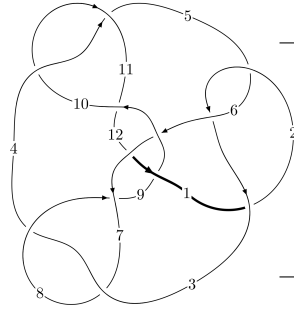
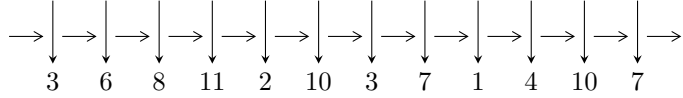


12n<sub>0417</sub> (K12n<sub>0417</sub>)

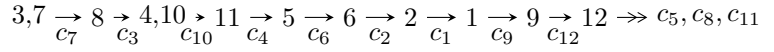


A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 536u^{11} - 335u^{10} + \dots + 239b + 523, -947u^{11} + 562u^{10} + \dots + 239a - 1324, \\ u^{12} - 4u^{10} + 13u^8 - 2u^7 - 24u^6 - 3u^5 + 18u^4 + 3u^3 - 7u^2 - u + 1 \rangle$$

$$I_2^u = \langle u^6 - 3u^4 + 3u^2 + b + u - 1, -u^6 + u^5 + 4u^4 - 3u^3 - 5u^2 + a + 2u + 3, u^7 - 4u^5 + 6u^3 + u^2 - 4u - 1 \rangle$$

$$I_3^u = \langle 68215362482207u^{19} + 127486835274380u^{18} + \dots + 1057281252711b + 705066157444833, \\ 298873575023330u^{19} + 558685165549478u^{18} + \dots + 3171843758133a + 3089653339595532, \\ u^{20} + u^{19} + \dots + 18u - 9 \rangle$$

$$I_4^u = \langle u^6 - 3u^4 - u^3 + 2u^2 + b - 2, -u^7 + 3u^5 + u^4 - 2u^3 + u^2 + a + 2u - 2, u^8 - 4u^6 - u^5 + 5u^4 + u^3 - 4u^2 + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 47 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 536u^{11} - 335u^{10} + \dots + 239b + 523, -947u^{11} + 562u^{10} + \dots + 239a - 1324, u^{12} - 4u^{10} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3.96234u^{11} - 2.35146u^{10} + \dots - 11.8033u + 5.53975 \\ -2.24268u^{11} + 1.40167u^{10} + \dots + 5.48954u - 2.18828 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3.96234u^{11} - 2.35146u^{10} + \dots - 11.8033u + 5.53975 \\ -2.24268u^{11} + 1.40167u^{10} + \dots + 5.48954u - 2.18828 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2.35146u^{11} - 1.71967u^{10} + \dots - 10.5021u + 3.96234 \\ -1.40167u^{11} + 1.25105u^{10} + \dots + 5.43096u - 2.24268 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.589958u^{11} - 0.493724u^{10} + \dots + 1.58577u + 0.543933 \\ 2.71130u^{11} - 1.69456u^{10} + \dots - 8.15900u + 3.13808 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 3.23431u^{11} - 2.14644u^{10} + \dots - 7.33473u + 3.97490 \\ 0.974895u^{11} - 0.234310u^{10} + \dots - 3.53556u + 1.35983 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 3.23431u^{11} - 2.14644u^{10} + \dots - 7.33473u + 3.97490 \\ -0.991632u^{11} + 0.744770u^{10} + \dots + 1.84519u - 0.786611 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2.24268u^{11} - 1.40167u^{10} + \dots - 5.48954u + 3.18828 \\ -0.991632u^{11} + 0.744770u^{10} + \dots + 1.84519u - 0.786611 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{1675}{239}u^{11} + \frac{1734}{239}u^{10} + \frac{5437}{239}u^9 - \frac{5818}{239}u^8 - \frac{17601}{239}u^7 + \frac{22148}{239}u^6 + \frac{23370}{239}u^5 - \frac{22069}{239}u^4 - \frac{17044}{239}u^3 + \frac{13395}{239}u^2 + \frac{5056}{239}u - \frac{6743}{239}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} + 6u^{11} + \dots + 848u + 64$
