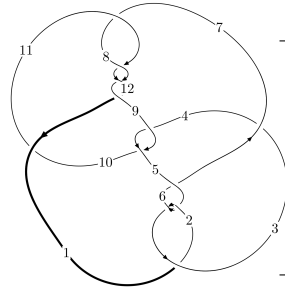
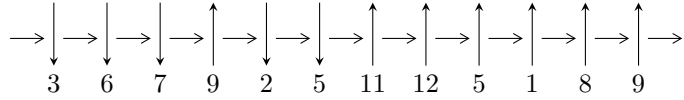


12n<sub>0304</sub> (K12n<sub>0304</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_5} 6 \xrightarrow{c_2} 3 \xrightarrow{c_6} 7,9 \xrightarrow{c_9} 10 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 11 \xrightarrow{c_4} 4 \xrightarrow{c_{12}} 12 \xrightarrow{c_8} 8 \twoheadrightarrow c_3, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2u^{40} - 5u^{39} + \dots + b - 2, 2u^{39} + 5u^{38} + \dots + 2a - 7, u^{41} + 3u^{40} + \dots - 4u + 1 \rangle$$

$$I_2^u = \langle b, a^2 - au - u^2 + a + 2u - 1, u^3 - u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 47 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2u^{40} - 5u^{39} + \dots + b - 2, 2u^{39} + 5u^{38} + \dots + 2a - 7, u^{41} + 3u^{40} + \dots - 4u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{39} - \frac{5}{2}u^{38} + \dots + 4u + \frac{7}{2} \\ 2u^{40} + 5u^{39} + \dots - 12u + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^{40} + 4u^{39} + \dots - 8u + \frac{11}{2} \\ 2u^{40} + 5u^{39} + \dots - 12u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{40} + \frac{3}{2}u^{39} + \dots - \frac{1}{2}u + 4 \\ \frac{3}{2}u^{40} + \frac{9}{2}u^{39} + \dots - \frac{21}{2}u + \frac{3}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^7 - 2u^5 + 2u^3 - 2u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^{38} - u^{37} + \dots - 6u - \frac{1}{2} \\ -u^{12} + 2u^{10} - 4u^8 + 4u^6 + 2u^5 - 3u^4 - 2u^3 + 2u^2 + 2u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u^{39} + u^{38} + \dots + \frac{5}{2}u + 2 \\ -\frac{1}{2}u^{40} - \frac{3}{2}u^{39} + \dots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-\frac{19}{2}u^{40} - 20u^{39} + \dots + 75u - \frac{1}{2}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{41} + 15u^{40} + \dots + 54u + 1$
$c_2, c_5$	$u^{41} + 3u^{40} + \dots - 4u + 1$
$c_3$	$u^{41} - 3u^{40} + \dots + 2u + 1$
$c_4, c_9$	$u^{41} - u^{40} + \dots + 32u + 64$
$c_7, c_8, c_{11}$ $c_{12}$	$u^{41} - 4u^{40} + \dots - u - 1$
$c_{10}$	$u^{41} + 6u^{40} + \dots - 25u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{41} + 25y^{40} + \dots + 1814y - 1$
$c_2, c_5$	$y^{41} - 15y^{40} + \dots + 54y - 1$
$c_3$	$y^{41} - 35y^{40} + \dots + 54y - 1$
$c_4, c_9$	$y^{41} + 35y^{40} + \dots - 23552y - 4096$
$c_7, c_8, c_{11}$ $c_{12}$	$y^{41} - 46y^{40} + \dots - y - 1$
$c_{10}$	$y^{41} + 38y^{40} + \dots + 419y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.554966 + 0.821093I$ $a = 0.497003 - 1.229360I$ $b = -0.36616 + 1.39788I$	$-2.41826 - 3.80802I$	$3.60583 + 3.47707I$
$u = -0.554966 - 0.821093I$ $a = 0.497003 + 1.229360I$ $b = -0.36616 - 1.39788I$	$-2.41826 + 3.80802I$	$3.60583 - 3.47707I$
$u = -0.827605 + 0.515025I$ $a = -0.328705 + 0.303123I$ $b = -0.241607 + 0.924234I$	$1.70931 + 2.07723I$	$4.47890 - 3.71404I$
$u = -0.827605 - 0.515025I$ $a = -0.328705 - 0.303123I$ $b = -0.241607 - 0.924234I$	$1.70931 - 2.07723I$	$4.47890 + 3.71404I$
$u = 0.776023 + 0.578782I$ $a = 1.72542 + 0.58271I$ $b = -0.884835 + 0.226791I$	$1.60480 - 0.80076I$	$5.09218 - 0.58482I$
$u = 0.776023 - 0.578782I$ $a = 1.72542 - 0.58271I$ $b = -0.884835 - 0.226791I$	$1.60480 + 0.80076I$	$5.09218 + 0.58482I$
$u = -1.04869$ $a = 0.0572806$ $b = -1.17662$	$3.30786$	$2.08440$
