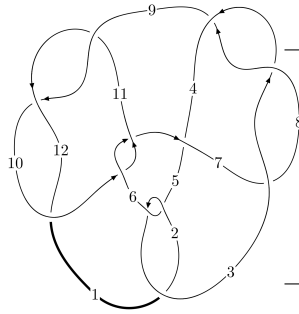
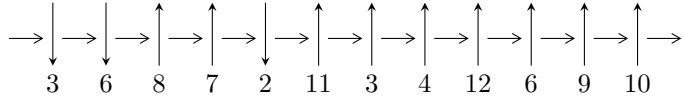


12n<sub>0344</sub> (K12n<sub>0344</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,7 \xrightarrow{c_7} 8 \xrightarrow{c_3} 4 \xrightarrow{c_8} 9,11 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \xrightarrow{c_{12}} 12 \rightsquigarrow c_4, c_9, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -1.57884 \times 10^{37} u^{43} + 4.19415 \times 10^{37} u^{42} + \dots + 3.14492 \times 10^{36} b + 2.00463 \times 10^{38}, \\ 5.51340 \times 10^{37} u^{43} - 1.47280 \times 10^{38} u^{42} + \dots + 3.14492 \times 10^{36} a - 7.82161 \times 10^{38}, u^{44} - 3u^{43} + \dots - 36u + 1 \rangle$$