$c_2, c_5$	$u^{12} + 8u^{11} + \dots + 52u + 8$
$c_3, c_4, c_7$ $c_{10}$	$u^{12} - 4u^{10} + 13u^8 + 2u^7 - 24u^6 + 3u^5 + 18u^4 - 3u^3 - 7u^2 + u + 1$
$c_6, c_9$	$u^{12} + u^{11} + \dots + 8u + 1$
$c_8, c_{11}$	$u^{12} + 8u^{11} + \dots + 15u + 1$
$c_{12}$	$u^{12} + 10u^{11} + \dots - 196u - 20$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} + 18y^{11} + \dots - 419072y + 4096$
$c_2, c_5$	$y^{12} - 6y^{11} + \dots - 848y + 64$
$c_3, c_4, c_7$ $c_{10}$	$y^{12} - 8y^{11} + \dots - 15y + 1$
$c_6, c_9$	$y^{12} + 11y^{11} + \dots - 16y + 1$
$c_8, c_{11}$	$y^{12} + 20y^{11} + \dots - 43y + 1$
$c_{12}$	$y^{12} - 40y^{11} + \dots - 4496y + 400$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.790520 + 0.392533I$ $a = -0.333077 - 0.431942I$ $b = 0.908183 + 0.435278I$	$-3.78101 + 0.45111I$	$-18.5516 - 2.4488I$
$u = -0.790520 - 0.392533I$ $a = -0.333077 + 0.431942I$ $b = 0.908183 - 0.435278I$	$-3.78101 - 0.45111I$	$-18.5516 + 2.4488I$
$u = -0.736086 + 0.101541I$ $a = 1.55509 + 1.56812I$ $b = 0.505873 - 0.967109I$	$-0.21900 + 4.19269I$	$-13.9112 - 5.3421I$
$u = -0.736086 - 0.101541I$ $a = 1.55509 - 1.56812I$ $b = 0.505873 + 0.967109I$	$-0.21900 - 4.19269I$	$-13.9112 + 5.3421I$
$u = 0.653112 + 0.249393I$ $a = 1.71916 - 0.21403I$ $b = -0.023047 + 0.696086I$	$-0.134851 + 0.667722I$	$-12.59936 + 0.82514I$
$u = 0.653112 - 0.249393I$ $a = 1.71916 + 0.21403I$ $b = -0.023047 - 0.696086I$	$-0.134851 - 0.667722I$	$-12.59936 - 0.82514I$
$u = 1.54915$ $a = -0.373370$ $b = 0.477327$	$-15.2923$	$-6.68440$
$u = 0.403757$ $a = 0.897573$ $b = 0.248749$	$-0.603932$	$-16.3720$
$u = -1.36080 + 0.93328I$ $a = -0.627613 - 0.831271I$ $b = -1.09936 + 1.61015I$	$5.78267 + 12.88920I$	$-12.7241 - 6.3496I$
$u = -1.36080 - 0.93328I$ $a = -0.627613 + 0.831271I$ $b = -1.09936 - 1.61015I$	$5.78267 - 12.88920I$	$-12.7241 + 6.3496I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.25783 + 1.10048I$	$7.12277 - 3.83904I$	$-10.68570 + 2.08253I$
$a = -0.575658 + 0.547864I$		
$b = -0.15469 - 1.93823I$		
$u = 1.25783 - 1.10048I$	$7.12277 + 3.83904I$	$-10.68570 - 2.08253I$
$a = -0.575658 - 0.547864I$		
$b = -0.15469 + 1.93823I$		

