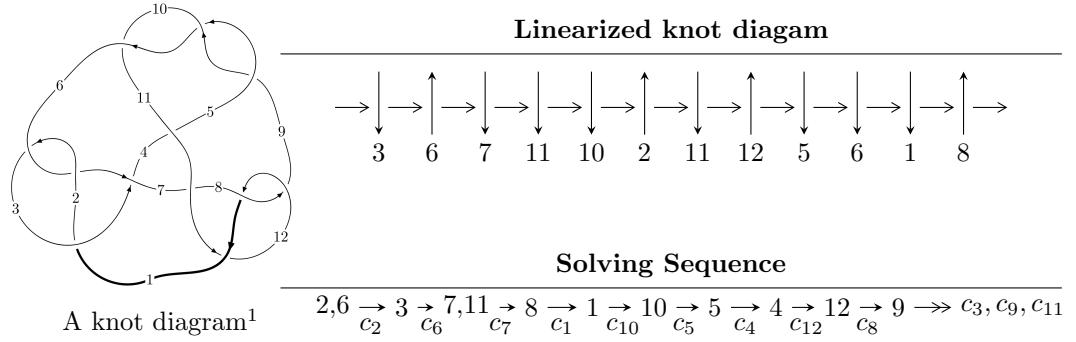


$12n_{0294}$  ( $K12n_{0294}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle u^{10} + u^9 + 5u^8 + 4u^7 + 9u^6 + 6u^5 + 3u^4 + 3u^3 - 5u^2 + 2b - 1, \\
 &\quad u^{10} + u^9 + 5u^8 + 4u^7 + 9u^6 + 6u^5 + 3u^4 + 3u^3 - 7u^2 + 2a - 3, \\
 &\quad u^{12} + u^{11} + 5u^{10} + 4u^9 + 10u^8 + 7u^7 + 7u^6 + 6u^5 - 2u^4 + 3u^3 - 3u^2 - 1 \rangle \\
 I_2^u &= \langle -78963686u^{21} - 109276521u^{20} + \dots + 272347738b + 755541991, \\
 &\quad 207732146u^{21} + 642690277u^{20} + \dots + 1906434166a + 152323303, u^{22} + 2u^{21} + \dots + u + 7 \rangle \\
 I_3^u &= \langle b - a - u, a^2 + 2u, u^2 - u + 1 \rangle \\
 I_4^u &= \langle b + u, a, u^2 + u + 1 \rangle \\
 I_5^u &= \langle b - a + 1, a^2 + 2u, u^2 - u + 1 \rangle \\
 I_6^u &= \langle b + 1, a, u^2 + u + 1 \rangle
 \end{aligned}$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 46 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{10} + u^9 + \cdots + 2b - 1, \ u^{10} + u^9 + \cdots + 2a - 3, \ u^{12} + u^{11} + \cdots - 3u^2 - 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}u^{10} - \frac{1}{2}u^9 + \cdots + \frac{7}{2}u^2 + \frac{3}{2} \\ -\frac{1}{2}u^{10} - \frac{1}{2}u^9 + \cdots + \frac{5}{2}u^2 + \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u^{11} + \frac{1}{2}u^{10} + \cdots - u^5 - \frac{7}{2}u^3 \\ \frac{1}{2}u^{11} + \frac{1}{2}u^{10} + \cdots - \frac{3}{2}u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u^{10} - \frac{1}{2}u^9 + \cdots + \frac{7}{2}u^2 + \frac{3}{2} \\ -\frac{1}{2}u^{10} - \frac{1}{2}u^9 + \cdots + \frac{5}{2}u^2 + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{10} + u^9 + \cdots - \frac{1}{2}u - \frac{1}{2} \\ \frac{1}{2}u^{10} + u^9 + \cdots - \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^{10} - \frac{1}{2}u^9 + \cdots + \frac{5}{2}u^2 + \frac{3}{2} \\ -\frac{1}{2}u^{10} - \frac{1}{2}u^9 + \cdots + \frac{5}{2}u^2 + \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}u^9 - \frac{1}{2}u^8 + \cdots - u^3 + \frac{3}{2}u \\ -\frac{1}{2}u^9 - \frac{1}{2}u^8 + \cdots + u^3 + \frac{3}{2}u \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$= -5u^{11} - 3u^{10} - 21u^9 - 9u^8 - 34u^7 - 12u^6 - 8u^5 - 10u^4 + 26u^3 - 12u^2 + 13u - 9$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{12} + 9u^{11} + \cdots + 6u + 1$
