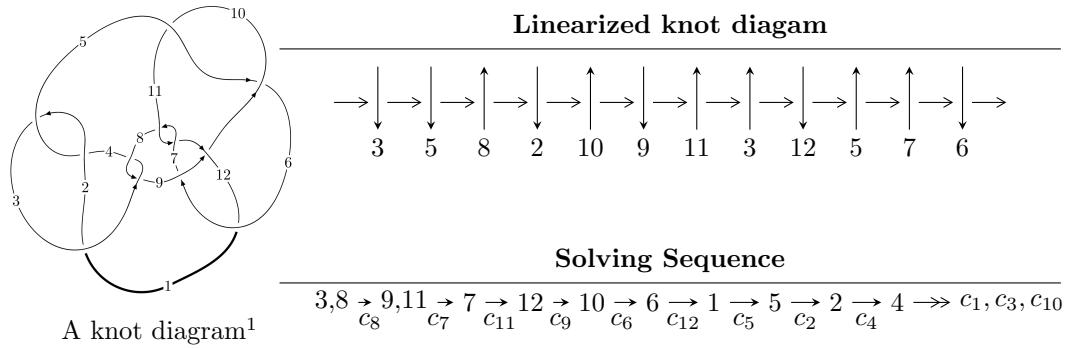


12n<sub>0265</sub> (K12n<sub>0265</sub>)



## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 2.44371 \times 10^{49} u^{24} - 2.09348 \times 10^{50} u^{23} + \dots + 2.28036 \times 10^{53} b - 8.49453 \times 10^{51}, \\ - 3.67178 \times 10^{50} u^{24} + 2.53945 \times 10^{51} u^{23} + \dots + 1.82429 \times 10^{54} a - 1.58059 \times 10^{54}, \\ u^{25} - 7u^{24} + \dots - 768u - 1024 \rangle$$

$$I_2^u = \langle 1765a^5u^4 - 1502a^4u^4 + \dots + 17362a - 4182, -2a^5u^4 + 22a^4u^4 + \dots - 398a - 265, \\ u^5 + u^4 + 5u^3 + u^2 + 2u - 2 \rangle$$

$$I_3^u = \langle 94430u^{13} - 176465u^{12} + \cdots + 3057583b - 933114, \\ 11442968u^{13} - 3792535u^{12} + \cdots + 3057583a + 15949942, \\ u^{14} + 3u^{12} + 3u^{11} - 5u^{10} - 4u^9 - 11u^8 - 8u^7 + 12u^6 - 8u^5 + 20u^4 + 6u^2 + u + 1 \rangle$$

$$I_1^v = \langle a, 8v^3 - 12v^2 + b + 10v - 3, 8v^4 - 12v^3 + 12v^2 - 5v + 1 \rangle$$

$$I_2^v = \langle a, b^6 - b^5 + 2b^4 - 2b^3 + 2b^2 - 2b + 1, v + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 79 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILS/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 2.44 \times 10^{49}u^{24} - 2.09 \times 10^{50}u^{23} + \dots + 2.28 \times 10^{53}b - 8.49 \times 10^{51}, -3.67 \times 10^{50}u^{24} + 2.54 \times 10^{51}u^{23} + \dots + 1.82 \times 10^{54}a - 1.58 \times 10^{54}, u^{25} - 7u^{24} + \dots - 768u - 1024 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.000201272u^{24} - 0.00139202u^{23} + \dots + 0.373312u + 0.866413 \\ -0.000107163u^{24} + 0.000918045u^{23} + \dots + 0.329212u + 0.0372508 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.000229394u^{24} - 0.00150305u^{23} + \dots + 0.0571684u + 0.797253 \\ 0.000436197u^{24} - 0.00314869u^{23} + \dots + 0.195357u - 0.517398 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.000142173u^{24} - 0.000866042u^{23} + \dots + 0.288083u + 0.794249 \\ 0.0000403596u^{24} - 0.000408965u^{23} + \dots + 0.135333u - 0.227239 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.000280396u^{24} - 0.00189155u^{23} + \dots + 0.798559u + 1.20818 \\ -0.000127304u^{24} + 0.00120796u^{23} + \dots + 0.0853997u + 0.470901 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.000729995u^{24} - 0.00506873u^{23} + \dots + 0.566298u + 0.385020 \\ 0.000193200u^{24} - 0.00159495u^{23} + \dots - 0.270058u - 0.454462 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.000602735u^{24} - 0.00397878u^{23} + \dots + 0.982564u + 0.885973 \\ -0.000178179u^{24} + 0.00103362u^{23} + \dots - 0.219803u - 0.141734 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.000548097u^{24} - 0.00349779u^{23} + \dots + 0.400564u + 0.781569 \\ -0.0000546374u^{24} + 0.000480983u^{23} + \dots - 0.582000u - 0.104403 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.000602735u^{24} - 0.00397878u^{23} + \dots + 0.982564u + 0.885973 \\ 0.0000546374u^{24} - 0.000480983u^{23} + \dots + 0.582000u + 0.104403 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.00281397u^{24} + 0.0194032u^{23} + \dots - 9.17416u + 2.20110$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{25} + 25u^{24} + \cdots - 39680u + 4096$
