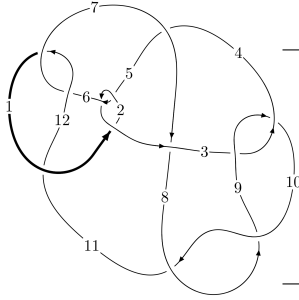
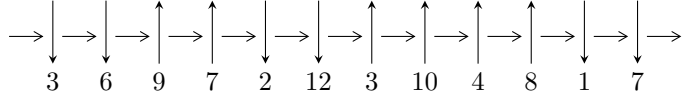


12n<sub>0380</sub> (K12n<sub>0380</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,9 \xrightarrow{c_3} 4 \xrightarrow{c_9} 6,10 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_8} 8 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \rightsquigarrow c_4, c_6, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{24} + 2u^{23} + \dots + b - 1, -u^{24} - u^{23} + \dots + 2a - 2, u^{25} + 3u^{24} + \dots - 4u - 2 \rangle$$

$$I_2^u = \langle -36u^{11}a + 71u^{11} + \dots + 286a - 731, -2u^{11}a + 2u^{10}a + \dots - 4a - 1, \\ u^{12} - 2u^{10} + u^9 + 4u^8 - u^7 - 3u^6 + 3u^5 + 3u^4 - u^3 - u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle b + 1, -u^3 + 2u^2 + 2a + u - 2, u^4 - u^2 + 2 \rangle$$

