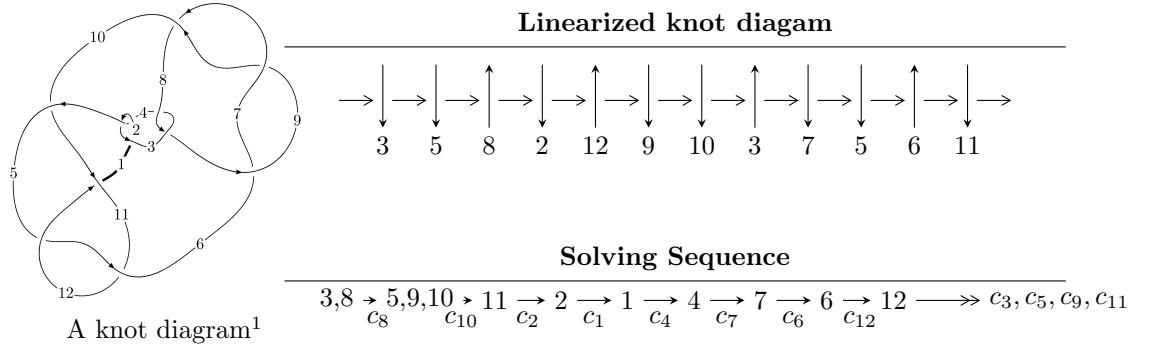


## $12n_{0261}$ ( $K12n_{0261}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 5.82214 \times 10^{22}u^{20} - 3.29635 \times 10^{23}u^{19} + \dots + 1.18107 \times 10^{25}d - 1.00440 \times 10^{25}, \\ - 6.72232 \times 10^{22}u^{20} + 3.09213 \times 10^{23}u^{19} + \dots + 2.36214 \times 10^{25}c - 1.53724 \times 10^{25}, \\ 5.37718 \times 10^{22}u^{20} - 1.64184 \times 10^{23}u^{19} + \dots + 1.18107 \times 10^{25}b + 1.07557 \times 10^{24}, \\ - 6.27749 \times 10^{23}u^{20} + 1.76680 \times 10^{24}u^{19} + \dots + 2.36214 \times 10^{25}a - 1.96176 \times 10^{25}, \\ u^{21} - 3u^{20} + \dots - 32u + 32 \rangle$$

$$I_2^u = \langle -182575u^{12} - 264525u^{11} + \dots + 1396412d - 304734, \\ 1091678u^{12}a - 2056829u^{12} + \dots + 8227316a + 8353986, \\ 182575u^{12}a - 236482u^{12} + \dots - 1091678a - 1127628, \\ 152367u^{12}a - 563814u^{12} + \dots - 1320834a + 1767620, \\ u^{13} + u^{12} + 8u^{11} + 7u^{10} + 22u^9 + 18u^8 + 20u^7 + 21u^6 - u^5 + 5u^4 + 8u^3 - 9u^2 + 4u - 4 \rangle$$