$c_2, c_4$	$u^{25} - 5u^{24} + \cdots - 272u + 64$
$c_3, c_8$	$u^{25} + 7u^{24} + \cdots - 768u + 1024$
$c_5, c_7, c_{10}$ $c_{11}$	$u^{25} + 16u^{23} + \cdots - 4u - 1$
$c_6, c_{12}$	$u^{25} - u^{24} + \cdots - 3u - 1$
$c_9$	$u^{25} - 17u^{24} + \cdots + 304u - 32$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{25} - 45y^{24} + \cdots + 260374528y - 16777216$
$c_2, c_4$	$y^{25} - 25y^{24} + \cdots - 39680y - 4096$
$c_3, c_8$	$y^{25} + 15y^{24} + \cdots + 3473408y - 1048576$
$c_5, c_7, c_{10}$ $c_{11}$	$y^{25} + 32y^{24} + \cdots + 6y - 1$
$c_6, c_{12}$	$y^{25} - 19y^{24} + \cdots - 27y - 1$
$c_9$	$y^{25} + 3y^{24} + \cdots + 6912y - 1024$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.239284 + 0.960930I$		
$a = 0.533027 - 0.309402I$	$-0.98698 - 2.00436I$	$0.63223 + 3.08678I$
$b = 0.493247 + 0.016890I$		
$u = -0.239284 - 0.960930I$		
$a = 0.533027 + 0.309402I$	$-0.98698 + 2.00436I$	$0.63223 - 3.08678I$
$b = 0.493247 - 0.016890I$		
$u = 0.966851$		
$a = 0.382684$	$-3.00634$	$-1.07640$
$b = -0.452501$		
$u = 1.116350 + 0.182242I$		
$a = 0.381438 - 0.739225I$	$0.48422 + 3.81324I$	$7.26566 - 4.06355I$
$b = -0.224461 - 0.800052I$		
$u = 1.116350 - 0.182242I$		
$a = 0.381438 + 0.739225I$	$0.48422 - 3.81324I$	$7.26566 + 4.06355I$
$b = -0.224461 + 0.800052I$		
$u = -0.697727 + 0.198752I$		
$a = -0.164828 + 0.368624I$	$-3.96011 + 7.15054I$	$0.209463 - 0.912602I$
$b = 0.521134 + 1.221040I$		
$u = -0.697727 - 0.198752I$		
$a = -0.164828 - 0.368624I$	$-3.96011 - 7.15054I$	$0.209463 + 0.912602I$
$b = 0.521134 - 1.221040I$		
$u = 0.407422 + 1.271680I$		
$a = 0.154193 + 0.247049I$	$-7.17114 + 4.86761I$	$3.67428 + 1.38704I$
$b = 0.470617 + 0.132952I$		
$u = 0.407422 - 1.271680I$		
$a = 0.154193 - 0.247049I$	$-7.17114 - 4.86761I$	$3.67428 - 1.38704I$
$b = 0.470617 - 0.132952I$		
$u = 0.356543 + 0.532418I$		
$a = 1.40268 - 0.66297I$	$-1.84591 - 0.75519I$	$-5.74786 - 0.43805I$
$b = 0.145873 - 0.427689I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.356543 - 0.532418I$		
$a = 1.40268 + 0.66297I$	$-1.84591 + 0.75519I$	$-5.74786 + 0.43805I$
$b = 0.145873 + 0.427689I$		
$u = -0.481170 + 0.308405I$		
$a = 0.517741 + 0.397349I$	$0.898356 - 0.808185I$	$6.63316 + 4.13450I$
$b = -0.458678 + 0.410360I$		
$u = -0.481170 - 0.308405I$		
$a = 0.517741 - 0.397349I$	$0.898356 + 0.808185I$	$6.63316 - 4.13450I$
$b = -0.458678 - 0.410360I$		
$u = -1.24876 + 0.83504I$		
$a = 0.202515 - 0.510317I$	$-0.688755 - 0.842359I$	$-3.27794 - 2.99522I$
$b = -0.516721 - 1.100670I$		
$u = -1.24876 - 0.83504I$		
$a = 0.202515 + 0.510317I$	$-0.688755 + 0.842359I$	$-3.27794 + 2.99522I$
$b = -0.516721 + 1.100670I$		
$u = -0.19971 + 2.12744I$		
$a = 0.089187 + 1.142770I$	$-12.2506 - 8.8129I$	$-5.58581 + 4.80434I$
$b = -0.29018 + 1.74806I$		
$u = -0.19971 - 2.12744I$		
$a = 0.089187 - 1.142770I$	$-12.2506 + 8.8129I$	$-5.58581 - 4.80434I$
$b = -0.29018 - 1.74806I$		
$u = 1.03266 + 1.89173I$		
$a = 0.583269 - 0.980042I$	$19.0826 + 15.6197I$	$-5.76128 - 6.47974I$
$b = -0.67321 - 1.74414I$		
$u = 1.03266 - 1.89173I$		
