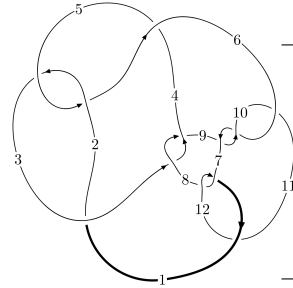
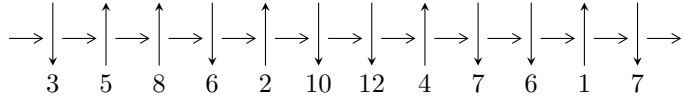


12n₀₂₆₉ (K12n₀₂₆₉)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$2,6 \xrightarrow{c_5} 5 \xrightarrow{c_2} 3 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4,11 \xrightarrow{c_{10}} 10 \xrightarrow{c_6} 7 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \Rightarrow c_3, c_7, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 6075798104u^{29} - 20035573492u^{28} + \dots + 94573295142b - 102785752178, \\ 52900187657u^{29} - 66435815226u^{28} + \dots + 189146590284a - 100941534777, \\ u^{30} - 2u^{29} + \dots - 11u + 4 \rangle$$

$$I_2^u = \langle 3u^{18}a - 3u^{18} + \dots - a - 1, 2u^{18} - 3u^{17} + \dots - 4a + 5, u^{19} - u^{18} + \dots + 2u + 1 \rangle$$

$$I_3^u = \langle -u^3 + au - u^2 + b + 1, -2u^3a - 4u^2a + u^3 + a^2 - 4au - 2u^2 - 4u - 5, u^4 + u^3 + u^2 + 1 \rangle$$

$$I_4^u = \langle b - 1, 2a + 2u + 1, u^2 - u + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 78 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 6.08 \times 10^9 u^{29} - 2.00 \times 10^{10} u^{28} + \dots + 9.46 \times 10^{10} b - 1.03 \times 10^{11}, 5.29 \times 10^{10} u^{29} - 6.64 \times 10^{10} u^{28} + \dots + 1.89 \times 10^{11} a - 1.01 \times 10^{11}, u^{30} - 2u^{29} + \dots - 11u + 4 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.279678u^{29} + 0.351240u^{28} + \dots - 2.48757u + 0.533668 \\ -0.0642443u^{29} + 0.211852u^{28} + \dots - 0.962626u + 1.08684 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.343923u^{29} + 0.563092u^{28} + \dots - 3.45020u + 1.62051 \\ -0.0642443u^{29} + 0.211852u^{28} + \dots - 0.962626u + 1.08684 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.293504u^{29} + 0.578779u^{28} + \dots - 3.77569u + 2.01661 \\ -0.0196924u^{29} + 0.238501u^{28} + \dots - 1.68736u + 1.14206 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.642162u^{29} + 1.14610u^{28} + \dots - 7.29055u + 2.93572 \\ -0.0853310u^{29} + 0.458919u^{28} + \dots - 2.98810u + 2.09785 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.565573u^{29} + 1.10421u^{28} + \dots - 7.29137u + 2.70821 \\ -0.0269374u^{29} + 0.494525u^{28} + \dots - 3.51309u + 2.26229 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.298240u^{29} + 0.583012u^{28} + \dots - 3.84035u + 1.31521 \\ -0.0210866u^{29} + 0.247066u^{28} + \dots - 1.02547u + 1.01102 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{13126781461}{15762215857} u^{29} - \frac{346887419065}{189146590284} u^{28} + \dots + \frac{2455780116659}{189146590284} u - \frac{364257663059}{47286647571}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^{30} + 10u^{29} + \dots - u + 16$
