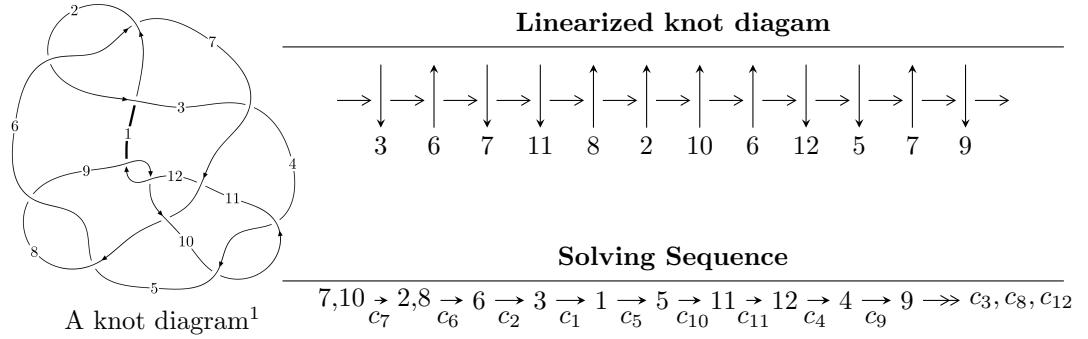


$12n_{0313}$  ( $K12n_{0313}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -41545u^{14} + 62711u^{13} + \dots + 83381b + 22577, \\
 &\quad -56191u^{14} + 116417u^{13} + \dots + 83381a + 99262, \\
 &\quad u^{15} - 2u^{14} + u^{13} + 2u^{12} + 4u^{11} - 12u^{10} + 7u^9 + 4u^8 + 10u^7 - 28u^6 + 13u^5 + 3u^4 - 5u^3 + 5u^2 - 3u + 1 \rangle \\
 I_2^u &= \langle -2u^8 - 6u^7 - 7u^6 + 4u^5 + 15u^4 + 8u^3 - 10u^2 + b - 15u - 5, \\
 &\quad -2u^8 - 6u^7 - 8u^6 + 3u^5 + 15u^4 + 12u^3 - 9u^2 + a - 16u - 8, \\
 &\quad u^9 + 3u^8 + 4u^7 - u^6 - 7u^5 - 6u^4 + 3u^3 + 8u^2 + 5u + 1 \rangle \\
 I_3^u &= \langle -u^5 - 3u^4 - 3u^3 - u^2 + b - u - 1, -u^5 - 3u^4 - 3u^3 - u^2 + a - u - 1, u^6 + 3u^5 + 4u^4 + 3u^3 + 3u^2 + 2u + 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 30 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -41545u^{14} + 62711u^{13} + \dots + 83381b + 22577, -5.62 \times 10^4 u^{14} + 1.16 \times 10^5 u^{13} + \dots + 8.34 \times 10^4 a + 9.93 \times 10^4, u^{15} - 2u^{14} + \dots - 3u + 1 \rangle$$

(i) **Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.673907u^{14} - 1.39621u^{13} + \dots + 1.05994u - 1.19046 \\ 0.498255u^{14} - 0.752102u^{13} + \dots + 1.28760u - 0.270769 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.828462u^{14} + 1.02276u^{13} + \dots - 3.35724u + 0.995263 \\ 0.862870u^{14} - 1.23046u^{13} + \dots + 2.60733u - 1.50841 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.651875u^{14} - 1.12205u^{13} + \dots + 0.0277281u - 0.890826 \\ 0.0258572u^{14} - 0.477447u^{13} + \dots + 0.528826u - 0.465442 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0135522u^{14} - 0.409794u^{13} + \dots - 1.03081u - 0.189216 \\ -0.240930u^{14} + 0.319773u^{13} + \dots - 1.40889u + 0.529341 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.22448u^{14} + 1.65231u^{13} + \dots - 4.89055u + 1.86951 \\ 1.00210u^{14} - 1.42187u^{13} + \dots + 2.69877u - 1.67090 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.582255u^{14} + 0.870858u^{13} + \dots - 0.677157u + 1.06481 \\ 0.560224u^{14} - 0.596707u^{13} + \dots + 1.64494u - 0.765174 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0220314u^{14} + 0.274151u^{13} + \dots + 0.967786u + 0.299637 \\ 0.560224u^{14} - 0.596707u^{13} + \dots + 1.64494u - 0.765174 