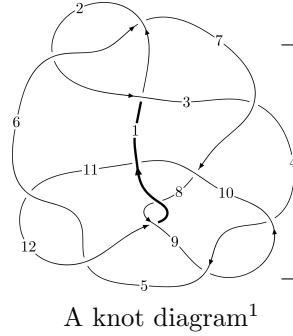
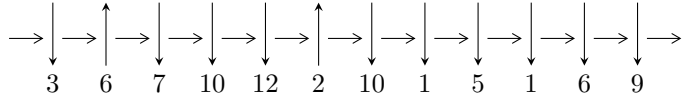


12n<sub>0299</sub> (K12n<sub>0299</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$3,6 \xrightarrow{c_2} 2 \xrightarrow{c_6} 7 \xrightarrow{c_3} 4,10 \xrightarrow{c_7} 8 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 11 \xrightarrow{c_{11}} 12 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \twoheadrightarrow c_4, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -5u^{28} - 22u^{27} + \dots + 2b + 4, -u^{28} - u^{27} + \dots + 2a - 5, u^{29} + 6u^{28} + \dots - 10u - 4 \rangle$$

$$I_2^u = \langle -123u^7a^3 + 644u^7a^2 + \dots - 2637a - 1781, -u^7a^3 - u^7a^2 + \dots + 4a - 1, \\ u^8 - u^7 + 3u^6 - 2u^5 + 3u^4 - 2u^3 - 1 \rangle$$

$$I_3^u = \langle u^{18} - u^{17} + \dots + b + 1, \\ u^{18} + 5u^{16} + u^{15} + 12u^{14} + 3u^{13} + 15u^{12} + 4u^{11} + 8u^{10} - 3u^8 - 4u^7 - 5u^6 - 4u^5 - u^4 + u^2 + a - u - 1, \\ u^{19} - u^{18} + \dots + u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 80 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -5u^{28} - 22u^{27} + \dots + 2b + 4, -u^{28} - u^{27} + \dots + 2a - 5, u^{29} + 6u^{28} + \dots - 10u - 4 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u^{28} + \frac{1}{2}u^{27} + \dots + 2u + \frac{5}{2} \\ \frac{5}{2}u^{28} + 11u^{27} + \dots - \frac{15}{2}u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{3}{4}u^{28} - 5u^{27} + \dots + \frac{71}{4}u + 18 \\ \frac{1}{2}u^{28} + 6u^{27} + \dots - \frac{19}{2}u + 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{28} - \frac{9}{2}u^{27} + \dots + \frac{21}{2}u + \frac{21}{2} \\ \frac{5}{2}u^{28} + 15u^{27} + \dots - \frac{27}{2}u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{28} - \frac{9}{2}u^{27} + \dots + \frac{21}{2}u + \frac{21}{2} \\ -\frac{5}{2}u^{28} - 8u^{27} + \dots - \frac{5}{2}u + 4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{3}{4}u^{28} - 4u^{27} + \dots + \frac{19}{4}u + 3 \\ -\frac{1}{2}u^{28} - 3u^{27} + \dots + \frac{11}{2}u + 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{4}u^{28} - u^{27} + \dots + \frac{5}{4}u + 1 \\ -\frac{5}{2}u^{28} - 11u^{27} + \dots + \frac{9}{2}u + 3 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= u^{28} + 6u^{27} + 26u^{26} + 78u^{25} + 195u^{24} + 404u^{23} + 742u^{22} + 1212u^{21} + 1814u^{20} + 2496u^{19} + 3192u^{18} + 3810u^{17} + 4264u^{16} + 4505u^{15} + 4511u^{14} + 4302u^{13} + 3916u^{12} + 3391u^{11} + 2793u^{10} + 2164u^9 + 1573u^8 + 1049u^7 + 629u^6 + 320u^5 + 122u^4 + 16u^3 - 19u^2 - 14u - 10$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{29} + 16u^{28} + \dots + 108u - 16$