c_2, c_5	$u^{30} + 2u^{29} + \dots + 11u + 4$
c_3, c_8	$u^{30} - 3u^{29} + \dots + 24u + 32$
c_6, c_7, c_9 c_{10}, c_{12}	$u^{30} + 2u^{29} + \dots - u + 1$
c_{11}	$u^{30} - 8u^{29} + \dots - 15u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^{30} + 22y^{29} + \cdots + 3743y + 256$
c_2, c_5	$y^{30} + 10y^{29} + \cdots - y + 16$
c_3, c_8	$y^{30} - 15y^{29} + \cdots - 6336y + 1024$
c_6, c_7, c_9 c_{10}, c_{12}	$y^{30} + 8y^{29} + \cdots + 15y + 1$
c_{11}	$y^{30} + 24y^{29} + \cdots + 19y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.460643 + 0.958497I$		
$a = 1.032200 - 0.246838I$	$-0.32179 - 2.57657I$	$1.59153 + 5.16266I$
$b = -0.299080 - 0.268098I$		
$u = -0.460643 - 0.958497I$		
$a = 1.032200 + 0.246838I$	$-0.32179 + 2.57657I$	$1.59153 - 5.16266I$
$b = -0.299080 + 0.268098I$		
$u = 0.117766 + 1.065450I$		
$a = -2.08067 + 0.32615I$	$-5.22441 + 3.04204I$	$-6.16892 - 2.76702I$
$b = 0.868345 - 0.853291I$		
$u = 0.117766 - 1.065450I$		
$a = -2.08067 - 0.32615I$	$-5.22441 - 3.04204I$	$-6.16892 + 2.76702I$
$b = 0.868345 + 0.853291I$		
$u = 0.892544 + 0.608188I$		
$a = 0.357885 - 0.459993I$	$3.48880 - 10.37700I$	$3.38979 + 5.72342I$
$b = -0.660894 - 1.208280I$		
$u = 0.892544 - 0.608188I$		
$a = 0.357885 + 0.459993I$	$3.48880 + 10.37700I$	$3.38979 - 5.72342I$
$b = -0.660894 + 1.208280I$		
$u = -0.835530 + 0.693005I$		
$a = -0.118947 - 0.761630I$	$1.29700 + 3.10575I$	$1.45147 - 3.18731I$
$b = 0.596590 - 0.966034I$		
$u = -0.835530 - 0.693005I$		
$a = -0.118947 + 0.761630I$	$1.29700 - 3.10575I$	$1.45147 + 3.18731I$
$b = 0.596590 + 0.966034I$		
$u = 0.513340 + 0.739634I$		
$a = -1.14053 - 0.97145I$	$-1.57253 + 1.48061I$	$1.51311 + 5.82808I$
$b = 1.145550 - 0.289264I$		
$u = 0.513340 - 0.739634I$		
$a = -1.14053 + 0.97145I$	$-1.57253 - 1.48061I$	$1.51311 - 5.82808I$
$b = 1.145550 + 0.289264I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.850935 + 0.293187I$ $a = 0.444169 - 0.489109I$ $b = -0.601963 - 1.009720I$	$1.66857 - 6.29086I$	$3.10303 + 6.83080I$