$$I_1^v = \langle a, d, c - 1, b + v + 1, v^2 + v + 1 \rangle$$

$$I_2^v = \langle c, d - 1, b, a - v, v^2 + v + 1 \rangle$$

$$I_3^v = \langle a, d - 1, c + a, b + 1, v + 1 \rangle$$

$$I_4^v = \langle c, d - 1, a^2v^2 - 2cav - v^2a + c^2 + cv + v^2, bv - 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 52 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\text{I. } I_1^u = \langle 5.82 \times 10^{22}u^{20} - 3.30 \times 10^{23}u^{19} + \dots + 1.18 \times 10^{25}d - 1.00 \times 10^{25}, -6.72 \times 10^{22}u^{20} + 3.09 \times 10^{23}u^{19} + \dots + 2.36 \times 10^{25}c - 1.54 \times 10^{25}, 5.38 \times 10^{22}u^{20} - 1.64 \times 10^{23}u^{19} + \dots + 1.18 \times 10^{25}b + 1.08 \times 10^{24}, -6.28 \times 10^{23}u^{20} + 1.77 \times 10^{24}u^{19} + \dots + 2.36 \times 10^{25}a - 1.96 \times 10^{25}, u^{21} - 3u^{20} + \dots - 32u + 32 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0265755u^{20} - 0.0747968u^{19} + \dots + 1.58156u + 0.830504 \\ -0.00455281u^{20} + 0.0139013u^{19} + \dots + 0.741851u - 0.0910676 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00284586u^{20} - 0.0130904u^{19} + \dots + 0.686169u + 0.650783 \\ -0.00492955u^{20} + 0.0279099u^{19} + \dots - 1.68092u + 0.850415 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0210595u^{20} + 0.0850046u^{19} + \dots - 3.46686u + 1.92380 \\ -0.00576337u^{20} + 0.0431394u^{19} + \dots - 2.97976u + 1.42272 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0311283u^{20} + 0.0886981u^{19} + \dots - 0.839713u - 0.921571 \\ -0.00455281u^{20} + 0.0139013u^{19} + \dots + 0.741851u - 0.0910676 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0311283u^{20} + 0.0886981u^{19} + \dots - 0.839713u - 0.921571 \\ -0.0204279u^{20} + 0.0622591u^{19} + \dots - 0.104280u - 0.241041 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.00284586u^{20} - 0.0130904u^{19} + \dots + 0.686169u + 0.650783 \\ 0.00468667u^{20} - 0.0299351u^{19} + \dots + 1.91768u - 0.996105 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.00777542u^{20} - 0.0410003u^{19} + \dots + 2.36709u - 0.199631 \\ 0.00392727u^{20} - 0.0344353u^{19} + \dots + 2.49530u - 1.41598 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.00320223u^{20} + 0.0332571u^{19} + \dots - 2.57523u + 0.998926 \\ 0.0165563u^{20} - 0.0374854u^{19} + \dots + 0.0371713u + 0.859283 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{203971647344418191706557}{1476335887006576019057698}u^{20} + \frac{2056765698754565732069615}{5905343548026304076230792}u^{19} + \dots + \frac{11041294381070090419087484}{738167943503288009528849}u - \frac{9937042912284907740395116}{738167943503288009528849}$$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{21} + 31u^{20} + \cdots - 4u + 1$
$c_2, c_4, c_6$ $c_7, c_9$	$u^{21} - 5u^{20} + \cdots - 2u + 1$
$c_3, c_8$	$u^{21} + 3u^{20} + \cdots - 32u - 32$
$c_5, c_{11}$	$u^{21} + u^{20} + \cdots - 12u - 4$
$c_{10}$	$u^{21} - u^{20} + \cdots - 636u - 612$
$c_{12}$	$u^{21} + 11u^{20} + \cdots + 40u - 16$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{21} - 71y^{20} + \cdots - 144y - 1$
$c_2, c_4, c_6$ $c_7, c_9$	$y^{21} - 31y^{20} + \cdots - 4y - 1$
$c_3, c_8$	$y^{21} + 15y^{20} + \cdots - 4096y - 1024$
$c_5, c_{11}$	$y^{21} + 11y^{20} + \cdots + 40y - 16$
$c_{10}$	$y^{21} - 13y^{20} + \cdots + 1093608y - 374544$
$c_{12}$	$y^{21} - y^{20} + \cdots + 3616y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.036987 + 1.146540I$		
$a = 0.578318 + 0.602865I$		
$b = -0.222232 + 0.595413I$	$-3.32924 + 4.98790I$	$-8.89610 - 7.00933I$
$c = 0.512526 + 0.210362I$		
$d = 0.669819 - 0.685364I$		
$u = 0.036987 - 1.146540I$		
$a = 0.578318 - 0.602865I$		