$a = 0.583269 + 0.980042I$	$19.0826 - 15.6197I$	$-5.76128 + 6.47974I$
$b = -0.67321 + 1.74414I$		
$u = -0.58061 + 2.17440I$		
$a = -0.286368 - 1.009020I$	$-11.69760 + 0.19520I$	$-6.36512 + 0.I$
$b = 0.12493 - 1.68098I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.58061 - 2.17440I$		
$a = -0.286368 + 1.009020I$	$-11.69760 - 0.19520I$	$-6.36512 + 0.I$
$b = 0.12493 + 1.68098I$		
$u = 1.23926 + 1.89887I$		
$a = -0.567788 + 0.851816I$	$-19.1706 + 7.3377I$	$-6.38194 - 3.47918I$
$b = 0.55518 + 1.55240I$		
$u = 1.23926 - 1.89887I$		
$a = -0.567788 - 0.851816I$	$-19.1706 - 7.3377I$	$-6.38194 + 3.47918I$
$b = 0.55518 - 1.55240I$		
$u = 2.31161 + 0.19224I$		
$a = -0.036412 + 0.377901I$	$-14.6508 + 4.4763I$	$-6.63166 - 2.50646I$
$b = 0.07852 + 1.79165I$		
$u = 2.31161 - 0.19224I$		
$a = -0.036412 - 0.377901I$	$-14.6508 - 4.4763I$	$-6.63166 + 2.50646I$
$b = 0.07852 - 1.79165I$		

$$\text{II. } I_2^u = \langle 1765a^5u^4 - 1502a^4u^4 + \dots + 17362a - 4182, -2a^5u^4 + 22a^4u^4 + \dots - 398a - 265, u^5 + u^4 + 5u^3 + u^2 + 2u - 2 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -1.22230a^5u^4 + 1.04017a^4u^4 + \dots - 12.0235a + 2.89612 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.407202a^5u^4 + 1.61911a^4u^4 + \dots - 12.4986a + 10.4488 \\ 1.02216a^5u^4 + 0.364266a^4u^4 + \dots + 4.14958a - 2.79778 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.26593a^5u^4 + 0.393352a^4u^4 + \dots - 13.1371a + 0.155125 \\ -1.72022a^5u^4 - 3.92521a^4u^4 + \dots + 10.4017a - 6.69252 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0117729a^5u^4 - 0.395429a^4u^4 + \dots + 4.60249a - 1.10665 \\ -1.61150a^5u^4 + 0.450831a^4u^4 + \dots - 6.61773a + 1.48061 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.407202a^5u^4 + 1.61911a^4u^4 + \dots - 12.4986a + 9.18560 \\ 1.02216a^5u^4 + 0.364266a^4u^4 + \dots + 4.14958a - 3.21884 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{4}u^4 + \frac{1}{2}u^3 + \dots + \frac{1}{2}u - \frac{1}{2} \\ \frac{1}{4}u^4 + \frac{3}{2}u^3 + \frac{7}{4}u^2 + u - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{4}u^4 + \frac{3}{4}u^2 - \frac{1}{2}u - \frac{1}{2} \\ -\frac{1}{2}u^3 - \frac{1}{2}u^2 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^4 + \frac{1}{2}u^3 + \dots + \frac{1}{2}u - \frac{1}{2} \\ \frac{1}{2}u^3 + \frac{1}{2}u^2 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-\frac{588}{361}a^4u^4 + \frac{53}{19}u^4a^3 + \dots + \frac{434}{19}a - \frac{9308}{361}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^5 + 8u^4 + 22u^3 + 25u^2 + 15u + 1)^6$
$c_2, c_4$	$(u^5 - 2u^4 - 2u^3 + 3u^2 + 3u - 1)^6$
$c_3, c_8$	$(u^5 - u^4 + 5u^3 - u^2 + 2u + 2)^6$
$c_5, c_7, c_{10}$ $c_{11}$	$u^{30} - 2u^{29} + \dots + 4896u + 1161$
$c_6, c_{12}$	$u^{30} - 6u^{29} + \dots - 2892u + 367$
$c_9$	$(u^3 + u^2 - 1)^{10}$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^5 - 20y^4 + 114y^3 + 19y^2 + 175y - 1)^6$
$c_2, c_4$	$(y^5 - 8y^4 + 22y^3 - 25y^2 + 15y - 1)^6$
$c_3, c_8$	$(y^5 + 9y^4 + 27y^3 + 23y^2 + 8y - 4)^6$
$c_5, c_7, c_{10}$ $c_{11}$	$y^{30} + 30y^{29} + \dots + 10260108y + 1347921$
$c_6, c_{12}$	$y^{30} - 10y^{29} + \dots - 2032180y + 134689$