$u = -0.850935 - 0.293187I$ $a = 0.444169 + 0.489109I$ $b = -0.601963 + 1.009720I$	$1.66857 + 6.29086I$	$3.10303 - 6.83080I$
$u = 0.590492 + 0.982207I$ $a = -0.644113 - 1.170090I$ $b = 1.149850 + 0.591978I$	$-2.48088 + 3.02207I$	$-2.21456 - 6.76782I$
$u = 0.590492 - 0.982207I$ $a = -0.644113 + 1.170090I$ $b = 1.149850 - 0.591978I$	$-2.48088 - 3.02207I$	$-2.21456 + 6.76782I$
$u = -0.120227 + 1.185320I$ $a = 1.71764 + 0.85667I$ $b = -0.727551 - 1.085270I$	$-3.53890 - 9.16679I$	$-2.72882 + 7.28806I$
$u = -0.120227 - 1.185320I$ $a = 1.71764 - 0.85667I$ $b = -0.727551 + 1.085270I$	$-3.53890 + 9.16679I$	$-2.72882 - 7.28806I$
$u = -0.537667 + 0.602506I$ $a = 0.295236 + 0.519101I$ $b = 0.023047 + 0.423163I$	$0.81059 - 1.39109I$	$1.55512 + 4.14990I$
$u = -0.537667 - 0.602506I$ $a = 0.295236 - 0.519101I$ $b = 0.023047 - 0.423163I$	$0.81059 + 1.39109I$	$1.55512 - 4.14990I$
$u = -0.530973 + 1.119350I$ $a = 0.144119 - 0.924498I$ $b = -0.645054 + 0.883761I$	$-0.91910 + 1.29166I$	$-0.69831 - 3.06877I$
$u = -0.530973 - 1.119350I$ $a = 0.144119 + 0.924498I$ $b = -0.645054 - 0.883761I$	$-0.91910 - 1.29166I$	$-0.69831 + 3.06877I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.730890 + 1.026770I$ $a = -1.64352 + 1.06510I$ $b = 0.646060 + 1.041760I$	$0.26873 - 8.97735I$	$0.28174 + 7.42318I$
$u = -0.730890 - 1.026770I$ $a = -1.64352 - 1.06510I$ $b = 0.646060 - 1.041760I$	$0.26873 + 8.97735I$	$0.28174 - 7.42318I$
$u = 0.896688 + 0.897515I$ $a = 0.544249 + 0.743729I$ $b = -0.269532 + 0.876061I$	$9.52166 + 4.35690I$	$1.93733 - 9.19475I$
$u = 0.896688 - 0.897515I$ $a = 0.544249 - 0.743729I$ $b = -0.269532 - 0.876061I$	$9.52166 - 4.35690I$	$1.93733 + 9.19475I$
$u = 0.875554 + 0.943207I$ $a = -0.406635 - 0.439577I$ $b = -0.231064 - 0.841743I$	$9.37686 + 2.17701I$	$0.69666 + 4.17919I$
$u = 0.875554 - 0.943207I$ $a = -0.406635 + 0.439577I$ $b = -0.231064 + 0.841743I$	$9.37686 - 2.17701I$	$0.69666 - 4.17919I$
$u = 0.719689 + 1.077380I$ $a = 2.03341 + 0.65165I$ $b = -0.70309 + 1.23931I$	$2.0453 + 16.3438I$	$1.41001 - 9.88978I$
$u = 0.719689 - 1.077380I$ $a = 2.03341 - 0.65165I$ $b = -0.70309 - 1.23931I$	$2.0453 - 16.3438I$	$1.41001 + 9.88978I$
$u = 0.460792 + 0.211623I$ $a = -0.159496 - 1.172690I$ $b = 0.708800 - 0.487048I$	$-1.26041 + 1.13919I$	$-3.24420 - 2.21188I$
$u = 0.460792 - 0.211623I$ $a = -0.159496 + 1.172690I$ $b = 0.708800 + 0.487048I$	$-1.26041 - 1.13919I$	$-3.24420 + 2.21188I$

II.

