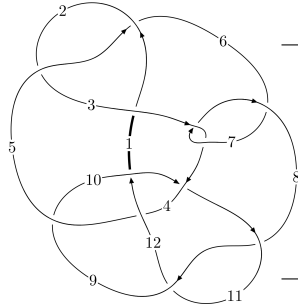
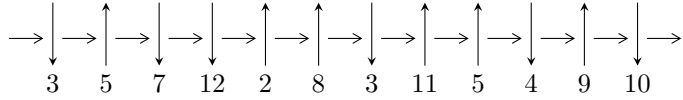


$12n_{0421}$  ( $K12n_{0421}$ )



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1,10 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \xrightarrow{c_4} 4 \xrightarrow{c_{11}} 11 \xrightarrow{c_8} 8 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \rightsquigarrow c_3, c_5, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 6.94451 \times 10^{73} u^{53} - 1.34116 \times 10^{74} u^{52} + \dots + 3.81141 \times 10^{75} b - 1.25088 \times 10^{75}, \\ - 3.43142 \times 10^{75} u^{53} + 7.05210 \times 10^{75} u^{52} + \dots + 3.23970 \times 10^{76} a + 1.89860 \times 10^{77}, \\ u^{54} - 2u^{53} + \dots - 112u + 17 \rangle$$

$$I_2^u = \langle -44u^{17} + 4u^{16} + \dots + 69b + 127u, -44u^{17} - 264u^{15} + \dots + 69a - 224, u^{18} + 6u^{16} + \dots + 3u + 1 \rangle$$

$$I_3^u = \langle a^4 - a^3u + 2a^2 - au + b - u + 2, a^5 - a^4 + 2a^3 - a^2 + a - 1, u^2 + 1 \rangle$$

