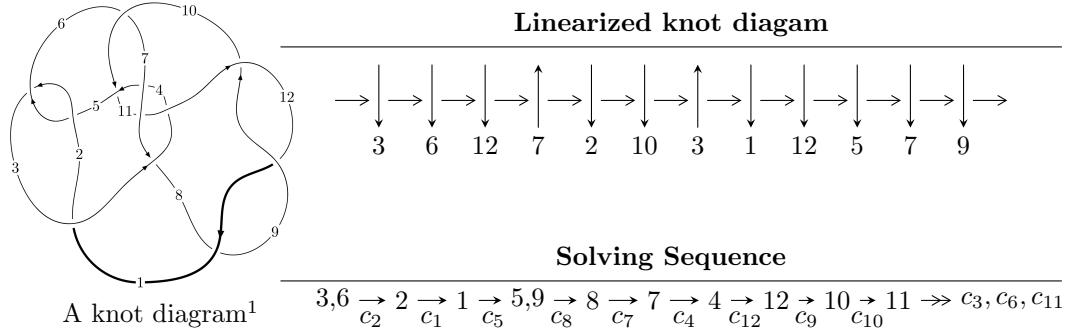


$12n_{0321}$  ( $K12n_{0321}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle -28u^8 + 32u^7 - 37u^6 - 26u^5 - 112u^4 - 40u^3 - 37u^2 + 59b + 86u - 72, \\ -7u^8 + 8u^7 - 24u^6 + 23u^5 - 28u^4 - 69u^3 - 24u^2 + 59a + 110u - 18, \\ u^9 - 2u^8 + 2u^7 + u^6 + 2u^5 - 2u^4 + u^3 - 3u^2 + 4u - 1 \rangle$$

$$I_2^u = \langle -u^2 + b - u + 2, a + 1, u^4 + u^3 - u^2 - u + 1 \rangle$$

$$I_3^u = \langle -2u^7 - 3u^6 - 2u^5 + 4u^4 + 7u^3 + 5u^2 + b - 5u - 5, -2u^7 - 2u^6 - u^5 + 5u^4 + 5u^3 + 3u^2 + a - 6u - 2, \\ u^8 + 2u^7 + 2u^6 - u^5 - 4u^4 - 4u^3 + u^2 + 3u + 1 \rangle$$

$$I_4^u = \langle -3u^5 + u^3 - 11u^2 + 19b + 7u - 18, -9u^5 + 19u^4 - 35u^3 + 43u^2 + 19a - 74u + 22, \\ u^6 - 3u^5 + 6u^4 - 8u^3 + 12u^2 - 6u + 1 \rangle$$

$$I_5^u = \langle b, a + u + 1, u^2 + u + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 29 representations.

---

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -28u^8 + 32u^7 + \dots + 59b - 72, -7u^8 + 8u^7 + \dots + 59a - 18, u^9 - 2u^8 + \dots + 4u - 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.118644u^8 - 0.135593u^7 + \dots - 1.86441u + 0.305085 \\ 0.474576u^8 - 0.542373u^7 + \dots - 1.45763u + 1.22034 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.355932u^8 - 0.406780u^7 + \dots - 1.59322u + 0.915254 \\ 0.355932u^8 - 0.406780u^7 + \dots - 0.593220u + 0.915254 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ 0.355932u^8 - 0.406780u^7 + \dots - 0.593220u + 0.915254 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.118644u^8 + 0.135593u^7 + \dots + 1.86441u - 0.305085 \\ 0.440678u^8 - 0.932203u^7 + \dots - 1.06780u + 0.847458 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.389831u^8 - 1.01695u^7 + \dots - 0.983051u + 1.28814 \\ -0.355932u^8 + 0.406780u^7 + \dots + 0.593220u - 0.915254 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0.915254u^8 - 1.47458u^7 + \dots - 2.52542u + 2.06780 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.305085u^8 + 0.491525u^7 + \dots + 0.508475u - 1.35593 \\ 0.711864u^8 - 0.813559u^7 + \dots - 2.18644u + 1.83051 \end{pmatrix}$$

