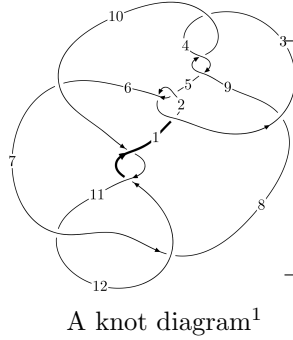
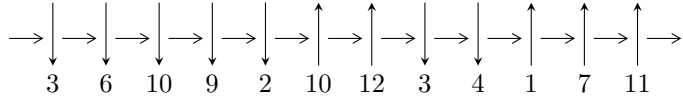


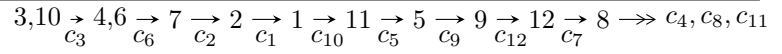
12n<sub>0342</sub> (K12n<sub>0342</sub>)



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.22257 \times 10^{23}u^{34} + 1.20633 \times 10^{24}u^{33} + \dots + 9.94460 \times 10^{24}b + 2.05358 \times 10^{25}, \\ 5.94554 \times 10^{24}u^{34} - 9.98345 \times 10^{24}u^{33} + \dots + 3.97784 \times 10^{25}a - 1.87822 \times 10^{26}, u^{35} - u^{34} + \dots + 16u + 8 \rangle$$

$$I_2^u = \langle b + 1, 4a^3 + 2a^2u - 4a - u, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - 1, v^3 - v^2 + 2v - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 44 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2.22 \times 10^{23} u^{34} + 1.21 \times 10^{24} u^{33} + \dots + 9.94 \times 10^{24} b + 2.05 \times 10^{25}, 5.95 \times 10^{24} u^{34} - 9.98 \times 10^{24} u^{33} + \dots + 3.98 \times 10^{25} a - 1.88 \times 10^{26}, u^{35} - u^{34} + \dots + 16u + 8 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.149467u^{34} + 0.250977u^{33} + \dots + 0.744011u + 4.72171 \\ 0.0223495u^{34} - 0.121305u^{33} + \dots - 3.13828u - 2.06502 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.149467u^{34} + 0.250977u^{33} + \dots + 0.744011u + 4.72171 \\ -0.0135884u^{34} - 0.0414490u^{33} + \dots - 2.70986u - 1.25294 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.135878u^{34} + 0.292426u^{33} + \dots + 3.45387u + 5.97465 \\ 0.0244551u^{34} - 0.00480744u^{33} + \dots + 1.29212u + 0.000559791 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.111423u^{34} + 0.287618u^{33} + \dots + 4.74599u + 5.97521 \\ 0.0244551u^{34} - 0.00480744u^{33} + \dots + 1.29212u + 0.000559791 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.182308u^{34} - 0.0553187u^{33} + \dots + 19.9927u + 4.90487 \\ -0.169723u^{34} + 0.180211u^{33} + \dots - 4.99372u - 0.555765 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.146821u^{34} - 0.205755u^{33} + \dots + 3.25395u - 3.12378 \\ -0.115099u^{34} + 0.0771834u^{33} + \dots - 4.79628u - 1.53754 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^3 - 2u \\ -u^3 - u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -\frac{14744603574080800564971959}{19889209336976177776682620} u^{34} + \frac{19140376741824556567023511}{19889209336976177776682620} u^{33} + \\ &\dots - \frac{13143547959375290290172530}{99446046684880888834131} u + \frac{1519825404502265762057644}{4972302334244044444170655} \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{35} + 8u^{34} + \dots - 52u + 1$
$c_2, c_5$	$u^{35} + 4u^{34} + \dots - 4u + 1$
$c_3, c_4, c_9$	$u^{35} - u^{34} + \dots + 16u + 8$
$c_6$	$u^{35} - 2u^{34} + \dots + 21u + 3$
$c_7, c_{11}$	$u^{35} + 2u^{34} + \dots + 9u + 3$
