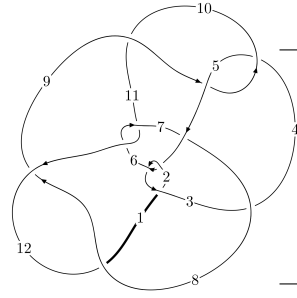
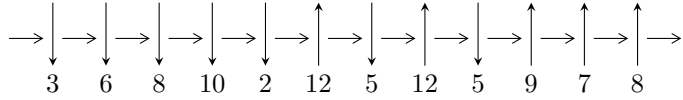


12n<sub>0382</sub> (K12n<sub>0382</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_5} 6 \xrightarrow{c_2} 3,12 \xrightarrow{c_6} 7 \xrightarrow{c_7} 8 \xrightarrow{c_8} 9 \xrightarrow{c_9} 10 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_{11}} 11 \Rightarrow c_3, c_{10}, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -579753405694973u^{23} - 472990592837092u^{22} + \dots + 1971269389223473b + 4407120302352329, \\ 2.83690 \times 10^{15}u^{23} + 6.39000 \times 10^{15}u^{22} + \dots + 2.16840 \times 10^{16}a - 5.46780 \times 10^{16}, u^{24} + 2u^{23} + \dots - 7u - 1 \rangle$$

$$I_2^u = \langle -u^{14} + u^{13} + 3u^{12} - 4u^{11} - 6u^{10} + 9u^9 + 7u^8 - 13u^7 - 6u^6 + 12u^5 + 2u^4 - 7u^3 + b + u, \\ -2u^{14} + u^{13} + 5u^{12} - 4u^{11} - 10u^{10} + 8u^9 + 10u^8 - 10u^7 - 8u^6 + 7u^5 - 2u^3 + u^2 + a - u, \\ u^{15} - u^{14} - 3u^{13} + 4u^{12} + 6u^{11} - 9u^{10} - 7u^9 + 13u^8 + 6u^7 - 13u^6 - 2u^5 + 8u^4 - 3u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 39 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -5.80 \times 10^{14}u^{23} - 4.73 \times 10^{14}u^{22} + \dots + 1.97 \times 10^{15}b + 4.41 \times 10^{15}, 2.84 \times 10^{15}u^{23} + 6.39 \times 10^{15}u^{22} + \dots + 2.17 \times 10^{16}a - 5.47 \times 10^{16}, u^{24} + 2u^{23} + \dots - 7u - 11 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.130829u^{23} - 0.294688u^{22} + \dots - 1.59763u + 2.52159 \\ 0.294102u^{23} + 0.239942u^{22} + \dots + 0.00494916u - 2.23568 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.534965u^{23} - 0.416078u^{22} + \dots - 0.624684u + 5.43098 \\ -0.310244u^{23} - 0.272323u^{22} + \dots - 0.324549u + 2.64692 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.224721u^{23} - 0.143755u^{22} + \dots - 0.300135u + 2.78406 \\ -0.310244u^{23} - 0.272323u^{22} + \dots - 0.324549u + 2.64692 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.201549u^{23} + 0.249559u^{22} + \dots - 0.113316u - 1.36979 \\ -0.111431u^{23} - 0.128131u^{22} + \dots - 0.277454u + 1.05051 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.312979u^{23} + 0.377690u^{22} + \dots + 0.164138u - 2.42030 \\ -0.111431u^{23} - 0.128131u^{22} + \dots - 0.277454u + 1.05051 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0617504u^{23} - 0.0392309u^{22} + \dots - 2.06682u + 0.542106 \\ 0.194220u^{23} + 0.176940u^{22} + \dots + 0.957672u - 1.78638 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0302642u^{23} + 0.0123334u^{22} + \dots + 0.976733u - 1.03269 \\ 0.119247u^{23} + 0.191200u^{22} + \dots + 0.994406u - 1.82283 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{2580377549362014}{1971269389223473}u^{23} + \frac{3507150554528052}{1971269389223473}u^{22} + \dots + \frac{45898132692487883}{1971269389223473}u - \frac{44289338047701926}{1971269389223473}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{24} + 16u^{23} + \dots + 819u + 121$
$c_2, c_5$	$u^{24} + 2u^{23} + \dots - 7u - 11$
$c_3$	$u^{24} + 26u^{22} + \dots + 39u - 11$
$c_4, c_9$	$u^{24} + u^{23} + \dots + 51u + 43$
$c_6, c_{11}$	$u^{24} - 2u^{23} + \dots - 472u - 163$
$c_7$	$u^{24} - 3u^{23} + \dots + 9u + 1$
$c_8, c_{12}$	$u^{24} + 4u^{23} + \dots - 138u - 23$
$c_{10}$	$u^{24} - 7u^{23} + \dots - 667u + 1849$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{24} - 8y^{23} + \dots + 75809y + 14641$
$c_2, c_5$	$y^{24} - 16y^{23} + \dots - 819y + 121$
$c_3$	$y^{24} + 52y^{23} + \dots - 1015y + 121$
$c_4, c_9$	$y^{24} + 7y^{23} + \dots + 667y + 1849$
$c_6, c_{11}$	$y^{24} + 36y^{23} + \dots - 234846y + 26569$
$c_7$	$y^{24} - 47y^{23} + \dots + 113y + 1$
$c_8, c_{12}$	$y^{24} + 34y^{23} + \dots - 65412y + 529$
$c_{10}$	$y^{24} + 35y^{23} + \dots - 209766481y + 3418801$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.840681 + 0.490024I$ $a = -0.724162 + 0.569771I$ $b = -0.34121 + 1.49688I$	$-2.96579 + 0.05300I$	$-5.61914 - 0.01464I$
$u = -0.840681 - 0.490024I$ $a = -0.724162 - 0.569771I$ $b = -0.34121 - 1.49688I$	$-2.96579 - 0.05300I$	$-5.61914 + 0.01464I$
$u = -1.022560 + 0.295401I$ $a = -1.05742 + 2.52587I$ $b = 0.33303 + 1.71764I$	$-3.54040 + 2.95826I$	$-5.57765 - 4.27465I$
$u = -1.022560 - 0.295401I$ $a = -1.05742 - 2.52587I$ $b = 0.33303 - 1.71764I$	$-3.54040 - 2.95826I$	$-5.57765 + 4.27465I$
$u = 0.962010 + 0.650431I$ $a = -0.070965 - 1.233660I$ $b = -0.070549 - 0.869894I$	$7.79911 - 2.52001I$	$-0.51262 + 2.53374I$
$u = 0.962010 - 0.650431I$ $a = -0.070965 + 1.233660I$ $b = -0.070549 + 0.869894I$	$7.79911 + 2.52001I$	$-0.51262 - 2.53374I$
$u = -0.927407 + 0.744557I$ $a = 0.713189 + 0.275798I$ $b = -0.014139 - 0.602418I$	$8.76252 + 2.82949I$	$-3.38778 - 2.96422I$
$u = -0.927407 - 0.744557I$ $a = 0.713189 - 0.275798I$ $b = -0.014139 + 0.602418I$	$8.76252 - 2.82949I$	$-3.38778 + 2.96422I$
$u = 1.133700 + 0.502318I$ $a = 0.53485 + 1.45879I$ $b = -1.02104 + 1.23446I$	$-2.58040 - 6.55097I$	$-3.00232 + 8.95233I$
$u = 1.133700 - 0.502318I$ $a = 0.53485 - 1.45879I$ $b = -1.02104 - 1.23446I$	$-2.58040 + 6.55097I$	$-3.00232 - 8.95233I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.759420$ $a = -0.396801$ $b = -0.537831$	-1.01372	-11.2860