$c_2, c_6$	$u^{29} - 6u^{28} + \dots - 10u + 4$
$c_3$	$u^{29} + 6u^{28} + \dots + 102u + 52$
$c_4, c_5, c_9$ $c_{11}$	$u^{29} + 7u^{27} + \dots + 2u + 1$
$c_7, c_{10}$	$u^{29} - 3u^{28} + \dots - 21u + 1$
$c_8, c_{12}$	$u^{29} + 19u^{28} + \dots + 2304u + 256$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{29} - 4y^{28} + \dots + 28400y - 256$
$c_2, c_6$	$y^{29} + 16y^{28} + \dots + 108y - 16$
$c_3$	$y^{29} - 24y^{28} + \dots + 12588y - 2704$
$c_4, c_5, c_9$ $c_{11}$	$y^{29} + 14y^{28} + \dots - 10y - 1$
$c_7, c_{10}$	$y^{29} - 49y^{28} + \dots + 83y - 1$
$c_8, c_{12}$	$y^{29} + 9y^{28} + \dots + 131072y - 65536$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.529936 + 0.817458I$		
$a = 0.234233 + 0.574816I$	$-1.24507 + 2.13242I$	$-1.54126 - 5.97211I$
$b = 0.345760 - 0.496091I$		
$u = 0.529936 - 0.817458I$		
$a = 0.234233 - 0.574816I$	$-1.24507 - 2.13242I$	$-1.54126 + 5.97211I$
$b = 0.345760 + 0.496091I$		
$u = -0.333397 + 0.883512I$		
$a = -0.369414 + 0.421127I$	$-0.53686 - 1.47819I$	$-4.90590 + 3.46156I$
$b = 0.248910 + 0.466784I$		
$u = -0.333397 - 0.883512I$		
$a = -0.369414 - 0.421127I$	$-0.53686 + 1.47819I$	$-4.90590 - 3.46156I$
$b = 0.248910 - 0.466784I$		
$u = 0.230674 + 1.031600I$		
$a = 0.622836 - 0.242190I$	$-3.27588 + 2.17781I$	$-14.9005 - 2.5155I$
$b = -0.393514 - 0.586648I$		
$u = 0.230674 - 1.031600I$		
$a = 0.622836 + 0.242190I$	$-3.27588 - 2.17781I$	$-14.9005 + 2.5155I$
$b = -0.393514 + 0.586648I$		
$u = 0.752784 + 0.560145I$		
$a = 0.141867 - 0.328248I$	$4.48557 - 3.54679I$	$-5.06701 + 3.83669I$
$b = -0.290661 + 0.167634I$		
$u = 0.752784 - 0.560145I$		
$a = 0.141867 + 0.328248I$	$4.48557 + 3.54679I$	$-5.06701 - 3.83669I$
$b = -0.290661 - 0.167634I$		
$u = -0.929027 + 0.116767I$		
$a = -2.22411 + 0.15082I$	$-2.62991 + 9.91881I$	$-5.74423 - 5.24249I$
$b = -2.04864 + 0.39982I$		
$u = -0.929027 - 0.116767I$		
$a = -2.22411 - 0.15082I$	$-2.62991 - 9.91881I$	$-5.74423 + 5.24249I$
$b = -2.04864 - 0.39982I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.755090 + 0.452937I$ $a = -0.606953 - 0.612743I$ $b = -0.735838 - 0.187764I$	$4.01496 - 0.67489I$	$-6.09853 + 2.29351I$
$u = -0.755090 - 0.452937I$ $a = -0.606953 + 0.612743I$ $b = -0.735838 + 0.187764I$	$4.01496 + 0.67489I$	$-6.09853 - 2.29351I$