$c_2, c_6, c_8$ $c_{12}$	$u^{12} - u^{11} + 5u^{10} - 4u^9 + 10u^8 - 7u^7 + 7u^6 - 6u^5 - 2u^4 - 3u^3 - 3u^2 - 1$
$c_3, c_7$	$u^{12} + u^{11} + \cdots - u - 2$
$c_4$	$u^{12} + 15u^{11} + \cdots + 596u + 32$
$c_5, c_9, c_{10}$	$u^{12} - 5u^{11} + \cdots - 4u - 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{12} - 7y^{11} + \cdots - 10y + 1$
$c_2, c_6, c_8$ $c_{12}$	$y^{12} + 9y^{11} + \cdots + 6y + 1$
$c_3, c_7$	$y^{12} - 23y^{11} + \cdots + 51y + 4$
$c_4$	$y^{12} - 35y^{11} + \cdots - 202128y + 1024$
$c_5, c_9, c_{10}$	$y^{12} - 15y^{11} + \cdots + 16y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.07086$		
$a = 1.66252$	-12.1281	-5.69090
$b = -0.484232$		
$u = 0.296087 + 0.741679I$		
$a = -0.55750 + 1.66481I$	-5.57527 + 2.63814I	-11.42884 - 2.06673I
$b = -1.09508 + 1.22561I$		
$u = 0.296087 - 0.741679I$		
$a = -0.55750 - 1.66481I$	-5.57527 - 2.63814I	-11.42884 + 2.06673I
$b = -1.09508 - 1.22561I$		
$u = -0.162478 + 1.257750I$		
$a = -0.651223 + 0.357840I$	-5.08721 - 2.66459I	-10.23667 + 3.12657I
$b = -0.095679 + 0.766555I$		
$u = -0.162478 - 1.257750I$		
$a = -0.651223 - 0.357840I$	-5.08721 + 2.66459I	-10.23667 - 3.12657I
$b = -0.095679 - 0.766555I$		
$u = 0.635067$		
$a = 1.51509$	-1.87851	-4.23810
$b = 0.111783$		
$u = 0.416797 + 1.329220I$		
$a = -0.199126 - 0.960314I$	-9.65412 + 7.95397I	-10.78779 - 5.64533I
$b = 0.39398 - 2.06834I$		
$u = 0.416797 - 1.329220I$		
$a = -0.199126 + 0.960314I$	-9.65412 - 7.95397I	-10.78779 + 5.64533I
$b = 0.39398 + 2.06834I$		
$u = -0.206233 + 0.541920I$		
$a = 0.438428 - 0.668694I$	-0.276323 - 1.063990I	-4.38658 + 6.25986I
$b = -0.310427 - 0.445170I$		
$u = -0.206233 - 0.541920I$		
$a = 0.438428 + 0.668694I$	-0.276323 + 1.063990I	-4.38658 - 6.25986I
$b = -0.310427 + 0.445170I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.62627 + 1.34351I$		
$a = 0.380614 + 1.171480I$	$19.3715 - 11.9727I$	$-10.19562 + 5.57211I$
$b = 0.79343 + 2.85430I$		
$u = -0.62627 - 1.34351I$		
$a = 0.380614 - 1.171480I$	$19.3715 + 11.9727I$	$-10.19562 - 5.57211I$
$b = 0.79343 - 2.85430I$		