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.626018u^{14} - 0.644607u^{13} + \dots - 0.501097u - 0.425385 \\ 0.0258572u^{14} - 0.477447u^{13} + \dots + 0.528826u - 0.465442 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.539284u^{14} - 0.621928u^{13} + \dots + 1.09609u - 0.0144038 \\ -0.201365u^{14} + 0.389765u^{13} + \dots + 0.0153152u + 0.510560 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-\frac{473234}{83381}u^{14} + \frac{693041}{83381}u^{13} + \dots - \frac{1183972}{83381}u + \frac{479281}{83381}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} + 19u^{14} + \cdots - 13464u - 2209$
$c_2, c_6$	$u^{15} - u^{14} + \cdots + 52u - 47$
$c_3$	$u^{15} + 16u^{14} + \cdots + 571220u - 516295$
$c_4, c_{10}$	$u^{15} - 4u^{14} + \cdots + 124u - 11$
$c_5, c_8$	$u^{15} + 2u^{14} + \cdots - 193u - 131$
$c_7$	$u^{15} + 2u^{14} + \cdots - 3u - 1$
$c_9, c_{12}$	$u^{15} - 4u^{13} + \cdots + 95u - 23$
$c_{11}$	$u^{15} - 10u^{14} + \cdots + 1544u - 1961$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} + 27y^{14} + \cdots + 93308080y - 4879681$
$c_2, c_6$	$y^{15} + 19y^{14} + \cdots - 13464y - 2209$
$c_3$	$y^{15} - 268y^{14} + \cdots - 3653087564750y - 266560527025$
$c_4, c_{10}$	$y^{15} + 28y^{14} + \cdots + 22856y - 121$
$c_5, c_8$	$y^{15} - 26y^{14} + \cdots + 40393y - 17161$
$c_7$	$y^{15} - 2y^{14} + \cdots - y - 1$
$c_9, c_{12}$	$y^{15} - 8y^{14} + \cdots + 2493y - 529$
$c_{11}$	$y^{15} + 12y^{14} + \cdots - 79903546y - 3845521$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.898089 + 0.122561I$		
$a = 0.851665 + 0.429887I$	$8.21514 + 3.43846I$	$8.39038 - 0.14759I$
$b = -0.813523 - 0.857386I$		
$u = 0.898089 - 0.122561I$		
$a = 0.851665 - 0.429887I$	$8.21514 - 3.43846I$	$8.39038 + 0.14759I$
$b = -0.813523 + 0.857386I$		
$u = -0.727637$		
$a = 0.282926$	1.43379	8.32270
$b = 0.679431$		
$u = -0.776726 + 1.064100I$		
$a = 0.198165 + 1.273550I$	1.61435 - 4.09120I	1.62171 + 2.87173I
$b = -0.90296 + 1.50976I$		
$u = -0.776726 - 1.064100I$		
$a = 0.198165 - 1.273550I$	1.61435 + 4.09120I	1.62171 - 2.87173I
$b = -0.90296 - 1.50976I$		
$u = -1.20953 + 0.78183I$		
$a = -0.907869 - 0.069228I$	3.12702 - 2.88040I	2.11466 + 1.70139I
$b = -0.45282 - 1.51307I$		
$u = -1.20953 - 0.78183I$		
$a = -0.907869 + 0.069228I$	3.12702 + 2.88040I	2.11466 - 1.70139I
$b = -0.45282 + 1.51307I$		