$u = -0.613160 + 0.856728I$ $a = -0.94977 + 1.28570I$ $b = 0.59049 - 1.37882I$	$4.75528 - 6.89936I$	$6.92603 + 2.94505I$
$u = -0.613160 - 0.856728I$ $a = -0.94977 - 1.28570I$ $b = 0.59049 + 1.37882I$	$4.75528 + 6.89936I$	$6.92603 - 2.94505I$
$u = -0.851706 + 0.644533I$ $a = 0.208645 - 1.142410I$ $b = 0.123688 - 0.806905I$	$10.80640 + 2.51167I$	$3.89555 - 1.99801I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.851706 - 0.644533I$ $a = 0.208645 + 1.142410I$ $b = 0.123688 + 0.806905I$	$10.80640 - 2.51167I$	$3.89555 + 1.99801I$
$u = 0.607006 + 0.678640I$ $a = -2.19270 - 0.14272I$ $b = 1.058510 - 0.256762I$	$8.39222 + 0.77239I$	$9.02070 + 0.54313I$
$u = 0.607006 - 0.678640I$ $a = -2.19270 + 0.14272I$ $b = 1.058510 + 0.256762I$	$8.39222 - 0.77239I$	$9.02070 - 0.54313I$
$u = -0.468903 + 0.772766I$ $a = 0.050516 + 1.153690I$ $b = 0.094850 - 1.373440I$	$-2.97142 + 0.55275I$	$2.30390 - 2.65158I$
$u = -0.468903 - 0.772766I$ $a = 0.050516 - 1.153690I$ $b = 0.094850 + 1.373440I$	$-2.97142 - 0.55275I$	$2.30390 + 2.65158I$
$u = 0.917493 + 0.603542I$ $a = -1.30840 - 0.95232I$ $b = 0.987613 - 0.046245I$	$1.14349 - 3.91148I$	$2.83783 + 7.19272I$
$u = 0.917493 - 0.603542I$ $a = -1.30840 + 0.95232I$ $b = 0.987613 + 0.046245I$	$1.14349 + 3.91148I$	$2.83783 - 7.19272I$
$u = 1.145870 + 0.098490I$ $a = 0.557107 + 1.022870I$ $b = -0.43743 + 1.53434I$	$-1.90305 - 5.90674I$	$0.65317 + 3.76442I$
$u = 1.145870 - 0.098490I$ $a = 0.557107 - 1.022870I$ $b = -0.43743 - 1.53434I$	$-1.90305 + 5.90674I$	$0.65317 - 3.76442I$
$u = 1.150510 + 0.030891I$ $a = -0.178270 - 1.012240I$ $b = 0.13939 - 1.59211I$	$-8.52969 - 2.39687I$	$-2.76728 + 3.02467I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.150510 - 0.030891I$ $a = -0.178270 + 1.012240I$ $b = 0.13939 + 1.59211I$	$-8.52969 + 2.39687I$	$-2.76728 - 3.02467I$
$u = 0.879522 + 0.766671I$ $a = 0.349468 - 0.635389I$ $b = -0.011712 + 0.469579I$	$3.60760 - 2.89390I$	$-5.91956 + 4.41976I$
$u = 0.879522 - 0.766671I$ $a = 0.349468 + 0.635389I$ $b = -0.011712 - 0.469579I$	$3.60760 + 2.89390I$	$-5.91956 - 4.41976I$
$u = -0.318016 + 0.760424I$ $a = -0.76042 - 1.22775I$ $b = 0.286457 + 1.371580I$	$3.09276 + 3.48744I$	$6.36068 - 3.00060I$
$u = -0.318016 - 0.760424I$ $a = -0.76042 + 1.22775I$ $b = 0.286457 - 1.371580I$	$3.09276 - 3.48744I$	$6.36068 + 3.00060I$
$u = -0.803311 + 0.150840I$ $a = 0.146401 - 0.020062I$ $b = 0.412782 - 0.447090I$	$-1.348790 + 0.350630I$	$-5.34995 - 0.74571I$
$u = -0.803311 - 0.150840I$ $a = 0.146401 + 0.020062I$ $b = 0.412782 + 0.447090I$	$-1.348790 - 0.350630I$	$-5.34995 + 0.74571I$
$u = -1.057040 + 0.554919I$ $a = -1.211900 - 0.182135I$ $b = -0.13020 + 1.48466I$	$0.94110 + 1.27702I$	$2.95191 - 1.84094I$
$u = -1.057040 - 0.554919I$ $a = -1.211900 + 0.182135I$ $b = -0.13020 - 1.48466I$	$0.94110 - 1.27702I$	$2.95191 + 1.84094I$
$u = 1.004470 + 0.646364I$ $a = 1.16107 + 1.33962I$ $b = -1.216110 - 0.239593I$	$7.24069 - 5.93073I$	$6.53956 + 5.01754I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.004470 - 0.646364I$ $a = 1.16107 - 1.33962I$ $b = -1.216110 + 0.239593I$	$7.24069 + 5.93073I$	$6.53956 - 5.01754I$
$u = 0.891105 + 0.826186I$ $a = -0.68311 + 1.33083I$ $b = 0.038155 - 1.007650I$	$10.04850 - 3.07313I$	$5.86480 + 2.85684I$