$b = -0.222232 - 0.595413I$	$-3.32924 - 4.98790I$	$-8.89610 + 7.00933I$
$c = 0.512526 - 0.210362I$		
$d = 0.669819 + 0.685364I$		
$u = -0.154679 + 0.793727I$		
$a = -0.412466 + 0.647829I$		
$b = 0.050314 + 0.532414I$	$-0.57334 - 1.34767I$	$-3.83291 + 5.35474I$
$c = 0.634334 - 0.187007I$		
$d = 0.450400 + 0.427591I$		
$u = -0.154679 - 0.793727I$		
$a = -0.412466 - 0.647829I$		
$b = 0.050314 - 0.532414I$	$-0.57334 + 1.34767I$	$-3.83291 - 5.35474I$
$c = 0.634334 + 0.187007I$		
$d = 0.450400 - 0.427591I$		
$u = -0.470495 + 0.448103I$		
$a = -0.409901 + 0.397885I$		
$b = -0.268303 + 0.555704I$	$0.53740 - 1.37698I$	$1.82779 + 4.46485I$
$c = 0.888871 - 0.334537I$		
$d = -0.014563 + 0.370881I$		
$u = -0.470495 - 0.448103I$		
$a = -0.409901 - 0.397885I$		
$b = -0.268303 - 0.555704I$	$0.53740 + 1.37698I$	$1.82779 - 4.46485I$
$c = 0.888871 + 0.334537I$		
$d = -0.014563 - 0.370881I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.128491 + 0.614288I$		
$a = 0.535926 + 1.193030I$		
$b = -0.103617 + 0.330827I$	$-2.84340 - 1.62330I$	$-11.63179 + 1.59969I$
$c = 0.549782 + 0.053680I$		
$d = 0.801726 - 0.175920I$		
$u = -0.128491 - 0.614288I$		
$a = 0.535926 - 1.193030I$		
$b = -0.103617 - 0.330827I$	$-2.84340 + 1.62330I$	$-11.63179 - 1.59969I$
$c = 0.549782 - 0.053680I$		
$d = 0.801726 + 0.175920I$		
$u = 0.518224 + 0.162575I$		
$a = 0.507737 + 0.210413I$		
$b = 0.583653 + 0.355856I$	$-0.25092 - 2.48183I$	$1.69657 + 3.99164I$
$c = 1.221470 + 0.303490I$		
$d = -0.228914 - 0.191587I$		
$u = 0.518224 - 0.162575I$		
$a = 0.507737 - 0.210413I$		
$b = 0.583653 - 0.355856I$	$-0.25092 + 2.48183I$	$1.69657 - 3.99164I$
$c = 1.221470 - 0.303490I$		
$d = -0.228914 + 0.191587I$		
$u = -1.63718$		
$a = 0.993823$		
$b = -0.623198$	$-10.0156$	$-8.03320$
$c = 0.380652$		
$d = 1.62707$		
$u = -0.11848 + 1.68160I$		
$a = -0.035721 - 0.977610I$		
$b = -0.04009 - 2.59088I$	$-10.91870 - 3.26339I$	$-9.90010 + 2.49959I$
$c = -1.53144 + 0.13174I$		
$d = -1.64818 - 0.05576I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.11848 - 1.68160I$ $a = -0.035721 + 0.977610I$ $b = -0.04009 + 2.59088I$ $c = -1.53144 - 0.13174I$ $d = -1.64818 + 0.05576I$	$-10.91870 + 3.26339I$	$-9.90010 - 2.49959I$
$u = 1.80226 + 0.29000I$ $a = -0.934416 + 0.075142I$ $b = 0.669749 + 0.073622I$ $c = 0.368644 - 0.018467I$ $d = 1.70586 + 0.13555I$	$-14.0445 - 5.1370I$	$-11.02836 + 2.94498I$
$u = 1.80226 - 0.29000I$ $a = -0.934416 - 0.075142I$ $b = 0.669749 - 0.073622I$ $c = 0.368644 + 0.018467I$ $d = 1.70586 - 0.13555I$	$-14.0445 + 5.1370I$	$-11.02836 - 2.94498I$
$u = -0.77417 + 1.65700I$ $a = -0.199071 - 0.900171I$ $b = -0.19629 - 2.45464I$ $c = -1.170520 + 0.665347I$ $d = -1.64570 - 0.36703I$	$-15.0920 - 8.4883I$	$-8.50111 + 3.29621I$
$u = -0.77417 - 1.65700I$ $a = -0.199071 + 0.900171I$ $b = -0.19629 + 2.45464I$ $c = -1.170520 - 0.665347I$ $d = -1.64570 + 0.36703I$	$-15.0920 + 8.4883I$	$-8.50111 - 3.29621I$
$u = 0.94230 + 1.60086I$ $a = 0.234926 - 0.876218I$ $b = 0.22253 - 2.40487I$ $c = -1.054920 - 0.759955I$ $d = -1.62407 + 0.44958I$	$-18.0417 + 14.4957I$	$-10.41632 - 6.77876I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.94230 - 1.60086I$		
$a = 0.234926 + 0.876218I$		
$b = 0.22253 + 2.40487I$	$-18.0417 - 14.4957I$	$-10.41632 + 6.77876I$
$c = -1.054920 + 0.759955I$		
$d = -1.62407 - 0.44958I$		
$u = 0.66513 + 1.94791I$		
$a = 0.137757 - 0.866713I$		
$b = 0.11588 - 2.45183I$	$18.5711 + 4.0668I$	$-12.30105 - 1.16982I$
$c = -1.109070 - 0.438193I$		
$d = -1.77991 + 0.30814I$		
$u = 0.66513 - 1.94791I$		
$a = 0.137757 + 0.866713I$		
$b = 0.11588 + 2.45183I$	$18.5711 - 4.0668I$	$-12.30105 + 1.16982I$
$c = -1.109070 + 0.438193I$		
$d = -1.77991 - 0.30814I$		