(ii) **Obstruction class = -1**

$$(iii) \text{ Cusp Shapes} = -\frac{15}{59}u^8 + \frac{93}{59}u^7 - \frac{43}{59}u^6 - \frac{94}{59}u^5 + \frac{235}{59}u^4 + \frac{282}{59}u^3 + \frac{193}{59}u^2 - \frac{93}{59}u - \frac{342}{59}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^9 + 12u^7 - u^6 + 8u^5 - 18u^4 + 7u^3 + 5u^2 + 10u + 1$
$c_2, c_5, c_6$	$u^9 + 2u^8 + 2u^7 - u^6 + 2u^5 + 2u^4 + u^3 + 3u^2 + 4u + 1$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$u^9 + 7u^7 + 5u^6 + 15u^5 + 13u^4 + 11u^3 + 7u^2 + u + 1$
$c_4$	$u^9 + 2u^8 - 7u^7 - 15u^6 + 13u^5 + 53u^4 + 71u^3 + 61u^2 + 29u + 5$
$c_7$	$u^9 - 7u^8 + 5u^7 + 42u^6 + 92u^5 + 125u^4 + 125u^3 + 88u^2 + 39u + 9$
$c_{11}$	$u^9 + u^8 + 14u^7 + 10u^6 + 39u^5 - 44u^4 - 45u^3 + 4u^2 + 20u + 9$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^9 + 24y^8 + \dots + 90y - 1$
$c_2, c_5, c_6$	$y^9 + 12y^7 + y^6 + 8y^5 + 18y^4 + 7y^3 - 5y^2 + 10y - 1$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$y^9 + 14y^8 + 79y^7 + 207y^6 + 251y^5 + 105y^4 - 41y^3 - 53y^2 - 13y - 1$
$c_4$	$y^9 - 18y^8 + \dots + 231y - 25$
$c_7$	$y^9 - 39y^8 + \dots - 63y - 81$
$c_{11}$	$y^9 + 27y^8 + \dots + 328y - 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.236649 + 0.987655I$		
$a = 1.59024 - 3.04254I$	$9.89350 + 2.31667I$	$0.86831 - 3.48815I$
$b = 1.32330 - 0.67194I$		
$u = -0.236649 - 0.987655I$		
$a = 1.59024 + 3.04254I$	$9.89350 - 2.31667I$	$0.86831 + 3.48815I$
$b = 1.32330 + 0.67194I$		
$u = -0.948444 + 0.610151I$		
$a = 0.291757 + 0.057514I$	$1.50288 + 4.69117I$	$-4.69492 - 7.49384I$
$b = -0.400025 - 0.194724I$		
$u = -0.948444 - 0.610151I$		
$a = 0.291757 - 0.057514I$	$1.50288 - 4.69117I$	$-4.69492 + 7.49384I$
$b = -0.400025 + 0.194724I$		
$u = 0.731097 + 0.406841I$		
$a = -0.967602 + 0.291558I$	$-1.11949 - 1.41007I$	$-6.06702 + 5.32264I$
$b = -0.297854 + 1.104540I$		
$u = 0.731097 - 0.406841I$		
$a = -0.967602 - 0.291558I$	$-1.11949 + 1.41007I$	$-6.06702 - 5.32264I$
$b = -0.297854 - 1.104540I$		
$u = 0.323158$		
$a = -0.211236$	$-1.09696$	$-5.76550$
$b = 0.860492$		
$u = 1.29242 + 1.30359I$		
$a = 1.69122 + 1.25994I$	$-13.8407 - 9.8067I$	$-4.22361 + 3.66185I$
$b = 2.44434 + 0.36799I$		
$u = 1.29242 - 1.30359I$		
$a = 1.69122 - 1.25994I$	$-13.8407 + 9.8067I$	$-4.22361 - 3.66185I$
$b = 2.44434 - 0.36799I$		