$$\text{II. } I_2^u = \langle u^6 - 3u^4 + 3u^2 + b + u - 1, -u^6 + u^5 + 4u^4 - 3u^3 - 5u^2 + a + 2u + 3, u^7 - 4u^5 + 6u^3 + u^2 - 4u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^6 - u^5 - 4u^4 + 3u^3 + 5u^2 - 2u - 3 \\ -u^6 + 3u^4 - 3u^2 - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^6 - u^5 - 4u^4 + 3u^3 + 6u^2 - 2u - 3 \\ -u^6 + 4u^4 - 4u^2 - u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^6 + 3u^4 - 3u^2 + 1 \\ u^3 - 2u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^6 + 4u^4 - u^3 - 6u^2 + u + 4 \\ -u^5 - u^4 + 3u^3 + 2u^2 - 3u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^6 - 4u^4 + 5u^2 + u - 3 \\ u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^6 - 4u^4 + 5u^2 + u - 3 \\ u^4 - u^2 + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^6 - 3u^4 + 4u^2 + u - 2 \\ u^4 - u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u^6 + 4u^5 + 13u^4 - 10u^3 - 11u^2 + 4u - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^7 - 7u^6 + 21u^5 - 37u^4 + 37u^3 - 24u^2 + 9u - 1$
$c_2$	$u^7 + u^6 - 3u^5 - 5u^4 + u^3 + 4u^2 + u - 1$
$c_3, c_{10}$	$u^7 - 4u^5 + 6u^3 - u^2 - 4u + 1$
$c_4, c_7$	$u^7 - 4u^5 + 6u^3 + u^2 - 4u - 1$
$c_5$	$u^7 - u^6 - 3u^5 + 5u^4 + u^3 - 4u^2 + u + 1$
$c_6, c_9$	$u^7 + u^6 + u^4 - u^3 - u^2 - u - 1$
$c_8, c_{11}$	$u^7 + 8u^6 + 28u^5 + 56u^4 + 68u^3 + 49u^2 + 18u + 1$
$c_{12}$	$u^7 + 7u^6 + 17u^5 + 30u^4 + 45u^3 + 27u^2 + 6u + 4$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^7 - 7y^6 - 3y^5 - 133y^4 - 43y^3 + 16y^2 + 33y - 1$
$c_2, c_5$	$y^7 - 7y^6 + 21y^5 - 37y^4 + 37y^3 - 24y^2 + 9y - 1$
$c_3, c_4, c_7$ $c_{10}$	$y^7 - 8y^6 + 28y^5 - 56y^4 + 68y^3 - 49y^2 + 18y - 1$
$c_6, c_9$	$y^7 - y^6 - 4y^5 - y^4 + 5y^3 + 3y^2 - y - 1$
$c_8, c_{11}$	$y^7 - 8y^6 + 24y^5 - 76y^4 + 128y^3 - 65y^2 + 226y - 1$
$c_{12}$	$y^7 - 15y^6 - 41y^5 + 264y^4 + 553y^3 - 429y^2 - 180y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.970575 + 0.467764I$ $a = 0.61390 + 1.62676I$ $b = 0.307176 - 1.007690I$	$-0.15907 + 5.95632I$	$-10.30399 - 9.49474I$
$u = -0.970575 - 0.467764I$ $a = 0.61390 - 1.62676I$ $b = 0.307176 + 1.007690I$	$-0.15907 - 5.95632I$	$-10.30399 + 9.49474I$
$u = 1.28252$ $a = -0.853969$ $b = -1.55070$	$-9.96367$	$-15.2580$
$u = 1.219310 + 0.473158I$ $a = 0.831288 - 0.514652I$ $b = -0.187678 + 0.823913I$	$-1.96867 - 1.64297I$	$-12.60937 + 1.83263I$
$u = 1.219310 - 0.473158I$ $a = 0.831288 + 0.514652I$ $b = -0.187678 - 0.823913I$	$-1.96867 + 1.64297I$	$-12.60937 - 1.83263I$
$u = -1.52200$ $a = 0.182606$ $b = -0.759603$	$-15.6521$	$-29.3740$
$u = -0.257994$ $a = -2.21901$ $b = 1.07131$	$-3.02746$	$-9.54090$