$$\text{II. } I_2^u = \langle -1.83 \times 10^5 u^{12} - 2.65 \times 10^5 u^{11} + \dots + 1.40 \times 10^6 d - 3.05 \times 10^5, 1.09 \times 10^6 a u^{12} - 2.06 \times 10^6 u^{12} + \dots + 8.23 \times 10^6 a + 8.35 \times 10^6, 1.83 \times 10^5 a u^{12} - 2.36 \times 10^5 u^{12} + \dots - 1.09 \times 10^6 a - 1.13 \times 10^6, 1.52 \times 10^5 a u^{12} - 5.64 \times 10^5 u^{12} + \dots - 1.32 \times 10^6 a + 1.77 \times 10^6, u^{13} + u^{12} + \dots + 4u - 4 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -0.130746 a u^{12} + 0.169350 u^{12} + \dots + 0.781774 a + 0.807518 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.195443 a u^{12} + 0.368235 u^{12} + \dots - 1.47294 a - 1.49562 \\ 0.130746 u^{12} + 0.189432 u^{11} + \dots - 0.691165 u + 0.218226 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.169350 a u^{12} + 0.368235 u^{12} + \dots - 0.807518 a - 1.49562 \\ 0.0521873 a u^{12} + 0.261492 u^{12} + \dots + 1.33084 a - 0.563547 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.130746 a u^{12} + 0.169350 u^{12} + \dots - 0.218226 a + 0.807518 \\ -0.130746 a u^{12} + 0.169350 u^{12} + \dots + 0.781774 a + 0.807518 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.130746 a u^{12} + 0.169350 u^{12} + \dots - 0.218226 a + 0.807518 \\ -0.112072 a u^{12} + 0.214783 u^{12} + \dots + 1.01652 a + 1.16237 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.195443 a u^{12} + 0.368235 u^{12} + \dots - 1.47294 a - 1.49562 \\ -0.0586861 a u^{12} - 0.0773597 a u^{11} + \dots - 0.522983 a - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.195443 a u^{12} + 0.237489 u^{12} + \dots - 1.47294 a - 1.71384 \\ -0.0586861 a u^{12} + 0.0186736 u^{12} + \dots - 0.522983 a - 0.765256 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.280165 a u^{12} + 0.0140927 u^{12} + \dots + 0.328803 a - 1.76474 \\ -0.00702658 a u^{12} + 0.208441 u^{12} + \dots + 1.44074 a - 0.142777 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{498055}{698206} u^{12} + \frac{527627}{698206} u^{11} + \dots - \frac{3711195}{698206} u - \frac{2197714}{349103}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{26} + 23u^{25} + \cdots + 1824u + 256$
$c_2, c_4, c_6$ $c_7, c_9$	$u^{26} - 3u^{25} + \cdots - 24u - 16$
$c_3, c_8$	$(u^{13} - u^{12} + \cdots + 4u + 4)^2$
$c_5, c_{11}$	$(u^{13} + 2u^{12} + \cdots + u - 1)^2$
$c_{10}$	$(u^{13} - 2u^{12} + \cdots + 3u - 1)^2$
$c_{12}$	$(u^{13} + 8u^{12} + \cdots + 5u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{26} - 43y^{25} + \cdots - 2728448y + 65536$
$c_2, c_4, c_6$ $c_7, c_9$	$y^{26} - 23y^{25} + \cdots - 1824y + 256$
$c_3, c_8$	$(y^{13} + 15y^{12} + \cdots - 56y - 16)^2$
$c_5, c_{11}$	$(y^{13} + 8y^{12} + \cdots + 5y - 1)^2$
$c_{10}$	$(y^{13} - 16y^{12} + \cdots + 5y - 1)^2$
$c_{12}$	$(y^{13} - 4y^{12} + \cdots + 85y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.997974 + 0.288600I$ $a = -0.683330 - 0.720692I$ $b = -0.91523 - 1.71878I$ $c = 0.429264 + 0.025235I$ $d = 1.321540 - 0.136474I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$-10.35428 + 4.38707I$
$u = -0.997974 + 0.288600I$ $a = 1.258530 + 0.227197I$ $b = -0.435677 + 0.098702I$ $c = 0.38670 + 1.83409I$ $d = -0.889938 - 0.522023I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$-10.35428 + 4.38707I$
$u = -0.997974 - 0.288600I$ $a = -0.683330 + 0.720692I$ $b = -0.91523 + 1.71878I$ $c = 0.429264 - 0.025235I$ $d = 1.321540 + 0.136474I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$-10.35428 - 4.38707I$
$u = -0.997974 - 0.288600I$ $a = 1.258530 - 0.227197I$ $b = -0.435677 - 0.098702I$ $c = 0.38670 - 1.83409I$ $d = -0.889938 + 0.522023I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$-10.35428 - 4.38707I$
$u = 0.452299 + 0.637242I$ $a = -1.050080 + 0.855900I$ $b = 0.262779 + 0.278726I$ $c = 0.752720 + 0.325368I$ $d = 0.119367 - 0.483853I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$-8.45638 - 0.58191I$