$c_9$	$(y^3 - y^2 + 2y - 1)^{10}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.375669 + 0.888717I$		
$a = -0.218883 + 0.638145I$	$-3.76205 + 3.93704I$	$-6.85572 - 5.02057I$
$b = -0.936331 - 0.693043I$		
$u = -0.375669 + 0.888717I$		
$a = -1.341030 + 0.088898I$	$-3.76205 - 1.71921I$	$-6.85572 + 0.93832I$
$b = 0.131979 + 0.509733I$		
$u = -0.375669 + 0.888717I$		
$a = -1.69246 - 1.78412I$	$-7.89964 + 1.10891I$	$-13.38499 - 2.04112I$
$b = -0.22064 - 1.80276I$		
$u = -0.375669 + 0.888717I$		
$a = 0.48486 + 2.82858I$	$-7.89964 + 1.10891I$	$-13.38499 - 2.04112I$
$b = 0.03993 + 1.45055I$		
$u = -0.375669 + 0.888717I$		
$a = -1.51063 - 2.46477I$	$-3.76205 - 1.71921I$	$-6.85572 + 0.93832I$
$b = 0.607737 - 1.057200I$		
$u = -0.375669 + 0.888717I$		
$a = 2.15895 + 2.52617I$	$-3.76205 + 3.93704I$	$-6.85572 - 5.02057I$
$b = 0.060199 + 0.974637I$		
$u = -0.375669 - 0.888717I$		
$a = -0.218883 - 0.638145I$	$-3.76205 - 3.93704I$	$-6.85572 + 5.02057I$
$b = -0.936331 + 0.693043I$		
$u = -0.375669 - 0.888717I$		
$a = -1.341030 - 0.088898I$	$-3.76205 + 1.71921I$	$-6.85572 - 0.93832I$
$b = 0.131979 - 0.509733I$		
$u = -0.375669 - 0.888717I$		
$a = -1.69246 + 1.78412I$	$-7.89964 - 1.10891I$	$-13.38499 + 2.04112I$
$b = -0.22064 + 1.80276I$		
$u = -0.375669 - 0.888717I$		
$a = 0.48486 - 2.82858I$	$-7.89964 - 1.10891I$	$-13.38499 + 2.04112I$
$b = 0.03993 - 1.45055I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.375669 - 0.888717I$		
$a = -1.51063 + 2.46477I$	$-3.76205 + 1.71921I$	$-6.85572 - 0.93832I$
$b = 0.607737 + 1.057200I$		
$u = -0.375669 - 0.888717I$		
$a = 2.15895 - 2.52617I$	$-3.76205 - 3.93704I$	$-6.85572 + 5.02057I$
$b = 0.060199 - 0.974637I$		
$u = 0.504107$		
$a = 0.528054 + 0.820274I$	$-4.84461$	$-2.07647 + 0.I$
$b = 0.237566 - 1.254220I$		
$u = 0.504107$		
$a = 0.528054 - 0.820274I$	$-4.84461$	$-2.07647 + 0.I$
$b = 0.237566 + 1.254220I$		
$u = 0.504107$		
$a = 0.538593 + 0.918461I$	$-0.70702 - 2.82812I$	$4.45279 + 2.97945I$
$b = -0.429107 + 0.992688I$		
$u = 0.504107$		
$a = 0.538593 - 0.918461I$	$-0.70702 + 2.82812I$	$4.45279 - 2.97945I$
$b = -0.429107 - 0.992688I$		
$u = 0.504107$		
$a = -0.13998 + 1.50412I$	$-0.70702 - 2.82812I$	$4.45279 + 2.97945I$
$b = 0.608440 + 0.097206I$		
$u = 0.504107$		
$a = -0.13998 - 1.50412I$	$-0.70702 + 2.82812I$	$4.45279 - 2.97945I$
$b = 0.608440 - 0.097206I$		
$u = -0.37638 + 2.02979I$		
$a = 0.221103 + 0.952099I$	$-17.9582 - 4.1249I$	$-12.12555 + 2.15443I$
$b = -1.08899 + 2.05323I$		
$u = -0.37638 + 2.02979I$		
$a = 0.136635 + 1.070190I$	$-13.82060 - 1.29678I$	$-5.59629 - 0.82502I$
$b = 0.16428 + 1.80622I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.37638 + 2.02979I$		
$a = -0.681231 - 0.969436I$	$-17.9582 - 4.1249I$	$-12.12555 + 2.15443I$
$b = 0.46229 - 1.40963I$		
$u = -0.37638 + 2.02979I$		
$a = -0.131733 - 1.324220I$	$-13.8206 - 6.9530I$	$-5.59629 + 5.13388I$
$b = 0.14268 - 1.60991I$		
$u = -0.37638 + 2.02979I$		
$a = -0.350074 - 0.021260I$	$-13.82060 - 1.29678I$	$-5.59629 - 0.82502I$
$b = 1.075530 - 0.125738I$		
$u = -0.37638 + 2.02979I$		
$a = -0.002169 + 0.262200I$	$-13.8206 - 6.9530I$	$-5.59629 + 5.13388I$
