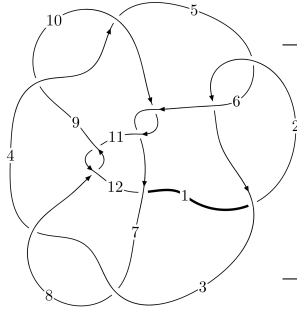
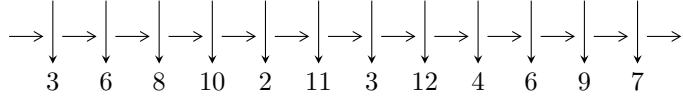


12n<sub>0374</sub> (K12n<sub>0374</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6, 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_6} 3, 7 \xrightarrow{c_7} 8 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \Rightarrow c_3, c_8, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -301149306547334u^{15} - 405785743495567u^{14} + \dots + 5460935417391053b - 2324129620964575, \\ 2521976827730410u^{15} + 4134029936992622u^{14} + \dots + 5460935417391053a - 8351550389039156, \\ u^{16} + 2u^{15} + \dots + u - 1 \rangle$$

$$I_2^u = \langle u^9 + u^8 - 2u^7 + 2u^6 + 3u^5 - 6u^4 + 2u^2 + b - 2u - 1, \\ u^{10} - 4u^8 + 2u^7 + 4u^6 - 6u^5 + u^4 + 4u^3 - u^2 + a - u + 1, \\ u^{11} + u^{10} - 3u^9 + 5u^7 - 4u^6 - 4u^5 + 4u^4 + u^3 - 3u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 27 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -3.01 \times 10^{14} u^{15} - 4.06 \times 10^{14} u^{14} + \dots + 5.46 \times 10^{15} b - 2.32 \times 10^{15}, 2.52 \times 10^{15} u^{15} + 4.13 \times 10^{15} u^{14} + \dots + 5.46 \times 10^{15} a - 8.35 \times 10^{15}, u^{16} + 2u^{15} + \dots + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.461821u^{15} - 0.757019u^{14} + \dots + 1.13267u + 1.52933 \\ 0.0551461u^{15} + 0.0743070u^{14} + \dots - 1.30799u + 0.425592 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1.16646u^{15} - 2.14400u^{14} + \dots - 0.648553u + 1.23228 \\ 0.142447u^{15} + 0.241985u^{14} + \dots - 2.03492u + 0.447884 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.461821u^{15} - 0.757019u^{14} + \dots + 1.13267u + 1.52933 \\ 0.0215283u^{15} + 0.0644709u^{14} + \dots - 0.679549u + 0.258968 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1.49486u^{15} + 2.51422u^{14} + \dots - 4.17011u - 0.263898 \\ -0.226698u^{15} - 0.0915071u^{14} + \dots + 4.12577u - 0.807954 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1.28737u^{15} + 2.32151u^{14} + \dots - 1.70682u - 1.04336 \\ -0.120918u^{15} - 0.177515u^{14} + \dots + 2.35537u - 0.188916 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1.16646u^{15} + 2.14400u^{14} + \dots + 0.648553u - 1.23228 \\ -0.120918u^{15} - 0.177515u^{14} + \dots + 2.35537u - 0.188916 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.802633u^{15} + 1.98845u^{14} + \dots + 8.96383u - 3.11463 \\ -0.352889u^{15} - 0.635726u^{14} + \dots + 0.487447u + 0.504102 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1.38603u^{15} + 2.45156u^{14} + \dots - 2.59193u - 0.500660 \\ -0.149090u^{15} - 0.0711014u^{14} + \dots + 2.28378u - 0.416208 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{9739656845787569}{5460935417391053} u^{15} - \frac{17595322506035493}{5460935417391053} u^{14} + \dots + \frac{16486080638841760}{5460935417391053} u - \frac{93508315704564998}{5460935417391053}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{16} - 22u^{15} + \dots + 28u + 1$