$u = 0.452299 + 0.637242I$ $a = 0.416509 + 0.482947I$ $b = 0.133116 + 0.626828I$ $c = 0.485499 - 0.067773I$ $d = 1.020370 + 0.282033I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$-8.45638 - 0.58191I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.452299 - 0.637242I$ $a = -1.050080 - 0.855900I$ $b = 0.262779 - 0.278726I$ $c = 0.752720 - 0.325368I$ $d = 0.119367 + 0.483853I$	$-2.32452 + 0.99909I$	$-8.45638 + 0.58191I$
$u = 0.452299 - 0.637242I$ $a = 0.416509 - 0.482947I$ $b = 0.133116 - 0.626828I$ $c = 0.485499 + 0.067773I$ $d = 1.020370 - 0.282033I$	$-2.32452 + 0.99909I$	$-8.45638 + 0.58191I$
$u = -0.032142 + 0.650070I$ $a = 0.289254 + 0.995266I$ $b = -0.055887 + 0.387220I$ $c = -5.95031 + 0.48273I$ $d = -1.166960 - 0.013545I$	$-2.68970 + 2.36301I$	$-10.56487 - 4.19898I$
$u = -0.032142 + 0.650070I$ $a = -0.06776 - 1.79178I$ $b = -0.12255 - 3.88363I$ $c = 0.598447 + 0.056382I$ $d = 0.656289 - 0.156046I$	$-2.68970 + 2.36301I$	$-10.56487 - 4.19898I$
$u = -0.032142 - 0.650070I$ $a = 0.289254 - 0.995266I$ $b = -0.055887 - 0.387220I$ $c = -5.95031 - 0.48273I$ $d = -1.166960 + 0.013545I$	$-2.68970 - 2.36301I$	$-10.56487 + 4.19898I$
$u = -0.032142 - 0.650070I$ $a = -0.06776 + 1.79178I$ $b = -0.12255 + 3.88363I$ $c = 0.598447 - 0.056382I$ $d = 0.656289 + 0.156046I$	$-2.68970 - 2.36301I$	$-10.56487 + 4.19898I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.612460$		
$a = 0.817082$		
$b = 1.22597$	-2.28684	-1.88180
$c = 0.464808$		
$d = 1.15142$		
$u = 0.612460$		
$a = -1.88000$		
$b = 0.284677$	-2.28684	-1.88180
$c = 2.00172$		
$d = -0.500430$		
$u = 0.25689 + 1.55234I$		
$a = 0.088362 - 1.008150I$		
$b = 0.10585 - 2.61952I$	$-7.65433 + 3.30324I$	$-7.16390 - 2.39821I$
$c = 0.441695 + 0.272101I$		
$d = 0.641176 - 1.011030I$		
$u = 0.25689 + 1.55234I$		
$a = 0.567403 + 0.506935I$		
$b = -0.308927 + 0.755560I$	$-7.65433 + 3.30324I$	$-7.16390 - 2.39821I$
$c = -1.63150 - 0.33817I$		
$d = -1.58768 + 0.12181I$		
$u = 0.25689 - 1.55234I$		
$a = 0.088362 + 1.008150I$		
$b = 0.10585 + 2.61952I$	$-7.65433 - 3.30324I$	$-7.16390 + 2.39821I$
$c = 0.441695 - 0.272101I$		
$d = 0.641176 + 1.011030I$		
$u = 0.25689 - 1.55234I$		
$a = 0.567403 - 0.506935I$		
$b = -0.308927 - 0.755560I$	$-7.65433 - 3.30324I$	$-7.16390 + 2.39821I$
$c = -1.63150 + 0.33817I$		
$d = -1.58768 - 0.12181I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.50699 + 1.66583I$ $a = -0.143355 - 0.943399I$ $b = -0.15313 - 2.52888I$ $c = 0.416555 - 0.312499I$ $d = 0.536120 + 1.152390I$	$-11.16570 - 8.60203I$	$-9.58542 + 5.32797I$
$u = -0.50699 + 1.66583I$ $a = -0.543494 + 0.487244I$ $b = 0.309381 + 0.852342I$ $c = -1.36379 + 0.50699I$ $d = -1.64422 - 0.23949I$	$-11.16570 - 8.60203I$	$-9.58542 + 5.32797I$
$u = -0.50699 - 1.66583I$ $a = -0.143355 + 0.943399I$ $b = -0.15313 + 2.52888I$ $c = 0.416555 + 0.312499I$ $d = 0.536120 - 1.152390I$	$-11.16570 + 8.60203I$	$-9.58542 - 5.32797I$
$u = -0.50699 - 1.66583I$ $a = -0.543494 - 0.487244I$ $b = 0.309381 - 0.852342I$ $c = -1.36379 - 0.50699I$ $d = -1.64422 + 0.23949I$	$-11.16570 + 8.60203I$	$-9.58542 - 5.32797I$
$u = 0.02169 + 1.76519I$ $a = 0.005990 - 0.955765I$ $b = 0.00639 - 2.56843I$ $c = 0.406243 - 0.232132I$ $d = 0.855680 + 1.060360I$	$-12.07010 + 1.38297I$	$-10.93425 - 0.71622I$
$u = 0.02169 + 1.76519I$ $a = -0.606568 + 0.477299I$ $b = 0.418568 + 0.712063I$ $c = -1.45478 - 0.02149I$ $d = -1.68724 + 0.01015I$	$-12.07010 + 1.38297I$	$-10.93425 - 0.71622I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.02169 - 1.76519I$		
$a = 0.005990 + 0.955765I$		
$b = 0.00639 + 2.56843I$	$-12.07010 - 1.38297I$	$-10.93425 + 0.71622I$
$c = 0.406243 + 0.232132I$		
$d = 0.855680 - 1.060360I$		
$u = 0.02169 - 1.76519I$		
$a = -0.606568 - 0.477299I$		
$b = 0.418568 - 0.712063I$	$-12.07010 - 1.38297I$	$-10.93425 + 0.71622I$
$c = -1.45478 + 0.02149I$		
$d = -1.68724 - 0.01015I$		