$$I_2^u = \langle au + b + 2a + 1, 2a^2 - au + 2a + 2u - 3, u^2 - 2 \rangle$$

$$I_1^v = \langle a, b + v - 2, v^2 - 3v + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 50 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.58 \times 10^{37} u^{43} + 4.19 \times 10^{37} u^{42} + \dots + 3.14 \times 10^{36} b + 2.00 \times 10^{38}, 5.51 \times 10^{37} u^{43} - 1.47 \times 10^{38} u^{42} + \dots + 3.14 \times 10^{36} a - 7.82 \times 10^{38}, u^{44} - 3u^{43} + \dots - 36u + 4 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -17.5312u^{43} + 46.8311u^{42} + \dots - 1316.37u + 248.706 \\ 5.02029u^{43} - 13.3363u^{42} + \dots + 367.657u - 63.7420 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 3.47461u^{43} - 10.7515u^{42} + \dots + 355.136u - 74.5401 \\ -1.68885u^{43} + 5.62072u^{42} + \dots - 173.747u + 30.1506 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -9.86564u^{43} + 26.8155u^{42} + \dots - 755.031u + 138.369 \\ -4.70217u^{43} + 10.4432u^{42} + \dots - 226.148u + 33.6781 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -9.86564u^{43} + 26.8155u^{42} + \dots - 755.031u + 138.369 \\ -4.03012u^{43} + 8.38511u^{42} + \dots - 165.479u + 22.5523 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -19.4067u^{43} + 52.8978u^{42} + \dots - 1495.34u + 274.133 \\ -4.36737u^{43} + 8.86394u^{42} + \dots - 164.017u + 21.4464 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -15.0159u^{43} + 40.6500u^{42} + \dots - 1164.20u + 225.930 \\ 5.45610u^{43} - 13.6789u^{42} + \dots + 357.423u - 61.0333 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-58.5401u^{43} + 159.424u^{42} + \dots - 4534.07u + 846.150$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{44} + 45u^{43} + \dots + 4203u + 81$
$c_2, c_5$	$u^{44} + 3u^{43} + \dots + 21u - 9$
$c_3, c_7, c_8$	$u^{44} - 3u^{43} + \dots - 36u + 4$
$c_4$	$u^{44} + 9u^{43} + \dots + 1500u - 964$
$c_6, c_{10}$	$u^{44} + 2u^{43} + \dots + 10u + 1$
$c_9, c_{11}, c_{12}$	$u^{44} + 4u^{43} + \dots - 18u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{44} - 85y^{43} + \dots - 6110883y + 6561$
$c_2, c_5$	$y^{44} - 45y^{43} + \dots - 4203y + 81$
$c_3, c_7, c_8$	$y^{44} - 39y^{43} + \dots - 368y + 16$
$c_4$	$y^{44} + 21y^{43} + \dots - 41187888y + 929296$
$c_6, c_{10}$	$y^{44} - 12y^{43} + \dots - 58y + 1$
$c_9, c_{11}, c_{12}$	$y^{44} - 36y^{43} + \dots - 242y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.361562 + 0.932667I$ $a = 0.23727 - 1.40400I$ $b = 0.961486 - 1.024300I$	$-4.54866 - 9.17617I$	$5.81808 + 6.48451I$
$u = -0.361562 - 0.932667I$ $a = 0.23727 + 1.40400I$ $b = 0.961486 + 1.024300I$	$-4.54866 + 9.17617I$	$5.81808 - 6.48451I$
$u = 0.242419 + 0.963914I$ $a = 0.542404 + 0.771039I$ $b = 0.650253 + 0.479584I$	$2.03227 + 3.85207I$	$10.41827 - 8.61488I$
$u = 0.242419 - 0.963914I$ $a = 0.542404 - 0.771039I$ $b = 0.650253 - 0.479584I$	$2.03227 - 3.85207I$	$10.41827 + 8.61488I$
$u = -0.155342 + 0.896950I$ $a = -0.31935 + 1.38694I$ $b = -0.99704 + 1.03670I$	$-8.52514 - 3.75610I$	$2.09209 + 2.89832I$
$u = -0.155342 - 0.896950I$ $a = -0.31935 - 1.38694I$ $b = -0.99704 - 1.03670I$	$-8.52514 + 3.75610I$	$2.09209 - 2.89832I$
$u = 1.125730 + 0.043899I$ $a = 0.058942 + 0.745233I$ $b = 0.556341 + 0.553872I$	$1.99922 - 0.04818I$	$6.00000 + 0.I$
$u = 1.125730 - 0.043899I$ $a = 0.058942 - 0.745233I$ $b = 0.556341 - 0.553872I$	$1.99922 + 0.04818I$	$6.00000 + 0.I$
$u = -0.851420 + 0.746270I$ $a = -0.677609 - 0.190566I$ $b = -0.609425 - 0.874938I$	$-3.05540 + 3.53185I$	$6.00000 + 0.I$