$$I_4^u = \langle b - 1, a - u, u^4 + 1 \rangle$$

$$I_5^u = \langle b, a + 1, u - 1 \rangle$$

$$I_6^u = \langle b + 1, a - 2, u - 1 \rangle$$

$$I_7^u = \langle b + 1, a - 3, u - 1 \rangle$$

$$I_8^u = \langle b + 1, a - 1, u + 1 \rangle$$

$$I_1^v = \langle a, b - 1, v + 1 \rangle$$

\* 9 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 62 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{24} + 2u^{23} + \dots + b - 1, -u^{24} - u^{23} + \dots + 2a - 2, u^{25} + 3u^{24} + \dots - 4u - 2 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^{24} + \frac{1}{2}u^{23} + \dots + u^2 + 1 \\ -u^{24} - 2u^{23} + \dots + 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u^{24} + \frac{5}{2}u^{23} + \dots - 3u - 2 \\ -u^{23} - u^{22} + \dots + 2u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u^{24} + \frac{3}{2}u^{23} + \dots - u - 1 \\ -u^{23} - u^{22} + \dots + 2u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{12} + u^{10} - 3u^8 + 2u^6 - 2u^4 + u^2 + 1 \\ u^{12} - 2u^{10} + 4u^8 - 4u^6 + 3u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^5 + u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^5 - u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^{24} - \frac{5}{2}u^{23} + \dots + 4u + 3 \\ u^{23} + u^{22} + \dots - u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -2u^{24} + 10u^{22} + 6u^{21} - 30u^{20} - 24u^{19} + 54u^{18} + 64u^{17} - 72u^{16} - 112u^{15} + 54u^{14} + 150u^{13} - 12u^{12} - 142u^{11} - 42u^{10} + 100u^9 + 66u^8 - 34u^7 - 56u^6 - 6u^5 + 22u^4 + 18u^3 - 2u - 4$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{25} + 5u^{24} + \dots + 11u + 1$
$c_2, c_5, c_6$ $c_{12}$	$u^{25} + u^{24} + \dots + u - 1$
$c_3, c_9$	$u^{25} + 3u^{24} + \dots - 4u - 2$
$c_4$	$u^{25} + 21u^{24} + \dots + 13332u + 2962$
$c_7$	$u^{25} - 3u^{24} + \dots - 92u - 26$
$c_8, c_{10}$	$u^{25} - 9u^{24} + \dots - 8u - 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{25} + 43y^{24} + \dots + 11y - 1$
$c_2, c_5, c_6$ $c_{12}$	$y^{25} - 5y^{24} + \dots + 11y - 1$
$c_3, c_9$	$y^{25} - 9y^{24} + \dots - 8y - 4$
$c_4$	$y^{25} - 33y^{24} + \dots - 42476552y - 8773444$
$c_7$	$y^{25} - 21y^{24} + \dots - 4952y - 676$
$c_8, c_{10}$	$y^{25} + 15y^{24} + \dots + 320y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.980316 + 0.233102I$ $a = 0.44130 + 2.47602I$ $b = -0.622808 - 0.762022I$	$2.82058 - 3.81422I$	$4.98039 + 6.61368I$
$u = -0.980316 - 0.233102I$ $a = 0.44130 - 2.47602I$ $b = -0.622808 + 0.762022I$	$2.82058 + 3.81422I$	$4.98039 - 6.61368I$
$u = -0.568077 + 0.832369I$ $a = 0.51973 - 1.50739I$ $b = -1.13721 + 0.86526I$	$4.15791 + 8.74016I$	$-1.84068 - 4.40634I$
$u = -0.568077 - 0.832369I$ $a = 0.51973 + 1.50739I$ $b = -1.13721 - 0.86526I$	$4.15791 - 8.74016I$	$-1.84068 + 4.40634I$
$u = -0.733592 + 0.747057I$ $a = 0.337972 - 0.198014I$ $b = 0.611523 + 0.222308I$	$-3.30756 - 0.71712I$	$-2.44059 + 3.90523I$
$u = -0.733592 - 0.747057I$ $a = 0.337972 + 0.198014I$ $b = 0.611523 - 0.222308I$	$-3.30756 + 0.71712I$	$-2.44059 - 3.90523I$
$u = 0.932488 + 0.483370I$ $a = 0.96761 + 1.60037I$ $b = -0.206915 - 0.805921I$	$1.59893 + 1.80276I$	$4.99535 - 2.09686I$
$u = 0.932488 - 0.483370I$ $a = 0.96761 - 1.60037I$ $b = -0.206915 + 0.805921I$	$1.59893 - 1.80276I$	$4.99535 + 2.09686I$
$u = 0.932840$ $a = 0.687051$ $b = -0.498290$	$1.77401$	$4.83650$
$u = 0.764755 + 0.774203I$ $a = 0.171446 - 0.325902I$ $b = 0.784319 + 0.533336I$	$-3.51376 - 2.47052I$	$-3.49276 + 4.45848I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.764755 - 0.774203I$ $a = 0.171446 + 0.325902I$ $b = 0.784319 - 0.533336I$	$-3.51376 + 2.47052I$	$-3.49276 - 4.45848I$
$u = -0.437237 + 0.783767I$ $a = 0.49146 + 1.67035I$ $b = -1.037150 - 0.927401I$	$4.93859 - 5.35756I$	$-1.01874 + 4.42089I$
$u = -0.437237 - 0.783767I$ $a = 0.49146 - 1.67035I$ $b = -1.037150 + 0.927401I$	$4.93859 + 5.35756I$	$-1.01874 - 4.42089I$
$u = 1.156340 + 0.047910I$ $a = -2.12651 + 3.13266I$ $b = 1.12099 - 0.93923I$	$10.42970 + 7.39157I$	$4.47957 - 4.57784I$
$u = 1.156340 - 0.047910I$ $a = -2.12651 - 3.13266I$ $b = 1.12099 + 0.93923I$	$10.42970 - 7.39157I$	$4.47957 + 4.57784I$
$u = -0.970077 + 0.698318I$ $a = 0.166009 + 0.595943I$ $b = -0.620681 + 0.170359I$	$-2.58593 - 4.79128I$	$-0.37722 + 2.00234I$
$u = -0.970077 - 0.698318I$ $a = 0.166009 - 0.595943I$ $b = -0.620681 - 0.170359I$	$-2.58593 + 4.79128I$	$-0.37722 - 2.00234I$
$u = 0.951621 + 0.731482I$ $a = -0.63483 - 1.61897I$ $b = -0.831342 + 0.569410I$	$-2.94773 + 8.15802I$	$-2.49516 - 9.64578I$
$u = 0.951621 - 0.731482I$ $a = -0.63483 + 1.61897I$ $b = -0.831342 - 0.569410I$	$-2.94773 - 8.15802I$	$-2.49516 + 9.64578I$
$u = -1.076120 + 0.616232I$ $a = -2.32949 + 1.21588I$ $b = 1.02897 - 0.98641I$	$6.80687 + 0.12880I$	$1.81794 + 0.42247I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.076120 - 0.616232I$		
$a = -2.32949 - 1.21588I$	$6.80687 - 0.12880I$	$1.81794 - 0.42247I$
$b = 1.02897 + 0.98641I$		
$u = -1.066850 + 0.683933I$		
$a = -0.18246 - 3.26046I$	$5.6578 - 14.4091I$	$0.10967 + 8.76133I$
$b = 1.16937 + 0.87177I$		
$u = -1.066850 - 0.683933I$		
$a = -0.18246 + 3.26046I$	$5.6578 + 14.4091I$	$0.10967 - 8.76133I$
$b = 1.16937 - 0.87177I$		
$u = 0.060646 + 0.510945I$		
$a = 0.334239 + 0.498112I$	$-0.268317 + 1.373590I$	$-2.13600 - 4.81420I$
$b = 0.490067 - 0.520637I$		
$u = 0.060646 - 0.510945I$		
$a = 0.334239 - 0.498112I$	$-0.268317 - 1.373590I$	$-2.13600 + 4.81420I$
$b = 0.490067 + 0.520637I$		