$c_2, c_5$	$u^{16} + 4u^{15} + \dots - 2u - 1$
$c_3, c_7$	$u^{16} - 14u^{15} + \dots + 152u^2 - 32$
$c_4, c_9$	$u^{16} + u^{15} + \dots - 184u - 85$
$c_6, c_{10}$	$u^{16} - 2u^{15} + \dots - u - 1$
$c_8, c_{11}$	$u^{16} - 2u^{15} + \dots + 2u + 1$
$c_{12}$	$u^{16} + 8u^{15} + \dots - 17328u - 2417$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{16} + 14y^{15} + \dots - 540y + 1$
$c_2, c_5$	$y^{16} + 22y^{15} + \dots - 28y + 1$
$c_3, c_7$	$y^{16} - 14y^{15} + \dots - 9728y + 1024$
$c_4, c_9$	$y^{16} + 15y^{15} + \dots - 36576y + 7225$
$c_6, c_{10}$	$y^{16} + 20y^{15} + \dots - 9y + 1$
$c_8, c_{11}$	$y^{16} + 10y^{15} + \dots - 14y + 1$
$c_{12}$	$y^{16} + 38y^{15} + \dots - 113705856y + 5841889$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.709961 + 0.302018I$ $a = 0.067289 - 0.371265I$ $b = -1.56748 + 0.56103I$	$-2.10600 - 5.42693I$	$-16.6708 + 2.3025I$
$u = 0.709961 - 0.302018I$ $a = 0.067289 + 0.371265I$ $b = -1.56748 - 0.56103I$	$-2.10600 + 5.42693I$	$-16.6708 - 2.3025I$
$u = -0.624053 + 0.414470I$ $a = 0.036931 + 0.619361I$ $b = -0.268149 + 0.147042I$	$2.12989 + 2.00985I$	$-8.08247 - 3.69887I$
$u = -0.624053 - 0.414470I$ $a = 0.036931 - 0.619361I$ $b = -0.268149 - 0.147042I$	$2.12989 - 2.00985I$	$-8.08247 + 3.69887I$
$u = -0.603403$ $a = 0.346440$ $b = 1.97720$	$-5.59033$	$-13.4830$
$u = 0.365789 + 0.462196I$ $a = 0.36041 - 1.55398I$ $b = 0.667180 + 0.526239I$	$-0.228166 + 0.909617I$	$-12.89785 - 1.13498I$
$u = 0.365789 - 0.462196I$ $a = 0.36041 + 1.55398I$ $b = 0.667180 - 0.526239I$	$-0.228166 - 0.909617I$	$-12.89785 + 1.13498I$
$u = -0.222804 + 0.369878I$ $a = 1.57769 + 3.86659I$ $b = 0.82840 - 1.19204I$	$-8.61028 - 1.60803I$	$-19.3772 + 7.1837I$
$u = -0.222804 - 0.369878I$ $a = 1.57769 - 3.86659I$ $b = 0.82840 + 1.19204I$	$-8.61028 + 1.60803I$	$-19.3772 - 7.1837I$
$u = 0.325252$ $a = 0.778005$ $b = 0.326406$	$-0.534698$	$-18.5610$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.14699 + 2.11502I$	$5.95217 - 5.11511I$	$-14.9917 + 2.0744I$
$a = 1.050490 + 0.062469I$		
$b = -5.41647 + 5.13168I$		
$u = 1.14699 - 2.11502I$	$5.95217 + 5.11511I$	$-14.9917 - 2.0744I$
$a = 1.050490 - 0.062469I$		
$b = -5.41647 - 5.13168I$		
$u = -0.86624 + 2.26332I$	$10.23600 + 0.21137I$	$-11.36887 + 0.55661I$
$a = -1.018240 + 0.164220I$		
$b = 6.83232 + 3.44115I$		
$u = -0.86624 - 2.26332I$	$10.23600 - 0.21137I$	$-11.36887 - 0.55661I$
$a = -1.018240 - 0.164220I$		
$b = 6.83232 - 3.44115I$		
$u = -1.37057 + 2.24654I$	$9.6708 + 10.3555I$	$-12.00000 - 4.83541I$
$a = -1.136800 + 0.049742I$		
$b = 5.77240 + 7.05674I$		
$u = -1.37057 - 2.24654I$	$9.6708 - 10.3555I$	$-12.00000 + 4.83541I$
$a = -1.136800 - 0.049742I$		
$b = 5.77240 - 7.05674I$		