$$\text{II. } I_2^u = \langle -u^2 + b - u + 2, a + 1, u^4 + u^3 - u^2 - u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1 \\ u^2 + u - 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^3 + u^2 - u - 1 \\ u^3 + u^2 - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^3 + u^2 - 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^3 - u^2 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u^2 - 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1 \\ u^3 + 2u^2 - 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^3 + u - 1 \\ u^3 + 2u^2 - u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $2u^3 + 5u^2 - 3u - 13$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^4 - 3u^3 + 5u^2 - 3u + 1$
$c_2, c_6$	$u^4 + u^3 - u^2 - u + 1$
$c_3, c_{12}$	$u^4 + u^3 + 2u^2 + 2u + 1$
$c_4$	$u^4 - 3u^3 + 2u^2 + 1$
$c_5$	$u^4 - u^3 - u^2 + u + 1$
$c_7$	$(u^2 - u + 1)^2$
$c_8, c_9, c_{10}$	$u^4 - u^3 + 2u^2 - 2u + 1$
$c_{11}$	$u^4 + 2u^2 + 3u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^4 + y^3 + 9y^2 + y + 1$
$c_2, c_5, c_6$	$y^4 - 3y^3 + 5y^2 - 3y + 1$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$y^4 + 3y^3 + 2y^2 + 1$
$c_4$	$y^4 - 5y^3 + 6y^2 + 4y + 1$
$c_7$	$(y^2 + y + 1)^2$
$c_{11}$	$y^4 + 4y^3 + 6y^2 - 5y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.692440 + 0.318148I$		
$a = -1.00000$	$-1.74699 - 0.56550I$	$-12.94255 + 2.09940I$
$b = -0.929304 + 0.758745I$		
$u = 0.692440 - 0.318148I$		
$a = -1.00000$	$-1.74699 + 0.56550I$	$-12.94255 - 2.09940I$
$b = -0.929304 - 0.758745I$		
$u = -1.192440 + 0.547877I$		
$a = -1.00000$	$5.03685 + 4.62527I$	$-5.05745 - 3.83145I$
$b = -2.07070 - 0.75874I$		
$u = -1.192440 - 0.547877I$		
$a = -1.00000$	$5.03685 - 4.62527I$	$-5.05745 + 3.83145I$
$b = -2.07070 + 0.75874I$		