$u = -0.851420 - 0.746270I$ $a = -0.677609 + 0.190566I$ $b = -0.609425 + 0.874938I$	$-3.05540 - 3.53185I$	$6.00000 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.060206 + 0.789681I$ $a = 0.420124 - 1.337940I$ $b = 1.05150 - 1.02729I$	$-4.31168 + 1.72166I$	$4.04968 - 1.22187I$
$u = 0.060206 - 0.789681I$ $a = 0.420124 + 1.337940I$ $b = 1.05150 + 1.02729I$	$-4.31168 - 1.72166I$	$4.04968 + 1.22187I$
$u = -1.104880 + 0.498321I$ $a = 0.424315 + 0.083138I$ $b = 0.625620 + 1.104260I$	$-5.61992 - 1.18304I$	0
$u = -1.104880 - 0.498321I$ $a = 0.424315 - 0.083138I$ $b = 0.625620 - 1.104260I$	$-5.61992 + 1.18304I$	0
$u = 1.22068$ $a = -1.07819$ $b = 1.88874$	10.3320	0
$u = 1.218830 + 0.333934I$ $a = 1.13833 - 0.87054I$ $b = -1.31850 - 0.66505I$	$-0.76043 + 2.33473I$	0
$u = 1.218830 - 0.333934I$ $a = 1.13833 + 0.87054I$ $b = -1.31850 + 0.66505I$	$-0.76043 - 2.33473I$	0
$u = -1.271900 + 0.268067I$ $a = -0.553133 - 1.124420I$ $b = 0.895901 - 0.644934I$	$2.75377 - 4.58010I$	0
$u = -1.271900 - 0.268067I$ $a = -0.553133 + 1.124420I$ $b = 0.895901 + 0.644934I$	$2.75377 + 4.58010I$	0
$u = -1.305420 + 0.064505I$ $a = 1.20456 + 0.91583I$ $b = -0.813618 + 0.359887I$	$5.20530 - 0.47373I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.305420 - 0.064505I$ $a = 1.20456 - 0.91583I$ $b = -0.813618 - 0.359887I$	$5.20530 + 0.47373I$	0
$u = 1.310900 + 0.166284I$ $a = -0.028578 + 0.886239I$ $b = -0.526233 + 0.907268I$	$5.87917 + 2.87968I$	0
$u = 1.310900 - 0.166284I$ $a = -0.028578 - 0.886239I$ $b = -0.526233 - 0.907268I$	$5.87917 - 2.87968I$	0
$u = -1.310400 + 0.345353I$ $a = -0.233101 - 0.138958I$ $b = -0.79762 - 1.32164I$	$-0.02123 - 5.81626I$	0
$u = -1.310400 - 0.345353I$ $a = -0.233101 + 0.138958I$ $b = -0.79762 + 1.32164I$	$-0.02123 + 5.81626I$	0
$u = -1.39785$ $a = 8.91764$ $b = -0.188474$	4.90257	0
$u = -0.006322 + 0.581193I$ $a = -0.89655 - 1.33079I$ $b = -0.503249 - 0.484782I$	$-1.17226 + 1.37524I$	$0.82630 - 4.37313I$
$u = -0.006322 - 0.581193I$ $a = -0.89655 + 1.33079I$ $b = -0.503249 + 0.484782I$	$-1.17226 - 1.37524I$	$0.82630 + 4.37313I$
$u = 1.37514 + 0.39616I$ $a = -0.881677 + 1.000200I$ $b = 1.24438 + 0.87011I$	$-3.70647 + 8.39508I$	0
$u = 1.37514 - 0.39616I$ $a = -0.881677 - 1.000200I$ $b = 1.24438 - 0.87011I$	$-3.70647 - 8.39508I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.33260 + 0.53021I$ $a = -0.126765 - 0.487206I$ $b = -0.626528 - 0.301390I$	$5.26881 + 2.02524I$	0
$u = 1.33260 - 0.53021I$ $a = -0.126765 + 0.487206I$ $b = -0.626528 + 0.301390I$	$5.26881 - 2.02524I$	0
$u = 1.45079$ $a = 0.972042$ $b = -0.251576$	3.37301	0
$u = -1.45928$ $a = -0.521642$ $b = 1.51795$	13.6404	0
$u = -1.41359 + 0.38694I$ $a = 0.320048 + 0.993129I$ $b = -0.997773 + 0.724464I$	$7.26218 - 8.61162I$	0
$u = -1.41359 - 0.38694I$ $a = 0.320048 - 0.993129I$ $b = -0.997773 - 0.724464I$	$7.26218 + 8.61162I$	0
$u = 1.48503 + 0.37724I$ $a = 0.730260 - 1.019420I$ $b = -1.20624 - 0.98697I$	$1.34332 + 13.91980I$	0
$u = 1.48503 - 0.37724I$ $a = 0.730260 + 1.019420I$ $b = -1.20624 + 0.98697I$	$1.34332 - 13.91980I$	0
$u = -0.115716 + 0.402697I$ $a = -0.38670 + 2.62883I$ $b = 0.377022 + 0.479190I$	$1.42746 - 0.71018I$	$6.25077 - 1.25816I$
$u = -0.115716 - 0.402697I$ $a = -0.38670 - 2.62883I$ $b = 0.377022 - 0.479190I$	$1.42746 + 0.71018I$	$6.25077 + 1.25816I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.339286$ $a = -1.00783$ $b = -1.53932$	7.49147	26.0080
$u = 0.302786$ $a = -0.689575$ $b = 0.583905$	0.759214	14.0520
$u = 0.266557$ $a = 9.48986$ $b = -0.525421$	-0.455563	39.4620
$u = 1.76844$ $a = -0.0279231$ $b = 0.581616$	6.40427	0

