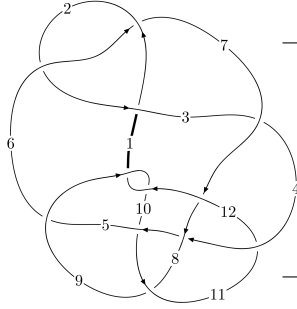
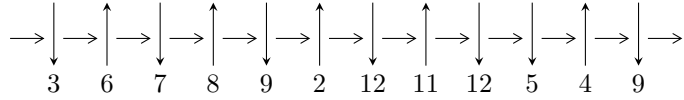


12n<sub>0283</sub> (K12n<sub>0283</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,8 \xrightarrow{c_4} 5,11 \xrightarrow{c_8} 9 \xrightarrow{c_5} 6 \xrightarrow{c_{11}} 12 \xrightarrow{c_{12}} 1 \xrightarrow{c_7} 7 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_{10}} 10 \twoheadrightarrow c_1, c_6, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle b - u, -3.85888 \times 10^{16}u^{31} + 4.26003 \times 10^{16}u^{30} + \dots + 3.07647 \times 10^{15}a - 2.04981 \times 10^{16}, \\ u^{32} - u^{31} + \dots + 13u^2 + 1 \rangle$$

$$I_2^u = \langle b + u, 3u^{16} - 3u^{15} + \dots + a - 1, \\ u^{17} - u^{16} - u^{15} + 2u^{14} + 4u^{13} - 6u^{12} - 3u^{11} + 8u^{10} + 5u^9 - 11u^8 - 2u^7 + 10u^6 + 2u^5 - 7u^4 - u^3 + 4u^2 - 1 \rangle$$

$$I_3^u = \langle -1.04996 \times 10^{43}u^{31} + 4.71287 \times 10^{42}u^{30} + \dots + 1.47931 \times 10^{44}b - 3.76971 \times 10^{43}, \\ 3.26424 \times 10^{44}u^{31} - 3.75981 \times 10^{44}u^{30} + \dots + 2.51482 \times 10^{45}a + 1.97058 \times 10^{44}, u^{32} - 2u^{31} + \dots - 3u + 1 \rangle$$

$$I_4^u = \langle -u^3 + u^2 + b - 3u + 1, a, u^4 - u^3 + 3u^2 - u + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 85 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, -3.86 \times 10^{16} u^{31} + 4.26 \times 10^{16} u^{30} + \dots + 3.08 \times 10^{15} a - 2.05 \times 10^{16}, u^{32} - u^{31} + \dots + 13u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 12.5432u^{31} - 13.8471u^{30} + \dots + 13.5866u + 6.66287 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -16.8410u^{31} + 25.7996u^{30} + \dots - 50.1828u + 26.0290 \\ -6.20203u^{31} + 7.81804u^{30} + \dots - 11.5432u + 1.30392 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -14.3847u^{31} + 10.0771u^{30} + \dots - 25.7395u - 5.74332 \\ -4.59634u^{31} + 4.24837u^{30} + \dots - 16.7216u - 4.58421 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 12.5432u^{31} - 13.8471u^{30} + \dots + 14.5866u + 6.66287 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 16.0624u^{31} - 21.2113u^{30} + \dots + 41.6901u - 20.5255 \\ 2.18153u^{31} - 4.28474u^{30} + \dots + 13.9678u - 8.31557 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -29.2451u^{31} + 41.4357u^{30} + \dots - 75.2692u + 28.6368 \\ -6.20203u^{31} + 7.81804u^{30} + \dots - 11.5432u + 1.30392 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2.97045u^{31} - 12.5885u^{30} + \dots + 19.9046u - 19.7914 \\ 1.28508u^{31} - 4.38219u^{30} + \dots + 9.58280u - 4.01243 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4.67800u^{31} - 35.4901u^{30} + \dots - 6.88392u - 73.8593 \\ 5.30418u^{31} - 11.1266u^{30} + \dots + 18.0833u - 20.0632 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 6.34118u^{31} - 6.02908u^{30} + \dots + 2.04336u + 7.96679 \\ -2.32875u^{31} + 3.30173u^{30} + \dots - 5.20203u + 1.61602 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{137669939372982157}{3076468870904633} u^{31} - \frac{10255547182342868}{3076468870904633} u^{30} + \dots + \frac{105136250462441589}{3076468870904633} u + \frac{471315500834574952}{3076468870904633}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{32} + 19u^{31} + \dots + 7u + 16$