$$\text{III. } I_3^u = \langle -2u^7 - 3u^6 + \dots + b - 5, -2u^7 - 2u^6 + \dots + a - 2, u^8 + 2u^7 + 2u^6 - u^5 - 4u^4 - 4u^3 + u^2 + 3u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2u^7 + 2u^6 + u^5 - 5u^4 - 5u^3 - 3u^2 + 6u + 2 \\ 2u^7 + 3u^6 + 2u^5 - 4u^4 - 7u^3 - 5u^2 + 5u + 5 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 4u^7 + 5u^6 + 4u^5 - 8u^4 - 12u^3 - 9u^2 + 11u + 6 \\ u^7 + 2u^6 + 2u^5 - u^4 - 4u^3 - 4u^2 + 2u + 3 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 3u^7 + 3u^6 + 2u^5 - 7u^4 - 8u^3 - 5u^2 + 9u + 3 \\ u^7 + 2u^6 + 2u^5 - u^4 - 4u^3 - 4u^2 + 2u + 3 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -10u^7 - 13u^6 - 11u^5 + 17u^4 + 27u^3 + 20u^2 - 23u - 12 \\ -u^7 - 2u^6 - 2u^5 + u^4 + 4u^3 + 4u^2 - u - 4 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 6u^7 + 9u^6 + 7u^5 - 11u^4 - 20u^3 - 14u^2 + 15u + 13 \\ -5u^7 - 7u^6 - 6u^5 + 8u^4 + 15u^3 + 11u^2 - 11u - 8 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -7u^7 - 10u^6 - 8u^5 + 12u^4 + 22u^3 + 16u^2 - 16u - 12 \\ 3u^7 + 4u^6 + 3u^5 - 6u^4 - 9u^3 - 6u^2 + 8u + 5 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -10u^7 - 14u^6 - 11u^5 + 17u^4 + 31u^3 + 22u^2 - 23u - 17 \\ u^7 + 2u^6 + u^5 - 3u^4 - 4u^3 - 2u^2 + 4u + 2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $2u^7 + 3u^6 + 3u^5 - 2u^4 - 5u^3 - 4u^2 + 3u - 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^8 + u^5 + 2u^4 - 14u^3 + 17u^2 - 7u + 1$
$c_2, c_6$	$u^8 + 2u^7 + 2u^6 - u^5 - 4u^4 - 4u^3 + u^2 + 3u + 1$
$c_3, c_{12}$	$u^8 - u^7 + 6u^6 - 5u^5 + 12u^4 - 8u^3 + 9u^2 - 4u + 1$
$c_4$	$(u^4 + 3u^3 + u^2 - 2u + 1)^2$
$c_5$	$u^8 - 2u^7 + 2u^6 + u^5 - 4u^4 + 4u^3 + u^2 - 3u + 1$
$c_7$	$u^8 + u^7 + 5u^6 + 8u^5 + 7u^4 + 11u^3 + 10u^2 + 1$
$c_8, c_9, c_{10}$	$u^8 + u^7 + 6u^6 + 5u^5 + 12u^4 + 8u^3 + 9u^2 + 4u + 1$
$c_{11}$	$u^8 - 2u^7 + 5u^6 + 3u^5 + 4u^4 + 27u^3 - 3u^2 - 16u + 52$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^8 + 4y^6 + 33y^5 + 34y^4 - 114y^3 + 97y^2 - 15y + 1$
$c_2, c_5, c_6$	$y^8 + y^5 + 2y^4 - 14y^3 + 17y^2 - 7y + 1$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$y^8 + 11y^7 + 50y^6 + 121y^5 + 166y^4 + 124y^3 + 41y^2 + 2y + 1$
$c_4$	$(y^4 - 7y^3 + 15y^2 - 2y + 1)^2$
$c_7$	$y^8 + 9y^7 + 23y^6 + 4y^5 - 25y^4 + 29y^3 + 114y^2 + 20y + 1$
$c_{11}$	$y^8 + 6y^7 + 45y^6 + 133y^5 - 136y^4 - 137y^3 + 1289y^2 - 568y + 2704$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.963269 + 0.149069I$		
$a = -0.307661 - 1.178810I$	$1.43393 - 3.16396I$	$-4.10488 + 1.55249I$
$b = 0.148192 - 0.911292I$		
$u = 0.963269 - 0.149069I$		
$a = -0.307661 + 1.178810I$	$1.43393 + 3.16396I$	$-4.10488 - 1.55249I$
$b = 0.148192 + 0.911292I$		
$u = -1.006590 + 0.790269I$		
$a = 0.550701 + 0.903791I$	$1.43393 + 3.16396I$	$-4.10488 - 1.55249I$
$b = 0.148192 + 0.911292I$		
$u = -1.006590 - 0.790269I$		
$a = 0.550701 - 0.903791I$	$1.43393 - 3.16396I$	$-4.10488 + 1.55249I$
$b = 0.148192 - 0.911292I$		
$u = -0.384833 + 1.326500I$		
$a = 1.24719 - 2.12175I$	$8.43568 + 1.41510I$	$-4.39512 - 0.50684I$
$b = 1.35181 - 0.72034I$		
$u = -0.384833 - 1.326500I$		
$a = 1.24719 + 2.12175I$	$8.43568 - 1.41510I$	$-4.39512 + 0.50684I$
$b = 1.35181 + 0.72034I$		
$u = -0.571852 + 0.099314I$		
$a = -1.99023 + 0.84034I$	$8.43568 - 1.41510I$	$-4.39512 + 0.50684I$
$b = 1.35181 + 0.72034I$		
$u = -0.571852 - 0.099314I$		
$a = -1.99023 - 0.84034I$	$8.43568 + 1.41510I$	$-4.39512 - 0.50684I$
$b = 1.35181 - 0.72034I$		