$$\text{II. } I_2^u = \langle -36u^{11}a + 71u^{11} + \dots + 286a - 731, -2u^{11}a + 2u^{10}a + \dots - 4a - 1, u^{12} - 2u^{10} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ 0.0599002au^{11} - 0.118136u^{11} + \dots - 0.475874a + 1.21631 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.118136au^{11} - 0.128120u^{11} + \dots + 1.21631a + 1.62895 \\ 0.0682196au^{11} + 0.0599002u^{11} + \dots - 0.153078a - 1.47587 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0499168au^{11} - 0.0682196u^{11} + \dots + 1.06323a + 0.153078 \\ 0.0682196au^{11} + 0.0599002u^{11} + \dots - 0.153078a - 1.47587 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{10} + u^9 + u^8 - u^7 - u^6 + 3u^5 + u^4 - u^3 + 2u + 2 \\ -u^9 + u^7 - u^6 - 3u^5 + u^3 - u^2 - 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^5 + u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^5 - u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.118136au^{11} - 0.128120u^{11} + \dots + 1.21631a - 0.371048 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 4u^{11} - 8u^9 + 4u^8 + 12u^7 - 4u^6 - 8u^5 + 8u^4 + 4u^3 - 4u^2 - 4u + 2$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{24} + 8u^{23} + \dots + 268u + 49$
$c_2, c_5, c_6$ $c_{12}$	$u^{24} + 2u^{23} + \dots + 4u - 7$
$c_3, c_9$	$(u^{12} - 2u^{10} + u^9 + 4u^8 - u^7 - 3u^6 + 3u^5 + 3u^4 - u^3 - u^2 + 2u + 1)^2$
$c_4$	$(u^{12} - 8u^{11} + \dots - 48u - 23)^2$
$c_7$	$(u^{12} + 2u^{11} + \dots + 4u + 1)^2$
$c_8, c_{10}$	$(u^{12} - 4u^{11} + \dots - 6u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{24} + 16y^{23} + \dots + 54988y + 2401$
$c_2, c_5, c_6$ $c_{12}$	$y^{24} - 8y^{23} + \dots - 268y + 49$
$c_3, c_9$	$(y^{12} - 4y^{11} + \dots - 6y + 1)^2$
$c_4$	$(y^{12} - 28y^{11} + \dots - 9802y + 529)^2$
$c_7$	$(y^{12} - 16y^{11} + \dots - 6y + 1)^2$
$c_8, c_{10}$	$(y^{12} + 8y^{11} + \dots - 14y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.511432 + 0.812623I$ $a = 0.67786 + 1.48575I$ $b = -0.900728 - 1.001250I$	$5.38423 - 1.70959I$	$-0.128193 + 0.167200I$
$u = 0.511432 + 0.812623I$ $a = 0.55283 - 1.54744I$ $b = -0.756837 + 1.060930I$	$5.38423 - 1.70959I$	$-0.128193 + 0.167200I$
$u = 0.511432 - 0.812623I$ $a = 0.67786 - 1.48575I$ $b = -0.900728 + 1.001250I$	$5.38423 + 1.70959I$	$-0.128193 - 0.167200I$
$u = 0.511432 - 0.812623I$ $a = 0.55283 + 1.54744I$ $b = -0.756837 - 1.060930I$	$5.38423 + 1.70959I$	$-0.128193 - 0.167200I$
$u = 0.850204 + 0.630914I$ $a = -0.132727 - 0.669979I$ $b = 1.145980 + 0.247522I$	$-5.05906 + 2.46907I$	$-5.52253 - 3.95252I$
$u = 0.850204 + 0.630914I$ $a = 0.07414 - 2.86500I$ $b = -1.068390 + 0.305673I$	$-5.05906 + 2.46907I$	$-5.52253 - 3.95252I$
$u = 0.850204 - 0.630914I$ $a = -0.132727 + 0.669979I$ $b = 1.145980 - 0.247522I$	$-5.05906 - 2.46907I$	$-5.52253 + 3.95252I$
$u = 0.850204 - 0.630914I$ $a = 0.07414 + 2.86500I$ $b = -1.068390 - 0.305673I$	$-5.05906 - 2.46907I$	$-5.52253 + 3.95252I$
$u = -0.635020 + 0.640255I$ $a = -0.226456 + 0.011257I$ $b = 1.204970 - 0.052489I$	$-3.08210 + 0.49850I$	$-1.36863 - 1.38008I$
$u = -0.635020 + 0.640255I$ $a = 1.55856 - 1.03377I$ $b = -0.457992 + 0.354536I$	$-3.08210 + 0.49850I$	$-1.36863 - 1.38008I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.635020 - 0.640255I$ $a = -0.226456 - 0.011257I$ $b = 1.204970 + 0.052489I$	$-3.08210 - 0.49850I$	$-1.36863 + 1.38008I$
$u = -0.635020 - 0.640255I$ $a = 1.55856 + 1.03377I$ $b = -0.457992 - 0.354536I$	$-3.08210 - 0.49850I$	$-1.36863 + 1.38008I$
$u = -1.16193$ $a = -1.91107 + 3.18977I$ $b = 0.855561 - 1.093600I$	11.2998	5.66710
$u = -1.16193$ $a = -1.91107 - 3.18977I$ $b = 0.855561 + 1.093600I$	11.2998	5.66710
$u = -0.985497 + 0.634576I$ $a = -0.67437 - 1.64764I$ $b = 0.301152 + 0.483288I$	$-2.05779 - 5.52285I$	$0.56374 + 6.48307I$
$u = -0.985497 + 0.634576I$ $a = 0.79418 + 1.81824I$ $b = -1.207840 - 0.138399I$	$-2.05779 - 5.52285I$	$0.56374 + 6.48307I$
$u = -0.985497 - 0.634576I$ $a = -0.67437 + 1.64764I$ $b = 0.301152 - 0.483288I$	$-2.05779 + 5.52285I$	$0.56374 - 6.48307I$
$u = -0.985497 - 0.634576I$ $a = 0.79418 - 1.81824I$ $b = -1.207840 + 0.138399I$	$-2.05779 + 5.52285I$	$0.56374 - 6.48307I$
$u = 1.075030 + 0.655125I$ $a = -2.21955 - 1.41327I$ $b = 0.739507 + 1.114900I$	$7.05914 + 7.20360I$	$2.08749 - 4.71657I$
$u = 1.075030 + 0.655125I$ $a = -0.12063 + 3.16354I$ $b = 0.949962 - 1.026010I$	$7.05914 + 7.20360I$	$2.08749 - 4.71657I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.075030 - 0.655125I$ $a = -2.21955 + 1.41327I$ $b = 0.739507 - 1.114900I$	$7.05914 - 7.20360I$	$2.08749 + 4.71657I$
$u = 1.075030 - 0.655125I$ $a = -0.12063 - 3.16354I$ $b = 0.949962 + 1.026010I$	$7.05914 - 7.20360I$	$2.08749 + 4.71657I$
$u = -0.470358$ $a = -0.00729607$ $b = 1.13611$	$-2.62918$	$3.06920$
$u = -0.470358$ $a = 4.26177$ $b = -0.746787$	$-2.62918$	$3.06920$