$u = -0.067561 + 0.552036I$		
$a = 1.49637 - 1.52360I$	-1.07742 - 1.06518I	-5.69949 + 4.71826I
$b = -0.032891 - 0.581799I$		
$u = -0.067561 - 0.552036I$		
$a = 1.49637 + 1.52360I$	-1.07742 + 1.06518I	-5.69949 - 4.71826I
$b = -0.032891 + 0.581799I$		
$u = 0.402433 + 0.347088I$		
$a = -1.35119 + 0.98940I$	0.07543 + 2.01877I	0.10830 - 4.30124I
$b = 0.547092 + 0.828723I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.402433 - 0.347088I$		
$a = -1.35119 - 0.98940I$	$0.07543 - 2.01877I$	$0.10830 + 4.30124I$
$b = 0.547092 - 0.828723I$		
$u = 1.10914 + 1.03230I$		
$a = -0.75781 + 1.35948I$	$-11.8911 + 11.0679I$	$2.10881 - 4.27183I$
$b = 1.04371 + 1.80853I$		
$u = 1.10914 - 1.03230I$		
$a = -0.75781 - 1.35948I$	$-11.8911 - 11.0679I$	$2.10881 + 4.27183I$
$b = 1.04371 - 1.80853I$		
$u = 1.00798 + 1.14054I$		
$a = 0.829204 - 0.703970I$	$-12.29490 - 3.15413I$	$1.69429 + 0.52217I$
$b = 0.77167 - 1.94892I$		
$u = 1.00798 - 1.14054I$		
$a = 0.829204 + 0.703970I$	$-12.29490 + 3.15413I$	$1.69429 - 0.52217I$
$b = 0.77167 + 1.94892I$		

II.

$$I_2^u = \langle -2u^8 - 6u^7 + \dots + b - 5, -2u^8 - 6u^7 + \dots + a - 8, u^9 + 3u^8 + \dots + 5u + 1 \rangle$$

(i) **Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^8 + 6u^7 + 8u^6 - 3u^5 - 15u^4 - 12u^3 + 9u^2 + 16u + 8 \\ 2u^8 + 6u^7 + 7u^6 - 4u^5 - 15u^4 - 8u^3 + 10u^2 + 15u + 5 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 4u^8 + 11u^7 + 13u^6 - 8u^5 - 27u^4 - 17u^3 + 18u^2 + 29u + 12 \\ u^8 + 2u^7 + 2u^6 - 3u^5 - 4u^4 - 2u^3 + 5u^2 + 3u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 7u^8 + 18u^7 + 21u^6 - 15u^5 - 42u^4 - 26u^3 + 31u^2 + 43u + 18 \\ 2u^7 + 4u^6 + 3u^5 - 7u^4 - 8u^3 + 10u + 5 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 10u^8 + 25u^7 + 28u^6 - 23u^5 - 58u^4 - 33u^3 + 44u^2 + 58u + 23 \\ -3u^8 - 6u^7 - 5u^6 + 10u^5 + 13u^4 + 2u^3 - 15u^2 - 10u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 3u^8 + 9u^7 + 11u^6 - 5u^5 - 23u^4 - 15u^3 + 13u^2 + 25u + 10 \\ 2u^8 + 4u^7 + 4u^6 - 6u^5 - 8u^4 - 3u^3 + 10u^2 + 7u + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 9u^8 + 22u^7 + 23u^6 - 23u^5 - 51u^4 - 23u^3 + 42u^2 + 49u + 15 \\ -4u^8 - 10u^7 - 10u^6 + 11u^5 + 24u^4 + 9u^3 - 20u^2 - 22u - 5 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 5u^8 + 12u^7 + 13u^6 - 12u^5 - 27u^4 - 14u^3 + 22u^2 + 27u + 10 \\ -4u^8 - 10u^7 - 