$u = 0.891105 - 0.826186I$ $a = -0.68311 - 1.33083I$ $b = 0.038155 + 1.007650I$	$10.04850 + 3.07313I$	$5.86480 - 2.85684I$
$u = -1.066370 + 0.630817I$ $a = 1.70734 + 0.08552I$ $b = -0.22070 - 1.52920I$	$-4.70291 + 4.72137I$	$0. - 2.49884I$
$u = -1.066370 - 0.630817I$ $a = 1.70734 - 0.08552I$ $b = -0.22070 + 1.52920I$	$-4.70291 - 4.72137I$	$0. + 2.49884I$
$u = -1.067020 + 0.674301I$ $a = -2.03641 - 0.00933I$ $b = 0.45680 + 1.50432I$	$-3.95261 + 9.40997I$	$2.00000 - 7.76812I$
$u = -1.067020 - 0.674301I$ $a = -2.03641 + 0.00933I$ $b = 0.45680 - 1.50432I$	$-3.95261 - 9.40997I$	$2.00000 + 7.76812I$
$u = -1.061600 + 0.708976I$ $a = 2.31095 - 0.08552I$ $b = -0.65644 - 1.43319I$	$3.38790 + 12.73300I$	$5.12799 - 7.34194I$
$u = -1.061600 - 0.708976I$ $a = 2.31095 + 0.08552I$ $b = -0.65644 + 1.43319I$	$3.38790 - 12.73300I$	$5.12799 + 7.34194I$
$u = 0.530791$ $a = -3.58500$ $b = 0.511824$	$8.14249$	$16.8230$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.153263$		
$a = 3.39924$	0.765123	13.2670
$b = -0.382289$		

$$\text{II. } I_2^u = \langle b, a^2 - au - u^2 + a + 2u - 1, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -au \\ -u^2a + au + a \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 - a - u \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} au - u + 1 \\ u^2a - au - a \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^2a - 3u^2 + a + 8u + 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4, c_9$	$u^6$
$c_5$	$(u^3 - u^2 + 1)^2$
$c_6$	$(u^3 + u^2 + 2u + 1)^2$
$c_7, c_8, c_{10}$	$(u^2 - u - 1)^3$
$c_{11}, c_{12}$	$(u^2 + u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_5$	$(y^3 - y^2 + 2y - 1)^2$
$c_4, c_9$	$y^6$
$c_7, c_8, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$ $a = -0.198308 + 1.205210I$ $b = 0$	$11.90680 - 2.82812I$	$11.55793 + 3.24268I$
$u = 0.877439 + 0.744862I$ $a = 0.075747 - 0.460350I$ $b = 0$	$4.01109 - 2.82812I$	$14.0681 + 1.5771I$
$u = 0.877439 - 0.744862I$ $a = -0.198308 - 1.205210I$ $b = 0$	$11.90680 + 2.82812I$	$11.55793 - 3.24268I$
$u = 0.877439 - 0.744862I$ $a = 0.075747 + 0.460350I$ $b = 0$	$4.01109 + 2.82812I$	$14.0681 - 1.5771I$
$u = -0.754878$ $a = 1.08457$ $b = 0$	$-0.126494$	$0.954070$
$u = -0.754878$ $a = -2.83945$ $b = 0$	$7.76919$	$-5.20600$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^3 - u^2 + 2u - 1)^2)(u^{41} + 15u^{40} + \dots + 54u + 1)$
$c_2$	$((u^3 + u^2 - 1)^2)(u^{41} + 3u^{40} + \dots - 4u + 1)$
$c_3$	$((u^3 - u^2 + 2u - 1)^2)(u^{41} - 3u^{40} + \dots + 2u + 1)$
$c_4, c_9$	$u^6(u^{41} - u^{40} + \dots + 32u + 64)$
$c_5$	$((u^3 - u^2 + 1)^2)(u^{41} + 3u^{40} + \dots - 4u + 1)$
$c_6$	$((u^3 + u^2 + 2u + 1)^2)(u^{41} + 15u^{40} + \dots + 54u + 1)$
$c_7, c_8$	$((u^2 - u - 1)^3)(u^{41} - 4u^{40} + \dots - u - 1)$
$c_{10}$	$((u^2 - u - 1)^3)(u^{41} + 6u^{40} + \dots - 25u - 1)$
$c_{11}, c_{12}$	$((u^2 + u - 1)^3)(u^{41} - 4u^{40} + \dots - u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{41} + 25y^{40} + \dots + 1814y - 1)$
$c_2, c_5$	$((y^3 - y^2 + 2y - 1)^2)(y^{41} - 15y^{40} + \dots + 54y - 1)$
$c_3$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{41} - 35y^{40} + \dots + 54y - 1)$
$c_4, c_9$	$y^6(y^{41} + 35y^{40} + \dots - 23552y - 4096)$
$c_7, c_8, c_{11}$ $c_{12}$	$((y^2 - 3y + 1)^3)(y^{41} - 46y^{40} + \dots - y - 1)$
$c_{10}$	$((y^2 - 3y + 1)^3)(y^{41} + 38y^{40} + \dots + 419y - 1)$