$c_2, c_6$	$u^{32} - 5u^{31} + \dots - 7u + 4$
$c_3$	$u^{32} + 5u^{31} + \dots + 89u + 4$
$c_4, c_{11}$	$u^{32} - u^{31} + \dots + 13u^2 + 1$
$c_5$	$u^{32} - 32u^{30} + \dots + u + 1$
$c_7$	$u^{32} + 35u^{31} + \dots + 147456u + 16384$
$c_8$	$u^{32} + 22u^{31} + \dots + 21u + 2$
$c_9, c_{12}$	$u^{32} + 2u^{31} + \dots - 17u + 1$
$c_{10}$	$u^{32} - 12u^{30} + \dots - 17u + 17$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{32} - 9y^{31} + \dots - 1425y + 256$
$c_2, c_6$	$y^{32} + 19y^{31} + \dots + 7y + 16$
$c_3$	$y^{32} - 37y^{31} + \dots - 3673y + 16$
$c_4, c_{11}$	$y^{32} + 13y^{31} + \dots + 26y + 1$
$c_5$	$y^{32} - 64y^{31} + \dots + 3y + 1$
$c_7$	$y^{32} - 17y^{31} + \dots + 3623878656y + 268435456$
$c_8$	$y^{32} + 60y^{30} + \dots + 19y + 4$
$c_9, c_{12}$	$y^{32} - 60y^{31} + \dots - 9y + 1$
$c_{10}$	$y^{32} - 24y^{31} + \dots - 5117y + 289$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.800209 + 0.679293I$		
$a = -0.512896 - 0.056292I$	$1.24992 + 2.03308I$	$-1.46651 - 1.63420I$
$b = 0.800209 + 0.679293I$		
$u = 0.800209 - 0.679293I$		
$a = -0.512896 + 0.056292I$	$1.24992 - 2.03308I$	$-1.46651 + 1.63420I$
$b = 0.800209 - 0.679293I$		
$u = -0.855632 + 0.391807I$		
$a = 0.459557 - 0.032989I$	$0.16119 + 2.51789I$	$-0.56583 - 5.72451I$
$b = -0.855632 + 0.391807I$		
$u = -0.855632 - 0.391807I$		
$a = 0.459557 + 0.032989I$	$0.16119 - 2.51789I$	$-0.56583 + 5.72451I$
$b = -0.855632 - 0.391807I$		
$u = 0.152358 + 1.111590I$		
$a = -0.201254 - 0.208299I$	$-3.34829 - 0.12486I$	$-9.98571 - 0.34747I$
$b = 0.152358 + 1.111590I$		
$u = 0.152358 - 1.111590I$		
$a = -0.201254 + 0.208299I$	$-3.34829 + 0.12486I$	$-9.98571 + 0.34747I$
$b = 0.152358 - 1.111590I$		
$u = -0.092710 + 0.862384I$		
$a = -0.384305 + 0.955600I$	$-3.61750 + 1.08846I$	$-11.50895 - 1.14763I$
$b = -0.092710 + 0.862384I$		
$u = -0.092710 - 0.862384I$		
$a = -0.384305 - 0.955600I$	$-3.61750 - 1.08846I$	$-11.50895 + 1.14763I$
$b = -0.092710 - 0.862384I$		
$u = 0.428817 + 0.727273I$		
$a = -0.07660 + 2.49273I$	$-11.71580 - 3.61170I$	$-9.63478 - 2.16413I$
$b = 0.428817 + 0.727273I$		
$u = 0.428817 - 0.727273I$		
$a = -0.07660 - 2.49273I$	$-11.71580 + 3.61170I$	$-9.63478 + 2.16413I$
$b = 0.428817 - 0.727273I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.386380 + 0.705787I$		
$a = -0.23876 + 2.54670I$	$-7.99069 - 1.31704I$	$-7.26287 + 5.35092I$
$b = -0.386380 + 0.705787I$		
$u = -0.386380 - 0.705787I$		
$a = -0.23876 - 2.54670I$	$-7.99069 + 1.31704I$	$-7.26287 - 5.35092I$
$b = -0.386380 - 0.705787I$		
$u = 0.391478 + 0.659853I$		
$a = 0.32637 + 2.90203I$	$-11.93460 + 6.10252I$	$-10.79983 - 9.08073I$
$b = 0.391478 + 0.659853I$		
$u = 0.391478 - 0.659853I$		
$a = 0.32637 - 2.90203I$	$-11.93460 - 6.10252I$	$-10.79983 + 9.08073I$
$b = 0.391478 - 0.659853I$		
$u = -0.699668 + 1.103420I$		
$a = 0.639142 - 0.193517I$	$-5.32466 - 1.51971I$	$-9.09663 + 1.51246I$