$b = -1.85557 + 0.41527I$		
$u = -0.37638 - 2.02979I$		
$a = 0.221103 - 0.952099I$	$-17.9582 + 4.1249I$	$-12.12555 - 2.15443I$
$b = -1.08899 - 2.05323I$		
$u = -0.37638 - 2.02979I$		
$a = 0.136635 - 1.070190I$	$-13.82060 + 1.29678I$	$-5.59629 + 0.82502I$
$b = 0.16428 - 1.80622I$		
$u = -0.37638 - 2.02979I$		
$a = -0.681231 + 0.969436I$	$-17.9582 + 4.1249I$	$-12.12555 - 2.15443I$
$b = 0.46229 + 1.40963I$		
$u = -0.37638 - 2.02979I$		
$a = -0.131733 + 1.324220I$	$-13.8206 + 6.9530I$	$-5.59629 - 5.13388I$
$b = 0.14268 + 1.60991I$		
$u = -0.37638 - 2.02979I$		
$a = -0.350074 + 0.021260I$	$-13.82060 + 1.29678I$	$-5.59629 + 0.82502I$
$b = 1.075530 + 0.125738I$		
$u = -0.37638 - 2.02979I$		
$a = -0.002169 - 0.262200I$	$-13.8206 + 6.9530I$	$-5.59629 - 5.13388I$
$b = -1.85557 - 0.41527I$		

### III.

$$I_3^u = \langle 9.44 \times 10^4 u^{13} - 1.76 \times 10^5 u^{12} + \dots + 3.06 \times 10^6 b - 9.33 \times 10^5, 1.14 \times 10^7 u^{13} - 3.79 \times 10^6 u^{12} + \dots + 3.06 \times 10^6 a + 1.59 \times 10^7, u^{14} + 3u^{12} + \dots + u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -3.74249u^{13} + 1.24037u^{12} + \dots - 13.2443u - 5.21652 \\ -0.0308839u^{13} + 0.0577139u^{12} + \dots - 1.36605u + 0.305180 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2.42006u^{13} - 0.985121u^{12} + \dots + 2.65790u - 6.80147 \\ -0.316204u^{13} - 0.0156306u^{12} + \dots - 1.02247u - 0.0647390 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.65230u^{13} - 0.528076u^{12} + \dots - 3.28689u - 9.41576 \\ 0.0490374u^{13} - 0.177945u^{12} + \dots - 2.06678u - 0.528005 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3.08993u^{13} + 1.27423u^{12} + \dots - 12.9284u - 3.82414 \\ -0.0308839u^{13} + 0.0577139u^{12} + \dots - 1.36605u + 0.305180 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1.81654u^{13} - 0.773320u^{12} + \dots + 5.04060u - 5.88109 \\ -0.349611u^{13} + 0.0608824u^{12} + \dots - 0.207156u + 0.147062 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.721149u^{13} + 0.347374u^{12} + \dots - 3.07386u - 0.461186 \\ -0.0528928u^{13} + 0.242971u^{12} + \dots + 0.414713u + 0.501461 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.671228u^{13} - 0.305180u^{12} + \dots + 3.86235u + 0.615272 \\ -0.0499215u^{13} + 0.0421941u^{12} + \dots + 0.788488u + 0.154087 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.721149u^{13} + 0.347374u^{12} + \dots - 3.07386u - 0.461186 \\ -0.0499215u^{13} + 0.0421941u^{12} + \dots + 0.788488u + 0.154087 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $\frac{9599746}{3057583}u^{13} - \frac{14270512}{3057583}u^{12} + \dots + \frac{101040801}{3057583}u - \frac{56545536}{3057583}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{14} - 14u^{13} + \cdots - 5u + 1$
$c_2$	$u^{14} + 6u^{13} + \cdots - 3u + 1$
$c_3$	$u^{14} + 3u^{12} + \cdots - u + 1$
$c_4$	$u^{14} - 6u^{13} + \cdots + 3u + 1$
$c_5, c_{11}$	$u^{14} + 7u^{12} + \cdots - 3u + 1$
$c_6, c_{12}$	$u^{14} - 3u^{13} + \cdots - 6u + 1$
$c_7, c_{10}$	$u^{14} + 7u^{12} + \cdots + 3u + 1$
$c_8$	$u^{14} + 3u^{12} + \cdots + u + 1$