$$I_2^u = \langle 3u^{18}a - 3u^{18} + \dots - a - 1, 2u^{18} - 3u^{17} + \dots - 4a + 5, u^{19} - u^{18} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -\frac{3}{2}u^{18}a + \frac{3}{2}u^{18} + \dots + \frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{3}{2}u^{18}a + \frac{3}{2}u^{18} + \dots + \frac{3}{2}a + \frac{1}{2} \\ -\frac{3}{2}u^{18}a + \frac{3}{2}u^{18} + \dots + \frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2u^{17}a - u^{17} + \dots - a + 4 \\ \frac{3}{2}u^{18}a - \frac{3}{2}u^{18} + \dots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{13} - 2u^{11} - 3u^9 - 2u^7 + u \\ -u^{15} - 3u^{13} - 6u^{11} - 7u^9 - 6u^7 - 4u^5 - 2u^3 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{18} + 3u^{16} + 6u^{14} + 7u^{12} + 5u^{10} + 3u^8 - u^2 - 1 \\ u^{18} - u^{17} + \dots - 3u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^{18}a + \frac{3}{2}u^{18} + \dots + \frac{1}{2}a - \frac{1}{2} \\ -2u^{18}a + 3u^{18} + \dots + au - 4u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^{17} + 4u^{16} - 12u^{15} + 12u^{14} - 28u^{13} + 24u^{12} - 36u^{11} + 32u^{10} - 36u^9 + 28u^8 - 28u^7 + 28u^6 - 12u^5 + 16u^4 - 12u^3 + 12u^2 + 4u + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$(u^{19} + 7u^{18} + \dots + 2u - 1)^2$
c_2, c_5	$(u^{19} + u^{18} + \dots + 2u - 1)^2$
c_3, c_8	$(u^{19} + u^{18} + \dots - u^2 + 1)^2$
c_6, c_7, c_9 c_{10}, c_{12}	$u^{38} - 5u^{37} + \dots - 173u + 34$
c_{11}	$u^{38} - 19u^{37} + \dots - 13387u + 1156$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$(y^{19} + 11y^{18} + \dots + 42y - 1)^2$
c_2, c_5	$(y^{19} + 7y^{18} + \dots + 2y - 1)^2$
c_3, c_8	$(y^{19} - 5y^{18} + \dots + 2y - 1)^2$
c_6, c_7, c_9 c_{10}, c_{12}	$y^{38} + 19y^{37} + \dots + 13387y + 1156$
c_{11}	$y^{38} - y^{37} + \dots + 7530783y + 1336336$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.787239 + 0.559366I$ $a = 0.516479 + 0.470519I$ $b = -0.991761 + 0.337645I$	$0.85217 - 4.39903I$	$0.93348 + 2.80289I$
$u = 0.787239 + 0.559366I$ $a = -0.195675 + 0.232139I$ $b = 0.689098 + 1.130990I$	$0.85217 - 4.39903I$	$0.93348 + 2.80289I$
$u = 0.787239 - 0.559366I$ $a = 0.516479 - 0.470519I$ $b = -0.991761 - 0.337645I$	$0.85217 + 4.39903I$	$0.93348 - 2.80289I$
$u = 0.787239 - 0.559366I$ $a = -0.195675 - 0.232139I$ $b = 0.689098 - 1.130990I$	$0.85217 + 4.39903I$	$0.93348 - 2.80289I$
$u = 0.709462 + 0.766103I$ $a = 0.585393 + 0.482577I$ $b = -0.678167 - 0.996758I$	$6.91199 - 0.16816I$	$6.16829 + 0.91431I$
$u = 0.709462 + 0.766103I$ $a = 1.214050 + 0.700043I$ $b = -0.19863 + 1.44121I$	$6.91199 - 0.16816I$	$6.16829 + 0.91431I$
$u = 0.709462 - 0.766103I$ $a = 0.585393 - 0.482577I$ $b = -0.678167 + 0.996758I$	$6.91199 + 0.16816I$	$6.16829 - 0.91431I$
$u = 0.709462 - 0.766103I$ $a = 1.214050 - 0.700043I$ $b = -0.19863 - 1.44121I$	$6.91199 + 0.16816I$	$6.16829 - 0.91431I$