$$\text{II. } I_2^u = \langle au + b + 2a + 1, 2a^2 - au + 2a + 2u - 3, u^2 - 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -au - 2a - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u \\ au + 2a + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u \\ au + 2a + u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u \\ au + 2a + 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} au + 2a + \frac{1}{2}u \\ au + 2a + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -au - a - 1 \\ -au - 2a - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u - 1)^4$
$c_2$	$(u + 1)^4$
$c_3, c_4, c_7$ $c_8$	$(u^2 - 2)^2$
$c_6, c_{11}, c_{12}$	$(u^2 + u - 1)^2$
$c_9, c_{10}$	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^4$
$c_3, c_4, c_7$ $c_8$	$(y - 2)^4$
$c_6, c_9, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$ $a = -0.473911$ $b = 0.618034$	4.27683	12.0000
$u = 1.41421$ $a = 0.181018$ $b = -1.61803$	12.1725	12.0000
$u = -1.41421$ $a = 1.05505$ $b = -1.61803$	12.1725	12.0000
$u = -1.41421$ $a = -2.76216$ $b = 0.618034$	4.27683	12.0000

$$\text{III. } I_1^v = \langle a, b + v - 2, v^2 - 3v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -v + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -v + 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v - 1 \\ v - 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ v - 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v - 2 \\ v - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -v + 2 \\ -v + 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -6

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_4, c_7$ $c_8$	$u^2$
$c_5$	$(u + 1)^2$
$c_6, c_9$	$u^2 - u - 1$
$c_{10}, c_{11}, c_{12}$	$u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^2$
$c_3, c_4, c_7$ $c_8$	$y^2$
$c_6, c_9, c_{10}$ $c_{11}, c_{12}$	$y^2 - 3y + 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.381966$ $a = 0$ $b = 1.61803$	7.23771	-6.00000
$v = 2.61803$ $a = 0$ $b = -0.618034$	-0.657974	-6.00000

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^6)(u^{44} + 45u^{43} + \dots + 4203u + 81)$
$c_2$	$((u - 1)^2)(u + 1)^4(u^{44} + 3u^{43} + \dots + 21u - 9)$
$c_3, c_7, c_8$	$u^2(u^2 - 2)^2(u^{44} - 3u^{43} + \dots - 36u + 4)$
$c_4$	$u^2(u^2 - 2)^2(u^{44} + 9u^{43} + \dots + 1500u - 964)$
$c_5$	$((u - 1)^4)(u + 1)^2(u^{44} + 3u^{43} + \dots + 21u - 9)$
$c_6$	$(u^2 - u - 1)(u^2 + u - 1)^2(u^{44} + 2u^{43} + \dots + 10u + 1)$
$c_9$	$((u^2 - u - 1)^3)(u^{44} + 4u^{43} + \dots - 18u + 1)$
$c_{10}$	$((u^2 - u - 1)^2)(u^2 + u - 1)(u^{44} + 2u^{43} + \dots + 10u + 1)$
$c_{11}, c_{12}$	$((u^2 + u - 1)^3)(u^{44} + 4u^{43} + \dots - 18u + 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^6)(y^{44} - 85y^{43} + \dots - 6110883y + 6561)$
$c_2, c_5$	$((y-1)^6)(y^{44} - 45y^{43} + \dots - 4203y + 81)$
$c_3, c_7, c_8$	$y^2(y-2)^4(y^{44} - 39y^{43} + \dots - 368y + 16)$
$c_4$	$y^2(y-2)^4(y^{44} + 21y^{43} + \dots - 4.11879 \times 10^7 y + 929296)$
$c_6, c_{10}$	$((y^2 - 3y + 1)^3)(y^{44} - 12y^{43} + \dots - 58y + 1)$
$c_9, c_{11}, c_{12}$	$((y^2 - 3y + 1)^3)(y^{44} - 36y^{43} + \dots - 242y + 1)$