$c_8$	$u^{35} + u^{34} + \dots + 480u + 200$
$c_{10}, c_{12}$	$u^{35} - 14u^{34} + \dots + 129u - 9$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{35} + 48y^{34} + \dots + 1020y - 1$
$c_2, c_5$	$y^{35} - 8y^{34} + \dots - 52y - 1$
$c_3, c_4, c_9$	$y^{35} + 49y^{34} + \dots - 768y - 64$
$c_6$	$y^{35} - 54y^{34} + \dots - 15y - 9$
$c_7, c_{11}$	$y^{35} - 14y^{34} + \dots + 129y - 9$
$c_8$	$y^{35} + 133y^{34} + \dots - 12598400y - 40000$
$c_{10}, c_{12}$	$y^{35} + 18y^{34} + \dots + 2313y - 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.001709 + 0.955912I$		
$a = 0.185156 - 0.791460I$	$1.60959 + 1.37990I$	$-0.61653 - 3.70044I$
$b = -0.661252 + 0.559258I$		
$u = 0.001709 - 0.955912I$		
$a = 0.185156 + 0.791460I$	$1.60959 - 1.37990I$	$-0.61653 + 3.70044I$
$b = -0.661252 - 0.559258I$		
$u = -0.457643 + 0.944024I$		
$a = -0.498093 - 1.222730I$	$1.28798 + 3.57056I$	$-1.83989 - 3.72840I$
$b = -0.873919 + 0.740811I$		
$u = -0.457643 - 0.944024I$		
$a = -0.498093 + 1.222730I$	$1.28798 - 3.57056I$	$-1.83989 + 3.72840I$
$b = -0.873919 - 0.740811I$		
$u = 0.578123 + 1.001790I$		
$a = -0.641074 + 1.123880I$	$2.89503 - 8.89111I$	$0.41854 + 7.86310I$
$b = -0.937353 - 0.867983I$		
$u = 0.578123 - 1.001790I$		
$a = -0.641074 - 1.123880I$	$2.89503 + 8.89111I$	$0.41854 - 7.86310I$
$b = -0.937353 + 0.867983I$		
$u = -0.280567 + 1.198240I$		
$a = 0.212983 + 0.307706I$	$2.89532 + 2.93605I$	$1.67114 - 3.26620I$
$b = -0.848880 - 0.653452I$		
$u = -0.280567 - 1.198240I$		
$a = 0.212983 - 0.307706I$	$2.89532 - 2.93605I$	$1.67114 + 3.26620I$
$b = -0.848880 + 0.653452I$		
$u = 0.746902 + 0.064874I$		
$a = 0.763197 + 0.046917I$	$-0.31975 - 4.37952I$	$-1.83091 + 6.07452I$
$b = 0.618050 + 0.742602I$		
$u = 0.746902 - 0.064874I$		
$a = 0.763197 - 0.046917I$	$-0.31975 + 4.37952I$	$-1.83091 - 6.07452I$
$b = 0.618050 - 0.742602I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.353706 + 1.218390I$ $a = -0.474249 + 0.899612I$ $b = -0.572481 - 0.845888I$	$6.57185 - 2.11496I$	$5.70868 + 2.44246I$
$u = 0.353706 - 1.218390I$ $a = -0.474249 - 0.899612I$ $b = -0.572481 + 0.845888I$	$6.57185 + 2.11496I$	$5.70868 - 2.44246I$
$u = 0.398585 + 0.473638I$ $a = 0.800117 - 0.238876I$ $b = -0.139739 + 0.561536I$	$1.46027 + 0.77126I$	$3.61366 - 0.98435I$
$u = 0.398585 - 0.473638I$ $a = 0.800117 + 0.238876I$ $b = -0.139739 - 0.561536I$	$1.46027 - 0.77126I$	$3.61366 + 0.98435I$
$u = -0.090108 + 0.598555I$ $a = 1.184960 + 0.064358I$ $b = 1.219850 + 0.040491I$	$-3.56638 - 2.55876I$	$-1.13575 + 2.02591I$
$u = -0.090108 - 0.598555I$ $a = 1.184960 - 0.064358I$ $b = 1.219850 - 0.040491I$	$-3.56638 + 2.55876I$	$-1.13575 - 2.02591I$
$u = 0.031695 + 1.407050I$ $a = -0.911900 + 0.239123I$ $b = -0.046000 - 0.170713I$	$1.93564 + 2.80926I$	0
