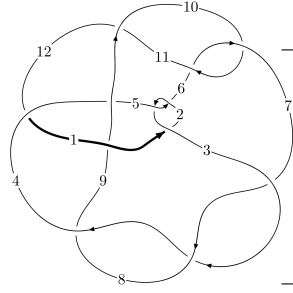
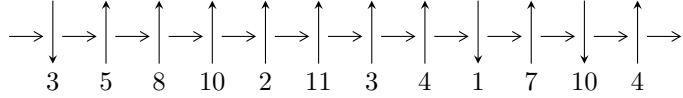


12n<sub>0349</sub> (K12n<sub>0349</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,8 \xrightarrow{c_8} 9,12 \xrightarrow{c_{12}} 1 \xrightarrow{c_9} 10 \xrightarrow{c_4} 5 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_5} 6 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \twoheadrightarrow c_1, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 5.03279 \times 10^{28} u^{21} + 1.41088 \times 10^{28} u^{20} + \dots + 3.11126 \times 10^{30} b - 1.47947 \times 10^{30}, \\ 2.83952 \times 10^{29} u^{21} + 2.39177 \times 10^{30} u^{20} + \dots + 5.38247 \times 10^{32} a - 1.28920 \times 10^{33}, \\ u^{22} - u^{21} + \dots + 570u - 173 \rangle$$

$$I_2^u = \langle 4u^{15} + u^{14} + \dots + b - 5, 5u^{15} + 2u^{14} + \dots + a - 5, \\ u^{16} - 7u^{14} - u^{13} + 22u^{12} + 6u^{11} - 43u^{10} - 15u^9 + 58u^8 + 19u^7 - 52u^6 - 13u^5 + 29u^4 + 5u^3 - 8u^2 - u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 38 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 5.03 \times 10^{28} u^{21} + 1.41 \times 10^{28} u^{20} + \dots + 3.11 \times 10^{30} b - 1.48 \times 10^{30}, 2.84 \times 10^{29} u^{21} + 2.39 \times 10^{30} u^{20} + \dots + 5.38 \times 10^{32} a - 1.29 \times 10^{33}, u^{22} - u^{21} + \dots + 570u - 173 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.000527549u^{21} - 0.00444362u^{20} + \dots - 2.94596u + 2.39519 \\ -0.0161761u^{21} - 0.00453474u^{20} + \dots + 4.84486u + 0.475523 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.000527549u^{21} - 0.00444362u^{20} + \dots - 2.94596u + 2.39519 \\ -0.0112823u^{21} - 0.00307489u^{20} + \dots + 2.10256u + 1.33554 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.00747297u^{21} - 0.00222999u^{20} + \dots + 1.32872u + 0.919896 \\ -0.0287409u^{21} + 0.00951872u^{20} + \dots + 15.0584u - 4.13187 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0176760u^{21} + 0.00338113u^{20} + \dots + 7.60759u - 1.52246 \\ -0.00312229u^{21} + 0.0168476u^{20} + \dots + 9.58458u - 3.73734 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0117801u^{21} - 0.0136133u^{20} + \dots - 11.9200u + 5.73898 \\ -0.0235899u^{21} + 0.00609484u^{20} + \dots + 11.0766u - 2.00826 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0114740u^{21} - 0.00633450u^{20} + \dots - 6.51280u + 1.90552 \\ -0.0333527u^{21} + 0.0105246u^{20} + \dots + 16.7996u - 4.51821 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0267510u^{21} - 0.00298230u^{20} + \dots + 5.83060u + 2.41175 \\ -0.0193326u^{21} + 0.0165589u^{20} + \dots + 15.3927u - 4.75155 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.0344880u^{21} - 0.0647662u^{20} + \dots - 54.7216u + 34.1950$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{22} + 3u^{21} + \dots + 129u + 121$
$c_2, c_5$	$u^{22} + 3u^{21} + \dots + 61u - 11$
$c_3, c_7, c_8$	$u^{22} + u^{21} + \dots - 570u - 173$
$c_4$	$u^{22} + 12u^{21} + \dots - 5056u - 1856$
$c_6, c_{10}$	$u^{22} - u^{21} + \dots + 387u - 119$
$c_9$	$u^{22} - 3u^{21} + \dots - 17u + 1$
