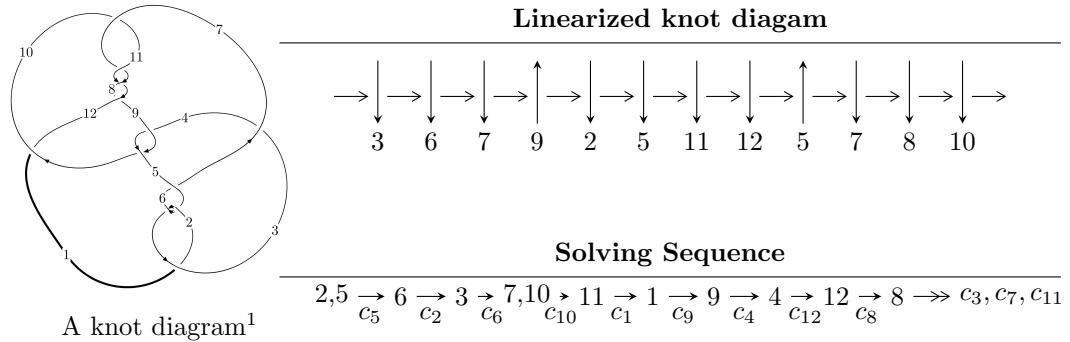


$12n_{0303}$ ($K12n_{0303}$)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{23} + u^{22} + \dots + b - 2u, -3u^{23} - 6u^{22} + \dots + 2a + 7, u^{26} + 3u^{25} + \dots - 9u^2 + 1 \rangle$$

$$I_2^u = \langle b, a^2 + au - u^2 - a + 2u - 1, u^3 - u^2 + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 32 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{23} + u^{22} + \cdots + b - 2u, -3u^{23} - 6u^{22} + \cdots + 2a + 7, u^{26} + 3u^{25} + \cdots - 9u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{3}{2}u^{23} + 3u^{22} + \cdots - 4u - \frac{7}{2} \\ -u^{23} - u^{22} + \cdots + 2u^2 + 2u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^{25} + \frac{7}{2}u^{24} + \cdots - \frac{11}{2}u - 3 \\ -\frac{1}{2}u^{25} - \frac{3}{2}u^{24} + \cdots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{5}{2}u^{23} + 4u^{22} + \cdots - 6u - \frac{7}{2} \\ -u^{23} - u^{22} + \cdots + 2u^2 + 2u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^7 - 2u^5 + 2u^3 - 2u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} \frac{1}{2}u^{23} + u^{22} + \cdots + 2u + \frac{1}{2} \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{1}{2}u^{24} - 2u^{22} + \cdots - \frac{7}{2}u + 1 \\ -\frac{1}{2}u^{25} - \frac{3}{2}u^{24} + \cdots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{11}{2}u^{25} - 12u^{24} + \frac{1}{2}u^{23} + 30u^{22} - 13u^{21} - 105u^{20} - 42u^{19} + \frac{337}{2}u^{18} + 57u^{17} - 325u^{16} - 196u^{15} + 356u^{14} + 198u^{13} - \frac{979}{2}u^{12} - 283u^{11} + \frac{789}{2}u^{10} + \frac{353}{2}u^9 - \frac{809}{2}u^8 - \frac{297}{2}u^7 + 250u^6 + 41u^5 - 154u^4 - 16u^3 + \frac{149}{2}u^2 + 13u - \frac{33}{2}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_6	$u^{26} + 5u^{25} + \cdots + 18u + 1$
c_2, c_5	$u^{26} + 3u^{25} + \cdots - 9u^2 + 1$
c_3	$u^{26} - 3u^{25} + \cdots + 6516u + 1009$
c_4, c_9	$u^{26} - u^{25} + \cdots + 96u + 64$
c_7, c_8, c_{10} c_{11}	$u^{26} + 4u^{25} + \cdots - 3u + 1$
c_{12}	$u^{26} + 28u^{24} + \cdots - 31u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_6	$y^{26} + 35y^{25} + \cdots - 74y + 1$
c_2, c_5	$y^{26} - 5y^{25} + \cdots - 18y + 1$
c_3	$y^{26} + 95y^{25} + \cdots - 36103574y + 1018081$
c_4, c_9	$y^{26} - 35y^{25} + \cdots - 58368y + 4096$
c_7, c_8, c_{10} c_{11}	$y^{26} - 28y^{25} + \cdots - 27y + 1$
c_{12}	$y^{26} + 56y^{25} + \cdots - 391y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.697878 + 0.750786I$		
$a = 0.950274 + 0.282069I$	$3.30312 - 1.30372I$	$-2.90180 + 1.28901I$
$b = -0.969430 + 0.478608I$		
$u = 0.697878 - 0.750786I$		
$a = 0.950274 - 0.282069I$	$3.30312 + 1.30372I$	$-2.90180 - 1.28901I$
$b = -0.969430 - 0.478608I$		