$b = -0.699668 + 1.103420I$		
$u = -0.699668 - 1.103420I$		
$a = 0.639142 + 0.193517I$	$-5.32466 + 1.51971I$	$-9.09663 - 1.51246I$
$b = -0.699668 - 1.103420I$		
$u = 0.008513 + 0.657799I$		
$a = 1.162970 + 0.228615I$	$-0.99449 + 1.29399I$	$-3.54121 - 4.20952I$
$b = 0.008513 + 0.657799I$		
$u = 0.008513 - 0.657799I$		
$a = 1.162970 - 0.228615I$	$-0.99449 - 1.29399I$	$-3.54121 + 4.20952I$
$b = 0.008513 - 0.657799I$		
$u = 0.868024 + 1.029180I$		
$a = -0.658984 - 0.058816I$	$-0.05539 + 4.40246I$	$-4.33829 - 3.27958I$
$b = 0.868024 + 1.029180I$		
$u = 0.868024 - 1.029180I$		
$a = -0.658984 + 0.058816I$	$-0.05539 - 4.40246I$	$-4.33829 + 3.27958I$
$b = 0.868024 - 1.029180I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.125746 + 0.622773I$		
$a = -1.88454 + 0.92438I$	$-3.33065 - 4.80034I$	$-9.65737 + 7.89620I$
$b = -0.125746 + 0.622773I$		
$u = -0.125746 - 0.622773I$		
$a = -1.88454 - 0.92438I$	$-3.33065 + 4.80034I$	$-9.65737 - 7.89620I$
$b = -0.125746 - 0.622773I$		
$u = -0.91505 + 1.10566I$		
$a = 0.731772 - 0.024127I$	$-2.06182 - 9.69561I$	$0. + 8.25119I$
$b = -0.91505 + 1.10566I$		
$u = -0.91505 - 1.10566I$		
$a = 0.731772 + 0.024127I$	$-2.06182 + 9.69561I$	$0. - 8.25119I$
$b = -0.91505 - 1.10566I$		
$u = -0.034652 + 0.486523I$		
$a = 0.705466 - 0.923628I$	$-0.06748 + 1.56172I$	$0.05355 - 4.52111I$
$b = -0.034652 + 0.486523I$		
$u = -0.034652 - 0.486523I$		
$a = 0.705466 + 0.923628I$	$-0.06748 - 1.56172I$	$0.05355 + 4.52111I$
$b = -0.034652 - 0.486523I$		
$u = -0.95977 + 1.23861I$		
$a = 1.033700 - 0.023141I$	$-9.7261 - 10.4089I$	$0$
$b = -0.95977 + 1.23861I$		
$u = -0.95977 - 1.23861I$		
$a = 1.033700 + 0.023141I$	$-9.7261 + 10.4089I$	$0$
$b = -0.95977 - 1.23861I$		
$u = 0.94787 + 1.25221I$		
$a = -1.027830 - 0.077389I$	$-14.1870 + 5.4411I$	$0$
$b = 0.94787 + 1.25221I$		
$u = 0.94787 - 1.25221I$		
$a = -1.027830 + 0.077389I$	$-14.1870 - 5.4411I$	$0$
$b = 0.94787 - 1.25221I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.97234 + 1.24005I$	$-13.4156 + 15.8053I$	0
$a = -1.073810 - 0.004329I$		
$b = 0.97234 + 1.24005I$		
$u = 0.97234 - 1.24005I$	$-13.4156 - 15.8053I$	0
$a = -1.073810 + 0.004329I$		
$b = 0.97234 - 1.24005I$		



$$\text{II. } I_2^u = \langle b + u, 3u^{16} - 3u^{15} + \dots + a - 1, u^{17} - u^{16} + \dots + 4u^2 - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -3u^{16} + 3u^{15} + \dots - 5u + 1 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^{16} - 3u^{15} + \dots + 5u - 4 \\ u^{16} - u^{15} + \dots - u^2 + 4u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -6u^{16} + 11u^{15} + \dots - 13u + 15 \\ -u^{16} + 4u^{15} + \dots - 5u + 6 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3u^{16} + 3u^{15} + \dots - 6u + 1 \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -8u^{16} + 12u^{15} + \dots - 23u + 10 \\ -4u^{16} + 4u^{15} + \dots - 10u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 4u^{16} - 5u^{15} + \dots + 11u - 4 \\ u^{16} - u^{15} + \dots - u^2 + 4u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 4u^{16} - 