$c_{11}$	$u^{22} + u^{21} + \dots - 50523u + 14161$
$c_{12}$	$u^{22} + u^{21} + \dots + 8u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{22} + 47y^{21} + \dots + 1408497y + 14641$
$c_2, c_5$	$y^{22} + 3y^{21} + \dots + 129y + 121$
$c_3, c_7, c_8$	$y^{22} - 33y^{21} + \dots - 222830y + 29929$
$c_4$	$y^{22} - 48y^{21} + \dots - 17842176y + 3444736$
$c_6, c_{10}$	$y^{22} + y^{21} + \dots - 50523y + 14161$
$c_9$	$y^{22} + 17y^{21} + \dots - 89y + 1$
$c_{11}$	$y^{22} + 57y^{21} + \dots - 20509146359y + 200533921$
$c_{12}$	$y^{22} + 49y^{21} + \dots - 52y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.888889 + 0.621508I$ $a = -0.785790 - 0.787936I$ $b = 1.41234 - 0.32273I$	$-2.09331 + 2.22663I$	$10.35334 - 5.55870I$
$u = 0.888889 - 0.621508I$ $a = -0.785790 + 0.787936I$ $b = 1.41234 + 0.32273I$	$-2.09331 - 2.22663I$	$10.35334 + 5.55870I$
$u = 1.125980 + 0.181359I$ $a = 0.194049 + 0.934438I$ $b = 0.533838 + 1.294670I$	$2.80761 - 4.32610I$	$7.93255 + 4.44451I$
$u = 1.125980 - 0.181359I$ $a = 0.194049 - 0.934438I$ $b = 0.533838 - 1.294670I$	$2.80761 + 4.32610I$	$7.93255 - 4.44451I$
$u = 0.468073 + 0.568730I$ $a = 0.033725 - 0.194825I$ $b = 0.67213 + 1.29726I$	$0.96204 - 3.13844I$	$5.33676 + 0.34451I$
$u = 0.468073 - 0.568730I$ $a = 0.033725 + 0.194825I$ $b = 0.67213 - 1.29726I$	$0.96204 + 3.13844I$	$5.33676 - 0.34451I$
$u = -1.219380 + 0.529046I$ $a = -1.29654 + 1.66639I$ $b = 0.021894 + 0.717525I$	$-9.56729 - 1.76902I$	$9.41797 + 0.67359I$
$u = -1.219380 - 0.529046I$ $a = -1.29654 - 1.66639I$ $b = 0.021894 - 0.717525I$	$-9.56729 + 1.76902I$	$9.41797 - 0.67359I$
$u = 1.138980 + 0.705814I$ $a = 0.762830 + 0.903956I$ $b = -1.373520 + 0.140422I$	$-5.89358 + 2.47710I$	$2.52368 - 2.07081I$
$u = 1.138980 - 0.705814I$ $a = 0.762830 - 0.903956I$ $b = -1.373520 - 0.140422I$	$-5.89358 - 2.47710I$	$2.52368 + 2.07081I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.390919 + 0.487203I$ $a = -0.142272 - 0.861639I$ $b = 0.433308 - 0.046954I$	$-1.67513 + 1.49906I$	$2.16861 - 5.00550I$
$u = 0.390919 - 0.487203I$ $a = -0.142272 + 0.861639I$ $b = 0.433308 + 0.046954I$	$-1.67513 - 1.49906I$	$2.16861 + 5.00550I$
$u = -0.486914$ $a = 0.684920$ $b = -0.232651$	$0.667389$	$15.1430$
$u = -1.51784 + 0.10872I$ $a = 0.152442 + 0.390876I$ $b = -0.0746395 + 0.0560374I$	$4.60852 - 3.54663I$	$3.76213 + 0.30741I$
$u = -1.51784 - 0.10872I$ $a = 0.152442 - 0.390876I$ $b = -0.0746395 - 0.0560374I$	$4.60852 + 3.54663I$	$3.76213 - 0.30741I$
$u = -1.16828 + 1.29949I$ $a = 0.771799 - 0.429092I$ $b = -0.50715 - 2.09278I$	$5.62161 - 3.04840I$	$8.24444 + 1.87699I$
$u = -1.16828 - 1.29949I$ $a = 0.771799 + 0.429092I$ $b = -0.50715 + 2.09278I$	$5.62161 + 3.04840I$	$8.24444 - 1.87699I$
$u = 1.88865 + 0.65161I$ $a = 0.557638 + 0.987237I$ $b = -1.32425 + 1.66024I$	$14.5063 + 11.3964I$	$7.17418 - 4.33997I$
$u = 1.88865 - 0.65161I$ $a = 0.557638 - 0.987237I$ $b = -1.32425 - 1.66024I$	$14.5063 - 11.3964I$	$7.17418 + 4.33997I$
$u = 2.18883$ $a = -0.226088$ $b = -2.17979$	$10.8028$	$8.45190$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.34694 + 0.29798I$	$16.2419 - 0.6601I$	$8.28889 + 0.I$