$c_9$	$u^{14} - 5u^{13} + \cdots + 2u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{14} - 22y^{13} + \cdots + 143y + 1$
$c_2, c_4$	$y^{14} - 14y^{13} + \cdots - 5y + 1$
$c_3, c_8$	$y^{14} + 6y^{13} + \cdots + 11y + 1$
$c_5, c_7, c_{10}$ $c_{11}$	$y^{14} + 14y^{13} + \cdots + 9y + 1$
$c_6, c_{12}$	$y^{14} - 5y^{13} + \cdots - 10y + 1$
$c_9$	$y^{14} + 5y^{13} + \cdots + 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.139126 + 0.855284I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.02309 - 2.89055I$	$-7.24127 - 0.77135I$	$-2.53833 - 3.61425I$
$b = 0.10927 - 1.56543I$		
$u = 0.139126 - 0.855284I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.02309 + 2.89055I$	$-7.24127 + 0.77135I$	$-2.53833 + 3.61425I$
$b = 0.10927 + 1.56543I$		
$u = -0.352449 + 1.175430I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.266214 + 0.045704I$	$-7.50206 - 5.05550I$	$-15.3583 + 8.9418I$
$b = -0.341781 + 0.418746I$		
$u = -0.352449 - 1.175430I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.266214 - 0.045704I$	$-7.50206 + 5.05550I$	$-15.3583 - 8.9418I$
$b = -0.341781 - 0.418746I$		
$u = 1.229090 + 0.054546I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.515481 - 0.846913I$	$0.04153 + 3.93339I$	$-9.88151 - 7.52594I$
$b = -0.262265 - 0.901818I$		
$u = 1.229090 - 0.054546I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.515481 + 0.846913I$	$0.04153 - 3.93339I$	$-9.88151 + 7.52594I$
$b = -0.262265 + 0.901818I$		
$u = 0.196848 + 0.556043I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -2.17999 - 0.00411I$	$-2.19156 + 3.21998I$	$-4.00004 - 4.18914I$
$b = -0.381345 - 0.641179I$		
$u = 0.196848 - 0.556043I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -2.17999 + 0.00411I$	$-2.19156 - 3.21998I$	$-4.00004 + 4.18914I$
$b = -0.381345 + 0.641179I$		
$u = -1.40215 + 0.37579I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.298006 - 0.417984I$	$-0.69469 - 1.77882I$	$-3.04716 + 4.98028I$
$b = -0.283501 - 1.095790I$		
$u = -1.40215 - 0.37579I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.298006 + 0.417984I$	$-0.69469 + 1.77882I$	$-3.04716 - 4.98028I$
$b = -0.283501 + 1.095790I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.229849 + 0.360057I$	$-3.49965 - 2.65520I$	$-8.3154 + 25.3017I$
$a = -9.97539 - 6.14831I$		
$b = 0.420766 - 0.730987I$		
$u = -0.229849 - 0.360057I$	$-3.49965 + 2.65520I$	$-8.3154 - 25.3017I$
$a = -9.97539 + 6.14831I$		
$b = 0.420766 + 0.730987I$		
$u = 0.41939 + 2.04733I$	$-16.7458 + 4.0257I$	$-3.85923 - 1.44990I$
$a = -0.414975 + 0.898851I$		
$b = 0.73885 + 1.60027I$		
$u = 0.41939 - 2.04733I$	$-16.7458 - 4.0257I$	$-3.85923 + 1.44990I$
$a = -0.414975 - 0.898851I$		
$b = 0.73885 - 1.60027I$		

$$\text{IV. } I_1^v = \langle a, 8v^3 - 12v^2 + b + 10v - 3, 8v^4 - 12v^3 + 12v^2 - 5v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -8v^3 + 12v^2 - 10v + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -8v^3 + 8v^2 - 8v + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -8v^3 + 12v^2 - 10v + 3 \\ -8v^3 + 8v^2 - 6v \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 8v^3 - 12v^2 + 10v - 3 \\ 16v^3 - 16v^2 + 14v - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -8v^3 + 8v^2 - 8v + 2 \\ -8v^3 + 8v^2 - 8v + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 8v^3 - 12v^2 + 12v - 5 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -8v^3 + 12v^2 - 12v + 5 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v - 1 \\ 8v^3 - 12v^2 + 12v - 5 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $72v^3 - 101v^2 + 96v - 31$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^4$
