18}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.140343 + 0.966856I$		
$a = -0.61869 + 1.39310I$	$5.73128 - 2.09337I$	$-7.48501 + 4.16283I$
$b = -0.42993 - 1.44275I$		
$u = 0.140343 + 0.966856I$		
$a = 1.38851 + 0.80504I$	$-2.16441 - 2.09337I$	$-7.48501 + 4.16283I$
$b = 0.128913 - 0.359883I$		
$u = 0.140343 + 0.966856I$		
$a = 0.243842 + 0.158886I$	$-2.16441 - 2.09337I$	$-7.48501 + 4.16283I$
$b = 1.351770 - 0.079224I$		
$u = 0.140343 + 0.966856I$		
$a = -0.00482 - 1.76129I$	$5.73128 - 2.09337I$	$-7.48501 + 4.16283I$
$b = -0.13564 + 1.61047I$		
$u = 0.140343 - 0.966856I$		
$a = -0.61869 - 1.39310I$	$5.73128 + 2.09337I$	$-7.48501 - 4.16283I$
$b = -0.42993 + 1.44275I$		
$u = 0.140343 - 0.966856I$		
$a = 1.38851 - 0.80504I$	$-2.16441 + 2.09337I$	$-7.48501 - 4.16283I$
$b = 0.128913 + 0.359883I$		
$u = 0.140343 - 0.966856I$		
$a = 0.243842 - 0.158886I$	$-2.16441 + 2.09337I$	$-7.48501 - 4.16283I$
$b = 1.351770 + 0.079224I$		
$u = 0.140343 - 0.966856I$		
$a = -0.00482 + 1.76129I$	$5.73128 + 2.09337I$	$-7.48501 - 4.16283I$
$b = -0.13564 - 1.61047I$		
$u = 0.628449 + 0.875112I$		
$a = -0.525443 + 0.462550I$	$-4.56478 - 2.45442I$	$-10.32792 + 2.91298I$
$b = 1.30414 - 0.74950I$		
$u = 0.628449 + 0.875112I$		
$a = 0.763452 - 1.086660I$	$3.33090 - 2.45442I$	$-10.32792 + 2.91298I$
$b = 0.294073 + 1.242760I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.628449 + 0.875112I$		
$a = -0.485650 + 0.077610I$	$3.33090 - 2.45442I$	$-10.32792 + 2.91298I$
$b = -0.523285 - 0.562963I$		
$u = 0.628449 + 0.875112I$		
$a = -0.20185 + 2.17919I$	$-4.56478 - 2.45442I$	$-10.32792 + 2.91298I$
$b = -0.704050 - 1.030220I$		
$u = 0.628449 - 0.875112I$		
$a = -0.525443 - 0.462550I$	$-4.56478 + 2.45442I$	$-10.32792 - 2.91298I$
$b = 1.30414 + 0.74950I$		
$u = 0.628449 - 0.875112I$		
$a = 0.763452 + 1.086660I$	$3.33090 + 2.45442I$	$-10.32792 - 2.91298I$
$b = 0.294073 - 1.242760I$		
$u = 0.628449 - 0.875112I$		
$a = -0.485650 - 0.077610I$	$3.33090 + 2.45442I$	$-10.32792 - 2.91298I$
$b = -0.523285 + 0.562963I$		
$u = -0.796005 + 0.733148I$		
$a = -0.880986 - 0.487136I$	$-8.31919 - 1.33617I$	$-15.2841 + 0.7017I$
$b = 0.964779 + 0.981447I$		
$u = -0.796005 + 0.733148I$		
$a = 0.892032 + 0.347149I$	$-0.423507 - 1.336170I$	$-15.2841 + 0.7017I$
$b = -0.127108 - 1.007800I$		
$u = -0.796005 + 0.733148I$		
$a = -0.187374 + 0.704738I$	$-0.423507 - 1.336170I$	$-15.2841 + 0.7017I$
$b = 0.186512 + 0.286438I$		
$u = -0.796005 + 0.733148I$		
$a = -0.96383 - 2.26674I$	$-8.31919 - 1.33617I$	$-15.2841 + 0.7017I$
$b = -1.12030 + 0.90709I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.796005 - 0.733148I$		
$a = -0.880986 + 0.487136I$	$-8.31919 + 1.33617I$	$-15.2841 - 0.7017I$
$b = 0.964779 - 0.981447I$		
$u = -0.796005 - 0.733148I$		
$a = 0.892032 - 0.347149I$	$-0.423507 + 1.336170I$	$-15.2841 - 0.7017I$