$u = -1.05556$		
$a = -1.13582$	-6.55918	-13.9020
$b = -1.20261$		
$u = -0.714104 + 0.530028I$		
$a = -0.308272 + 1.024340I$	$-7.39553 + 1.99902I$	$-12.68261 - 2.64464I$
$b = -0.222426 + 0.888370I$		
$u = -0.714104 - 0.530028I$		
$a = -0.308272 - 1.024340I$	$-7.39553 - 1.99902I$	$-12.68261 + 2.64464I$
$b = -0.222426 - 0.888370I$		
$u = 0.426539 + 0.776149I$		
$a = -1.244140 - 0.230526I$	$-1.37386 + 1.46827I$	$-7.40504 - 0.61110I$
$b = 1.405990 + 0.009237I$		
$u = 0.426539 - 0.776149I$		
$a = -1.244140 + 0.230526I$	$-1.37386 - 1.46827I$	$-7.40504 + 0.61110I$
$b = 1.405990 - 0.009237I$		
$u = 0.924653 + 0.644299I$		
$a = -0.192140 - 0.877647I$	$2.53585 - 3.91698I$	$-4.21369 + 6.80514I$
$b = 0.922849 + 0.070450I$		
$u = 0.924653 - 0.644299I$		
$a = -0.192140 + 0.877647I$	$2.53585 + 3.91698I$	$-4.21369 - 6.80514I$
$b = 0.922849 - 0.070450I$		
$u = 1.032140 + 0.523292I$		
$a = 0.16264 + 1.48931I$	$-3.36202 - 6.28703I$	$-10.76890 + 5.79025I$
$b = -1.372650 + 0.239227I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.032140 - 0.523292I$		
$a = 0.16264 - 1.48931I$	$-3.36202 + 6.28703I$	$-10.76890 - 5.79025I$
$b = -1.372650 - 0.239227I$		
$u = -0.826543$		
$a = 0.499620$	-1.35750	-5.74160
$b = 0.424946$		
$u = 0.904709 + 0.855635I$		
$a = -0.749040 + 0.396223I$	$0.45711 - 3.16518I$	$-10.09379 + 2.71963I$
$b = 0.015583 - 1.255880I$		
$u = 0.904709 - 0.855635I$		
$a = -0.749040 - 0.396223I$	$0.45711 + 3.16518I$	$-10.09379 - 2.71963I$
$b = 0.015583 + 1.255880I$		
$u = -0.874451 + 0.958708I$		
$a = -1.34597 + 0.77169I$	$6.92052 - 3.79217I$	$-7.74212 + 0.87029I$
$b = 1.85003 - 0.54896I$		
$u = -0.874451 - 0.958708I$		
$a = -1.34597 - 0.77169I$	$6.92052 + 3.79217I$	$-7.74212 - 0.87029I$
$b = 1.85003 + 0.54896I$		
$u = -0.932825 + 0.952507I$		
$a = 1.48560 - 0.97786I$	$13.70930 + 0.63054I$	$-5.09956 + 0.08472I$
$b = -2.02844 + 0.13031I$		
$u = -0.932825 - 0.952507I$		
$a = 1.48560 + 0.97786I$	$13.70930 - 0.63054I$	$-5.09956 - 0.08472I$
$b = -2.02844 - 0.13031I$		
$u = -1.007520 + 0.885407I$		
$a = 1.72924 - 1.22466I$	$6.48279 + 10.56660I$	$-8.37835 - 5.32202I$
$b = -1.78041 - 0.65102I$		
$u = -1.007520 - 0.885407I$		
$a = 1.72924 + 1.22466I$	$6.48279 - 10.56660I$	$-8.37835 + 5.32202I$
$b = -1.78041 + 0.65102I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.977518 + 0.926314I$		
$a = -1.61355 + 1.11637I$	$13.5604 + 6.2675I$	$-5.43427 - 4.61670I$
$b = 1.99598 + 0.29162I$		
$u = -0.977518 - 0.926314I$		
$a = -1.61355 - 1.11637I$	$13.5604 - 6.2675I$	$-5.43427 + 4.61670I$
$b = 1.99598 - 0.29162I$		
$u = 0.605940$		
$a = 3.65946$	-9.68489	0.985630
$b = -0.461168$		
$u = -0.507505 + 0.285828I$		
$a = 0.417815 - 0.836271I$	$-0.698170 + 0.981366I$	$-8.43360 - 6.86703I$
$b = 0.046187 - 0.679181I$		