10u^6 + 11u^5 + 24u^4 + 9u^3 - 20u^2 - 22u - 5 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 7u^8 + 16u^7 + 17u^6 - 18u^5 - 35u^4 - 18u^3 + 31u^2 + 33u + 13 \\ 2u^7 + 4u^6 + 3u^5 - 7u^4 - 8u^3 + 10u + 5 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -4u^8 - 11u^7 - 13u^6 + 8u^5 + 27u^4 + 17u^3 - 18u^2 - 29u - 12 \\ -4u^8 - 9u^7 - 9u^6 + 11u^5 + 20u^4 + 8u^3 - 19u^2 - 18u - 5 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-6u^8 - 13u^7 - 11u^6 + 19u^5 + 27u^4 + 5u^3 - 30u^2 - 16u - 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^9 - 3u^8 + 6u^7 - 9u^6 + 12u^5 - 10u^4 + 3u^3 + 4u^2 - 4u + 1$
$c_2$	$u^9 - u^8 + 2u^7 - u^6 + 2u^5 + u^3 + 2u^2 + 1$
$c_3$	$u^9 + u^8 + 5u^7 + 10u^6 + u^5 + u^4 + 12u^3 + 9u^2 + 2u + 1$
$c_4$	$u^9 + 5u^7 + u^6 + 7u^5 + 5u^4 + u^3 + 6u^2 - 2u + 1$
$c_5$	$u^9 + 3u^8 + u^7 - 5u^6 - 5u^5 + 4u^4 + 9u^3 - 4u + 1$
$c_6$	$u^9 + u^8 + 2u^7 + u^6 + 2u^5 + u^3 - 2u^2 - 1$
$c_7$	$u^9 + 3u^8 + 4u^7 - u^6 - 7u^5 - 6u^4 + 3u^3 + 8u^2 + 5u + 1$
$c_8$	$u^9 - 3u^8 + u^7 + 5u^6 - 5u^5 - 4u^4 + 9u^3 - 4u - 1$
$c_9$	$u^9 + 2u^7 - u^6 - 2u^4 - u^3 - 2u^2 - u - 1$
$c_{10}$	$u^9 + 5u^7 - u^6 + 7u^5 - 5u^4 + u^3 - 6u^2 - 2u - 1$
$c_{11}$	$u^9 + 6u^8 + 10u^7 + 4u^6 + 11u^5 + 23u^4 + 10u^3 + 6u^2 + 13u + 5$
$c_{12}$	$u^9 + 2u^7 + u^6 + 2u^4 - u^3 + 2u^2 - u + 1$



**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^9 + 3y^8 + 6y^7 + 9y^6 + 16y^5 + 2y^4 + 11y^3 - 20y^2 + 8y - 1$
$c_2, c_6$	$y^9 + 3y^8 + 6y^7 + 9y^6 + 12y^5 + 10y^4 + 3y^3 - 4y^2 - 4y - 1$
$c_3$	$y^9 + 9y^8 + 7y^7 - 68y^6 + 87y^5 - 139y^4 + 110y^3 - 35y^2 - 14y - 1$
$c_4, c_{10}$	$y^9 + 10y^8 + 39y^7 + 71y^6 + 45y^5 - 43y^4 - 89y^3 - 50y^2 - 8y - 1$
$c_5, c_8$	$y^9 - 7y^8 + 21y^7 - 41y^6 + 75y^5 - 120y^4 + 131y^3 - 80y^2 + 16y - 1$
$c_7$	$y^9 - y^8 + 8y^7 - 15y^6 + 23y^5 - 28y^4 + 37y^3 - 22y^2 + 9y - 1$
$c_9, c_{12}$	$y^9 + 4y^8 + 4y^7 - 3y^6 - 10y^5 - 12y^4 - 9y^3 - 6y^2 - 3y - 1$
$c_{11}$	$y^9 - 16y^8 + 74y^7 - 52y^6 + 91y^5 - 157y^4 + 70y^3 - 6y^2 + 109y - 25$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.072880 + 0.352289I$		
$a = -1.056530 - 0.568290I$	$7.45475 + 1.27338I$	$5.64490 - 0.43727I$
$b = -0.054519 + 0.730817I$		
$u = 1.072880 - 0.352289I$		
$a = -1.056530 + 0.568290I$	$7.45475 - 1.27338I$	$5.64490 + 0.43727I$
$b = -0.054519 - 0.730817I$		
$u = -0.692006 + 0.938897I$		