$a = 0.184555 - 0.987184I$		
$b = -0.08772 - 2.56787I$		
$u = -2.34694 - 0.29798I$	$16.2419 + 0.6601I$	$8.28889 + 0.I$
$a = 0.184555 + 0.987184I$		
$b = -0.08772 + 2.56787I$		

**II.**

$$I_2^u = \langle 4u^{15} + u^{14} + \dots + b - 5, 5u^{15} + 2u^{14} + \dots + a - 5, u^{16} - 7u^{14} + \dots - u + 1 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -5u^{15} - 2u^{14} + \dots + 10u + 5 \\ -4u^{15} - u^{14} + \dots + 9u + 5 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -5u^{15} - 2u^{14} + \dots + 10u + 5 \\ -2u^{15} + 14u^{13} + \dots + 6u + 3 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^{14} + 6u^{12} + \dots - 8u^2 - u \\ -4u^{15} - 2u^{14} + \dots + 7u + 6 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 2u^{15} - 13u^{13} + \dots + 3u^2 - 2u \\ 2u^{15} + u^{14} + \dots - 2u - 5 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -3u^{15} - u^{14} + \dots + 5u + 3 \\ -4u^{15} - u^{14} + \dots + 11u + 5 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 5u^{15} + u^{14} + \dots - 12u - 5 \\ 4u^{15} + 2u^{14} + \dots - 10u - 6 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -2u^{15} - 2u^{14} + \dots + 3u + 2 \\ -5u^{15} - 2u^{14} + \dots + 9u + 7 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**  $= -14u^{15} - 7u^{14} + 93u^{13} + 59u^{12} - 272u^{11} - 213u^{10} + 485u^9 + 439u^8 - 583u^7 - 544u^6 + 451u^5 + 409u^4 - 202u^3 - 183u^2 + 22u + 36$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{16} - 14u^{15} + \dots - 18u + 1$
$c_2$	$u^{16} + 2u^{15} + \dots + 2u + 1$
$c_3$	$u^{16} - 7u^{14} + \dots + u + 1$
$c_4$	$u^{16} + 2u^{14} + \dots - u + 1$
$c_5$	$u^{16} - 2u^{15} + \dots - 2u + 1$
$c_6$	$u^{16} + 8u^{14} + \dots + 2u + 1$
$c_7, c_8$	$u^{16} - 7u^{14} + \dots - u + 1$
$c_9$	$u^{16} - 4u^{15} + \dots + 4u^3 + 1$
$c_{10}$	$u^{16} + 8u^{14} + \dots - 2u + 1$
$c_{11}$	$u^{16} + 16u^{15} + \dots + 18u + 1$
$c_{12}$	$u^{16} + 14u^{14} + \dots + 7u + 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{16} - 10y^{15} + \dots - 42y + 1$
$c_2, c_5$	$y^{16} + 14y^{15} + \dots + 18y + 1$
$c_3, c_7, c_8$	$y^{16} - 14y^{15} + \dots - 17y + 1$
$c_4$	$y^{16} + 4y^{15} + \dots + y + 1$
$c_6, c_{10}$	$y^{16} + 16y^{15} + \dots + 18y + 1$
$c_9$	$y^{16} - 4y^{15} + \dots - 12y^2 + 1$
$c_{11}$	$y^{16} - 16y^{15} + \dots - 18y + 1$
$c_{12}$	$y^{16} + 28y^{15} + \dots + 1505y + 49$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.895121 + 0.512839I$ $a = -0.764453 - 0.786216I$ $b = 1.48200 - 0.38704I$	$-2.57741 + 2.02646I$	$-4.32270 - 0.49641I$
$u = 0.895121 - 0.512839I$ $a = -0.764453 + 0.786216I$ $b = 1.48200 + 0.38704I$	$-2.57741 - 2.02646I$	$-4.32270 + 0.49641I$
$u = -0.991446 + 0.300154I$ $a = 0.72110 - 1.52416I$ $b = -1.200410 - 0.280363I$	$-5.52393 - 1.17654I$	$4.37675 - 1.28594I$
$u = -0.991446 - 0.300154I$ $a = 0.72110 + 1.52416I$ $b = -1.200410 + 0.280363I$	$-5.52393 + 1.17654I$	$4.37675 + 1.28594I$
$u = 1.042540 + 0.498206I$ $a = 1.57083 + 2.03165I$ $b = -0.562512 + 0.129135I$	$-10.21970 + 1.92477I$	$-2.98411 - 3.89934I$
$u = 1.042540 - 0.498206I$ $a = 1.57083 - 2.03165I$ $b = -0.562512 - 0.129135I$	$-10.21970 - 1.92477I$	$-2.98411 + 3.89934I$