$$\text{IV. } I_4^u = \langle -3u^5 + u^3 - 11u^2 + 19b + 7u - 18, -9u^5 + 19u^4 + \cdots + 19a + 22, u^6 - 3u^5 + 6u^4 - 8u^3 + 12u^2 - 6u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{9}{19}u^5 - u^4 + \cdots + \frac{74}{19}u - \frac{22}{19} \\ 0.157895u^5 - 0.0526316u^3 + \cdots - 0.368421u + 0.947368 \end{pmatrix} \\ a_8 &= \begin{pmatrix} \frac{9}{19}u^5 - 2u^4 + \cdots + \frac{55}{19}u - \frac{3}{19} \\ \frac{3}{19}u^5 - u^4 + \cdots - \frac{7}{19}u + \frac{18}{19} \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{6}{19}u^5 - u^4 + \cdots + \frac{62}{19}u - \frac{21}{19} \\ \frac{3}{19}u^5 - u^4 + \cdots - \frac{19}{19}u + \frac{18}{19} \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{8}{19}u^5 - u^4 + \cdots + \frac{51}{19}u - \frac{9}{19} \\ \frac{10}{19}u^5 - u^4 + \cdots + \frac{6}{19}u + \frac{9}{19} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -\frac{6}{19}u^5 + u^4 + \cdots - \frac{81}{19}u + \frac{40}{19} \\ -0.105263u^5 + 0.368421u^3 + \cdots - 0.421053u - 0.631579 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.684211u^5 - 2u^4 + \cdots + 7.73684u - 2.89474 \\ -0.105263u^5 + 0.368421u^3 + \cdots + 0.578947u + 1.36842 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{7}{19}u^5 - u^4 + \cdots + \frac{123}{19}u - \frac{53}{19} \\ -1.57895u^5 + 3u^4 + \cdots - 1.31579u + 1.52632 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-\frac{2}{19}u^5 + \frac{7}{19}u^3 - \frac{20}{19}u^2 + \frac{11}{19}u - \frac{107}{19}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^6 - 3u^5 + 12u^4 - 46u^3 + 60u^2 + 12u + 1$
$c_2, c_5, c_6$	$u^6 + 3u^5 + 6u^4 + 8u^3 + 12u^2 + 6u + 1$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$u^6 + 9u^4 + 8u^3 + 27u^2 + 45u + 19$
$c_4$	$(u^3 - 3u - 1)^2$
$c_7$	$u^6 + 9u^5 + 48u^4 + 349u^3 + 1647u^2 + 2058u + 757$
$c_{11}$	$u^6 + 9u^4 - 9u^3 + 54u^2 + 81u + 27$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^6 + 15y^5 - 12y^4 - 602y^3 + 4728y^2 - 24y + 1$
$c_2, c_5, c_6$	$y^6 + 3y^5 + 12y^4 + 46y^3 + 60y^2 - 12y + 1$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$y^6 + 18y^5 + 135y^4 + 460y^3 + 351y^2 - 999y + 361$
$c_4$	$(y^3 - 6y^2 + 9y - 1)^2$
$c_7$	$y^6 + 15y^5 - 684y^4 + 781y^3 + 1348797y^2 - 1741806y + 573049$
$c_{11}$	$y^6 + 18y^5 + 189y^4 + 945y^3 + 4860y^2 - 3645y + 729$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.26604 + 1.50881I$ $a = -1.17365 + 0.98481I$ $b = -1.34730$	12.0628	$-2.12061 + 0.I$
$u = -0.26604 - 1.50881I$ $a = -1.17365 - 0.98481I$ $b = -1.34730$	12.0628	$-2.12061 + 0.I$
$u = 0.326352 + 0.118782I$ $a = -0.060307 + 0.342020I$ $b = 0.879385$	-1.09662	$-5.53209 + 0.I$
$u = 0.326352 - 0.118782I$ $a = -0.060307 - 0.342020I$ $b = 0.879385$	-1.09662	$-5.53209 + 0.I$
$u = 1.43969 + 1.20805I$ $a = -1.76604 - 0.64279I$ $b = -2.53209$	-14.2561	$-4.34730 + 0.I$
$u = 1.43969 - 1.20805I$ $a = -1.76604 + 0.64279I$ $b = -2.53209$	-14.2561	$-4.34730 + 0.I$