$c_3, c_8$	$u^4$
$c_4$	$(u + 1)^4$
$c_5, c_7$	$u^4 + u^2 + u + 1$
$c_6$	$u^4 - 2u^3 + 3u^2 - u + 1$
$c_9$	$u^4 + 3u^3 + 4u^2 + 3u + 2$
$c_{10}, c_{11}$	$u^4 + u^2 - u + 1$
$c_{12}$	$u^4 + 2u^3 + 3u^2 + u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_8$	$y^4$
$c_5, c_7, c_{10}$ $c_{11}$	$y^4 + 2y^3 + 3y^2 + y + 1$
$c_6, c_{12}$	$y^4 + 2y^3 + 7y^2 + 5y + 1$
$c_9$	$y^4 - y^3 + 2y^2 + 7y + 4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.447562 + 0.776246I$		
$a = 0$	$-0.66484 - 1.39709I$	$0.79646 + 4.25046I$
$b = -0.547424 + 0.585652I$		
$v = 0.447562 - 0.776246I$		
$a = 0$	$-0.66484 + 1.39709I$	$0.79646 - 4.25046I$
$b = -0.547424 - 0.585652I$		
$v = 0.302438 + 0.253422I$		
$a = 0$	$-4.26996 - 7.64338I$	$-6.9215 + 12.6814I$
$b = 0.547424 - 1.120870I$		
$v = 0.302438 - 0.253422I$		
$a = 0$	$-4.26996 + 7.64338I$	$-6.9215 - 12.6814I$
$b = 0.547424 + 1.120870I$		

$$\mathbf{V. } I_2^v = \langle a, b^6 - b^5 + 2b^4 - 2b^3 + 2b^2 - 2b + 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ b^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} b \\ b^3 + b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b^4 + b^2 + 1 \\ b^5 + 2b^3 - b^2 + 2b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b^2 + 1 \\ b^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -b^5 - 2b^3 - b + 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} b^5 + 2b^3 + b - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -b^5 - 2b^3 - b \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4b^3 + 4b - 8$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^6$
$c_3, c_8$	$u^6$
$c_4$	$(u + 1)^6$
$c_5, c_7$	$u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$
$c_6$	$u^6 - 3u^5 + 4u^4 - 2u^3 + 1$
$c_9$	$(u^3 - u^2 + 1)^2$
$c_{10}, c_{11}$	$u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$
$c_{12}$	$u^6 + 3u^5 + 4u^4 + 2u^3 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^6$
$c_3, c_8$	$y^6$
$c_5, c_7, c_{10}$ $c_{11}$	$y^6 + 3y^5 + 4y^4 + 2y^3 + 1$
$c_6, c_{12}$	$y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$
$c_9$	$(y^3 - y^2 + 2y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	$-1.91067 - 2.82812I$	$-4.49024 + 2.97945I$
$b = -0.498832 + 1.001300I$		
$v = -1.00000$		
$a = 0$	$-1.91067 + 2.82812I$	$-4.49024 - 2.97945I$
$b = -0.498832 - 1.001300I$		
$v = -1.00000$		
$a = 0$	$-6.04826$	$-11.01951 + 0.I$
$b = 0.284920 + 1.115140I$		
$v = -1.00000$		
$a = 0$	$-6.04826$	$-11.01951 + 0.I$
$b = 0.284920 - 1.115140I$		
$v = -1.00000$		
$a = 0$	$-1.91067 - 2.82812I$	$-4.49024 + 2.97945I$
$b = 0.713912 + 0.305839I$		
$v = -1.00000$		
$a = 0$	$-1.91067 + 2.82812I$	$-4.49024 - 2.97945I$