$u = -0.864712 + 0.123739I$ $a = 2.27119 + 0.52125I$ $b = 2.02843 + 0.16969I$	$-4.98255 + 2.50011I$	$-6.07998 - 2.74065I$
$u = -0.864712 - 0.123739I$ $a = 2.27119 - 0.52125I$ $b = 2.02843 - 0.16969I$	$-4.98255 - 2.50011I$	$-6.07998 + 2.74065I$
$u = 0.018688 + 1.158270I$ $a = -0.390605 + 0.430620I$ $b = 0.506072 + 0.444376I$	$-1.41808 - 2.24811I$	$-11.36469 + 3.43943I$
$u = 0.018688 - 1.158270I$ $a = -0.390605 - 0.430620I$ $b = 0.506072 - 0.444376I$	$-1.41808 + 2.24811I$	$-11.36469 - 3.43943I$
$u = 0.643120 + 0.992128I$ $a = -0.240554 - 0.246860I$ $b = -0.090211 + 0.397421I$	$3.21603 + 8.80773I$	$-6.26763 - 8.83895I$
$u = 0.643120 - 0.992128I$ $a = -0.240554 + 0.246860I$ $b = -0.090211 - 0.397421I$	$3.21603 - 8.80773I$	$-6.26763 + 8.83895I$
$u = -0.593156 + 1.076560I$ $a = 0.559837 + 0.468168I$ $b = 0.836083 - 0.325004I$	$2.16507 - 4.43085I$	$-9.17518 + 3.77414I$
$u = -0.593156 - 1.076560I$ $a = 0.559837 - 0.468168I$ $b = 0.836083 + 0.325004I$	$2.16507 + 4.43085I$	$-9.17518 - 3.77414I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.396847 + 1.258520I$ $a = 0.13510 - 1.71384I$ $b = -2.10328 - 0.85015I$	$-9.21490 - 1.83630I$	$-10.54114 + 0.46853I$
$u = -0.396847 - 1.258520I$ $a = 0.13510 + 1.71384I$ $b = -2.10328 + 0.85015I$	$-9.21490 + 1.83630I$	$-10.54114 - 0.46853I$
$u = -0.525425 + 1.223980I$ $a = -0.68573 - 1.73877I$ $b = -2.48851 - 0.07427I$	$-8.26868 - 7.55554I$	$-8.73863 + 5.55556I$
$u = -0.525425 - 1.223980I$ $a = -0.68573 + 1.73877I$ $b = -2.48851 + 0.07427I$	$-8.26868 + 7.55554I$	$-8.73863 - 5.55556I$
$u = -0.398180 + 1.298960I$ $a = 0.28856 + 1.51336I$ $b = 2.08069 + 0.22776I$	$-7.09003 + 5.31029I$	$-9.76890 - 2.61442I$
$u = -0.398180 - 1.298960I$ $a = 0.28856 - 1.51336I$ $b = 2.08069 - 0.22776I$	$-7.09003 - 5.31029I$	$-9.76890 + 2.61442I$
$u = -0.533945 + 1.252430I$ $a = 0.25821 + 1.84759I$ $b = 2.45185 + 0.66312I$	$-6.0854 - 15.1894I$	$-8.50713 + 8.09278I$
$u = -0.533945 - 1.252430I$ $a = 0.25821 - 1.84759I$ $b = 2.45185 - 0.66312I$	$-6.0854 + 15.1894I$	$-8.50713 - 8.09278I$
$u = 0.309156$ $a = -0.988933$ $b = 0.305734$	$-0.776150$	$-12.5990$