$u = -0.588600 + 0.865037I$ $a = -0.49489 - 2.57683I$ $b = 0.138356 - 1.097670I$	$3.75823 - 2.32534I$	$-1.72826 + 3.09456I$
$u = -0.588600 + 0.865037I$ $a = -3.97835 + 1.04025I$ $b = 0.197824 + 0.975432I$	$3.75823 - 2.32534I$	$-1.72826 + 3.09456I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.588600 - 0.865037I$ $a = -0.49489 + 2.57683I$ $b = 0.138356 + 1.097670I$	$3.75823 + 2.32534I$	$-1.72826 - 3.09456I$
$u = -0.588600 - 0.865037I$ $a = -3.97835 - 1.04025I$ $b = 0.197824 - 0.975432I$	$3.75823 + 2.32534I$	$-1.72826 - 3.09456I$
$u = -0.745489 + 0.500016I$ $a = 0.352472 + 0.544649I$ $b = -0.564915 + 0.608349I$	$0.45606 - 1.53005I$	$0.20605 + 2.54963I$
$u = -0.745489 + 0.500016I$ $a = -0.147251 + 0.364183I$ $b = 0.536858 + 0.708989I$	$0.45606 - 1.53005I$	$0.20605 + 2.54963I$
$u = -0.745489 - 0.500016I$ $a = 0.352472 - 0.544649I$ $b = -0.564915 - 0.608349I$	$0.45606 + 1.53005I$	$0.20605 - 2.54963I$
$u = -0.745489 - 0.500016I$ $a = -0.147251 - 0.364183I$ $b = 0.536858 - 0.708989I$	$0.45606 + 1.53005I$	$0.20605 - 2.54963I$
$u = -0.021471 + 1.128170I$ $a = -1.52252 - 1.09613I$ $b = 0.800008 + 0.907616I$	$-5.01775 - 3.11880I$	$-5.58624 + 2.69239I$
$u = -0.021471 + 1.128170I$ $a = 1.81596 - 0.53999I$ $b = -0.913287 + 0.607157I$	$-5.01775 - 3.11880I$	$-5.58624 + 2.69239I$
$u = -0.021471 - 1.128170I$ $a = -1.52252 + 1.09613I$ $b = 0.800008 - 0.907616I$	$-5.01775 + 3.11880I$	$-5.58624 - 2.69239I$
$u = -0.021471 - 1.128170I$ $a = 1.81596 + 0.53999I$ $b = -0.913287 - 0.607157I$	$-5.01775 + 3.11880I$	$-5.58624 - 2.69239I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.167515 + 0.839557I$ $a = 0.857565 - 0.800159I$ $b = -0.003570 + 1.177280I$	$1.87881 - 1.72326I$	$-3.81965 + 5.18112I$
$u = -0.167515 + 0.839557I$ $a = 0.78439 + 2.81455I$ $b = -0.197548 - 0.604455I$	$1.87881 - 1.72326I$	$-3.81965 + 5.18112I$
$u = -0.167515 - 0.839557I$ $a = 0.857565 + 0.800159I$ $b = -0.003570 - 1.177280I$	$1.87881 + 1.72326I$	$-3.81965 - 5.18112I$
$u = -0.167515 - 0.839557I$ $a = 0.78439 - 2.81455I$ $b = -0.197548 + 0.604455I$	$1.87881 + 1.72326I$	$-3.81965 - 5.18112I$
$u = 0.687512 + 0.928828I$ $a = -0.992722 - 0.197204I$ $b = -0.09297 - 1.48296I$	$6.41945 + 5.52702I$	$4.42794 - 7.00248I$
$u = 0.687512 + 0.928828I$ $a = 1.93781 + 0.22445I$ $b = -0.765375 + 0.868851I$	$6.41945 + 5.52702I$	$4.42794 - 7.00248I$
$u = 0.687512 - 0.928828I$ $a = -0.992722 + 0.197204I$ $b = -0.09297 + 1.48296I$	$6.41945 - 5.52702I$	$4.42794 + 7.00248I$
$u = 0.687512 - 0.928828I$ $a = 1.93781 - 0.22445I$ $b = -0.765375 - 0.868851I$	$6.41945 - 5.52702I$	$4.42794 + 7.00248I$
$u = -0.636878 + 1.050560I$ $a = -0.005727 + 0.813937I$ $b = 0.717895 - 0.570311I$	$-1.12421 - 3.71612I$	$-2.19900 + 2.45937I$
$u = -0.636878 + 1.050560I$ $a = 1.69165 - 0.73976I$ $b = -0.636967 - 0.819328I$	$-1.12421 - 3.71612I$	$-2.19900 + 2.45937I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.636878 - 1.050560I$		