$$\mathbf{V. } I_5^u = \langle b, a+u+1, u^2+u+1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u+2 \\ u+1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u-1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u-1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u+1 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u+1 \\ u+1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u-1 \\ -u-1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = -3

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6, c_8$ $c_9, c_{10}, c_{12}$	$u^2 - u + 1$
$c_4, c_7$	$(u - 1)^2$
$c_{11}$	$u^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6, c_8$ $c_9, c_{10}, c_{12}$	$y^2 + y + 1$
$c_4, c_7$	$(y - 1)^2$
$c_{11}$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = -0.500000 - 0.866025I$	3.28987	-3.00000
$b = 0$		
$u = -0.500000 - 0.866025I$		
$a = -0.500000 + 0.866025I$	3.28987	-3.00000
$b = 0$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)(u^4 - 3u^3 + 5u^2 - 3u + 1)$ $\cdot (u^6 - 3u^5 + 12u^4 - 46u^3 + 60u^2 + 12u + 1)$ $\cdot (u^8 + u^5 + 2u^4 - 14u^3 + 17u^2 - 7u + 1)$ $\cdot (u^9 + 12u^7 - u^6 + 8u^5 - 18u^4 + 7u^3 + 5u^2 + 10u + 1)$
$c_2, c_6$	$(u^2 - u + 1)(u^4 + u^3 - u^2 - u + 1)(u^6 + 3u^5 + \dots + 6u + 1)$ $\cdot (u^8 + 2u^7 + 2u^6 - u^5 - 4u^4 - 4u^3 + u^2 + 3u + 1)$ $\cdot (u^9 + 2u^8 + 2u^7 - u^6 + 2u^5 + 2u^4 + u^3 + 3u^2 + 4u + 1)$
$c_3, c_{12}$	$(u^2 - u + 1)(u^4 + u^3 + 2u^2 + 2u + 1)(u^6 + 9u^4 + \dots + 45u + 19)$ $\cdot (u^8 - u^7 + 6u^6 - 5u^5 + 12u^4 - 8u^3 + 9u^2 - 4u + 1)$ $\cdot (u^9 + 7u^7 + 5u^6 + 15u^5 + 13u^4 + 11u^3 + 7u^2 + u + 1)$
$c_4$	$((u - 1)^2)(u^3 - 3u - 1)^2(u^4 - 3u^3 + 2u^2 + 1)(u^4 + 3u^3 + \dots - 2u + 1)^2$ $\cdot (u^9 + 2u^8 - 7u^7 - 15u^6 + 13u^5 + 53u^4 + 71u^3 + 61u^2 + 29u + 5)$
$c_5$	$(u^2 - u + 1)(u^4 - u^3 - u^2 + u + 1)(u^6 + 3u^5 + \dots + 6u + 1)$ $\cdot (u^8 - 2u^7 + 2u^6 + u^5 - 4u^4 + 4u^3 + u^2 - 3u + 1)$ $\cdot (u^9 + 2u^8 + 2u^7 - u^6 + 2u^5 + 2u^4 + u^3 + 3u^2 + 4u + 1)$