$u = -0.507505 - 0.285828I$		
$a = 0.417815 + 0.836271I$	$-0.698170 - 0.981366I$	$-8.43360 + 6.86703I$
$b = 0.046187 + 0.679181I$		
$u = 0.332169$		
$a = -2.60819$	-1.32945	-6.03470
$b = 0.512315$		

$$\text{II. } I_2^u = \langle b, a^2 + au - u^2 - a + 2u - 1, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ -u^2 + u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} au + 2a \\ u^2a - au - a \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^2 - a + u - 2 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -au - 2a + u - 1 \\ -u^2a + au + a \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-u^2a - 3u^2 - a + 8u - 13$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$(u^3 - u^2 + 2u - 1)^2$
c_2	$(u^3 + u^2 - 1)^2$
c_4, c_9	u^6
c_5	$(u^3 - u^2 + 1)^2$
c_6	$(u^3 + u^2 + 2u + 1)^2$
c_7, c_8	$(u^2 + u - 1)^3$
c_{10}, c_{11}, c_{12}	$(u^2 - u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_5	$(y^3 - y^2 + 2y - 1)^2$
c_4, c_9	y^6
c_7, c_8, c_{10} c_{11}, c_{12}	$(y^2 - 3y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$		
$a = 0.198308 - 1.205210I$	$-5.85852 - 2.82812I$	$-8.44207 + 3.24268I$
$b = 0$		
$u = 0.877439 + 0.744862I$		
$a = -0.075747 + 0.460350I$	$2.03717 - 2.82812I$	$-5.93195 + 1.57712I$
$b = 0$		
$u = 0.877439 - 0.744862I$		
$a = 0.198308 + 1.205210I$	$-5.85852 + 2.82812I$	$-8.44207 - 3.24268I$
$b = 0$		
$u = 0.877439 - 0.744862I$		
$a = -0.075747 - 0.460350I$	$2.03717 + 2.82812I$	$-5.93195 - 1.57712I$
$b = 0$		
$u = -0.754878$		
$a = -1.08457$	-2.10041	-19.0460
$b = 0$		
$u = -0.754878$		
$a = 2.83945$	-9.99610	-25.2060
$b = 0$		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^3 - u^2 + 2u - 1)^2)(u^{26} + 5u^{25} + \dots + 18u + 1)$
c_2	$((u^3 + u^2 - 1)^2)(u^{26} + 3u^{25} + \dots - 9u^2 + 1)$
c_3	$((u^3 - u^2 + 2u - 1)^2)(u^{26} - 3u^{25} + \dots + 6516u + 1009)$
c_4, c_9	$u^6(u^{26} - u^{25} + \dots + 96u + 64)$
c_5	$((u^3 - u^2 + 1)^2)(u^{26} + 3u^{25} + \dots - 9u^2 + 1)$
c_6	$((u^3 + u^2 + 2u + 1)^2)(u^{26} + 5u^{25} + \dots + 18u + 1)$
c_7, c_8	$((u^2 + u - 1)^3)(u^{26} + 4u^{25} + \dots - 3u + 1)$
c_{10}, c_{11}	$((u^2 - u - 1)^3)(u^{26} + 4u^{25} + \dots - 3u + 1)$
c_{12}	$((u^2 - u - 1)^3)(u^{26} + 28u^{24} + \dots - 31u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_6	$((y^3 + 3y^2 + 2y - 1)^2)(y^{26} + 35y^{25} + \dots - 74y + 1)$
c_2, c_5	$((y^3 - y^2 + 2y - 1)^2)(y^{26} - 5y^{25} + \dots - 18y + 1)$
c_3	$((y^3 + 3y^2 + 2y - 1)^2)(y^{26} + 95y^{25} + \dots - 3.61036 \times 10^7 y + 1018081)$
c_4, c_9	$y^6(y^{26} - 35y^{25} + \dots - 58368y + 4096)$
c_7, c_8, c_{10} c_{11}	$((y^2 - 3y + 1)^3)(y^{26} - 28y^{25} + \dots - 27y + 1)$
c_{12}	$((y^2 - 3y + 1)^3)(y^{26} + 56y^{25} + \dots - 391y + 1)$