$u = 0.031695 - 1.407050I$ $a = -0.911900 - 0.239123I$ $b = -0.046000 + 0.170713I$	$1.93564 - 2.80926I$	0
$u = -0.576386 + 0.100273I$ $a = 0.859064 + 0.075571I$ $b = 0.794836 + 0.430575I$	$-1.361170 + 0.009026I$	$-6.02384 - 1.12650I$
$u = -0.576386 - 0.100273I$ $a = 0.859064 - 0.075571I$ $b = 0.794836 - 0.430575I$	$-1.361170 - 0.009026I$	$-6.02384 + 1.12650I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.07940 + 1.54042I$ $a = 0.1203980 + 0.0430251I$ $b = -1.303940 - 0.164109I$	$3.74701 - 1.80891I$	0
$u = -0.07940 - 1.54042I$ $a = 0.1203980 - 0.0430251I$ $b = -1.303940 + 0.164109I$	$3.74701 + 1.80891I$	0
$u = -0.020066 + 0.420369I$ $a = 3.70274 - 0.63177I$ $b = -0.763223 + 0.037247I$	$-4.12675 + 2.92147I$	$3.70844 - 4.07635I$
$u = -0.020066 - 0.420369I$ $a = 3.70274 + 0.63177I$ $b = -0.763223 - 0.037247I$	$-4.12675 - 2.92147I$	$3.70844 + 4.07635I$
$u = -0.361397$ $a = 0.932708$ $b = 0.810295$	$-1.03588$	$-12.2760$
$u = -0.14043 + 1.72815I$ $a = -0.16477 + 1.41522I$ $b = 1.14266 - 0.93268I$	$10.72680 + 6.05251I$	0
$u = -0.14043 - 1.72815I$ $a = -0.16477 - 1.41522I$ $b = 1.14266 + 0.93268I$	$10.72680 - 6.05251I$	0
$u = 0.18174 + 1.73920I$ $a = -0.077993 - 1.391040I$ $b = 1.23438 + 0.93163I$	$12.4359 - 12.0719I$	0
$u = 0.18174 - 1.73920I$ $a = -0.077993 + 1.391040I$ $b = 1.23438 - 0.93163I$	$12.4359 + 12.0719I$	0
$u = -0.00142 + 1.75473I$ $a = -0.393349 + 1.254280I$ $b = 0.860192 - 1.095830I$	$11.66250 + 1.36680I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.00142 - 1.75473I$		
$a = -0.393349 - 1.254280I$	$11.66250 - 1.36680I$	0
$b = 0.860192 + 1.095830I$		
$u = -0.05090 + 1.79450I$		
$a = -0.401616 - 1.156030I$	$13.9358 + 4.2732I$	0
$b = 0.78741 + 1.23198I$		
$u = -0.05090 - 1.79450I$		
$a = -0.401616 + 1.156030I$	$13.9358 - 4.2732I$	0
$b = 0.78741 - 1.23198I$		
$u = 0.08516 + 1.80955I$		
$a = -0.231921 - 1.248780I$	$17.6851 - 4.1242I$	0
$b = 1.08426 + 1.14113I$		
$u = 0.08516 - 1.80955I$		
$a = -0.231921 + 1.248780I$	$17.6851 + 4.1242I$	0
$b = 1.08426 - 1.14113I$		



$$\text{II. } I_2^u = \langle b + 1, 4a^3 + 2a^2u - 4a - u, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ 2a - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^2u \\ -au + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a^2u - a - \frac{1}{2}u \\ 2a^2 - 2a - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-8a^2 - 4au + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u - 1)^6$
$c_2$	$(u + 1)^6$
$c_3, c_4, c_8$ $c_9$	$(u^2 + 2)^3$
$c_6, c_{12}$	$(u^3 - u^2 + 2u - 1)^2$
$c_7$	$(u^3 + u^2 - 1)^2$
$c_{10}$	$(u^3 + u^2 + 2u + 1)^2$
$c_{11}$	$(u^3 - u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^6$
$c_3, c_4, c_8$ $c_9$	$(y + 2)^6$
$c_6, c_{10}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_7, c_{11}$	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.414210I$ $a = 0.924288 - 0.152084I$ $b = -1.00000$	$0.26574 + 2.82812I$	$-3.50976 - 2.97945I$