$$\text{II. } I_2^u = \langle -123u^7a^3 + 644u^7a^2 + \cdots - 2637a - 1781, -u^7a^3 - u^7a^2 + \cdots + 4a - 1, u^8 - u^7 + 3u^6 - 2u^5 + 3u^4 - 2u^3 - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0.0617160a^3u^7 - 0.323131a^2u^7 + \cdots + 1.32313a + 0.893628 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.205218a^3u^7 + 0.497240a^2u^7 + \cdots + 0.502760a - 2.00401 \\ 0.0145509a^3u^7 + 0.517311a^2u^7 + \cdots - 1.51731a - 1.06573 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.202208a^3u^7 - 0.0180632a^2u^7 + \cdots + 0.0180632a - 0.844456 \\ 0.255896a^3u^7 - 0.730055a^2u^7 + \cdots + 1.73006a + 0.119920 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.202208a^3u^7 - 0.0180632a^2u^7 + \cdots + 0.0180632a - 0.844456 \\ 0.0842950a^3u^7 - 0.416959a^2u^7 + \cdots + 1.41696a - 1.24285 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0496739a^3u^7 + 0.406422a^2u^7 + \cdots - 0.406422a - 0.499749 \\ 0.308580a^3u^7 + 1.38435a^2u^7 + \cdots + 0.615655a - 4.53186 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.186653a^3u^7 + 0.708981a^2u^7 + \cdots + 1.29102a - 2.60512 \\ 0.238334a^3u^7 + 0.231811a^2u^7 + \cdots - 1.23181a - 1.66282 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{1636}{1993}u^7a^3 + \frac{3964}{1993}u^7a^2 + \cdots + \frac{4008}{1993}a - \frac{11990}{1993}$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^8 + 5u^7 + 11u^6 + 10u^5 - u^4 - 10u^3 - 6u^2 + 1)^4$
$c_2, c_6$	$(u^8 + u^7 + 3u^6 + 2u^5 + 3u^4 + 2u^3 - 1)^4$
$c_3$	$(u^8 - u^7 - 5u^6 + 4u^5 + 7u^4 - 4u^3 - 2u^2 + 2u - 1)^4$
$c_4, c_5, c_9$ $c_{11}$	$u^{32} - u^{31} + \dots + 830u + 361$
$c_7, c_{10}$	$u^{32} - 5u^{31} + \dots - 27238u + 3169$
$c_8, c_{12}$	$(u^2 - u + 1)^{16}$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^8 - 3y^7 + 19y^6 - 34y^5 + 71y^4 - 66y^3 + 34y^2 - 12y + 1)^4$
$c_2, c_6$	$(y^8 + 5y^7 + 11y^6 + 10y^5 - y^4 - 10y^3 - 6y^2 + 1)^4$
$c_3$	$(y^8 - 11y^7 + 47y^6 - 98y^5 + 103y^4 - 50y^3 + 6y^2 + 1)^4$
$c_4, c_5, c_9$ $c_{11}$	$y^{32} + 15y^{31} + \dots + 1378908y + 130321$
$c_7, c_{10}$	$y^{32} - 21y^{31} + \dots + 68151136y + 10042561$
$c_8, c_{12}$	$(y^2 + y + 1)^{16}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.914675$		
$a = 1.89629 + 0.39729I$	$-5.24109 - 2.02988I$	$-5.82210 + 3.46410I$
$b = 1.88389 + 0.10461I$		
$u = 0.914675$		
$a = 1.89629 - 0.39729I$	$-5.24109 + 2.02988I$	$-5.82210 - 3.46410I$
$b = 1.88389 - 0.10461I$		
$u = 0.914675$		
$a = -2.05963 + 0.11437I$	$-5.24109 + 2.02988I$	$-5.82210 - 3.46410I$
$b = -1.73449 + 0.36339I$		
$u = 0.914675$		
$a = -2.05963 - 0.11437I$	$-5.24109 - 2.02988I$	$-5.82210 + 3.46410I$
$b = -1.73449 - 0.36339I$		
$u = 0.252896 + 0.819281I$		
$a = 0.839815 + 0.637967I$	$4.44352 - 0.75456I$	$-3.18053 - 1.62107I$
$b = 0.38233 + 2.21666I$		
$u = 0.252896 + 0.819281I$		