$$\text{III. } I_3^u = \langle b + 1, -u^3 + 2u^2 + 2a + u - 2, u^4 - u^2 + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^3 - u^2 - \frac{1}{2}u + 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u^3 - u^2 - \frac{1}{2}u + 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u^3 - u^2 - \frac{1}{2}u + 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 - u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 + u \\ -u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{3}{2}u^3 - u^2 - \frac{3}{2}u + 1 \\ u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4u^2 - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_{11}$ $c_{12}$	$(u - 1)^4$
$c_2, c_6$	$(u + 1)^4$
$c_3, c_4, c_7$ $c_9$	$u^4 - u^2 + 2$
$c_8$	$(u^2 + u + 2)^2$
$c_{10}$	$(u^2 - u + 2)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_{11}, c_{12}$	$(y - 1)^4$
$c_3, c_4, c_7$ $c_9$	$(y^2 - y + 2)^2$
$c_8, c_{10}$	$(y^2 + 3y + 4)^2$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.978318 + 0.676097I$ $a = -0.191776 - 0.844803I$ $b = -1.00000$	$-4.11234 + 5.33349I$	$-6.00000 - 5.29150I$
$u = 0.978318 - 0.676097I$ $a = -0.191776 + 0.844803I$ $b = -1.00000$	$-4.11234 - 5.33349I$	$-6.00000 + 5.29150I$
$u = -0.978318 + 0.676097I$ $a = 1.19178 + 1.80095I$ $b = -1.00000$	$-4.11234 - 5.33349I$	$-6.00000 + 5.29150I$
$u = -0.978318 - 0.676097I$ $a = 1.19178 - 1.80095I$ $b = -1.00000$	$-4.11234 + 5.33349I$	$-6.00000 - 5.29150I$