**III.**

$$I_3^u = \langle 6.82 \times 10^{13}u^{19} + 1.27 \times 10^{14}u^{18} + \dots + 1.06 \times 10^{12}b + 7.05 \times 10^{14}, 2.99 \times 10^{14}u^{19} + 5.59 \times 10^{14}u^{18} + \dots + 3.17 \times 10^{12}a + 3.09 \times 10^{15}, u^{20} + u^{19} + \dots + 18u - 9 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -94.2271u^{19} - 176.139u^{18} + \dots + 828.728u - 974.087 \\ -64.5196u^{19} - 120.580u^{18} + \dots + 565.622u - 666.867 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -27.9506u^{19} - 52.2643u^{18} + \dots + 246.326u - 288.781 \\ -80.6876u^{19} - 150.746u^{18} + \dots + 707.746u - 833.790 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 4.98357u^{19} + 9.51307u^{18} + \dots - 45.9289u + 48.9194 \\ -99.9143u^{19} - 186.269u^{18} + \dots + 873.984u - 1037.72 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -68.8452u^{19} - 128.348u^{18} + \dots + 604.749u - 717.167 \\ -76.2363u^{19} - 142.302u^{18} + \dots + 674.421u - 794.311 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 69.0216u^{19} + 129.223u^{18} + \dots - 608.826u + 712.093 \\ 105.226u^{19} + 196.557u^{18} + \dots - 922.384u + 1090.86 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 69.0216u^{19} + 129.223u^{18} + \dots - 608.826u + 712.093 \\ 52.6964u^{19} + 98.1510u^{18} + \dots - 459.959u + 549.054 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 121.718u^{19} + 227.374u^{18} + \dots - 1068.79u + 1261.15 \\ 52.6964u^{19} + 98.1510u^{18} + \dots - 459.959u + 549.054 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes**

$$= -\frac{128749727823573}{352427084237}u^{19} - \frac{240297448875642}{352427084237}u^{18} + \dots + \frac{1127484403652596}{352427084237}u - \frac{1338735790487557}{352427084237}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{10} + u^9 + 8u^8 + 12u^7 - 8u^6 - 6u^5 - 4u^4 + 21u^3 + 21u^2 + 14u + 1)^2$
$c_2, c_5$	$(u^{10} - 3u^9 + 4u^8 - 2u^7 + 2u^6 - 4u^5 - u^3 + 5u^2 - 2u - 1)^2$
$c_3, c_4, c_7$ $c_{10}$	$u^{20} - u^{19} + \dots - 18u - 9$
$c_6, c_9$	$u^{20} - 3u^{19} + \dots - 6u - 1$
$c_8, c_{11}$	$u^{20} + 5u^{19} + \dots + 576u + 81$
$c_{12}$	$(u^{10} - 4u^9 - u^8 + 23u^7 - 31u^6 + 7u^5 + 6u^4 + 4u^3 - 10u^2 + 5u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{10} + 15y^9 + \dots - 154y + 1)^2$
$c_2, c_5$	$(y^{10} - y^9 + 8y^8 - 12y^7 - 8y^6 + 6y^5 - 4y^4 - 21y^3 + 21y^2 - 14y + 1)^2$
$c_3, c_4, c_7$ $c_{10}$	$y^{20} - 5y^{19} + \dots - 576y + 81$
$c_6, c_9$	$y^{20} + 9y^{19} + \dots + 144y + 1$
$c_8, c_{11}$	$y^{20} + 7y^{19} + \dots - 23004y + 6561$
$c_{12}$	$(y^{10} - 18y^9 + \dots - 5y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.388171 + 0.947508I$ $a = 0.0090099 + 0.1229930I$ $b = -1.35420 + 0.42025I$	$2.99056 - 3.56450I$	$-10.26354 + 3.14852I$
$u = 0.388171 - 0.947508I$ $a = 0.0090099 - 0.1229930I$ $b = -1.35420 - 0.42025I$	$2.99056 + 3.56450I$	$-10.26354 - 3.14852I$
$u = -0.992473 + 0.348531I$ $a = 0.17968 + 1.68020I$ $b = 0.0378360 - 0.0943430I$	$-1.26454 + 5.52673I$	$-18.1850 - 5.9531I$