$a = 1.61466 + 0.45267I$	$4.44352 + 3.30520I$	$-3.18053 - 8.54928I$
$b = -1.49292 + 1.35353I$		
$u = 0.252896 + 0.819281I$		
$a = -0.99481 - 2.12932I$	$4.44352 + 3.30520I$	$-3.18053 - 8.54928I$
$b = -0.03748 - 1.43734I$		
$u = 0.252896 + 0.819281I$		
$a = -2.60176 - 0.33644I$	$4.44352 - 0.75456I$	$-3.18053 - 1.62107I$
$b = 0.310288 - 0.849384I$		
$u = 0.252896 - 0.819281I$		
$a = 0.839815 - 0.637967I$	$4.44352 + 0.75456I$	$-3.18053 + 1.62107I$
$b = 0.38233 - 2.21666I$		
$u = 0.252896 - 0.819281I$		
$a = 1.61466 - 0.45267I$	$4.44352 - 3.30520I$	$-3.18053 + 8.54928I$
$b = -1.49292 - 1.35353I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.252896 - 0.819281I$ $a = -0.99481 + 2.12932I$ $b = -0.03748 + 1.43734I$	$4.44352 - 3.30520I$	$-3.18053 + 8.54928I$
$u = 0.252896 - 0.819281I$ $a = -2.60176 + 0.33644I$ $b = 0.310288 + 0.849384I$	$4.44352 + 0.75456I$	$-3.18053 + 1.62107I$
$u = -0.394459 + 1.112500I$ $a = -0.559029 + 1.096920I$ $b = 0.095737 + 0.849097I$	$0.58960 - 1.60295I$	$-8.42240 + 1.05392I$
$u = -0.394459 + 1.112500I$ $a = -0.650891 + 0.316842I$ $b = 0.99981 + 1.05461I$	$0.58960 - 1.60295I$	$-8.42240 + 1.05392I$
$u = -0.394459 + 1.112500I$ $a = 1.265140 + 0.509213I$ $b = 0.035342 - 0.694019I$	$0.58960 - 5.66272I$	$-8.42240 + 7.98213I$
$u = -0.394459 + 1.112500I$ $a = 0.564174 - 0.168272I$ $b = 1.06554 - 1.20660I$	$0.58960 - 5.66272I$	$-8.42240 + 7.98213I$
$u = -0.394459 - 1.112500I$ $a = -0.559029 - 1.096920I$ $b = 0.095737 - 0.849097I$	$0.58960 + 1.60295I$	$-8.42240 - 1.05392I$
$u = -0.394459 - 1.112500I$ $a = -0.650891 - 0.316842I$ $b = 0.99981 - 1.05461I$	$0.58960 + 1.60295I$	$-8.42240 - 1.05392I$
$u = -0.394459 - 1.112500I$ $a = 1.265140 - 0.509213I$ $b = 0.035342 + 0.694019I$	$0.58960 + 5.66272I$	$-8.42240 - 7.98213I$
$u = -0.394459 - 1.112500I$ $a = 0.564174 + 0.168272I$ $b = 1.06554 + 1.20660I$	$0.58960 + 5.66272I$	$-8.42240 - 7.98213I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.473514 + 1.273020I$ $a = -0.278598 + 1.324080I$ $b = -2.19588 + 0.14617I$	$-9.13765 + 2.90536I$	$-8.98443 + 0.46988I$
$u = 0.473514 + 1.273020I$ $a = 0.15293 - 1.46513I$ $b = 2.23599 - 0.76370I$	$-9.13765 + 6.96513I$	$-8.98443 - 6.45832I$
$u = 0.473514 + 1.273020I$ $a = 0.46276 - 1.55281I$ $b = 1.81750 - 0.27231I$	$-9.13765 + 2.90536I$	$-8.98443 + 0.46988I$
$u = 0.473514 + 1.273020I$ $a = -0.04692 + 1.73899I$ $b = -1.93756 + 0.49908I$	$-9.13765 + 6.96513I$	$-8.98443 - 6.45832I$