$a = -0.73796 - 1.40715I$	$-0.18404 - 4.42541I$	$-3.46550 + 5.77063I$
$b = 0.497907 - 0.965644I$		
$u = -0.692006 - 0.938897I$		
$a = -0.73796 + 1.40715I$	$-0.18404 + 4.42541I$	$-3.46550 - 5.77063I$
$b = 0.497907 + 0.965644I$		
$u = -0.654771 + 0.355732I$		
$a = 1.208170 + 0.025665I$	$7.61597 - 3.90243I$	$0.00196 + 5.82113I$
$b = -0.976768 + 0.741048I$		
$u = -0.654771 - 0.355732I$		
$a = 1.208170 - 0.025665I$	$7.61597 + 3.90243I$	$0.00196 - 5.82113I$
$b = -0.976768 - 0.741048I$		
$u = -0.396548$		
$a = 3.50035$	0.137068	-0.229590
$b = 0.810638$		
$u = -1.02783 + 1.24961I$		
$a = 0.336146 + 1.247420I$	$3.13906 - 5.52199I$	$4.93343 + 8.47719I$
$b = -0.371939 + 1.075240I$		
$u = -1.02783 - 1.24961I$		
$a = 0.336146 - 1.247420I$	$3.13906 + 5.52199I$	$4.93343 - 8.47719I$
$b = -0.371939 - 1.075240I$		

$$\text{III. } I_3^u = \langle -u^5 - 3u^4 - 3u^3 - u^2 + b - u - 1, -u^5 - 3u^4 - 3u^3 - u^2 + a - u - 1, u^6 + 3u^5 + 4u^4 + 3u^3 + 3u^2 + 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^5 + 3u^4 + 3u^3 + u^2 + u + 1 \\ u^5 + 3u^4 + 3u^3 + u^2 + u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^5 + 3u^4 + 4u^3 + 3u^2 + 3u + 2 \\ u^5 + 3u^4 + 4u^3 + 3u^2 + 3u + 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 2u^5 + 5u^4 + 4u^3 + u^2 + 3u + 2 \\ u^5 + 2u^4 + u^3 + 2u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^5 + 2u^4 + 2u^3 + 2u^2 + 3u \\ u^5 + 3u^4 + 4u^3 + 3u^2 + 2u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u + 1 \\ u^5 + 3u^4 + 3u^3 + 2u^2 + 2u + 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^3 - 2u^2 - u \\ u^5 + 2u^4 + 2u^3 + 2u^2 + 3u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^5 + 2u^4 + u^3 + 2u + 1 \\ u^5 + 2u^4 + 2u^3 + 2u^2 + 3u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^5 + 3u^4 + 3u^3 + u^2 + u + 1 \\ u^5 + 2u^4 + u^3 + 2u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^5 - 2u^4 - u^3 + u^2 + 1 \\ u^4 + 3u^3 + 3u^2 + 2u + 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $2u^5 + 2u^4 - 2u^2 - u + 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^6 - 4u^5 + 8u^4 - 9u^3 + 8u^2 - 4u + 1$
$c_2, c_{12}$	$u^6 + 2u^4 + u^3 + 2u^2 + 1$
$c_3$	$u^6 + 3u^5 + 4u^4 + 6u^3 + 6u^2 + 2u + 1$
$c_4$	$(u^3 + u^2 + 2u + 1)^2$
$c_5$	$u^6 - u^5 - 3u^4 + 4u^2 + 3u + 1$
$c_6, c_9$	$u^6 + 2u^4 - u^3 + 2u^2 + 1$
$c_7$	$u^6 + 3u^5 + 4u^4 + 3u^3 + 3u^2 + 2u + 1$