**II.**

$$I_2^u = \langle u^9 + u^8 + \dots + b - 1, u^{10} - 4u^8 + \dots + a + 1, u^{11} + u^{10} + \dots - 3u^2 + 1 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^{10} + 4u^8 - 2u^7 - 4u^6 + 6u^5 - u^4 - 4u^3 + u^2 + u - 1 \\ -u^9 - u^8 + 2u^7 - 2u^6 - 3u^5 + 6u^4 - 2u^2 + 2u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^9 - u^8 + 3u^7 - 5u^5 + 3u^4 + 3u^3 - 2u^2 - u + 1 \\ 2u^9 + 2u^8 - 5u^7 + 6u^5 - 6u^4 - 3u^3 + 2u^2 - u - 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^{10} + 4u^8 - 2u^7 - 4u^6 + 6u^5 - u^4 - 4u^3 + u^2 + u - 1 \\ -2u^9 - 2u^8 + 5u^7 - u^6 - 7u^5 + 8u^4 + 3u^3 - 4u^2 + u + 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^9 + u^8 - 3u^7 - u^6 + 4u^5 - u^4 - 2u^3 \\ -2u^9 - 3u^8 + 4u^7 + 3u^6 - 4u^5 + 2u^4 + u^3 + u^2 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^9 + u^8 - 3u^7 - u^6 + 4u^5 - u^4 - 3u^3 + 2u \\ u^6 + u^5 - 2u^4 + 2u^2 - u - 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^9 + u^8 - 3u^7 + 5u^5 - 3u^4 - 3u^3 + 2u^2 + u - 1 \\ u^6 + u^5 - 2u^4 + 2u^2 - u - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 - 3u^2 + 2 \\ u^{10} + u^9 - 3u^8 - u^7 + 4u^6 - 2u^5 - 3u^4 + 2u^3 - u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^4 - 2u^2 + 1 \\ -u^9 - u^8 + 2u^7 - 2u^5 + 2u^4 + u^2 + u \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**

$$= 4u^{10} + 10u^9 - 2u^8 - 14u^7 + 9u^6 + 15u^5 - 26u^4 - 23u^3 + 22u^2 - 2u - 29$$