## II.

$$I_2^u = \langle -7.90 \times 10^7 u^{21} - 1.09 \times 10^8 u^{20} + \dots + 2.72 \times 10^8 b + 7.56 \times 10^8, 2.08 \times 10^8 u^{21} + 6.43 \times 10^8 u^{20} + \dots + 1.91 \times 10^9 a + 1.52 \times 10^8, u^{22} + 2u^{21} + \dots + u + 7 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.108964u^{21} - 0.337116u^{20} + \dots - 2.45446u - 0.0798996 \\ 0.289937u^{21} + 0.401239u^{20} + \dots - 0.514832u - 2.77418 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0918453u^{21} + 0.174181u^{20} + \dots + 0.699627u - 0.598884 \\ 0.113601u^{21} + 0.0746372u^{20} + \dots + 2.03280u - 0.388234 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.108964u^{21} - 0.337116u^{20} + \dots - 2.45446u - 0.0798996 \\ 0.308189u^{21} + 0.280109u^{20} + \dots - 1.39677u - 3.60850 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0436157u^{21} + 0.236816u^{20} + \dots + 0.624511u + 1.17524 \\ 0.202828u^{21} + 0.763930u^{20} + \dots + 1.77903u + 1.62345 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0937967u^{21} + 0.208563u^{20} + \dots - 0.352346u + 1.14461 \\ 0.592510u^{21} + 1.09915u^{20} + \dots + 0.751139u - 3.19574 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.121487u^{21} + 0.427747u^{20} + \dots + 2.44535u + 0.605555 \\ -0.158323u^{21} + 0.138552u^{20} + \dots + 1.87374u + 4.80979 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $-\frac{89419702}{136173869}u^{21} - \frac{42120566}{136173869}u^{20} + \dots + \frac{1416145048}{136173869}u + \frac{452453139}{136173869}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{22} + 14u^{21} + \cdots + 307u + 49$
$c_2, c_6, c_8$ $c_{12}$	$u^{22} - 2u^{21} + \cdots - u + 7$
$c_3, c_7$	$u^{22} + 2u^{21} + \cdots - 145u + 35$
$c_4$	$(u^{11} - 6u^{10} + \cdots - 48u + 32)^2$
$c_5, c_9, c_{10}$	$(u^{11} + 2u^{10} - 7u^9 - 14u^8 + 17u^7 + 32u^6 - 20u^5 - 30u^4 + 9u^3 + 8u^2 - 2)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{22} - 10y^{21} + \cdots - 14085y + 2401$
$c_2, c_6, c_8$ $c_{12}$	$y^{22} + 14y^{21} + \cdots + 307y + 49$
$c_3, c_7$	$y^{22} - 34y^{21} + \cdots + 17965y + 1225$
$c_4$	$(y^{11} - 58y^{10} + \cdots + 12928y - 1024)^2$
$c_5, c_9, c_{10}$	$(y^{11} - 18y^{10} + \cdots + 32y - 4)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.315297 + 0.937809I$	$-0.82409 + 3.69934I$	$-10.27594 - 2.30433I$
$a = -0.373766 + 0.436547I$		
$b = 0.57981 + 1.45156I$		
$u = 0.315297 - 0.937809I$	$-0.82409 - 3.69934I$	$-10.27594 + 2.30433I$
$a = -0.373766 - 0.436547I$		
$b = 0.57981 - 1.45156I$		
$u = -0.621678 + 0.900743I$	$-0.82409 - 3.69934I$	$-10.27594 + 2.30433I$
$a = 0.433725 + 0.285994I$		
$b = 0.477184 - 0.282729I$		
$u = -0.621678 - 0.900743I$	$-0.82409 + 3.69934I$	$-10.27594 - 2.30433I$
$a = 0.433725 - 0.285994I$		
$b = 0.477184 + 0.282729I$		
$u = -1.140860 + 0.146410I$	$-16.3894 + 5.6976I$	$-8.38395 - 2.57135I$
$a = -1.58475 - 0.10382I$		
$b = 0.383248 + 0.166816I$		
$u = -1.140860 - 0.146410I$	$-16.3894 - 5.6976I$	$-8.38395 + 2.57135I$
$a = -1.58475 + 0.10382I$		
$b = 0.383248 - 0.166816I$		
$u = -0.528041 + 0.663736I$	$-0.153907 - 1.029650I$	$-5.69847 + 5.62903I$
$a = 0.036886 - 0.596779I$		
$b = -0.411020 - 0.383825I$		
$u = -0.528041 - 0.663736I$	$-0.153907 + 1.029650I$	$-5.69847 - 5.62903I$
$a = 0.036886 + 0.596779I$		
$b = -0.411020 + 0.383825I$		
$u = 0.797910 + 0.128505I$	$-5.23581 + 3.47501I$	$-8.51244 - 3.77183I$
$a = -1.42715 + 0.64453I$		
$b = -0.302057 + 0.565900I$		
$u = 0.797910 - 0.128505I$	$-5.23581 - 3.47501I$	$-8.51244 + 3.77183I$
$a = -1.42715 - 0.64453I$		
$b = -0.302057 - 0.565900I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.026101 + 1.195750I$	$-7.69899 - 1.57384I$	$-11.44703 + 1.61053I$
$a = -0.193214 - 1.265770I$		
$b = 0.79244 - 2.46937I$		
$u = 0.026101 - 1.195750I$	$-7.69899 + 1.57384I$	$-11.44703 - 1.61053I$
$a = -0.193214 + 1.265770I$		
$b = 0.79244 + 2.46937I$		
$u = 0.306447 + 1.162800I$	$-5.23581 + 3.47501I$	$-8.51244 - 3.77183I$
$a = 0.007196 + 1.052430I$		
$b = -0.56018 + 1.99198I$		
$u = 0.306447 - 1.162800I$	$-5.23581 - 3.47501I$	$-8.51244 + 3.77183I$
$a = 0.007196 - 1.052430I$		
$b = -0.56018 - 1.99198I$		
$u = 0.174005 + 0.725075I$	$-0.153907 - 1.029650I$	$-5.69847 + 5.62903I$
$a = 0.560735 - 0.384864I$		
$b = -0.654598 - 0.645346I$		
$u = 0.174005 - 0.725075I$	$-0.153907 + 1.029650I$	$-5.69847 - 5.62903I$
$a = 0.560735 + 0.384864I$		
$b = -0.654598 + 0.645346I$		
$u = 0.648660 + 1.107420I$	$-7.69899 + 1.57384I$	$-11.44703 - 1.61053I$
$a = 0.771605 - 0.910213I$		
$b = 0.461513 - 1.169360I$		
$u = 0.648660 - 1.107420I$	$-7.69899 - 1.57384I$	$-11.44703 + 1.61053I$
$a = 0.771605 + 0.910213I$		
$b = 0.461513 + 1.169360I$		
$u = -0.53111 + 1.36431I$	$-16.3894 - 5.6976I$	$-8.38395 + 2.57135I$
$a = -0.379457 - 1.188610I$		
$b = -0.55682 - 2.99037I$		
$u = -0.53111 - 1.36431I$	$-16.3894 + 5.6976I$	$-8.38395 - 2.57135I$
$a = -0.379457 + 1.188610I$		
$b = -0.55682 + 2.99037I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.44674 + 1.47157I$		
$a = 0.362471 + 1.193990I$	17.8360	$-11.36432 + 0.I$
$b = 0.29049 + 2.82389I$		
$u = -0.44674 - 1.47157I$		
$a = 0.362471 - 1.193990I$	17.8360	$-11.36432 + 0.I$
$b = 0.29049 - 2.82389I$		