$c_8$	$u^6 + u^5 - 3u^4 + 4u^2 - 3u + 1$
$c_{10}$	$(u^3 - u^2 + 2u - 1)^2$
$c_{11}$	$u^6 + 2u^5 + 4u^4 + 6u^3 + 4u^2 + 5u + 5$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^6 + 8y^4 + 17y^3 + 8y^2 + 1$
$c_2, c_6, c_9$ $c_{12}$	$y^6 + 4y^5 + 8y^4 + 9y^3 + 8y^2 + 4y + 1$
$c_3$	$y^6 - y^5 - 8y^4 + 2y^3 + 20y^2 + 8y + 1$
$c_4, c_{10}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_5, c_8$	$y^6 - 7y^5 + 17y^4 - 16y^3 + 10y^2 - y + 1$
$c_7$	$y^6 - y^5 + 4y^4 + 5y^3 + 5y^2 + 2y + 1$
$c_{11}$	$y^6 + 4y^5 - 14y^3 - 4y^2 + 15y + 25$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.319307 + 0.797712I$ $a = -0.425318 - 1.270190I$ $b = -0.425318 - 1.270190I$	$4.66906 + 2.82812I$	$2.68686 - 3.21164I$
$u = 0.319307 - 0.797712I$ $a = -0.425318 + 1.270190I$ $b = -0.425318 + 1.270190I$	$4.66906 - 2.82812I$	$2.68686 + 3.21164I$
$u = -0.500000 + 0.565544I$ $a = 0.662359 + 0.749187I$ $b = 0.662359 + 0.749187I$	0.531480	$1.235367 + 0.288289I$
$u = -0.500000 - 0.565544I$ $a = 0.662359 - 0.749187I$ $b = 0.662359 - 0.749187I$	0.531480	$1.235367 - 0.288289I$
$u = -1.31931 + 0.79771I$ $a = -0.237041 - 0.707911I$ $b = -0.237041 - 0.707911I$	$4.66906 - 2.82812I$	$9.57778 + 1.25753I$
$u = -1.31931 - 0.79771I$ $a = -0.237041 + 0.707911I$ $b = -0.237041 + 0.707911I$	$4.66906 + 2.82812I$	$9.57778 - 1.25753I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^6 - 4u^5 + 8u^4 - 9u^3 + 8u^2 - 4u + 1)$ $\cdot (u^9 - 3u^8 + 6u^7 - 9u^6 + 12u^5 - 10u^4 + 3u^3 + 4u^2 - 4u + 1)$ $\cdot (u^{15} + 19u^{14} + \dots - 13464u - 2209)$
$c_2$	$(u^6 + 2u^4 + u^3 + 2u^2 + 1)(u^9 - u^8 + 2u^7 - u^6 + 2u^5 + u^3 + 2u^2 + 1)$ $\cdot (u^{15} - u^{14} + \dots + 52u - 47)$
$c_3$	$(u^6 + 3u^5 + 4u^4 + 6u^3 + 6u^2 + 2u + 1)$ $\cdot (u^9 + u^8 + 5u^7 + 10u^6 + u^5 + u^4 + 12u^3 + 9u^2 + 2u + 1)$ $\cdot (u^{15} + 16u^{14} + \dots + 571220u - 516295)$
$c_4$	$(u^3 + u^2 + 2u + 1)^2(u^9 + 5u^7 + u^6 + 7u^5 + 5u^4 + u^3 + 6u^2 - 2u + 1)$ $\cdot (u^{15} - 4u^{14} + \dots + 124u - 11)$
$c_5$	$(u^6 - u^5 - 3u^4 + 4u^2 + 3u + 1)$ $\cdot (u^9 + 3u^8 + u^7 - 5u^6 - 5u^5 + 4u^4 + 9u^3 - 4u + 1)$ $\cdot (u^{15} + 2u^{14} + \dots - 193u - 131)$
$c_6$	$(u^6 + 2u^4 - u^3 + 2u^2 + 1)(u^9 + u^8 + 2u^7 + u^6 + 2u^5 + u^3 - 2u^2 - 1)$ $\cdot (u^{15} - u^{14} + \dots + 52u - 47)$