$u = -0.238482 + 1.223910I$ $a = 0.037299 - 0.531429I$ $b = 0.12489 - 1.74552I$	$-9.56824 - 4.63986I$	$-2.53665 + 1.77990I$
$u = -0.238482 - 1.223910I$ $a = 0.037299 + 0.531429I$ $b = 0.12489 + 1.74552I$	$-9.56824 + 4.63986I$	$-2.53665 - 1.77990I$
$u = 1.25828$ $a = -1.11711$ $b = 0.135805$	-0.844274	-6.82360
$u = 0.264664 + 0.670266I$ $a = -0.018243 - 0.736439I$ $b = 0.587531 + 0.857775I$	$-0.06550 + 2.02589I$	$0.03613 - 4.27604I$
$u = 0.264664 - 0.670266I$ $a = -0.018243 + 0.736439I$ $b = 0.587531 - 0.857775I$	$-0.06550 - 2.02589I$	$0.03613 + 4.27604I$
$u = -1.330090 + 0.222342I$ $a = -0.92490 + 1.09593I$ $b = 0.094519 + 1.136320I$	$-4.70867 + 0.81596I$	$-5.59655 - 0.54882I$
$u = -1.330090 - 0.222342I$ $a = -0.92490 - 1.09593I$ $b = 0.094519 - 1.136320I$	$-4.70867 - 0.81596I$	$-5.59655 + 0.54882I$
$u = 0.538622 + 0.352121I$ $a = 0.147046 + 1.001000I$ $b = 0.216583 - 0.106477I$	$0.98010 - 1.26540I$	$3.01329 + 5.29615I$
$u = 0.538622 - 0.352121I$ $a = 0.147046 - 1.001000I$ $b = 0.216583 + 0.106477I$	$0.98010 + 1.26540I$	$3.01329 - 5.29615I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.34887 + 0.69749I$	$-13.0253 + 11.4321I$	$-3.86498 - 4.79478I$
$a = 1.08996 - 1.58558I$		
$b = -0.23003 - 1.81299I$		
$u = -1.34887 - 0.69749I$	$-13.0253 - 11.4321I$	$-3.86498 + 4.79478I$
$a = 1.08996 + 1.58558I$		
$b = -0.23003 + 1.81299I$		
$u = 1.55966 + 0.42079I$	$-15.5246 - 1.3214I$	$-5.39704 + 0.62510I$
$a = -0.69697 - 1.79236I$		
$b = 0.02142 - 1.78671I$		
$u = 1.55966 - 0.42079I$	$-15.5246 + 1.3214I$	$-5.39704 - 0.62510I$
$a = -0.69697 + 1.79236I$		
$b = 0.02142 + 1.78671I$		

**II.**

$$I_2^u = \langle -u^{14} + u^{13} + \dots + b + u, -2u^{14} + u^{13} + \dots + a - u, u^{15} - u^{14} + \dots - 3u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^{14} - u^{13} + \dots - u^2 + u \\ u^{14} - u^{13} + \dots + 7u^3 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{14} - u^{13} + \dots - u + 3 \\ -u^{12} + 3u^{10} - u^9 - 6u^8 + 2u^7 + 7u^6 - 3u^5 - 6u^4 + 2u^3 + 2u^2 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{14} - u^{13} + \dots - 9u^2 + 3 \\ -u^{12} + 3u^{10} - u^9 - 6u^8 + 2u^7 + 7u^6 - 3u^5 - 6u^4 + 2u^3 + 2u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{14} - 2u^{13} + \dots + 2u + 2 \\ -u^{13} + 3u^{11} - u^{10} - 7u^9 + 2u^8 + 9u^7 - 4u^6 - 9u^5 + 3u^4 + 4u^3 - 2u^2 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{14} - u^{13} + \dots + 3u + 2 \\ -u^{13} + 3u^{11} - u^{10} - 7u^9 + 2u^8 + 9u^7 - 4u^6 - 9u^5 + 3u^4 + 4u^3 - 2u^2 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{14} + 5u^{12} + \dots + 3u + 4 \\ -u^{14} + 3u^{12} - 7u^{10} + 10u^8 - 11u^6 + 7u^4 - 3u^2 + u + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 4u^{14} - 11u^{12} + \dots - u - 1 \\ u^{14} - 3u^{12} + \dots + 3u^3 + 2u^2 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**