$u = -0.992473 - 0.348531I$ $a = 0.17968 - 1.68020I$ $b = 0.0378360 + 0.0943430I$	$-1.26454 - 5.52673I$	$-18.1850 + 5.9531I$
$u = 0.872812 + 0.011238I$ $a = 1.102060 - 0.425174I$ $b = 0.274355 - 0.471998I$	$-0.136787 - 0.639555I$	$-12.53187 - 0.40948I$
$u = 0.872812 - 0.011238I$ $a = 1.102060 + 0.425174I$ $b = 0.274355 + 0.471998I$	$-0.136787 + 0.639555I$	$-12.53187 + 0.40948I$
$u = 0.866881$ $a = -1.65529$ $b = -1.53301$	$-12.1512$	$-23.7630$
$u = 1.001390 + 0.640706I$ $a = 0.418488 - 1.217960I$ $b = 0.531023 + 1.236570I$	$-1.26454 - 5.52673I$	$-18.1850 + 5.9531I$
$u = 1.001390 - 0.640706I$ $a = 0.418488 + 1.217960I$ $b = 0.531023 - 1.236570I$	$-1.26454 + 5.52673I$	$-18.1850 - 5.9531I$
$u = 0.468108 + 0.513336I$ $a = 1.40798 - 1.10900I$ $b = -0.102915 + 0.895664I$	$-0.136787 + 0.639555I$	$-12.53187 + 0.40948I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.468108 - 0.513336I$ $a = 1.40798 + 1.10900I$ $b = -0.102915 - 0.895664I$	$-0.136787 - 0.639555I$	$-12.53187 - 0.40948I$
$u = -0.605174$ $a = 0.762515$ $b = 1.92560$	$-7.31763$	$-2.93760$
$u = -1.07994 + 0.93851I$ $a = 0.617818 + 0.827405I$ $b = 0.59658 - 1.52167I$	$2.99056 + 3.56450I$	$-10.26354 - 3.14852I$
$u = -1.07994 - 0.93851I$ $a = 0.617818 - 0.827405I$ $b = 0.59658 + 1.52167I$	$2.99056 - 3.56450I$	$-10.26354 + 3.14852I$
$u = -1.45778$ $a = -1.23121$ $b = -0.970112$	$-7.31763$	$-2.93760$
$u = 0.91975 + 1.23722I$ $a = -0.446520 + 0.963248I$ $b = -0.95499 - 1.76369I$	$8.14515 - 4.60681I$	$-10.16934 + 2.47582I$
$u = 0.91975 - 1.23722I$ $a = -0.446520 - 0.963248I$ $b = -0.95499 + 1.76369I$	$8.14515 + 4.60681I$	$-10.16934 - 2.47582I$
$u = -0.63701 + 1.40514I$ $a = -0.447242 - 0.786229I$ $b = 0.22554 + 1.94609I$	$8.14515 - 4.60681I$	$-10.16934 + 2.47582I$
$u = -0.63701 - 1.40514I$ $a = -0.447242 + 0.786229I$ $b = 0.22554 - 1.94609I$	$8.14515 + 4.60681I$	$-10.16934 - 2.47582I$
$u = -1.68554$ $a = -0.225221$ $b = -0.928948$	$-12.1512$	$-23.7630$

$$\text{IV. } I_4^u = \langle u^6 - 3u^4 - u^3 + 2u^2 + b - 2, -u^7 + 3u^5 + u^4 - 2u^3 + u^2 + a + 2u - 2, u^8 - 4u^6 - u^5 + 5u^4 + u^3 - 4u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^7 - 3u^5 - u^4 + 2u^3 - u^2 - 2u + 2 \\ -u^6 + 3u^4 + u^3 - 2u^2 + 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^7 - 3u^5 - u^4 + 2u^3 - u^2 - 2u + 1 \\ -u^6 + 3u^4 + u^3 - 3u^2 + 3 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^7 - u^6 - 4u^5 + 2u^4 + 6u^3 - u^2 - 4u + 2 \\ 3u^7 - 11u^5 - 3u^4 + 11u^3 + 2u^2 - 8u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2u^7 + 7u^5 + 2u^4 - 6u^3 - u^2 + 4u - 1 \\ u^7 + 2u^6 - 3u^5 - 8u^4 + 6u^2 - u - 4 