$b = -0.127108 + 1.007800I$		
$u = -0.796005 - 0.733148I$		
$a = -0.187374 - 0.704738I$	$-0.423507 + 1.336170I$	$-15.2841 - 0.7017I$
$b = 0.186512 - 0.286438I$		
$u = -0.796005 - 0.733148I$		
$a = -0.96383 + 2.26674I$	$-8.31919 + 1.33617I$	$-15.2841 - 0.7017I$
$b = -1.12030 - 0.90709I$		
$u = -0.728966 + 0.986295I$		
$a = 0.501545 + 1.033540I$	$0.34972 + 7.08493I$	$-13.5768 - 5.9133I$
$b = 0.646764 - 1.177390I$		
$u = -0.728966 + 0.986295I$		
$a = -0.593832 - 0.265649I$	$-7.54597 + 7.08493I$	$-13.5768 - 5.9133I$
$b = 1.49815 + 0.97115I$		
$u = -0.728966 + 0.986295I$		
$a = -0.124651 - 0.247951I$	$0.34972 + 7.08493I$	$-13.5768 - 5.9133I$
$b = -0.919556 + 0.288684I$		
$u = -0.728966 + 0.986295I$		
$a = -0.39289 - 1.79104I$	$-7.54597 + 7.08493I$	$-13.5768 - 5.9133I$
$b = -0.78397 + 1.35550I$		
$u = -0.728966 - 0.986295I$		
$a = 0.501545 - 1.033540I$	$0.34972 - 7.08493I$	$-13.5768 + 5.9133I$
$b = 0.646764 + 1.177390I$		
$u = -0.728966 - 0.986295I$		
$a = -0.593832 + 0.265649I$	$-7.54597 - 7.08493I$	$-13.5768 + 5.9133I$
$b = 1.49815 - 0.97115I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.728966 - 0.986295I$		
$a = -0.124651 + 0.247951I$	$0.34972 - 7.08493I$	$-13.5768 + 5.9133I$
$b = -0.919556 - 0.288684I$		
$u = -0.728966 - 0.986295I$		
$a = -0.39289 + 1.79104I$	$-7.54597 - 7.08493I$	$-13.5768 + 5.9133I$
$b = -0.78397 - 1.35550I$		
$u = 0.512358$		
$a = -4.03622$	$-5.14629$	$-16.6520$
$b = 0.558485$		
$u = 0.512358$		
$a = 2.66334 + 4.93805I$	$2.74940$	$-16.6520$
$b = 0.081120 + 1.296290I$		
$u = 0.512358$		
$a = 2.66334 - 4.93805I$	$2.74940$	$-16.6520$
$b = 0.081120 - 1.296290I$		
$u = 0.512358$		
$a = -9.90920$	$-5.14629$	$-16.6520$
$b = -0.983236$		

$$\text{IV. } I_1^v = \langle a, b + 2v + 2, 4v^2 + 6v + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -2v - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -2v - 3 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2v - 2 \\ -2v - 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 4v + 5 \\ 4v + 6 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2v - 2 \\ -2v - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -4v - 5 \\ -4v - 6 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 5v + 5 \\ 4v + 6 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 4v + 6 \\ 6v + 8 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $\frac{45}{2}v + \frac{55}{4}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_8$	$u^2$
$c_4$	$(u + 1)^2$
$c_5, c_7, c_{10}$	$u^2 + u - 1$
$c_6$	$u^2 - 3u + 1$
$c_9, c_{12}$	$u^2 + 3u + 1$
$c_{11}$	$u^2 - u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_8$	$y^2$
$c_5, c_7, c_{10}$ $c_{11}$	$y^2 - 3y + 1$
$c_6, c_9, c_{12}$	$y^2 - 7y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.30902$		
$a = 0$	-2.63189	-15.7030
$b = 0.618034$		
$v = -0.190983$		