(iv)  $u$ -Polynomials at the component



Crossings	u-Polynomials at each crossing
$c_1$	$u^{11} - 9u^{10} + \dots + 5u - 1$
$c_2$	$u^{11} + 3u^{10} - 6u^8 - 2u^7 + 2u^6 + 3u^5 + 4u^4 + 2u^3 - 2u^2 - 3u - 1$
$c_3$	$u^{11} + 2u^{10} + \dots - 5u + 1$
$c_4$	$u^{11} - 4u^9 - 6u^8 + 10u^7 + 23u^6 - 10u^5 - 23u^4 - 2u^3 + 16u^2 - 3u - 1$
$c_5$	$u^{11} - 3u^{10} + 6u^8 - 2u^7 - 2u^6 + 3u^5 - 4u^4 + 2u^3 + 2u^2 - 3u + 1$
$c_6$	$u^{11} - u^{10} - 3u^9 + 5u^7 + 4u^6 - 4u^5 - 4u^4 + u^3 + 3u^2 - 1$
$c_7$	$u^{11} - 2u^{10} + \dots - 5u - 1$
$c_8$	$u^{11} - 3u^{10} + \dots - u + 1$
$c_9$	$u^{11} - 4u^9 + 6u^8 + 10u^7 - 23u^6 - 10u^5 + 23u^4 - 2u^3 - 16u^2 - 3u + 1$
$c_{10}$	$u^{11} + u^{10} - 3u^9 + 5u^7 - 4u^6 - 4u^5 + 4u^4 + u^3 - 3u^2 + 1$
$c_{11}$	$u^{11} + 3u^{10} + \dots - u - 1$
$c_{12}$	$u^{11} - 7u^{10} + \dots - 85u + 29$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{11} - 17y^{10} + \dots + 9y - 1$
$c_2, c_5$	$y^{11} - 9y^{10} + \dots + 5y - 1$
$c_3, c_7$	$y^{11} - 14y^{10} + \dots + 21y - 1$
$c_4, c_9$	$y^{11} - 8y^{10} + \dots + 41y - 1$
$c_6, c_{10}$	$y^{11} - 7y^{10} + \dots + 6y - 1$
$c_8, c_{11}$	$y^{11} + 7y^{10} + \dots + 3y - 1$
$c_{12}$	$y^{11} - 21y^{10} + \dots + 10821y - 841$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.636123 + 0.670136I$ $a = 1.114440 - 0.543604I$ $b = -0.780678 + 0.831560I$	$1.01561 - 3.68794I$	$-9.46045 + 4.33638I$
$u = 0.636123 - 0.670136I$ $a = 1.114440 + 0.543604I$ $b = -0.780678 - 0.831560I$	$1.01561 + 3.68794I$	$-9.46045 - 4.33638I$
$u = 0.579598 + 0.909451I$ $a = -0.53978 + 1.76442I$ $b = -1.78870 - 1.78170I$	$-8.26462 + 1.07707I$	$-11.60559 + 3.04504I$
$u = 0.579598 - 0.909451I$ $a = -0.53978 - 1.76442I$ $b = -1.78870 + 1.78170I$	$-8.26462 - 1.07707I$	$-11.60559 - 3.04504I$
$u = 1.16659$ $a = -0.621653$ $b = -1.35028$	$-8.04334$	$-20.3040$
$u = -0.693012 + 0.407011I$ $a = 0.911623 - 0.220211I$ $b = -2.23098 - 0.93364I$	$-1.97384 + 6.11246I$	$-15.4629 - 13.1582I$
$u = -0.693012 - 0.407011I$ $a = 0.911623 + 0.220211I$ $b = -2.23098 + 0.93364I$	$-1.97384 - 6.11246I$	$-15.4629 + 13.1582I$
$u = -0.733849$ $a = -1.28586$ $b = 0.269849$	$-2.65454$	$-14.9220$
$u = 0.710299$ $a = -0.858009$ $b = 2.21118$	$-6.08165$	$-31.1290$
$u = -1.59423 + 0.15020I$ $a = -0.103519 + 0.553154I$ $b = 0.73498 + 1.21716I$	$-5.41647 - 2.99510I$	$-12.79336 + 4.15050I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.59423 - 0.15020I$		
$a = -0.103519 - 0.553154I$	$-5.41647 + 2.99510I$	$-12.79336 - 4.15050I$
$b = 0.73498 - 1.21716I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{11} - 9u^{10} + \dots + 5u - 1)(u^{16} - 22u^{15} + \dots + 28u + 1)$
$c_2$	$(u^{11} + 3u^{10} - 6u^8 - 2u^7 + 2u^6 + 3u^5 + 4u^4 + 2u^3 - 2u^2 - 3u - 1) \cdot (u^{16} + 4u^{15} + \dots - 2u - 1)$
$c_3$	$(u^{11} + 2u^{10} + \dots - 5u + 1)(u^{16} - 14u^{15} + \dots + 152u^2 - 32)$
$c_4$	$(u^{11} - 4u^9 - 6u^8 + 10u^7 + 23u^6 - 10u^5 - 23u^4 - 2u^3 + 16u^2 - 3u - 1) \cdot (u^{16} + u^{15} + \dots - 184u - 85)$
$c_5$	$(u^{11} - 3u^{10} + 6u^8 - 2u^7 - 2u^6 + 3u^5 - 4u^4 + 2u^3 + 2u^2 - 3u + 1) \cdot (u^{16} + 4u^{15} + \dots - 2u - 1)$
$c_6$	$(u^{11} - u^{10} - 3u^9 + 5u^7 + 4u^6 - 4u^5 - 4u^4 + u^3 + 3u^2 - 1) \cdot (u^{16} - 2u^{15} + \dots - u - 1)$
$c_7$	$(u^{11} - 2u^{10} + \dots - 5u - 1)(u^{16} - 14u^{15} + \dots + 152u^2 - 32)$
$c_8$	$(u^{11} - 3u^{10} + \dots - u + 1)(u^{16} - 2u^{15} + \dots + 2u + 1)$
$c_9$	$(u^{11} - 4u^9 + 6u^8 + 10u^7 - 23u^6 - 10u^5 + 23u^4 - 2u^3 - 16u^2 - 3u + 1) \cdot (u^{16} + u^{15} + \dots - 184u - 85)$
$c_{10}$	$(u^{11} + u^{10} - 3u^9 + 5u^7 - 4u^6 - 4u^5 + 4u^4 + u^3 - 3u^2 + 1) \cdot (u^{16} - 2u^{15} + \dots - u - 1)$
$c_{11}$	$(u^{11} + 3u^{10} + \dots - u - 1)(u^{16} - 2u^{15} + \dots + 2u + 1)$
$c_{12}$	$(u^{11} - 7u^{10} + \dots - 85u + 29)(u^{16} + 8u^{15} + \dots - 17328u - 2417)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{11} - 17y^{10} + \dots + 9y - 1)(y^{16} + 14y^{15} + \dots - 540y + 1)$
$c_2, c_5$	$(y^{11} - 9y^{10} + \dots + 5y - 1)(y^{16} + 22y^{15} + \dots - 28y + 1)$
$c_3, c_7$	$(y^{11} - 14y^{10} + \dots + 21y - 1)(y^{16} - 14y^{15} + \dots - 9728y + 1024)$
$c_4, c_9$	$(y^{11} - 8y^{10} + \dots + 41y - 1)(y^{16} + 15y^{15} + \dots - 36576y + 7225)$
$c_6, c_{10}$	$(y^{11} - 7y^{10} + \dots + 6y - 1)(y^{16} + 20y^{15} + \dots - 9y + 1)$
$c_8, c_{11}$	$(y^{11} + 7y^{10} + \dots + 3y - 1)(y^{16} + 10y^{15} + \dots - 14y + 1)$
$c_{12}$	$(y^{11} - 21y^{10} + \dots + 10821y - 841)$ $\cdot (y^{16} + 38y^{15} + \dots - 113705856y + 5841889)$