$$\text{III. } I_1^v = \langle a, d, c - 1, b + v + 1, v^2 + v + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -v - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v \\ v + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ v + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v + 1 \\ v \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes =  $4v - 1$**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_6, c_7$ $c_8, c_9$	$u^2$
$c_4$	$(u + 1)^2$
$c_5, c_{10}, c_{12}$	$u^2 + u + 1$
$c_{11}$	$u^2 - u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_6, c_7$ $c_8, c_9$	$y^2$
$c_5, c_{10}, c_{11}$ $c_{12}$	$y^2 + y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$		
$a = 0$		
$b = -0.500000 - 0.866025I$	$-1.64493 - 2.02988I$	$-3.00000 + 3.46410I$
$c = 1.00000$		
$d = 0$		
$v = -0.500000 - 0.866025I$		
$a = 0$		
$b = -0.500000 + 0.866025I$	$-1.64493 + 2.02988I$	$-3.00000 - 3.46410I$
$c = 1.00000$		
$d = 0$		

$$\text{IV. } I_2^v = \langle c, d-1, b, a-v, v^2 + v + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v+1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v+1 \\ -v \end{pmatrix}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** =  $-4v - 5$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8$	$u^2$
$c_5, c_{10}$	$u^2 - u + 1$
$c_6, c_7$	$(u - 1)^2$
$c_9$	$(u + 1)^2$
$c_{11}, c_{12}$	$u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_8$	$y^2$
$c_5, c_{10}, c_{11}$ $c_{12}$	$y^2 + y + 1$
$c_6, c_7, c_9$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$		
$a = -0.500000 + 0.866025I$		
$b = 0$	$-1.64493 + 2.02988I$	$-3.00000 - 3.46410I$
$c = 0$		
$d = 1.00000$		
$v = -0.500000 - 0.866025I$		
$a = -0.500000 - 0.866025I$		
$b = 0$	$-1.64493 - 2.02988I$	$-3.00000 + 3.46410I$
$c = 0$		
$d = 1.00000$		