$$\text{IV. } I_4^u = \langle b - 1, a - u, u^4 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ -u^3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -u^3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -u^3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^3 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -8

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$ $c_{11}$	$(u - 1)^4$
$c_3, c_4, c_7$ $c_9$	$u^4 + 1$
$c_5, c_{12}$	$(u + 1)^4$
$c_8, c_{10}$	$(u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_{11}, c_{12}$	$(y - 1)^4$
$c_3, c_4, c_7$ $c_9$	$(y^2 + 1)^2$
$c_8, c_{10}$	$(y + 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.707107 + 0.707107I$ $a = 0.707107 + 0.707107I$ $b = 1.00000$	-4.93480	-8.00000
$u = 0.707107 - 0.707107I$ $a = 0.707107 - 0.707107I$ $b = 1.00000$	-4.93480	-8.00000
$u = -0.707107 + 0.707107I$ $a = -0.707107 + 0.707107I$ $b = 1.00000$	-4.93480	-8.00000
$u = -0.707107 - 0.707107I$ $a = -0.707107 - 0.707107I$ $b = 1.00000$	-4.93480	-8.00000

$$\mathbf{V}. I_5^u = \langle b, a + 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = 6**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_5$	$u$
$c_3, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{12}$	$u - 1$
$c_4, c_{11}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$y$
$c_3, c_4, c_6$ $c_7, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$y - 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -1.00000$	1.64493	6.00000
$b = 0$		

$$\text{VI. } I_6^u = \langle b + 1, a - 2, u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class =  $-1$

(iii) Cusp Shapes =  $6$

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u + 1$
$c_2, c_3, c_5$ $c_7, c_8, c_9$ $c_{10}$	$u - 1$
$c_6, c_{11}, c_{12}$	$u$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_7$ $c_8, c_9, c_{10}$	$y - 1$
$c_6, c_{11}, c_{12}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$	1.64493	6.00000
$a = 2.00000$		
$b = -1.00000$		

VII.  $I_7^u = \langle b + 1, a - 3, u - 1 \rangle$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$ $c_{10}, c_{11}, c_{12}$	$u - 1$
$c_2, c_4, c_6$ $c_7, c_8, c_9$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$	$y - 1$
$c_4, c_5, c_6$	
$c_7, c_8, c_9$	
$c_{10}, c_{11}, c_{12}$	



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_7^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 3.00000$	0	0
$b = -1.00000$		