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^7 + u^6 + 4u^5 - 3u^4 - 6u^3 + 4u^2 + 5u - 3 \\ u^6 - 4u^4 - u^3 + 5u^2 + 2u - 4 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^7 + u^6 + 4u^5 - 3u^4 - 6u^3 + 4u^2 + 5u - 3 \\ u^6 - 4u^4 - u^3 + 4u^2 + u - 3 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^7 + 2u^6 + 4u^5 - 7u^4 - 7u^3 + 8u^2 + 6u - 6 \\ u^6 - 4u^4 - u^3 + 4u^2 + u - 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = 15u^7 + 5u^6 - 53u^5 - 35u^4 + 49u^3 + 28u^2 - 33u - 25$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^4 - 4u^3 + 6u^2 - 5u + 1)^2$
$c_2$	$(u^4 - 2u^2 + u + 1)^2$
$c_3, c_{10}$	$u^8 - 4u^6 + u^5 + 5u^4 - u^3 - 4u^2 + 1$
$c_4, c_7$	$u^8 - 4u^6 - u^5 + 5u^4 + u^3 - 4u^2 + 1$
$c_5$	$(u^4 - 2u^2 - u + 1)^2$
$c_6, c_9$	$u^8 - 4u^7 + 5u^6 - u^5 - 4u^4 + 5u^3 - 2u^2 + 1$
$c_8, c_{11}$	$u^8 + 8u^7 + 26u^6 + 49u^5 + 61u^4 + 49u^3 + 26u^2 + 8u + 1$
$c_{12}$	$(u^4 - 4u^3 + 4u^2 - u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^4 - 4y^3 - 2y^2 - 13y + 1)^2$
$c_2, c_5$	$(y^4 - 4y^3 + 6y^2 - 5y + 1)^2$
$c_3, c_4, c_7$ $c_{10}$	$y^8 - 8y^7 + 26y^6 - 49y^5 + 61y^4 - 49y^3 + 26y^2 - 8y + 1$
$c_6, c_9$	$y^8 - 6y^7 + 9y^6 - 5y^5 + 8y^4 + y^3 - 4y^2 - 4y + 1$
$c_8, c_{11}$	$y^8 - 12y^7 + 14y^6 + 39y^5 + 145y^4 + 39y^3 + 14y^2 - 12y + 1$
$c_{12}$	$(y^4 - 8y^3 + 10y^2 + 7y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.744022 + 0.443105I$		
$a = 1.42333 - 1.57383I$	$-0.24852 - 1.96274I$	$-13.4834 + 4.4361I$
$b = 0.758066 + 0.777626I$		
$u = 0.744022 - 0.443105I$		
$a = 1.42333 + 1.57383I$	$-0.24852 + 1.96274I$	$-13.4834 - 4.4361I$
$b = 0.758066 - 0.777626I$		
$u = -0.992148 + 0.590877I$		
$a = 1.145330 + 0.258001I$	$-0.24852 - 1.96274I$	$-13.4834 + 4.4361I$
$b = 0.241934 - 0.777626I$		
$u = -0.992148 - 0.590877I$		
$a = 1.145330 - 0.258001I$	$-0.24852 + 1.96274I$	$-13.4834 - 4.4361I$
$b = 0.241934 + 0.777626I$		
$u = 0.701343$		
$a = 0.127840$	$-7.58970$	$-33.0820$
$b = 1.96805$		
$u = -1.42584$		
$a = -1.41328$	$-7.58970$	$-33.0820$
$b = -0.968048$		
$u = -0.561188$		
$a = 2.50424$	$-11.6525$	$-6.95090$
$b = 1.45971$		
$u = 1.78193$		
$a = -0.356111$	$-11.6525$	$-6.95090$
$b = -0.459710$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^4 - 4u^3 + 6u^2 - 5u + 1)^2$ $\cdot (u^7 - 7u^6 + 21u^5 - 37u^4 + 37u^3 - 24u^2 + 9u - 1)$ $\cdot (u^{10} + u^9 + 8u^8 + 12u^7 - 8u^6 - 6u^5 - 4u^4 + 21u^3 + 21u^2 + 14u + 1)^2$ $\cdot (u^{12} + 6u^{11} + \dots + 848u + 64)$
$c_2$	$(u^4 - 2u^2 + u + 1)^2(u^7 + u^6 - 3u^5 - 5u^4 + u^3 + 4u^2 + u - 1)$ $\cdot (u^{10} - 3u^9 + 4u^8 - 2u^7 + 2u^6 - 4u^5 - u^3 + 5u^2 - 2u - 1)^2$ $\cdot (u^{12} + 8u^{11} + \dots + 52u + 8)$