$$\text{III. } I_3^u = \langle b - a - u, a^2 + 2u, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a \\ a + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} au - a + u \\ au - a + u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ -au + 2a + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2u + 2 \\ au - a - 3u + 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} a + 1 \\ a + u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -a \\ -a - u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-8u - 4$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_8$ $c_{11}$	$(u^2 - u + 1)^2$
$c_3, c_6, c_7$ $c_{12}$	$(u^2 + u + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(u^2 - 2)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 + y + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(y - 2)^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$		
$a = 0.707110 - 1.224740I$	$-4.93480 + 4.05977I$	$-8.00000 - 6.92820I$
$b = 1.207110 - 0.358719I$		
$u = 0.500000 + 0.866025I$		
$a = -0.707110 + 1.224740I$	$-4.93480 + 4.05977I$	$-8.00000 - 6.92820I$
$b = -0.20711 + 2.09077I$		
$u = 0.500000 - 0.866025I$		
$a = 0.707110 + 1.224740I$	$-4.93480 - 4.05977I$	$-8.00000 + 6.92820I$
$b = 1.207110 + 0.358719I$		
$u = 0.500000 - 0.866025I$		
$a = -0.707110 - 1.224740I$	$-4.93480 - 4.05977I$	$-8.00000 + 6.92820I$
$b = -0.20711 - 2.09077I$		

$$\text{IV. } I_4^u = \langle b + u, a, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u+1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u+1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $8u + 4$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_{11}, c_{12}$	$u^2 - u + 1$
$c_2, c_8$	$u^2 + u + 1$
$c_4, c_5, c_9$ $c_{10}$	$u^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^2 + y + 1$
$c_4, c_5, c_9$ $c_{10}$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0$	$-4.05977I$	$0. + 6.92820I$
$b = 0.500000 - 0.866025I$		
$u = -0.500000 - 0.866025I$		
$a = 0$	$4.05977I$	$0. - 6.92820I$
$b = 0.500000 + 0.866025I$		

$$\text{V. } I_5^u = \langle b - a + 1, a^2 + 2u, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a \\ a - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -au + u \\ -au + 2u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ -au + 2a - 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2u + 2 \\ -au - 3u + 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} a + u - 1 \\ a + u - 2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -a \\ -a + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -8