$u = 0.473514 - 1.273020I$ $a = -0.278598 - 1.324080I$ $b = -2.19588 - 0.14617I$	$-9.13765 - 2.90536I$	$-8.98443 - 0.46988I$
$u = 0.473514 - 1.273020I$ $a = 0.15293 + 1.46513I$ $b = 2.23599 + 0.76370I$	$-9.13765 - 6.96513I$	$-8.98443 + 6.45832I$
$u = 0.473514 - 1.273020I$ $a = 0.46276 + 1.55281I$ $b = 1.81750 + 0.27231I$	$-9.13765 - 2.90536I$	$-8.98443 - 0.46988I$
$u = 0.473514 - 1.273020I$ $a = -0.04692 - 1.73899I$ $b = -1.93756 - 0.49908I$	$-9.13765 - 6.96513I$	$-8.98443 + 6.45832I$
$u = -0.578577$ $a = -1.046970 + 0.657077I$ $b = -0.322351 + 1.227360I$	$3.58052 - 2.02988I$	$-5.00319 + 3.46410I$
$u = -0.578577$ $a = -1.046970 - 0.657077I$ $b = -0.322351 - 1.227360I$	$3.58052 + 2.02988I$	$-5.00319 - 3.46410I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.578577$		
$a = -0.55714 + 2.12134I$	$3.58052 - 2.02988I$	$-5.00319 + 3.46410I$
$b = -0.605755 + 0.380170I$		
$u = -0.578577$		
$a = -0.55714 - 2.12134I$	$3.58052 + 2.02988I$	$-5.00319 - 3.46410I$
$b = -0.605755 - 0.380170I$		

**III.**

$$I_3^u = \langle u^{18} - u^{17} + \dots + b + 1, u^{18} + 5u^{16} + \dots + a - 1, u^{19} - u^{18} + \dots + u - 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{18} - 5u^{16} + \dots + u + 1 \\ -u^{18} + u^{17} + \dots + 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2u^{18} - 3u^{17} + \dots - 4u + 2 \\ -u^{18} - 4u^{16} + \dots + u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{18} - 5u^{16} + \dots + u + 1 \\ -2u^{18} + 2u^{17} + \dots + 3u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{18} - 5u^{16} + \dots + u + 1 \\ -2u^{18} + 2u^{17} + \dots + 3u - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{18} + 2u^{17} + \dots + 4u - 2 \\ u^{18} - u^{17} + \dots - 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^{18} - 2u^{17} + \dots - 4u + 1 \\ -u^{17} + u^{16} + \dots - u + 3 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $-2u^{17} + 3u^{16} - 11u^{15} + 15u^{14} - 28u^{13} + 35u^{12} - 39u^{11} + 41u^{10} - 30u^9 + 20u^8 - 10u^7 - 4u^6 - 3u^5 - 5u^3 + 8u^2 - 3u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{19} - 11u^{18} + \dots - 5u + 1$
$c_2$	$u^{19} - u^{18} + \dots + u - 1$
$c_3$	$u^{19} + u^{18} + \dots - u - 1$
$c_4, c_{11}$	$u^{19} + 8u^{17} + \dots + 3u - 1$
$c_5, c_9$	$u^{19} + 8u^{17} + \dots + 3u + 1$
$c_6$	$u^{19} + u^{18} + \dots + u + 1$
$c_7, c_{10}$	$u^{19} - 3u^{18} + \dots - 2u - 1$
$c_8$	$u^{19} + 2u^{18} + \dots + 3u - 1$