$a = 0$	-10.5276	9.45290
$b = -1.61803$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^2(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^4 \\ \cdot (u^{17} - 10u^{16} + \dots + 17u - 1)(u^{30} + 17u^{29} + \dots + 6768u + 256)$
$c_2$	$(u - 1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^4 \\ \cdot (u^{17} + 4u^{16} + \dots - u + 1)(u^{30} - 3u^{29} + \dots - 44u - 16)$
$c_3$	$u^2(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^4 \\ \cdot (u^{17} + 3u^{15} + \dots - 3u + 1)(u^{30} - 5u^{29} + \dots + 208u - 64)$
$c_4$	$(u + 1)^2(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^4 \\ \cdot (u^{17} - 4u^{16} + \dots - u - 1)(u^{30} - 3u^{29} + \dots - 44u - 16)$
$c_5$	$(u^2 + u - 1)(u^{17} + 6u^{15} + \dots - 3u - 1)(u^{30} - u^{29} + \dots + 2u^2 - 1) \\ \cdot (u^{36} + 3u^{35} + \dots - 136u - 31)$
$c_6$	$(u^2 - 3u + 1)(u^{17} - 3u^{16} + \dots + 6u^2 + 1)(u^{30} - 30u^{28} + \dots - u + 1) \\ \cdot (u^{36} - 3u^{35} + \dots + 18264u - 3559)$
$c_7$	$(u^2 + u - 1)(u^{17} + 6u^{15} + \dots - 3u + 1)(u^{30} - u^{29} + \dots + 2u^2 - 1) \\ \cdot (u^{36} + 3u^{35} + \dots - 136u - 31)$
$c_8$	$u^2(u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1)^4 \\ \cdot (u^{17} + 3u^{15} + \dots - 3u - 1)(u^{30} - 5u^{29} + \dots + 208u - 64)$
$c_9$	$(u^2 + 3u + 1)(u^{17} + 3u^{16} + \dots - 6u^2 - 1)(u^{30} - 30u^{28} + \dots - u + 1) \\ \cdot (u^{36} - 3u^{35} + \dots + 18264u - 3559)$
$c_{10}$	$((u^2 + u - 1)^{19})(u^{17} - 5u^{16} + \dots + 5u - 1) \\ \cdot (u^{30} - 19u^{29} + \dots + 2048u - 512)$
$c_{11}$	$(u^2 - u - 1)(u^{17} + 6u^{15} + \dots - 3u - 1)(u^{30} - u^{29} + \dots + 2u^2 - 1) \\ \cdot (u^{36} + 3u^{35} + \dots - 136u - 31)$
$c_{12}$	$(u^2 + 3u + 1)(u^{17} - 3u^{16} + \dots + 6u^2 + 1)(u^{30} - 30u^{28} + \dots - u + 1) \\ \cdot (u^{36} - 3u^{35} + \dots + 18264u - 3559)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^2(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^4 \cdot (y^{17} - 2y^{16} + \dots + 157y - 1)(y^{30} - 5y^{29} + \dots - 31895296y + 65536)$
$c_2, c_4$	$(y - 1)^2(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^4 \cdot (y^{17} - 10y^{16} + \dots + 17y - 1)(y^{30} - 17y^{29} + \dots - 6768y + 256)$
$c_3, c_8$	$y^2(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^4 \cdot (y^{17} + 6y^{16} + \dots + 13y - 1)(y^{30} + 9y^{29} + \dots - 21248y + 4096)$
$c_5, c_7, c_{11}$	$(y^2 - 3y + 1)(y^{17} + 12y^{16} + \dots + 5y - 1)(y^{30} + y^{29} + \dots - 4y + 1) \cdot (y^{36} + 11y^{35} + \dots + 16224y + 961)$
$c_6, c_9, c_{12}$	$(y^2 - 7y + 1)(y^{17} - 5y^{16} + \dots - 12y - 1)(y^{30} - 60y^{29} + \dots - 63y + 1) \cdot (y^{36} - 25y^{35} + \dots + 545224y + 12666481)$
$c_{10}$	$((y^2 - 3y + 1)^{19})(y^{17} - 17y^{16} + \dots + 11y - 1) \cdot (y^{30} - 23y^{29} + \dots - 3145728y + 262144)$