$a = -0.005727 - 0.813937I$	$-1.12421 + 3.71612I$	$-2.19900 - 2.45937I$
$b = 0.717895 + 0.570311I$		
$u = -0.636878 - 1.050560I$		
$a = 1.69165 + 0.73976I$	$-1.12421 + 3.71612I$	$-2.19900 - 2.45937I$
$b = -0.636967 + 0.819328I$		
$u = 0.666721 + 1.052350I$		
$a = 0.652896 + 1.081010I$	$-0.60648 + 9.88550I$	$-1.13872 - 7.31129I$
$b = -1.105990 - 0.392926I$		
$u = 0.666721 + 1.052350I$		
$a = -2.00964 - 0.51551I$	$-0.60648 + 9.88550I$	$-1.13872 - 7.31129I$
$b = 0.792055 - 1.166900I$		
$u = 0.666721 - 1.052350I$		
$a = 0.652896 - 1.081010I$	$-0.60648 - 9.88550I$	$-1.13872 + 7.31129I$
$b = -1.105990 + 0.392926I$		
$u = 0.666721 - 1.052350I$		
$a = -2.00964 + 0.51551I$	$-0.60648 - 9.88550I$	$-1.13872 + 7.31129I$
$b = 0.792055 + 1.166900I$		
$u = -0.381963$		
$a = 2.43810 + 0.93795I$	4.19724	7.47220
$b = -0.222910 - 1.071950I$		
$u = -0.381963$		
$a = 2.43810 - 0.93795I$	4.19724	7.47220
$b = -0.222910 + 1.071950I$		

$$\text{III. } I_3^u = \langle -u^3 + au - u^2 + b + 1, -2u^3a + u^3 + \dots + a^2 - 5, u^4 + u^3 + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^3 + u^2 + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ u^3 - au + u^2 - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 - au + u^2 + a - 1 \\ u^3 - au + u^2 - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3a - u^2a - 3u^3 - 5u^2 + a - 5u - 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 - au + u^2 - 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3a - u^2a - a - 1 \\ -u^2a + au - a + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 + a \\ 2u^3 - au + 2u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4u^2 - 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
c_2	$(u^4 - u^3 + u^2 + 1)^2$
c_3, c_8	$u^8 - 5u^6 + 7u^4 - 2u^2 + 1$
c_5	$(u^4 + u^3 + u^2 + 1)^2$
c_6, c_7, c_9 c_{10}, c_{12}	$(u^2 + 1)^4$
c_{11}	$(u + 1)^8$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
c_2, c_5	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$
c_3, c_8	$(y^4 - 5y^3 + 7y^2 - 2y + 1)^2$
c_6, c_7, c_9 c_{10}, c_{12}	$(y + 1)^8$
c_{11}	$(y - 1)^8$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.351808 + 0.720342I$ $a = -1.71161 + 1.80064I$ $b = 1.000000I$	$3.07886 + 1.41510I$	$4.17326 - 4.90874I$
$u = 0.351808 + 0.720342I$ $a = 0.53013 + 2.89548I$ $b = -1.000000I$	$3.07886 + 1.41510I$	$4.17326 - 4.90874I$
$u = 0.351808 - 0.720342I$ $a = -1.71161 - 1.80064I$ $b = -1.000000I$	$3.07886 - 1.41510I$	$4.17326 + 4.90874I$
$u = 0.351808 - 0.720342I$ $a = 0.53013 - 2.89548I$ $b = 1.000000I$	$3.07886 - 1.41510I$	$4.17326 + 4.90874I$
$u = -0.851808 + 0.911292I$ $a = -0.994913 + 0.491876I$ $b = 1.000000I$	$10.08060 - 3.16396I$	$7.82674 + 2.56480I$
$u = -0.851808 + 0.911292I$ $a = 0.176391 - 0.602971I$ $b = -1.000000I$	$10.08060 - 3.16396I$	$7.82674 + 2.56480I$