$$= -u^{12} - u^{11} + 3u^{10} + u^9 - 5u^8 - 4u^7 + 7u^6 + 4u^5 - 7u^4 - 3u^3 + 5u^2 - 2u - 4$$



(iv)  $u$ -Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} - 7u^{14} + \dots + 6u - 1$
$c_2$	$u^{15} + u^{14} + \dots + 3u^2 - 1$
$c_3$	$u^{15} - u^{14} + \dots - 2u - 1$
$c_4$	$u^{15} + 8u^{13} + \dots + 4u + 1$
$c_5$	$u^{15} - u^{14} + \dots - 3u^2 + 1$
$c_6$	$u^{15} - u^{14} + \dots + 3u + 1$
$c_7$	$u^{15} + 2u^{14} + \dots + 4u + 1$
$c_8$	$u^{15} + 3u^{14} + \dots - u + 1$
$c_9$	$u^{15} + 8u^{13} + \dots + 4u - 1$
$c_{10}$	$u^{15} - 16u^{14} + \dots + 4u + 1$
$c_{11}$	$u^{15} + u^{14} + \dots + 3u - 1$
$c_{12}$	$u^{15} - 3u^{14} + \dots - u - 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} + 9y^{14} + \dots - 14y - 1$
$c_2, c_5$	$y^{15} - 7y^{14} + \dots + 6y - 1$
$c_3$	$y^{15} + 29y^{14} + \dots - 14y - 1$
$c_4, c_9$	$y^{15} + 16y^{14} + \dots + 4y - 1$
$c_6, c_{11}$	$y^{15} - 3y^{14} + \dots + y - 1$
$c_7$	$y^{15} - 2y^{14} + \dots + 18y - 1$
$c_8, c_{12}$	$y^{15} - y^{14} + \dots + 3y - 1$
$c_{10}$	$y^{15} - 20y^{14} + \dots + 252y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.899781 + 0.286994I$ $a = -0.44937 + 1.89015I$ $b = 0.304958 + 0.973459I$	$6.68911 - 1.23661I$	$-4.15485 - 0.98307I$
$u = 0.899781 - 0.286994I$ $a = -0.44937 - 1.89015I$ $b = 0.304958 - 0.973459I$	$6.68911 + 1.23661I$	$-4.15485 + 0.98307I$
$u = -0.893982$ $a = 0.674370$ $b = -0.525910$	$0.237359$	$1.17550$
$u = -0.896890 + 0.731944I$ $a = -0.254396 - 0.626802I$ $b = 0.153159 + 0.059677I$	$9.57728 + 2.79903I$	$7.57416 - 2.89020I$
$u = -0.896890 - 0.731944I$ $a = -0.254396 + 0.626802I$ $b = 0.153159 - 0.059677I$	$9.57728 - 2.79903I$	$7.57416 + 2.89020I$
$u = -1.107400 + 0.432221I$ $a = -1.13757 + 1.78331I$ $b = -0.01538 + 1.93584I$	$-4.12042 + 1.58492I$	$-8.26166 - 0.30703I$
$u = -1.107400 - 0.432221I$ $a = -1.13757 - 1.78331I$ $b = -0.01538 - 1.93584I$	$-4.12042 - 1.58492I$	$-8.26166 + 0.30703I$
$u = 0.550933 + 0.586599I$ $a = 0.901557 - 0.875340I$ $b = 0.45418 + 1.47368I$	$-1.53674 + 1.05029I$	$-3.10144 - 0.84326I$
$u = 0.550933 - 0.586599I$ $a = 0.901557 + 0.875340I$ $b = 0.45418 - 1.47368I$	$-1.53674 - 1.05029I$	$-3.10144 + 0.84326I$