$c_7$	$(u - 1)^2(u^2 - u + 1)^2$ $\cdot (u^6 + 9u^5 + 48u^4 + 349u^3 + 1647u^2 + 2058u + 757)$ $\cdot (u^8 + u^7 + 5u^6 + 8u^5 + 7u^4 + 11u^3 + 10u^2 + 1)$ $\cdot (u^9 - 7u^8 + 5u^7 + 42u^6 + 92u^5 + 125u^4 + 125u^3 + 88u^2 + 39u + 9)$
$c_8, c_9, c_{10}$	$(u^2 - u + 1)(u^4 - u^3 + 2u^2 - 2u + 1)(u^6 + 9u^4 + \dots + 45u + 19)$ $\cdot (u^8 + u^7 + 6u^6 + 5u^5 + 12u^4 + 8u^3 + 9u^2 + 4u + 1)$ $\cdot (u^9 + 7u^7 + 5u^6 + 15u^5 + 13u^4 + 11u^3 + 7u^2 + u + 1)$
$c_{11}$	$u^2(u^4 + 2u^2 + 3u + 1)(u^6 + 9u^4 - 9u^3 + 54u^2 + 81u + 27)$ $\cdot (u^8 - 2u^7 + 5u^6 + 3u^5 + 4u^4 + 27u^3 - 3u^2 - 16u + 52)$ $\cdot (u^9 + u^8 + 14u^7 + 10u^6 + 39u^5 - 44u^4 - 45u^3 + 4u^2 + 20u + 9)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)(y^4 + y^3 + 9y^2 + y + 1)$ $\cdot (y^6 + 15y^5 - 12y^4 - 602y^3 + 4728y^2 - 24y + 1)$ $\cdot (y^8 + 4y^6 + 33y^5 + 34y^4 - 114y^3 + 97y^2 - 15y + 1)$ $\cdot (y^9 + 24y^8 + \dots + 90y - 1)$
$c_2, c_5, c_6$	$(y^2 + y + 1)(y^4 - 3y^3 + 5y^2 - 3y + 1)$ $\cdot (y^6 + 3y^5 + 12y^4 + 46y^3 + 60y^2 - 12y + 1)$ $\cdot (y^8 + y^5 + 2y^4 - 14y^3 + 17y^2 - 7y + 1)$ $\cdot (y^9 + 12y^7 + y^6 + 8y^5 + 18y^4 + 7y^3 - 5y^2 + 10y - 1)$
$c_3, c_8, c_9$ $c_{10}, c_{12}$	$(y^2 + y + 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^6 + 18y^5 + 135y^4 + 460y^3 + 351y^2 - 999y + 361)$ $\cdot (y^8 + 11y^7 + 50y^6 + 121y^5 + 166y^4 + 124y^3 + 41y^2 + 2y + 1)$ $\cdot (y^9 + 14y^8 + 79y^7 + 207y^6 + 251y^5 + 105y^4 - 41y^3 - 53y^2 - 13y - 1)$
$c_4$	$(y - 1)^2(y^3 - 6y^2 + 9y - 1)^2(y^4 - 7y^3 + 15y^2 - 2y + 1)^2$ $\cdot (y^4 - 5y^3 + 6y^2 + 4y + 1)(y^9 - 18y^8 + \dots + 231y - 25)$
$c_7$	$(y - 1)^2(y^2 + y + 1)^2$ $\cdot (y^6 + 15y^5 - 684y^4 + 781y^3 + 1348797y^2 - 1741806y + 573049)$ $\cdot (y^8 + 9y^7 + 23y^6 + 4y^5 - 25y^4 + 29y^3 + 114y^2 + 20y + 1)$ $\cdot (y^9 - 39y^8 + \dots - 63y - 81)$
$c_{11}$	$y^2(y^4 + 4y^3 + 6y^2 - 5y + 1)$ $\cdot (y^6 + 18y^5 + 189y^4 + 945y^3 + 4860y^2 - 3645y + 729)$ $\cdot (y^8 + 6y^7 + 45y^6 + 133y^5 - 136y^4 - 137y^3 + 1289y^2 - 568y + 2704)$ $\cdot (y^9 + 27y^8 + \dots + 328y - 81)$