9u^{15} + \dots + 12u - 12 \\ -u^{15} + u^{14} + \dots + u - 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 14u^{16} - 22u^{15} + \dots + 26u - 17 \\ 6u^{16} - 10u^{15} + \dots + 12u - 11 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -4u^{16} + 4u^{15} + \dots - 9u + 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -u^{16} + 4u^{15} - 4u^{14} - 4u^{13} + 3u^{12} + 17u^{11} - 25u^{10} - 11u^9 + 23u^8 + 23u^7 - 48u^6 - 5u^5 + 30u^4 + 11u^3 - 33u^2 - 3u + 8$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{17} - 10u^{16} + \dots - 4u + 1$
$c_2$	$u^{17} - 2u^{16} + \dots + 2u - 1$
$c_3$	$u^{17} + 2u^{16} + \dots - 6u^2 - 1$
$c_4, c_{11}$	$u^{17} - u^{16} + \dots + 4u^2 - 1$
$c_5$	$u^{17} + 2u^{16} + \dots + 3u - 1$
$c_6$	$u^{17} + 2u^{16} + \dots + 2u + 1$
$c_7$	$u^{17} + 6u^{16} + \dots - 3u - 1$
$c_8$	$u^{17} + 9u^{16} + \dots - 118u - 21$
$c_9$	$u^{17} - 8u^{16} + \dots + 3u - 1$
$c_{10}$	$u^{17} - 4u^{15} + \dots + u - 1$
$c_{12}$	$u^{17} + 8u^{16} + \dots + 3u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{17} - 2y^{16} + \dots + 74y^3 - 1$
$c_2, c_6$	$y^{17} + 10y^{16} + \dots - 4y - 1$
$c_3$	$y^{17} - 14y^{16} + \dots - 12y - 1$
$c_4, c_{11}$	$y^{17} - 3y^{16} + \dots + 8y - 1$
$c_5$	$y^{17} - 8y^{16} + \dots - y - 1$
$c_7$	$y^{17} - 16y^{16} + \dots - 5y - 1$
$c_8$	$y^{17} - 5y^{16} + \dots + 946y - 441$
$c_9, c_{12}$	$y^{17} - 4y^{16} + \dots - 17y - 1$
$c_{10}$	$y^{17} - 8y^{16} + \dots + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.621825 + 0.705881I$ $a = -1.69701 - 0.12364I$ $b = 0.621825 - 0.705881I$	$0.16835 - 3.69444I$	$-3.43345 + 6.20569I$
$u = -0.621825 - 0.705881I$ $a = -1.69701 + 0.12364I$ $b = 0.621825 + 0.705881I$	$0.16835 + 3.69444I$	$-3.43345 - 6.20569I$
$u = 0.985112 + 0.472102I$ $a = 0.650559 + 0.351279I$ $b = -0.985112 - 0.472102I$	$0.03052 - 1.55891I$	$-2.18552 - 2.08462I$
$u = 0.985112 - 0.472102I$ $a = 0.650559 - 0.351279I$ $b = -0.985112 + 0.472102I$	$0.03052 + 1.55891I$	$-2.18552 + 2.08462I$
$u = -0.924919 + 0.614200I$ $a = -0.886710 + 0.219548I$ $b = 0.924919 - 0.614200I$	$1.80526 - 3.09805I$	$2.71378 + 6.00667I$
$u = -0.924919 - 0.614200I$ $a = -0.886710 - 0.219548I$ $b = 0.924919 + 0.614200I$	$1.80526 + 3.09805I$	$2.71378 - 6.00667I$
$u = 0.700967 + 0.501936I$ $a = 1.39448 + 0.81847I$ $b = -0.700967 - 0.501936I$	$-1.94678 + 5.32379I$	$-4.18293 - 7.79972I$
$u = 0.700967 - 0.501936I$ $a = 1.39448 - 0.81847I$ $b = -0.700967 + 0.501936I$	$-1.94678 - 5.32379I$	$-4.18293 + 7.79972I$
$u = 0.677004 + 0.917206I$ $a = 1.157990 - 0.482730I$ $b = -0.677004 - 0.917206I$	$-1.93385 + 1.63299I$	$-5.94728 - 2.28105I$
$u = 0.677004 - 0.917206I$ $a = 1.157990 + 0.482730I$ $b = -0.677004 + 0.917206I$	$-1.93385 - 1.63299I$	$-5.94728 + 2.28105I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.856536 + 0.852054I$ $a = -0.984611 - 0.179626I$ $b = 0.856536 - 0.852054I$	$1.50462 - 4.39558I$	$2.29329 + 4.97306I$
$u = -0.856536 - 0.852054I$ $a = -0.984611 + 0.179626I$ $b = 0.856536 + 0.852054I$	$1.50462 + 4.39558I$	$2.29329 - 4.97306I$