$b = 0.713912 - 0.305839I$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^{10}(u^5 + 8u^4 + 22u^3 + 25u^2 + 15u + 1)^6$ $\cdot (u^{14} - 14u^{13} + \dots - 5u + 1)(u^{25} + 25u^{24} + \dots - 39680u + 4096)$
$c_2$	$((u - 1)^{10})(u^5 - 2u^4 + \dots + 3u - 1)^6(u^{14} + 6u^{13} + \dots - 3u + 1)$ $\cdot (u^{25} - 5u^{24} + \dots - 272u + 64)$
$c_3$	$u^{10}(u^5 - u^4 + \dots + 2u + 2)^6(u^{14} + 3u^{12} + \dots - u + 1)$ $\cdot (u^{25} + 7u^{24} + \dots - 768u + 1024)$
$c_4$	$((u + 1)^{10})(u^5 - 2u^4 + \dots + 3u - 1)^6(u^{14} - 6u^{13} + \dots + 3u + 1)$ $\cdot (u^{25} - 5u^{24} + \dots - 272u + 64)$
$c_5$	$(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{14} + 7u^{12} + \dots - 3u + 1)(u^{25} + 16u^{23} + \dots - 4u - 1)$ $\cdot (u^{30} - 2u^{29} + \dots + 4896u + 1161)$
$c_6$	$(u^4 - 2u^3 + 3u^2 - u + 1)(u^6 - 3u^5 + 4u^4 - 2u^3 + 1)$ $\cdot (u^{14} - 3u^{13} + \dots - 6u + 1)(u^{25} - u^{24} + \dots - 3u - 1)$ $\cdot (u^{30} - 6u^{29} + \dots - 2892u + 367)$
$c_7$	$(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{14} + 7u^{12} + \dots + 3u + 1)(u^{25} + 16u^{23} + \dots - 4u - 1)$ $\cdot (u^{30} - 2u^{29} + \dots + 4896u + 1161)$
$c_8$	$u^{10}(u^5 - u^4 + \dots + 2u + 2)^6(u^{14} + 3u^{12} + \dots + u + 1)$ $\cdot (u^{25} + 7u^{24} + \dots - 768u + 1024)$
$c_9$	$(u^3 - u^2 + 1)^2(u^3 + u^2 - 1)^{10}(u^4 + 3u^3 + 4u^2 + 3u + 2)$ $\cdot (u^{14} - 5u^{13} + \dots + 2u^2 + 1)(u^{25} - 17u^{24} + \dots + 304u - 32)$
$c_{10}$	$(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{14} + 7u^{12} + \dots + 3u + 1)(u^{25} + 16u^{23} + \dots - 4u - 1)$ $\cdot (u^{30} - 2u^{29} + \dots + 4896u + 1161)$
$c_{11}$	$(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{14} + 7u^{12} + \dots - 3u + 1)(u^{25} + 16u^{23} + \dots - 4u - 1)$ $\cdot (u^{30} - 2u^{29} + \dots + 4896u + 1161)$
$c_{12}$	$(u^4 + 2u^3 + 3u^2 + u + 1)^{27}(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)$ $\cdot (u^{14} - 3u^{13} + \dots - 6u + 1)(u^{25} - u^{24} + \dots - 3u - 1)$ $\cdot (u^{30} - 6u^{29} + \dots - 2892u + 367)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^{10}(y^5 - 20y^4 + 114y^3 + 19y^2 + 175y - 1)^6$ $\cdot (y^{14} - 22y^{13} + \dots + 143y + 1)$ $\cdot (y^{25} - 45y^{24} + \dots + 260374528y - 16777216)$
$c_2, c_4$	$(y - 1)^{10}(y^5 - 8y^4 + 22y^3 - 25y^2 + 15y - 1)^6$ $\cdot (y^{14} - 14y^{13} + \dots - 5y + 1)(y^{25} - 25y^{24} + \dots - 39680y - 4096)$
$c_3, c_8$	$y^{10}(y^5 + 9y^4 + \dots + 8y - 4)^6(y^{14} + 6y^{13} + \dots + 11y + 1)$ $\cdot (y^{25} + 15y^{24} + \dots + 3473408y - 1048576)$
$c_5, c_7, c_{10}$ $c_{11}$	$(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{14} + 14y^{13} + \dots + 9y + 1)(y^{25} + 32y^{24} + \dots + 6y - 1)$ $\cdot (y^{30} + 30y^{29} + \dots + 10260108y + 1347921)$
$c_6, c_{12}$	$(y^4 + 2y^3 + 7y^2 + 5y + 1)(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)$ $\cdot (y^{14} - 5y^{13} + \dots - 10y + 1)(y^{25} - 19y^{24} + \dots - 27y - 1)$ $\cdot (y^{30} - 10y^{29} + \dots - 2032180y + 134689)$
$c_9$	$((y^3 - y^2 + 2y - 1)^{12})(y^4 - y^3 + 2y^2 + 7y + 4)(y^{14} + 5y^{13} + \dots + 4y + 1)$ $\cdot (y^{25} + 3y^{24} + \dots + 6912y - 1024)$