$u = -0.851808 - 0.911292I$ $a = -0.994913 - 0.491876I$ $b = -1.000000I$	$10.08060 + 3.16396I$	$7.82674 - 2.56480I$
$u = -0.851808 - 0.911292I$ $a = 0.176391 + 0.602971I$ $b = 1.000000I$	$10.08060 + 3.16396I$	$7.82674 - 2.56480I$

$$\text{IV. } I_4^u = \langle b - 1, 2a + 2u + 1, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u - \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u + \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u + \frac{3}{2} \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u + 2 \\ 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2u + 2 \\ 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u + \frac{1}{2} \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-\frac{31}{4}u + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_5	$u^2 - u + 1$
c_2	$u^2 + u + 1$
c_3, c_8	u^2
c_6, c_7, c_{11}	$(u - 1)^2$
c_9, c_{10}, c_{12}	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5	$y^2 + y + 1$
c_3, c_8	y^2
c_6, c_7, c_9 c_{10}, c_{11}, c_{12}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -1.000000 - 0.866025I$ $b = 1.000000$	$-1.64493 + 2.02988I$	$-1.87500 - 6.71170I$
$u = 0.500000 - 0.866025I$ $a = -1.000000 + 0.866025I$ $b = 1.000000$	$-1.64493 - 2.02988I$	$-1.87500 + 6.71170I$

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_4	$(u^2 - u + 1)(u^4 - u^3 + 3u^2 - 2u + 1)^2(u^{19} + 7u^{18} + \dots + 2u - 1)^2$ $\cdot (u^{30} + 10u^{29} + \dots - u + 16)$
c_2	$(u^2 + u + 1)(u^4 - u^3 + u^2 + 1)^2(u^{19} + u^{18} + \dots + 2u - 1)^2$ $\cdot (u^{30} + 2u^{29} + \dots + 11u + 4)$
c_3, c_8	$u^2(u^8 - 5u^6 + \dots - 2u^2 + 1)(u^{19} + u^{18} + \dots - u^2 + 1)^2$ $\cdot (u^{30} - 3u^{29} + \dots + 24u + 32)$
c_5	$(u^2 - u + 1)(u^4 + u^3 + u^2 + 1)^2(u^{19} + u^{18} + \dots + 2u - 1)^2$ $\cdot (u^{30} + 2u^{29} + \dots + 11u + 4)$
c_6, c_7	$((u - 1)^2)(u^2 + 1)^4(u^{30} + 2u^{29} + \dots - u + 1)$ $\cdot (u^{38} - 5u^{37} + \dots - 173u + 34)$
c_9, c_{10}, c_{12}	$((u + 1)^2)(u^2 + 1)^4(u^{30} + 2u^{29} + \dots - u + 1)$ $\cdot (u^{38} - 5u^{37} + \dots - 173u + 34)$
c_{11}	$((u - 1)^2)(u + 1)^8(u^{30} - 8u^{29} + \dots - 15u + 1)$ $\cdot (u^{38} - 19u^{37} + \dots - 13387u + 1156)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$(y^2 + y + 1)(y^4 + 5y^3 + \dots + 2y + 1)^2(y^{19} + 11y^{18} + \dots + 42y - 1)^2$ $\cdot (y^{30} + 22y^{29} + \dots + 3743y + 256)$
c_2, c_5	$(y^2 + y + 1)(y^4 + y^3 + 3y^2 + 2y + 1)^2(y^{19} + 7y^{18} + \dots + 2y - 1)^2$ $\cdot (y^{30} + 10y^{29} + \dots - y + 16)$
c_3, c_8	$y^2(y^4 - 5y^3 + \dots - 2y + 1)^2(y^{19} - 5y^{18} + \dots + 2y - 1)^2$ $\cdot (y^{30} - 15y^{29} + \dots - 6336y + 1024)$
c_6, c_7, c_9 c_{10}, c_{12}	$((y - 1)^2)(y + 1)^8(y^{30} + 8y^{29} + \dots + 15y + 1)$ $\cdot (y^{38} + 19y^{37} + \dots + 13387y + 1156)$
c_{11}	$((y - 1)^{10})(y^{30} + 24y^{29} + \dots + 19y + 1)$ $\cdot (y^{38} - y^{37} + \dots + 7530783y + 1336336)$