$u = 0.707184$ $a = -1.41344$ $b = -0.707184$	$-7.59564$	$-3.54960$
$u = 0.863394 + 0.964445I$ $a = 0.890585 - 0.307806I$ $b = -0.863394 - 0.964445I$	$-0.71548 + 8.94334I$	$-2.29262 - 7.34583I$
$u = 0.863394 - 0.964445I$ $a = 0.890585 + 0.307806I$ $b = -0.863394 + 0.964445I$	$-0.71548 - 8.94334I$	$-2.29262 + 7.34583I$
$u = -0.676789 + 0.041582I$ $a = 1.68144 + 0.49673I$ $b = 0.676789 - 0.041582I$	$-11.56420 - 5.02914I$	$-6.69047 + 2.68447I$
$u = -0.676789 - 0.041582I$ $a = 1.68144 - 0.49673I$ $b = 0.676789 + 0.041582I$	$-11.56420 + 5.02914I$	$-6.69047 - 2.68447I$

$$\text{III. } I_3^u = \langle -1.05 \times 10^{43} u^{31} + 4.71 \times 10^{42} u^{30} + \dots + 1.48 \times 10^{44} b - 3.77 \times 10^{43}, 3.26 \times 10^{44} u^{31} - 3.76 \times 10^{44} u^{30} + \dots + 2.51 \times 10^{45} a + 1.97 \times 10^{44}, u^{32} - 2u^{31} + \dots - 3u + 17 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.129800u^{31} + 0.149506u^{30} + \dots - 7.89817u - 0.0783584 \\ 0.0709764u^{31} - 0.0318586u^{30} + \dots + 0.0746396u + 0.254829 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.112910u^{31} + 0.209924u^{30} + \dots - 2.19568u + 1.23577 \\ -0.0168898u^{31} - 0.0604187u^{30} + \dots - 4.70249u - 1.31413 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.00441307u^{31} - 0.108854u^{30} + \dots - 2.15238u - 2.06675 \\ 0.143271u^{31} - 0.0431300u^{30} + \dots + 3.60055u + 2.54054 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0588235u^{31} + 0.117647u^{30} + \dots - 7.82353u + 0.176471 \\ 0.0709764u^{31} - 0.0318586u^{30} + \dots + 0.0746396u + 0.254829 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0706474u^{31} + 0.301908u^{30} + \dots - 1.93782u + 2.98528 \\ -0.0346426u^{31} + 0.271751u^{30} + \dots + 2.53465u + 3.05041 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0588235u^{31} + 0.117647u^{30} + \dots - 7.82353u + 0.176471 \\ 0.0709764u^{31} - 0.0318586u^{30} + \dots + 1.07464u + 0.254829 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0149899u^{31} - 0.100956u^{30} + \dots - 5.35030u - 0.119609 \\ -0.127897u^{31} + 0.0824258u^{30} + \dots - 7.92285u - 3.64080 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.182759u^{31} - 0.207627u^{30} + \dots + 5.96598u + 4.51980 \\ -0.230768u^{31} + 0.589230u^{30} + \dots - 6.71849u + 4.83964 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.101574u^{31} + 0.282734u^{30} + \dots - 5.94721u + 2.04807 \\ -0.0632789u^{31} + 0.328608u^{30} + \dots - 0.0145611u + 3.47938 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.112903u^{31} - 0.364793u^{30} + \dots - 1.27394u - 15.4783$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{16} + 10u^{15} + \dots + 4u + 1)^2$
$c_2, c_6$	$(u^{16} + 2u^{15} + \dots + 2u^2 + 1)^2$
$c_3$	$(u^{16} - 2u^{15} + \dots - 4u + 1)^2$
$c_4, c_{11}$	$u^{32} - 2u^{31} + \dots - 3u + 17$
$c_5$	$u^{32} - 20u^{30} + \dots + 147u + 11483$
$c_7$	$(u - 1)^{32}$
$c_8$	$(u^{16} - 5u^{15} + \dots - 10u + 4)^2$
$c_9, c_{12}$	$u^{32} + 5u^{31} + \dots - 40346u + 7837$