$c_{12}$	$u^{19} - 2u^{18} + \dots + 3u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{19} - y^{18} + \dots - y - 1$
$c_2, c_6$	$y^{19} + 11y^{18} + \dots - 5y - 1$
$c_3$	$y^{19} - 13y^{18} + \dots - 11y - 1$
$c_4, c_5, c_9$ $c_{11}$	$y^{19} + 16y^{18} + \dots - 21y - 1$
$c_7, c_{10}$	$y^{19} - 3y^{18} + \dots - 8y - 1$
$c_8, c_{12}$	$y^{19} + 8y^{18} + \dots + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.432409 + 0.844316I$ $a = -0.329441 + 0.448815I$ $b = -0.236489 - 0.472224I$	$-1.79244 - 1.81593I$	$-13.41650 + 0.65086I$
$u = -0.432409 - 0.844316I$ $a = -0.329441 - 0.448815I$ $b = -0.236489 + 0.472224I$	$-1.79244 + 1.81593I$	$-13.41650 - 0.65086I$
$u = 0.355611 + 1.040830I$ $a = 1.62344 + 0.58218I$ $b = -0.02864 + 1.89676I$	$2.78146 - 0.05347I$	$-7.84525 - 1.09777I$
$u = 0.355611 - 1.040830I$ $a = 1.62344 - 0.58218I$ $b = -0.02864 - 1.89676I$	$2.78146 + 0.05347I$	$-7.84525 + 1.09777I$
$u = 0.890704$ $a = -2.06630$ $b = -1.84047$	$-5.60220$	$-6.95090$
$u = -0.326702 + 1.147210I$ $a = -0.125098 - 0.538940I$ $b = 0.659149 + 0.032559I$	$1.46823 - 3.78813I$	$-6.32142 + 3.96435I$
$u = -0.326702 - 1.147210I$ $a = -0.125098 + 0.538940I$ $b = 0.659149 - 0.032559I$	$1.46823 + 3.78813I$	$-6.32142 - 3.96435I$
$u = 0.536152 + 1.067450I$ $a = -1.382960 - 0.137280I$ $b = -0.59494 - 1.54985I$	$4.08792 + 6.74742I$	$-5.06014 - 6.00387I$
$u = 0.536152 - 1.067450I$ $a = -1.382960 + 0.137280I$ $b = -0.59494 + 1.54985I$	$4.08792 - 6.74742I$	$-5.06014 + 6.00387I$
$u = 0.101153 + 0.760282I$ $a = 1.81914 + 1.18798I$ $b = -0.71919 + 1.50323I$	$4.29021 + 2.32381I$	$-5.29787 - 0.37944I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.101153 - 0.760282I$	$4.29021 - 2.32381I$	$-5.29787 + 0.37944I$
$a = 1.81914 - 1.18798I$		
$b = -0.71919 - 1.50323I$		
$u = -0.682478 + 0.327459I$	$5.43330 - 0.84474I$	$0.382477 + 1.325719I$
$a = -0.427115 + 0.321033I$		
$b = 0.186371 - 0.358960I$		
$u = -0.682478 - 0.327459I$	$5.43330 + 0.84474I$	$0.382477 - 1.325719I$
$a = -0.427115 - 0.321033I$		
$b = 0.186371 + 0.358960I$		
$u = -0.557218 + 1.113290I$	$3.17508 - 3.96127I$	$-2.77988 + 1.70184I$
$a = 0.172420 + 0.230688I$		
$b = -0.352897 + 0.063409I$		
$u = -0.557218 - 1.113290I$	$3.17508 + 3.96127I$	$-2.77988 - 1.70184I$
$a = 0.172420 - 0.230688I$		
$b = -0.352897 - 0.063409I$		
$u = 0.587141 + 0.436351I$	$5.94319 - 2.22864I$	$-0.25827 + 1.68244I$
$a = -0.56266 - 1.67318I$		
$b = 0.399733 - 1.227910I$		
$u = 0.587141 - 0.436351I$	$5.94319 + 2.22864I$	$-0.25827 - 1.68244I$