$$\mathbf{V} \cdot I_3^v = \langle a, d-1, c+a, b+1, v+1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$ $c_7$	$u - 1$
$c_3, c_5, c_8$ $c_{10}, c_{11}, c_{12}$	$u$
$c_4, c_9$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_7, c_9$	$y - 1$
$c_3, c_5, c_8$ $c_{10}, c_{11}, c_{12}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = -1.00000$	-3.28987	-12.0000
$c = 0$		
$d = 1.00000$		

$$\text{VI. } I_4^v = \langle c, d - 1, a^2v^2 - 2cav - v^2a + c^2 + cv + v^2, bv - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} a \\ b \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -a + 1 \\ -ba + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -a + v \\ -b \end{pmatrix} \\ a_1 &= \begin{pmatrix} -a \\ -b \end{pmatrix} \\ a_4 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -a + 1 \\ -ba + a \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-b^2 - v^2 + 4a - 12$

(iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.

(v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

**(iv) Complex Volumes and Cusp Shapes**

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	$-3.28987 + 2.02988I$	$-11.65094 + 3.33332I$
$c = \dots$		
$d = \dots$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^2(u - 1)^3(u^{21} + 31u^{20} + \dots - 4u + 1)$ $\cdot (u^{26} + 23u^{25} + \dots + 1824u + 256)$
$c_2, c_6, c_7$	$u^2(u - 1)^3(u^{21} - 5u^{20} + \dots - 2u + 1)(u^{26} - 3u^{25} + \dots - 24u - 16)$
$c_3, c_8$	$u^5(u^{13} - u^{12} + \dots + 4u + 4)^2(u^{21} + 3u^{20} + \dots - 32u - 32)$
$c_4, c_9$	$u^2(u + 1)^3(u^{21} - 5u^{20} + \dots - 2u + 1)(u^{26} - 3u^{25} + \dots - 24u - 16)$
$c_5, c_{11}$	$u(u^2 - u + 1)(u^2 + u + 1)(u^{13} + 2u^{12} + \dots + u - 1)^2$ $\cdot (u^{21} + u^{20} + \dots - 12u - 4)$
$c_{10}$	$u(u^2 - u + 1)(u^2 + u + 1)(u^{13} - 2u^{12} + \dots + 3u - 1)^2$ $\cdot (u^{21} - u^{20} + \dots - 636u - 612)$
$c_{12}$	$u(u^2 + u + 1)^2(u^{13} + 8u^{12} + \dots + 5u - 1)^2$ $\cdot (u^{21} + 11u^{20} + \dots + 40u - 16)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^2(y - 1)^3(y^{21} - 71y^{20} + \dots - 144y - 1)$ $\cdot (y^{26} - 43y^{25} + \dots - 2728448y + 65536)$
$c_2, c_4, c_6$ $c_7, c_9$	$y^2(y - 1)^3(y^{21} - 31y^{20} + \dots - 4y - 1)$ $\cdot (y^{26} - 23y^{25} + \dots - 1824y + 256)$
$c_3, c_8$	$y^5(y^{13} + 15y^{12} + \dots - 56y - 16)^2$ $\cdot (y^{21} + 15y^{20} + \dots - 4096y - 1024)$
$c_5, c_{11}$	$y(y^2 + y + 1)^2(y^{13} + 8y^{12} + \dots + 5y - 1)^2$ $\cdot (y^{21} + 11y^{20} + \dots + 40y - 16)$
$c_{10}$	$y(y^2 + y + 1)^2(y^{13} - 16y^{12} + \dots + 5y - 1)^2$ $\cdot (y^{21} - 13y^{20} + \dots + 1093608y - 374544)$
$c_{12}$	$y(y^2 + y + 1)^2(y^{13} - 4y^{12} + \dots + 85y - 1)^2$ $\cdot (y^{21} - y^{20} + \dots + 3616y - 256)$