$c_{10}$	$u^{32} - 10u^{30} + \dots - 52147u + 13057$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{16} - 6y^{15} + \dots + 52y^2 + 1)^2$
$c_2, c_6$	$(y^{16} + 10y^{15} + \dots + 4y + 1)^2$
$c_3$	$(y^{16} - 22y^{15} + \dots + 4y + 1)^2$
$c_4, c_{11}$	$y^{32} + 46y^{30} + \dots + 4513y + 289$
$c_5$	$y^{32} - 40y^{31} + \dots + 4819370525y + 131859289$
$c_7$	$(y - 1)^{32}$
$c_8$	$(y^{16} + 5y^{15} + \dots + 84y + 16)^2$
$c_9, c_{12}$	$y^{32} - 37y^{31} + \dots - 3847924y + 61418569$
$c_{10}$	$y^{32} - 20y^{31} + \dots - 1430609823y + 170485249$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.595671 + 0.842379I$ $a = -1.48043 - 0.22659I$ $b = 0.920809 - 0.564799I$	$-0.08555 - 5.00887I$	$-2.04817 + 9.54125I$
$u = -0.595671 - 0.842379I$ $a = -1.48043 + 0.22659I$ $b = 0.920809 + 0.564799I$	$-0.08555 + 5.00887I$	$-2.04817 - 9.54125I$
$u = 0.445704 + 0.827008I$ $a = -1.006630 + 0.127867I$ $b = 1.51162 - 1.06489I$	$-12.05440 + 7.15239I$	$-8.17635 - 6.88764I$
$u = 0.445704 - 0.827008I$ $a = -1.006630 - 0.127867I$ $b = 1.51162 + 1.06489I$	$-12.05440 - 7.15239I$	$-8.17635 + 6.88764I$
$u = 0.920809 + 0.564799I$ $a = 1.38479 + 0.35836I$ $b = -0.595671 - 0.842379I$	$-0.08555 + 5.00887I$	$-2.04817 - 9.54125I$
$u = 0.920809 - 0.564799I$ $a = 1.38479 - 0.35836I$ $b = -0.595671 + 0.842379I$	$-0.08555 - 5.00887I$	$-2.04817 + 9.54125I$
$u = 0.304893 + 0.861352I$ $a = -1.122090 + 0.066210I$ $b = 1.48728 - 1.09791I$	$-12.74750 - 3.22124I$	$-9.99417 + 0.06529I$
$u = 0.304893 - 0.861352I$ $a = -1.122090 - 0.066210I$ $b = 1.48728 + 1.09791I$	$-12.74750 + 3.22124I$	$-9.99417 - 0.06529I$
$u = -0.371450 + 0.797625I$ $a = 1.037300 + 0.063551I$ $b = -1.51710 - 1.09383I$	$-8.33008 - 1.76073I$	$-6.56613 + 3.85252I$
$u = -0.371450 - 0.797625I$ $a = 1.037300 - 0.063551I$ $b = -1.51710 + 1.09383I$	$-8.33008 + 1.76073I$	$-6.56613 - 3.85252I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.702474 + 0.876922I$		
$a = 1.195520 - 0.248497I$	$0.59866 + 2.73963I$	$0.340477 + 0.446917I$
$b = -0.639086 - 0.446115I$		
$u = 0.702474 - 0.876922I$		
$a = 1.195520 + 0.248497I$	$0.59866 - 2.73963I$	$0.340477 - 0.446917I$
$b = -0.639086 + 0.446115I$		
$u = 0.275864 + 0.794362I$		
$a = 1.52812 - 0.20094I$	$-3.72434 + 5.60445I$	$-9.51726 - 7.00610I$
$b = -1.13799 - 0.92245I$		
$u = 0.275864 - 0.794362I$		
$a = 1.52812 + 0.20094I$	$-3.72434 - 5.60445I$	$-9.51726 + 7.00610I$
$b = -1.13799 + 0.92245I$		
$u = -0.639086 + 0.446115I$		
$a = -1.75455 + 0.14252I$	$0.59866 - 2.73963I$	$0.340477 - 0.446917I$
$b = 0.702474 - 0.876922I$		
$u = -0.639086 - 0.446115I$		
$a = -1.75455 - 0.14252I$	$0.59866 + 2.73963I$	$0.340477 + 0.446917I$
$b = 0.702474 + 0.876922I$		
$u = 0.865485 + 1.019380I$		
$a = 0.834505 - 0.032645I$	$0.10305 + 2.86220I$	$-3.06555 - 3.98366I$
$b = -0.350507 - 0.537414I$		
$u = 0.865485 - 1.019380I$		
$a = 0.834505 + 0.032645I$	$0.10305 - 2.86220I$	$-3.06555 + 3.98366I$
$b = -0.350507 + 0.537414I$		
$u = -0.350507 + 0.537414I$		
$a = -1.71691 - 0.28607I$	$0.10305 - 2.86220I$	$-3.06555 + 3.98366I$
$b = 0.865485 - 1.019380I$		
$u = -0.350507 - 0.537414I$		
$a = -1.71691 + 0.28607I$	$0.10305 + 2.86220I$	$-3.06555 - 3.98366I$