$c_3, c_{10}$	$(u^7 - 4u^5 + 6u^3 - u^2 - 4u + 1)(u^8 - 4u^6 + u^5 + 5u^4 - u^3 - 4u^2 + 1)$ $\cdot (u^{12} - 4u^{10} + 13u^8 + 2u^7 - 24u^6 + 3u^5 + 18u^4 - 3u^3 - 7u^2 + u + 1)$ $\cdot (u^{20} - u^{19} + \dots - 18u - 9)$
$c_4, c_7$	$(u^7 - 4u^5 + 6u^3 + u^2 - 4u - 1)(u^8 - 4u^6 - u^5 + 5u^4 + u^3 - 4u^2 + 1)$ $\cdot (u^{12} - 4u^{10} + 13u^8 + 2u^7 - 24u^6 + 3u^5 + 18u^4 - 3u^3 - 7u^2 + u + 1)$ $\cdot (u^{20} - u^{19} + \dots - 18u - 9)$
$c_5$	$(u^4 - 2u^2 - u + 1)^2(u^7 - u^6 - 3u^5 + 5u^4 + u^3 - 4u^2 + u + 1)$ $\cdot (u^{10} - 3u^9 + 4u^8 - 2u^7 + 2u^6 - 4u^5 - u^3 + 5u^2 - 2u - 1)^2$ $\cdot (u^{12} + 8u^{11} + \dots + 52u + 8)$
$c_6, c_9$	$(u^7 + u^6 + u^4 - u^3 - u^2 - u - 1)(u^8 - 4u^7 + \dots - 2u^2 + 1)$ $\cdot (u^{12} + u^{11} + \dots + 8u + 1)(u^{20} - 3u^{19} + \dots - 6u - 1)$
$c_8, c_{11}$	$(u^7 + 8u^6 + 28u^5 + 56u^4 + 68u^3 + 49u^2 + 18u + 1)$ $\cdot (u^8 + 8u^7 + 26u^6 + 49u^5 + 61u^4 + 49u^3 + 26u^2 + 8u + 1)$ $\cdot (u^{12} + 8u^{11} + \dots + 15u + 1)(u^{20} + 5u^{19} + \dots + 576u + 81)$
$c_{12}$	$(u^4 - 4u^3 + 4u^2 - u + 1)^2$ $\cdot (u^7 + 7u^6 + 17u^5 + 30u^4 + 45u^3 + 27u^2 + 6u + 4)$ $\cdot (u^{10} - 4u^9 - u^8 + 23u^7 - 31u^6 + 7u^5 + 6u^4 + 4u^3 - 10u^2 + 5u - 1)^2$ $\cdot (u^{12} + 10u^{11} + \dots - 196u - 20)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^4 - 4y^3 - 2y^2 - 13y + 1)^2$ $\cdot (y^7 - 7y^6 - 3y^5 - 133y^4 - 43y^3 + 16y^2 + 33y - 1)$ $\cdot (y^{10} + 15y^9 + \dots - 154y + 1)^2$ $\cdot (y^{12} + 18y^{11} + \dots - 419072y + 4096)$
$c_2, c_5$	$(y^4 - 4y^3 + 6y^2 - 5y + 1)^2$ $\cdot (y^7 - 7y^6 + 21y^5 - 37y^4 + 37y^3 - 24y^2 + 9y - 1)$ $\cdot (y^{10} - y^9 + 8y^8 - 12y^7 - 8y^6 + 6y^5 - 4y^4 - 21y^3 + 21y^2 - 14y + 1)^2$ $\cdot (y^{12} - 6y^{11} + \dots - 848y + 64)$
$c_3, c_4, c_7$ $c_{10}$	$(y^7 - 8y^6 + 28y^5 - 56y^4 + 68y^3 - 49y^2 + 18y - 1)$ $\cdot (y^8 - 8y^7 + 26y^6 - 49y^5 + 61y^4 - 49y^3 + 26y^2 - 8y + 1)$ $\cdot (y^{12} - 8y^{11} + \dots - 15y + 1)(y^{20} - 5y^{19} + \dots - 576y + 81)$
$c_6, c_9$	$(y^7 - y^6 - 4y^5 - y^4 + 5y^3 + 3y^2 - y - 1)$ $\cdot (y^8 - 6y^7 + 9y^6 - 5y^5 + 8y^4 + y^3 - 4y^2 - 4y + 1)$ $\cdot (y^{12} + 11y^{11} + \dots - 16y + 1)(y^{20} + 9y^{19} + \dots + 144y + 1)$
$c_8, c_{11}$	$(y^7 - 8y^6 + 24y^5 - 76y^4 + 128y^3 - 65y^2 + 226y - 1)$ $\cdot (y^8 - 12y^7 + 14y^6 + 39y^5 + 145y^4 + 39y^3 + 14y^2 - 12y + 1)$ $\cdot (y^{12} + 20y^{11} + \dots - 43y + 1)(y^{20} + 7y^{19} + \dots - 23004y + 6561)$
$c_{12}$	$(y^4 - 8y^3 + 10y^2 + 7y + 1)^2$ $\cdot (y^7 - 15y^6 - 41y^5 + 264y^4 + 553y^3 - 429y^2 - 180y - 16)$ $\cdot ((y^{10} - 18y^9 + \dots - 5y + 1)^2)(y^{12} - 40y^{11} + \dots - 4496y + 400)$