$u = 1.096940 + 0.544029I$ $a = 1.21180 + 1.50559I$ $b = -0.72158 + 1.69669I$	$-3.32611 - 5.65603I$	$-6.88663 + 4.31157I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.096940 - 0.544029I$		
$a = 1.21180 - 1.50559I$	$-3.32611 + 5.65603I$	$-6.88663 - 4.31157I$
$b = -0.72158 - 1.69669I$		
$u = 0.914301 + 0.849307I$		
$a = -0.569444 - 0.431437I$	$6.12893 - 3.15877I$	$-4.60445 + 3.34743I$
$b = -0.039917 - 0.985105I$		
$u = 0.914301 - 0.849307I$		
$a = -0.569444 + 0.431437I$	$6.12893 + 3.15877I$	$-4.60445 - 3.34743I$
$b = -0.039917 + 0.985105I$		
$u = -0.510671 + 0.420907I$		
$a = -1.53976 + 1.37826I$	$-2.01618 + 2.10877I$	$-1.65286 - 2.85205I$
$b = 0.12754 + 1.51005I$		
$u = -0.510671 - 0.420907I$		
$a = -1.53976 - 1.37826I$	$-2.01618 - 2.10877I$	$-1.65286 + 2.85205I$
$b = 0.12754 - 1.51005I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{15} - 7u^{14} + \dots + 6u - 1)(u^{24} + 16u^{23} + \dots + 819u + 121)$
$c_2$	$(u^{15} + u^{14} + \dots + 3u^2 - 1)(u^{24} + 2u^{23} + \dots - 7u - 11)$
$c_3$	$(u^{15} - u^{14} + \dots - 2u - 1)(u^{24} + 26u^{22} + \dots + 39u - 11)$
$c_4$	$(u^{15} + 8u^{13} + \dots + 4u + 1)(u^{24} + u^{23} + \dots + 51u + 43)$
$c_5$	$(u^{15} - u^{14} + \dots - 3u^2 + 1)(u^{24} + 2u^{23} + \dots - 7u - 11)$
$c_6$	$(u^{15} - u^{14} + \dots + 3u + 1)(u^{24} - 2u^{23} + \dots - 472u - 163)$
$c_7$	$(u^{15} + 2u^{14} + \dots + 4u + 1)(u^{24} - 3u^{23} + \dots + 9u + 1)$
$c_8$	$(u^{15} + 3u^{14} + \dots - u + 1)(u^{24} + 4u^{23} + \dots - 138u - 23)$
$c_9$	$(u^{15} + 8u^{13} + \dots + 4u - 1)(u^{24} + u^{23} + \dots + 51u + 43)$
$c_{10}$	$(u^{15} - 16u^{14} + \dots + 4u + 1)(u^{24} - 7u^{23} + \dots - 667u + 1849)$
$c_{11}$	$(u^{15} + u^{14} + \dots + 3u - 1)(u^{24} - 2u^{23} + \dots - 472u - 163)$
$c_{12}$	$(u^{15} - 3u^{14} + \dots - u - 1)(u^{24} + 4u^{23} + \dots - 138u - 23)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{15} + 9y^{14} + \dots - 14y - 1)(y^{24} - 8y^{23} + \dots + 75809y + 14641)$
$c_2, c_5$	$(y^{15} - 7y^{14} + \dots + 6y - 1)(y^{24} - 16y^{23} + \dots - 819y + 121)$
$c_3$	$(y^{15} + 29y^{14} + \dots - 14y - 1)(y^{24} + 52y^{23} + \dots - 1015y + 121)$
$c_4, c_9$	$(y^{15} + 16y^{14} + \dots + 4y - 1)(y^{24} + 7y^{23} + \dots + 667y + 1849)$
$c_6, c_{11}$	$(y^{15} - 3y^{14} + \dots + y - 1)(y^{24} + 36y^{23} + \dots - 234846y + 26569)$
$c_7$	$(y^{15} - 2y^{14} + \dots + 18y - 1)(y^{24} - 47y^{23} + \dots + 113y + 1)$
$c_8, c_{12}$	$(y^{15} - y^{14} + \dots + 3y - 1)(y^{24} + 34y^{23} + \dots - 65412y + 529)$
$c_{10}$	$(y^{15} - 20y^{14} + \dots + 252y - 1)$ $\cdot (y^{24} + 35y^{23} + \dots - 209766481y + 3418801)$