$c_7$	$(u^6 + 3u^5 + 4u^4 + 3u^3 + 3u^2 + 2u + 1)$ $\cdot (u^9 + 3u^8 + 4u^7 - u^6 - 7u^5 - 6u^4 + 3u^3 + 8u^2 + 5u + 1)$ $\cdot (u^{15} + 2u^{14} + \dots - 3u - 1)$
$c_8$	$(u^6 + u^5 - 3u^4 + 4u^2 - 3u + 1)$ $\cdot (u^9 - 3u^8 + u^7 + 5u^6 - 5u^5 - 4u^4 + 9u^3 - 4u - 1)$ $\cdot (u^{15} + 2u^{14} + \dots - 193u - 131)$
$c_9$	$(u^6 + 2u^4 - u^3 + 2u^2 + 1)(u^9 + 2u^7 - u^6 - 2u^4 - u^3 - 2u^2 - u - 1)$ $\cdot (u^{15} - 4u^{13} + \dots + 95u - 23)$
$c_{10}$	$(u^3 - u^2 + 2u - 1)^2(u^9 + 5u^7 - u^6 + 7u^5 - 5u^4 + u^3 - 6u^2 - 2u - 1)$ $\cdot (u^{15} - 4u^{14} + \dots + 124u - 11)$
$c_{11}$	$(u^6 + 2u^5 + 4u^4 + 6u^3 + 4u^2 + 5u + 5)$ $\cdot (u^9 + 6u^8 + 10u^7 + 4u^6 + 11u^5 + 23u^4 + 10u^3 + 6u^2 + 13u + 5)$ $\cdot (u^{15} - 10u^{14} + \dots + 1544u - 1961)$
$c_{12}$	$(u^6 + 2u^4 + u^3 + 2u^2 + 1)(u^9 + 2u^7 + u^6 + 2u^4 - u^3 + 2u^2 - u + 1)$ $\cdot (u^{15} - 4u^{13} + \dots + 95u - 23)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^6 + 8y^4 + 17y^3 + 8y^2 + 1)$ $\cdot (y^9 + 3y^8 + 6y^7 + 9y^6 + 16y^5 + 2y^4 + 11y^3 - 20y^2 + 8y - 1)$ $\cdot (y^{15} + 27y^{14} + \dots + 93308080y - 4879681)$
$c_2, c_6$	$(y^6 + 4y^5 + 8y^4 + 9y^3 + 8y^2 + 4y + 1)$ $\cdot (y^9 + 3y^8 + 6y^7 + 9y^6 + 12y^5 + 10y^4 + 3y^3 - 4y^2 - 4y - 1)$ $\cdot (y^{15} + 19y^{14} + \dots - 13464y - 2209)$
$c_3$	$(y^6 - y^5 - 8y^4 + 2y^3 + 20y^2 + 8y + 1)$ $\cdot (y^9 + 9y^8 + 7y^7 - 68y^6 + 87y^5 - 139y^4 + 110y^3 - 35y^2 - 14y - 1)$ $\cdot (y^{15} - 268y^{14} + \dots - 3653087564750y - 266560527025)$
$c_4, c_{10}$	$(y^3 + 3y^2 + 2y - 1)^2$ $\cdot (y^9 + 10y^8 + 39y^7 + 71y^6 + 45y^5 - 43y^4 - 89y^3 - 50y^2 - 8y - 1)$ $\cdot (y^{15} + 28y^{14} + \dots + 22856y - 121)$
$c_5, c_8$	$(y^6 - 7y^5 + 17y^4 - 16y^3 + 10y^2 - y + 1)$ $\cdot (y^9 - 7y^8 + 21y^7 - 41y^6 + 75y^5 - 120y^4 + 131y^3 - 80y^2 + 16y - 1)$ $\cdot (y^{15} - 26y^{14} + \dots + 40393y - 17161)$
$c_7$	$(y^6 - y^5 + 4y^4 + 5y^3 + 5y^2 + 2y + 1)$ $\cdot (y^9 - y^8 + 8y^7 - 15y^6 + 23y^5 - 28y^4 + 37y^3 - 22y^2 + 9y - 1)$ $\cdot (y^{15} - 2y^{14} + \dots - y - 1)$
$c_9, c_{12}$	$(y^6 + 4y^5 + 8y^4 + 9y^3 + 8y^2 + 4y + 1)$ $\cdot (y^9 + 4y^8 + 4y^7 - 3y^6 - 10y^5 - 12y^4 - 9y^3 - 6y^2 - 3y - 1)$ $\cdot (y^{15} - 8y^{14} + \dots + 2493y - 529)$
$c_{11}$	$(y^6 + 4y^5 - 14y^3 - 4y^2 + 15y + 25)$ $\cdot (y^9 - 16y^8 + 74y^7 - 52y^6 + 91y^5 - 157y^4 + 70y^3 - 6y^2 + 109y - 25)$ $\cdot (y^{15} + 12y^{14} + \dots - 79903546y - 3845521)$