$a = -0.56266 + 1.67318I$		
$b = 0.399733 + 1.227910I$		
$u = 0.473398 + 1.262070I$	$-9.42638 + 4.85839I$	$-9.92768 - 3.28951I$
$a = 0.24543 - 1.57752I$		
$b = 2.10713 - 0.43705I$		
$u = 0.473398 - 1.262070I$	$-9.42638 - 4.85839I$	$-9.92768 + 3.28951I$
$a = 0.24543 + 1.57752I$		
$b = 2.10713 + 0.43705I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^8 + 5u^7 + 11u^6 + 10u^5 - u^4 - 10u^3 - 6u^2 + 1)^4$ $\cdot (u^{19} - 11u^{18} + \dots - 5u + 1)(u^{29} + 16u^{28} + \dots + 108u - 16)$
$c_2$	$((u^8 + u^7 + \dots + 2u^3 - 1)^4)(u^{19} - u^{18} + \dots + u - 1)$ $\cdot (u^{29} - 6u^{28} + \dots - 10u + 4)$
$c_3$	$(u^8 - u^7 - 5u^6 + 4u^5 + 7u^4 - 4u^3 - 2u^2 + 2u - 1)^4$ $\cdot (u^{19} + u^{18} + \dots - u - 1)(u^{29} + 6u^{28} + \dots + 102u + 52)$
$c_4, c_{11}$	$(u^{19} + 8u^{17} + \dots + 3u - 1)(u^{29} + 7u^{27} + \dots + 2u + 1)$ $\cdot (u^{32} - u^{31} + \dots + 830u + 361)$
$c_5, c_9$	$(u^{19} + 8u^{17} + \dots + 3u + 1)(u^{29} + 7u^{27} + \dots + 2u + 1)$ $\cdot (u^{32} - u^{31} + \dots + 830u + 361)$
$c_6$	$((u^8 + u^7 + \dots + 2u^3 - 1)^4)(u^{19} + u^{18} + \dots + u + 1)$ $\cdot (u^{29} - 6u^{28} + \dots - 10u + 4)$
$c_7, c_{10}$	$(u^{19} - 3u^{18} + \dots - 2u - 1)(u^{29} - 3u^{28} + \dots - 21u + 1)$ $\cdot (u^{32} - 5u^{31} + \dots - 27238u + 3169)$
$c_8$	$((u^2 - u + 1)^{16})(u^{19} + 2u^{18} + \dots + 3u - 1)$ $\cdot (u^{29} + 19u^{28} + \dots + 2304u + 256)$
$c_{12}$	$((u^2 - u + 1)^{16})(u^{19} - 2u^{18} + \dots + 3u + 1)$ $\cdot (u^{29} + 19u^{28} + \dots + 2304u + 256)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^8 - 3y^7 + 19y^6 - 34y^5 + 71y^4 - 66y^3 + 34y^2 - 12y + 1)^4$ $\cdot (y^{19} - y^{18} + \dots - y - 1)(y^{29} - 4y^{28} + \dots + 28400y - 256)$
$c_2, c_6$	$(y^8 + 5y^7 + 11y^6 + 10y^5 - y^4 - 10y^3 - 6y^2 + 1)^4$ $\cdot (y^{19} + 11y^{18} + \dots - 5y - 1)(y^{29} + 16y^{28} + \dots + 108y - 16)$
$c_3$	$(y^8 - 11y^7 + 47y^6 - 98y^5 + 103y^4 - 50y^3 + 6y^2 + 1)^4$ $\cdot (y^{19} - 13y^{18} + \dots - 11y - 1)(y^{29} - 24y^{28} + \dots + 12588y - 2704)$
$c_4, c_5, c_9$ $c_{11}$	$(y^{19} + 16y^{18} + \dots - 21y - 1)(y^{29} + 14y^{28} + \dots - 10y - 1)$ $\cdot (y^{32} + 15y^{31} + \dots + 1378908y + 130321)$
$c_7, c_{10}$	$(y^{19} - 3y^{18} + \dots - 8y - 1)(y^{29} - 49y^{28} + \dots + 83y - 1)$ $\cdot (y^{32} - 21y^{31} + \dots + 68151136y + 10042561)$
$c_8, c_{12}$	$((y^2 + y + 1)^{16})(y^{19} + 8y^{18} + \dots + 3y - 1)$ $\cdot (y^{29} + 9y^{28} + \dots + 131072y - 65536)$