$b = 0.865485 + 1.019380I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.13799 + 0.92245I$		
$a = -0.806166 + 0.364503I$	$-3.72434 - 5.60445I$	$-9.51726 + 7.00610I$
$b = 0.275864 - 0.794362I$		
$u = -1.13799 - 0.92245I$		
$a = -0.806166 - 0.364503I$	$-3.72434 + 5.60445I$	$-9.51726 - 7.00610I$
$b = 0.275864 + 0.794362I$		
$u = 0.086773 + 0.477663I$		
$a = 1.35727 - 0.63772I$	$-1.59332 - 1.36627I$	$-7.47286 - 3.74224I$
$b = -0.98910 - 1.38893I$		
$u = 0.086773 - 0.477663I$		
$a = 1.35727 + 0.63772I$	$-1.59332 + 1.36627I$	$-7.47286 + 3.74224I$
$b = -0.98910 + 1.38893I$		
$u = -0.98910 + 1.38893I$		
$a = -0.426970 - 0.000051I$	$-1.59332 + 1.36627I$	$-7.47286 + 3.74224I$
$b = 0.086773 - 0.477663I$		
$u = -0.98910 - 1.38893I$		
$a = -0.426970 + 0.000051I$	$-1.59332 - 1.36627I$	$-7.47286 - 3.74224I$
$b = 0.086773 + 0.477663I$		
$u = 1.48728 + 1.09791I$		
$a = 0.130314 + 0.540083I$	$-12.74750 + 3.22124I$	0
$b = 0.304893 - 0.861352I$		
$u = 1.48728 - 1.09791I$		
$a = 0.130314 - 0.540083I$	$-12.74750 - 3.22124I$	0
$b = 0.304893 + 0.861352I$		
$u = 1.51162 + 1.06489I$		
$a = -0.003578 + 0.515545I$	$-12.05440 - 7.15239I$	0
$b = 0.445704 - 0.827008I$		
$u = 1.51162 - 1.06489I$		
$a = -0.003578 - 0.515545I$	$-12.05440 + 7.15239I$	0
$b = 0.445704 + 0.827008I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.51710 + 1.09383I$	$-8.33008 + 1.76073I$	0
$a = -0.062247 + 0.484928I$		
$b = -0.371450 - 0.797625I$		
$u = -1.51710 - 1.09383I$	$-8.33008 - 1.76073I$	0
$a = -0.062247 - 0.484928I$		
$b = -0.371450 + 0.797625I$		

$$\text{IV. } I_4^u = \langle -u^3 + u^2 + b - 3u + 1, a, u^4 - u^3 + 3u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u^3 - u^2 + 3u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 - u^2 + 3u - 1 \\ u^3 - u^2 + 3u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - u^2 + 3u - 1 \\ u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 + u^2 - 3u + 1 \\ -u^3 + u^2 - 2u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + 2u + 2 \\ u^3 - u^2 + 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 2 \\ u^3 - u^2 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 - u^2 + 3u - 1 \\ u^3 - u^2 + 4u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-9u^3 + 9u^2 - 18u - 3$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$u^4 - u^3 + 3u^2 - u + 1$
$c_7, c_9$	$(u - 1)^4$
$c_8$	$u^4$
$c_{12}$	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6$	$(y^2 + y + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$y^4 + 5y^3 + 9y^2 + 5y + 1$
$c_7, c_9, c_{12}$	$(y - 1)^4$
$c_8$	$y^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.148403 + 0.632502I$	$-1.64493 + 2.02988I$	$-7.50000 - 7.79423I$
$a = 0$		
$b = -0.35160 + 1.49853I$		
$u = 0.148403 - 0.632502I$	$-1.64493 - 2.02988I$	$-7.50000 + 7.79423I$
$a = 0$		
$b = -0.35160 - 1.49853I$		
$u = 0.35160 + 1.49853I$	$-1.64493 - 2.02988I$	$-7.50000 + 7.79423I$
$a = 0$		
$b = -0.148403 + 0.632502I$		
$u = 0.35160 - 1.49853I$	$-1.64493 + 2.02988I$	$-7.50000 - 7.79423I$
$a = 0$		
$b = -0.148403 - 0.632502I$		



## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^2)(u^{16} + 10u^{15} + \dots + 4u + 1)^2$ $\cdot (u^{17} - 10u^{16} + \dots - 4u + 1)(u^{32} + 19u^{31} + \dots + 7u + 16)$
$c_2$	$((u^2 + u + 1)^2)(u^{16} + 2u^{15} + \dots + 2u^2 + 1)^2(u^{17} - 2u^{16} + \dots + 2u - 1)$ $\cdot (u^{32} - 5u^{31} + \dots - 7u + 4)$
$c_3$	$((u^2 - u + 1)^2)(u^{16} - 2u^{15} + \dots - 4u + 1)^2(u^{17} + 2u^{16} + \dots - 6u^2 - 1)$ $\cdot (u^{32} + 5u^{31} + \dots + 89u + 4)$
$c_4, c_{11}$	$(u^4 - u^3 + 3u^2 - u + 1)(u^{17} - u^{16} + \dots + 4u^2 - 1)$ $\cdot (u^{32} - 2u^{31} + \dots - 3u + 17)(u^{32} - u^{31} + \dots + 13u^2 + 1)$
$c_5$	$(u^4 - u^3 + 3u^2 - u + 1)(u^{17} + 2u^{16} + \dots + 3u - 1)$ $\cdot (u^{32} - 32u^{30} + \dots + u + 1)(u^{32} - 20u^{30} + \dots + 147u + 11483)$
$c_6$	$((u^2 - u + 1)^2)(u^{16} + 2u^{15} + \dots + 2u^2 + 1)^2(u^{17} + 2u^{16} + \dots + 2u + 1)$ $\cdot (u^{32} - 5u^{31} + \dots - 7u + 4)$
$c_7$	$((u - 1)^{36})(u^{17} + 6u^{16} + \dots - 3u - 1)$ $\cdot (u^{32} + 35u^{31} + \dots + 147456u + 16384)$
$c_8$	$u^4(u^{16} - 5u^{15} + \dots - 10u + 4)^2(u^{17} + 9u^{16} + \dots - 118u - 21)$ $\cdot (u^{32} + 22u^{31} + \dots + 21u + 2)$
$c_9$	$((u - 1)^4)(u^{17} - 8u^{16} + \dots + 3u - 1)(u^{32} + 2u^{31} + \dots - 17u + 1)$ $\cdot (u^{32} + 5u^{31} + \dots - 40346u + 7837)$
$c_{10}$	$(u^4 - u^3 + 3u^2 - u + 1)(u^{17} - 4u^{15} + \dots + u - 1)$ $\cdot (u^{32} - 12u^{30} + \dots - 17u + 17)(u^{32} - 10u^{30} + \dots - 52147u + 13057)$
$c_{12}$	$((u + 1)^4)(u^{17} + 8u^{16} + \dots + 3u + 1)(u^{32} + 2u^{31} + \dots - 17u + 1)$ $\cdot (u^{32} + 5u^{31} + \dots - 40346u + 7837)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^2)(y^{16} - 6y^{15} + \dots + 52y^2 + 1)^2$ $\cdot (y^{17} - 2y^{16} + \dots + 74y^3 - 1)(y^{32} - 9y^{31} + \dots - 1425y + 256)$
$c_2, c_6$	$((y^2 + y + 1)^2)(y^{16} + 10y^{15} + \dots + 4y + 1)^2$ $\cdot (y^{17} + 10y^{16} + \dots - 4y - 1)(y^{32} + 19y^{31} + \dots + 7y + 16)$
$c_3$	$((y^2 + y + 1)^2)(y^{16} - 22y^{15} + \dots + 4y + 1)^2$ $\cdot (y^{17} - 14y^{16} + \dots - 12y - 1)(y^{32} - 37y^{31} + \dots - 3673y + 16)$
$c_4, c_{11}$	$(y^4 + 5y^3 + 9y^2 + 5y + 1)(y^{17} - 3y^{16} + \dots + 8y - 1)$ $\cdot (y^{32} + 46y^{30} + \dots + 4513y + 289)(y^{32} + 13y^{31} + \dots + 26y + 1)$
$c_5$	$(y^4 + 5y^3 + 9y^2 + 5y + 1)(y^{17} - 8y^{16} + \dots - y - 1)$ $\cdot (y^{32} - 64y^{31} + \dots + 3y + 1)$ $\cdot (y^{32} - 40y^{31} + \dots + 4819370525y + 131859289)$
$c_7$	$((y - 1)^{36})(y^{17} - 16y^{16} + \dots - 5y - 1)$ $\cdot (y^{32} - 17y^{31} + \dots + 3623878656y + 268435456)$
$c_8$	$y^4(y^{16} + 5y^{15} + \dots + 84y + 16)^2(y^{17} - 5y^{16} + \dots + 946y - 441)$ $\cdot (y^{32} + 60y^{30} + \dots + 19y + 4)$
$c_9, c_{12}$	$((y - 1)^4)(y^{17} - 4y^{16} + \dots - 17y - 1)(y^{32} - 60y^{31} + \dots - 9y + 1)$ $\cdot (y^{32} - 37y^{31} + \dots - 3847924y + 61418569)$
$c_{10}$	$(y^4 + 5y^3 + 9y^2 + 5y + 1)(y^{17} - 8y^{16} + \dots + 3y - 1)$ $\cdot (y^{32} - 24y^{31} + \dots - 5117y + 289)$ $\cdot (y^{32} - 20y^{31} + \dots - 1430609823y + 170485249)$