$u = 1.414210I$ $a = -0.924288 - 0.152084I$ $b = -1.00000$	$0.26574 - 2.82812I$	$-3.50976 + 2.97945I$
$u = 1.414210I$ $a = -0.402938I$ $b = -1.00000$	4.40332	3.01950
$u = -1.414210I$ $a = 0.924288 + 0.152084I$ $b = -1.00000$	$0.26574 - 2.82812I$	$-3.50976 + 2.97945I$
$u = -1.414210I$ $a = -0.924288 + 0.152084I$ $b = -1.00000$	$0.26574 + 2.82812I$	$-3.50976 - 2.97945I$
$u = -1.414210I$ $a = 0.402938I$ $b = -1.00000$	4.40332	3.01950

$$\text{III. } I_1^v = \langle a, b - 1, v^3 - v^2 + 2v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v^2 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ -v \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v^2 \\ -v^2 - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $10v^2 - 6v + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_4, c_8$ $c_9$	$u^3$
$c_5$	$(u + 1)^3$
$c_6, c_{10}$	$u^3 + u^2 + 2u + 1$
$c_7$	$u^3 - u^2 + 1$
$c_{11}$	$u^3 + u^2 - 1$
$c_{12}$	$u^3 - u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^3$
$c_3, c_4, c_8$ $c_9$	$y^3$
$c_6, c_{10}, c_{12}$	$y^3 + 3y^2 + 2y - 1$
$c_7, c_{11}$	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.215080 + 1.307140I$ $a = 0$ $b = 1.00000$	$-4.66906 + 2.82812I$	$-11.91407 - 2.22005I$
$v = 0.215080 - 1.307140I$ $a = 0$ $b = 1.00000$	$-4.66906 - 2.82812I$	$-11.91407 + 2.22005I$
$v = 0.569840$ $a = 0$ $b = 1.00000$	$-0.531480$	$5.82810$



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^9)(u^{35} + 8u^{34} + \dots - 52u + 1)$
$c_2$	$((u - 1)^3)(u + 1)^6(u^{35} + 4u^{34} + \dots - 4u + 1)$
$c_3, c_4, c_9$	$u^3(u^2 + 2)^3(u^{35} - u^{34} + \dots + 16u + 8)$
$c_5$	$((u - 1)^6)(u + 1)^3(u^{35} + 4u^{34} + \dots - 4u + 1)$
$c_6$	$((u^3 - u^2 + 2u - 1)^2)(u^3 + u^2 + 2u + 1)(u^{35} - 2u^{34} + \dots + 21u + 3)$
$c_7$	$(u^3 - u^2 + 1)(u^3 + u^2 - 1)^2(u^{35} + 2u^{34} + \dots + 9u + 3)$
$c_8$	$u^3(u^2 + 2)^3(u^{35} + u^{34} + \dots + 480u + 200)$
$c_{10}$	$((u^3 + u^2 + 2u + 1)^3)(u^{35} - 14u^{34} + \dots + 129u - 9)$
$c_{11}$	$((u^3 - u^2 + 1)^2)(u^3 + u^2 - 1)(u^{35} + 2u^{34} + \dots + 9u + 3)$
$c_{12}$	$((u^3 - u^2 + 2u - 1)^3)(u^{35} - 14u^{34} + \dots + 129u - 9)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^9)(y^{35} + 48y^{34} + \dots + 1020y - 1)$
$c_2, c_5$	$((y - 1)^9)(y^{35} - 8y^{34} + \dots - 52y - 1)$
$c_3, c_4, c_9$	$y^3(y + 2)^6(y^{35} + 49y^{34} + \dots - 768y - 64)$
$c_6$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{35} - 54y^{34} + \dots - 15y - 9)$
$c_7, c_{11}$	$((y^3 - y^2 + 2y - 1)^3)(y^{35} - 14y^{34} + \dots + 129y - 9)$
$c_8$	$y^3(y + 2)^6(y^{35} + 133y^{34} + \dots - 1.25984 \times 10^7 y - 40000)$
$c_{10}, c_{12}$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{35} + 18y^{34} + \dots + 2313y - 81)$