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_8$ $c_{11}$	$(u^2 - u + 1)^2$
$c_3, c_6, c_7$ $c_{12}$	$(u^2 + u + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(u^2 - 2)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 + y + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(y - 2)^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$		
$a = 0.707110 - 1.224740I$	-4.93480	-8.00000
$b = -0.292893 - 1.224750I$		
$u = 0.500000 + 0.866025I$		
$a = -0.707110 + 1.224740I$	-4.93480	-8.00000
$b = -1.70711 + 1.22474I$		
$u = 0.500000 - 0.866025I$		
$a = 0.707110 + 1.224740I$	-4.93480	-8.00000
$b = -0.292893 + 1.224750I$		
$u = 0.500000 - 0.866025I$		
$a = -0.707110 - 1.224740I$	-4.93480	-8.00000
$b = -1.70711 - 1.22474I$		

$$\text{VI. } I_6^u = \langle b+1, a, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u-1 \\ -u-2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -6

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_{11}, c_{12}$	$u^2 - u + 1$
$c_2, c_8$	$u^2 + u + 1$
$c_4, c_5, c_9$ $c_{10}$	$u^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^2 + y + 1$
$c_4, c_5, c_9$ $c_{10}$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0$	0	-6.00000
$b = -1.00000$		
$u = -0.500000 - 0.866025I$		
$a = 0$	0	-6.00000
$b = -1.00000$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$((u^2 - u + 1)^6)(u^{12} + 9u^{11} + \dots + 6u + 1)$ $\cdot (u^{22} + 14u^{21} + \dots + 307u + 49)$
$c_2, c_8$	$(u^2 - u + 1)^4(u^2 + u + 1)^2$ $\cdot (u^{12} - u^{11} + 5u^{10} - 4u^9 + 10u^8 - 7u^7 + 7u^6 - 6u^5 - 2u^4 - 3u^3 - 3u^2 - 1)$ $\cdot (u^{22} - 2u^{21} + \dots - u + 7)$
$c_3, c_7$	$((u^2 - u + 1)^2)(u^2 + u + 1)^4(u^{12} + u^{11} + \dots - u - 2)$ $\cdot (u^{22} + 2u^{21} + \dots - 145u + 35)$
$c_4$	$u^4(u^2 - 2)^4(u^{11} - 6u^{10} + \dots - 48u + 32)^2$ $\cdot (u^{12} + 15u^{11} + \dots + 596u + 32)$
$c_5, c_9, c_{10}$	$u^4(u^2 - 2)^4$ $\cdot (u^{11} + 2u^{10} - 7u^9 - 14u^8 + 17u^7 + 32u^6 - 20u^5 - 30u^4 + 9u^3 + 8u^2 - 2)^2$ $\cdot (u^{12} - 5u^{11} + \dots - 4u - 4)$
$c_6, c_{12}$	$(u^2 - u + 1)^2(u^2 + u + 1)^4$ $\cdot (u^{12} - u^{11} + 5u^{10} - 4u^9 + 10u^8 - 7u^7 + 7u^6 - 6u^5 - 2u^4 - 3u^3 - 3u^2 - 1)$ $\cdot (u^{22} - 2u^{21} + \dots - u + 7)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$((y^2 + y + 1)^6)(y^{12} - 7y^{11} + \dots - 10y + 1)$ $\cdot (y^{22} - 10y^{21} + \dots - 14085y + 2401)$
$c_2, c_6, c_8$ $c_{12}$	$((y^2 + y + 1)^6)(y^{12} + 9y^{11} + \dots + 6y + 1)$ $\cdot (y^{22} + 14y^{21} + \dots + 307y + 49)$
$c_3, c_7$	$((y^2 + y + 1)^6)(y^{12} - 23y^{11} + \dots + 51y + 4)$ $\cdot (y^{22} - 34y^{21} + \dots + 17965y + 1225)$
$c_4$	$y^4(y - 2)^8(y^{11} - 58y^{10} + \dots + 12928y - 1024)^2$ $\cdot (y^{12} - 35y^{11} + \dots - 202128y + 1024)$
$c_5, c_9, c_{10}$	$y^4(y - 2)^8(y^{11} - 18y^{10} + \dots + 32y - 4)^2$ $\cdot (y^{12} - 15y^{11} + \dots + 16y + 16)$