$u = -0.947353 + 0.893061I$ $a = -0.995021 + 0.545877I$ $b = 1.157010 + 0.171797I$	$-5.04353 - 3.27906I$	$6.96610 + 5.21245I$
$u = -0.947353 - 0.893061I$ $a = -0.995021 - 0.545877I$ $b = 1.157010 - 0.171797I$	$-5.04353 + 3.27906I$	$6.96610 - 5.21245I$
$u = -0.535533 + 0.224627I$ $a = -0.50673 - 1.96194I$ $b = 0.091098 - 1.093350I$	$0.313495 - 1.189950I$	$7.79460 + 1.38246I$
$u = -0.535533 - 0.224627I$ $a = -0.50673 + 1.96194I$ $b = 0.091098 + 1.093350I$	$0.313495 + 1.189950I$	$7.79460 - 1.38246I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.42936 + 0.19543I$		
$a = 0.667578 + 0.371646I$	$3.92703 - 0.68720I$	$9.16301 - 0.40551I$
$b = -0.005180 + 0.635975I$		
$u = -1.42936 - 0.19543I$		
$a = 0.667578 - 0.371646I$	$3.92703 + 0.68720I$	$9.16301 + 0.40551I$
$b = -0.005180 - 0.635975I$		
$u = 1.46404 + 0.03561I$		
$a = 0.004983 - 0.187762I$	$5.03010 + 4.12297I$	$11.6031 - 8.8115I$
$b = 0.403326 - 0.712059I$		
$u = 1.46404 - 0.03561I$		
$a = 0.004983 + 0.187762I$	$5.03010 - 4.12297I$	$11.6031 + 8.8115I$
$b = 0.403326 + 0.712059I$		
$u = 0.501986 + 0.071058I$		
$a = -0.69829 - 1.53708I$	$0.93447 + 4.27246I$	$4.40321 - 6.78367I$
$b = 0.634668 - 1.218490I$		
$u = 0.501986 - 0.071058I$		
$a = -0.69829 + 1.53708I$	$0.93447 - 4.27246I$	$4.40321 + 6.78367I$
$b = 0.634668 + 1.218490I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{16} - 14u^{15} + \dots - 18u + 1)(u^{22} + 3u^{21} + \dots + 129u + 121)$
$c_2$	$(u^{16} + 2u^{15} + \dots + 2u + 1)(u^{22} + 3u^{21} + \dots + 61u - 11)$
$c_3$	$(u^{16} - 7u^{14} + \dots + u + 1)(u^{22} + u^{21} + \dots - 570u - 173)$
$c_4$	$(u^{16} + 2u^{14} + \dots - u + 1)(u^{22} + 12u^{21} + \dots - 5056u - 1856)$
$c_5$	$(u^{16} - 2u^{15} + \dots - 2u + 1)(u^{22} + 3u^{21} + \dots + 61u - 11)$
$c_6$	$(u^{16} + 8u^{14} + \dots + 2u + 1)(u^{22} - u^{21} + \dots + 387u - 119)$
$c_7, c_8$	$(u^{16} - 7u^{14} + \dots - u + 1)(u^{22} + u^{21} + \dots - 570u - 173)$
$c_9$	$(u^{16} - 4u^{15} + \dots + 4u^3 + 1)(u^{22} - 3u^{21} + \dots - 17u + 1)$
$c_{10}$	$(u^{16} + 8u^{14} + \dots - 2u + 1)(u^{22} - u^{21} + \dots + 387u - 119)$
$c_{11}$	$(u^{16} + 16u^{15} + \dots + 18u + 1)(u^{22} + u^{21} + \dots - 50523u + 14161)$
$c_{12}$	$(u^{16} + 14u^{14} + \dots + 7u + 7)(u^{22} + u^{21} + \dots + 8u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{16} - 10y^{15} + \dots - 42y + 1)(y^{22} + 47y^{21} + \dots + 1408497y + 14641)$
$c_2, c_5$	$(y^{16} + 14y^{15} + \dots + 18y + 1)(y^{22} + 3y^{21} + \dots + 129y + 121)$
$c_3, c_7, c_8$	$(y^{16} - 14y^{15} + \dots - 17y + 1)(y^{22} - 33y^{21} + \dots - 222830y + 29929)$
$c_4$	$(y^{16} + 4y^{15} + \dots + y + 1)(y^{22} - 48y^{21} + \dots - 1.78422 \times 10^7 y + 3444736)$
$c_6, c_{10}$	$(y^{16} + 16y^{15} + \dots + 18y + 1)(y^{22} + y^{21} + \dots - 50523y + 14161)$
$c_9$	$(y^{16} - 4y^{15} + \dots - 12y^2 + 1)(y^{22} + 17y^{21} + \dots - 89y + 1)$
$c_{11}$	$(y^{16} - 16y^{15} + \dots - 18y + 1)$ $\cdot (y^{22} + 57y^{21} + \dots - 20509146359y + 200533921)$
$c_{12}$	$(y^{16} + 28y^{15} + \dots + 1505y + 49)(y^{22} + 49y^{21} + \dots - 52y + 1)$