VIII.  $I_g^u = \langle b + 1, a - 1, u + 1 \rangle$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_4, c_5$ $c_7, c_9, c_{10}$ $c_{11}, c_{12}$	$u - 1$
$c_2, c_3, c_6$ $c_8$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$	$y - 1$
$c_4, c_5, c_6$	
$c_7, c_8, c_9$	
$c_{10}, c_{11}, c_{12}$	

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_g^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.00000$	0	0
$b = -1.00000$		

$$\text{IX. } I_1^v = \langle a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_6$ $c_{11}$	$u - 1$
$c_3, c_4, c_7$ $c_8, c_9, c_{10}$	$u$
$c_5, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_{11}, c_{12}$	$y - 1$
$c_3, c_4, c_7$ $c_8, c_9, c_{10}$	$y$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	$-3.28987$	$-12.0000$
$b = 1.00000$		

## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u(u-1)^{11}(u+1)(u^{24} + 8u^{23} + \dots + 268u + 49)$ $\cdot (u^{25} + 5u^{24} + \dots + 11u + 1)$
$c_2, c_6$	$u(u-1)^6(u+1)^6(u^{24} + 2u^{23} + \dots + 4u - 7)(u^{25} + u^{24} + \dots + u - 1)$
$c_3, c_9$	$u(u-1)^3(u+1)(u^4+1)(u^4-u^2+2)$ $\cdot (u^{12} - 2u^{10} + u^9 + 4u^8 - u^7 - 3u^6 + 3u^5 + 3u^4 - u^3 - u^2 + 2u + 1)^2$ $\cdot (u^{25} + 3u^{24} + \dots - 4u - 2)$
$c_4$	$u(u-1)(u+1)^3(u^4+1)(u^4-u^2+2)(u^{12} - 8u^{11} + \dots - 48u - 23)^2$ $\cdot (u^{25} + 21u^{24} + \dots + 13332u + 2962)$
$c_5, c_{12}$	$u(u-1)^7(u+1)^5(u^{24} + 2u^{23} + \dots + 4u - 7)(u^{25} + u^{24} + \dots + u - 1)$
$c_7$	$u(u-1)^3(u+1)(u^4+1)(u^4-u^2+2)(u^{12} + 2u^{11} + \dots + 4u + 1)^2$ $\cdot (u^{25} - 3u^{24} + \dots - 92u - 26)$
$c_8$	$u(u-1)^2(u+1)^2(u^2+1)^2(u^2+u+2)^2$ $\cdot ((u^{12} - 4u^{11} + \dots - 6u + 1)^2)(u^{25} - 9u^{24} + \dots - 8u - 4)$
$c_{10}$	$u(u-1)^4(u^2+1)^2(u^2-u+2)^2(u^{12} - 4u^{11} + \dots - 6u + 1)^2$ $\cdot (u^{25} - 9u^{24} + \dots - 8u - 4)$

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y(y-1)^{12}(y^{24} + 16y^{23} + \dots + 54988y + 2401)$ $\cdot (y^{25} + 43y^{24} + \dots + 11y - 1)$
$c_2, c_5, c_6$ $c_{12}$	$y(y-1)^{12}(y^{24} - 8y^{23} + \dots - 268y + 49)(y^{25} - 5y^{24} + \dots + 11y - 1)$
$c_3, c_9$	$y(y-1)^4(y^2+1)^2(y^2-y+2)^2(y^{12}-4y^{11}+\dots-6y+1)^2$ $\cdot (y^{25}-9y^{24}+\dots-8y-4)$
$c_4$	$y(y-1)^4(y^2+1)^2(y^2-y+2)^2$ $\cdot (y^{12}-28y^{11}+\dots-9802y+529)^2$ $\cdot (y^{25}-33y^{24}+\dots-42476552y-8773444)$
$c_7$	$y(y-1)^4(y^2+1)^2(y^2-y+2)^2(y^{12}-16y^{11}+\dots-6y+1)^2$ $\cdot (y^{25}-21y^{24}+\dots-4952y-676)$
$c_8, c_{10}$	$y(y-1)^4(y+1)^4(y^2+3y+4)^2(y^{12}+8y^{11}+\dots-14y+1)^2$ $\cdot (y^{25}+15y^{24}+\dots+320y-16)$