$$I_4^u = \langle -3u^3 + 6u^2 + 4b - 5u + 1, u^3 + 2a - u + 3, u^4 - u^3 + u^2 + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 86 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 6.94 \times 10^{73} u^{53} - 1.34 \times 10^{74} u^{52} + \dots + 3.81 \times 10^{75} b - 1.25 \times 10^{75}, -3.43 \times 10^{75} u^{53} + 7.05 \times 10^{75} u^{52} + \dots + 3.24 \times 10^{76} a + 1.90 \times 10^{77}, u^{54} - 2u^{53} + \dots - 112u + 17 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.105918u^{53} - 0.217677u^{52} + \dots + 63.2432u - 5.86042 \\ -0.0182203u^{53} + 0.0351879u^{52} + \dots - 10.1732u + 0.328192 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.105918u^{53} - 0.217677u^{52} + \dots + 63.2432u - 5.86042 \\ -0.0293505u^{53} + 0.0578164u^{52} + \dots - 12.6281u + 0.427504 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0377580u^{53} + 0.0561954u^{52} + \dots + 17.7971u - 6.35371 \\ -0.0210496u^{53} + 0.0288416u^{52} + \dots - 9.16703u + 1.99686 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0736388u^{53} - 0.109834u^{52} + \dots + 5.97498u + 3.87914 \\ -0.00164042u^{53} + 0.00683312u^{52} + \dots - 1.67223u - 0.577146 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0157800u^{53} - 0.0231466u^{52} + \dots + 29.3692u - 3.16089 \\ -0.0328608u^{53} + 0.0646084u^{52} + \dots - 11.4634u + 0.980987 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0000582809u^{53} + 0.00965479u^{52} + \dots + 26.4948u - 4.19485 \\ -0.0248738u^{53} + 0.0481071u^{52} + \dots - 11.7942u + 1.11363 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0248155u^{53} + 0.0577619u^{52} + \dots + 14.7006u - 3.08122 \\ -0.0248738u^{53} + 0.0481071u^{52} + \dots - 11.7942u + 1.11363 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 - u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.0961909u^{53} - 0.214297u^{52} + \dots + 61.1959u + 0.495059$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{54} + 60u^{53} + \dots + 17614u + 289$
$c_2, c_5$	$u^{54} + 2u^{53} + \dots + 112u + 17$
$c_3, c_7$	$u^{54} + 2u^{53} + \dots + 20u + 17$
$c_4$	$u^{54} - 7u^{53} + \dots - 8u + 4$
$c_6$	$u^{54} - 20u^{53} + \dots - 15886u + 289$
$c_8, c_{11}$	$u^{54} + 4u^{53} + \dots + 481u + 16$
$c_9$	$2(2u^{54} + 11u^{53} + \dots + 27633u + 3982)$
$c_{10}$	$2(2u^{54} + 3u^{53} + \dots - 26787u + 17894)$
$c_{12}$	$u^{54} - 8u^{53} + \dots - 2976u + 256$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{54} - 120y^{53} + \dots - 34842354y + 83521$
$c_2, c_5$	$y^{54} + 60y^{53} + \dots + 17614y + 289$
$c_3, c_7$	$y^{54} + 20y^{53} + \dots + 15886y + 289$
$c_4$	$y^{54} + 17y^{53} + \dots + 152y + 16$
$c_6$	$y^{54} + 40y^{53} + \dots - 35600546y + 83521$
$c_8, c_{11}$	$y^{54} - 32y^{53} + \dots - 95457y + 256$
$c_9$	$4(4y^{54} - 173y^{53} + \dots + 1.70212 \times 10^8 y + 1.58563 \times 10^7)$
$c_{10}$	$4(4y^{54} - 205y^{53} + \dots + 5.53025 \times 10^9 y + 3.20195 \times 10^8)$
$c_{12}$	$y^{54} - 12y^{53} + \dots - 1545216y + 65536$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.957433 + 0.281564I$ $a = -0.366782 + 0.368685I$ $b = -0.536027 - 0.041780I$	$0.08167 - 4.27758I$	$0. + 6.47467I$
$u = -0.957433 - 0.281564I$ $a = -0.366782 - 0.368685I$ $b = -0.536027 + 0.041780I$	$0.08167 + 4.27758I$	$0. - 6.47467I$
$u = 0.793853 + 0.517771I$ $a = -0.989605 - 0.419229I$ $b = -0.745351 + 0.352281I$	$-1.69843 + 5.87991I$	$-0.83203 - 7.69197I$
$u = 0.793853 - 0.517771I$ $a = -0.989605 + 0.419229I$ $b = -0.745351 - 0.352281I$	$-1.69843 - 5.87991I$	$-0.83203 + 7.69197I$
$u = 1.013690 + 0.409819I$ $a = 1.40509 + 0.61654I$ $b = 1.023680 - 0.012588I$	$1.51017 + 11.89510I$	$0. - 8.55352I$
$u = 1.013690 - 0.409819I$ $a = 1.40509 - 0.61654I$ $b = 1.023680 + 0.012588I$	$1.51017 - 11.89510I$	$0. + 8.55352I$
$u = 0.037687 + 0.876774I$ $a = -0.411613 - 0.841558I$ $b = -0.730721 - 0.454623I$	$-1.21558 - 1.50306I$	$-6.28567 + 3.87694I$
$u = 0.037687 - 0.876774I$ $a = -0.411613 + 0.841558I$ $b = -0.730721 + 0.454623I$	$-1.21558 + 1.50306I$	$-6.28567 - 3.87694I$
$u = 0.001197 + 1.155080I$ $a = 0.344466 + 1.134660I$ $b = 0.086158 + 0.503268I$	$4.74660 - 4.32144I$	$0$
$u = 0.001197 - 1.155080I$ $a = 0.344466 - 1.134660I$ $b = 0.086158 - 0.503268I$	$4.74660 + 4.32144I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.904014 + 0.749313I$ $a = 0.409227 - 0.949421I$ $b = 0.254579 - 0.478630I$	$-0.351082 - 0.581835I$	0
$u = -0.904014 - 0.749313I$ $a = 0.409227 + 0.949421I$ $b = 0.254579 + 0.478630I$	$-0.351082 + 0.581835I$	0
$u = -0.409754 + 0.654267I$ $a = 0.670688 - 0.470147I$ $b = 0.024664 - 0.332222I$	$-0.11724 - 1.46636I$	$-1.51920 + 4.74355I$
$u = -0.409754 - 0.654267I$ $a = 0.670688 + 0.470147I$ $b = 0.024664 + 0.332222I$	$-0.11724 + 1.46636I$	$-1.51920 - 4.74355I$
$u = 0.897207 + 0.878746I$ $a = 0.412964 + 0.196074I$ $b = 0.230506 + 0.127637I$	$8.36051 + 3.29219I$	0
$u = 0.897207 - 0.878746I$ $a = 0.412964 - 0.196074I$ $b = 0.230506 - 0.127637I$	$8.36051 - 3.29219I$	0
$u = 0.611149 + 0.347151I$ $a = 1.350850 - 0.353105I$ $b = 1.28376 + 1.02238I$	$3.32384 + 4.22762I$	$7.57484 - 8.95989I$
$u = 0.611149 - 0.347151I$ $a = 1.350850 + 0.353105I$ $b = 1.28376 - 1.02238I$	$3.32384 - 4.22762I$	$7.57484 + 8.95989I$
$u = -0.483135 + 0.456682I$ $a = -2.56114 - 3.18734I$ $b = -1.88415 + 0.56985I$	$1.86209 - 1.74879I$	$7.3853 - 15.6719I$
$u = -0.483135 - 0.456682I$ $a = -2.56114 + 3.18734I$ $b = -1.88415 - 0.56985I$	$1.86209 + 1.74879I$	$7.3853 + 15.6719I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.246711 + 0.521269I$ $a = 2.52817 + 2.38441I$ $b = 0.71366 - 1.77517I$	$1.60277 - 1.13073I$	$16.4890 + 3.6045I$
$u = -0.246711 - 0.521269I$ $a = 2.52817 - 2.38441I$ $b = 0.71366 + 1.77517I$	$1.60277 + 1.13073I$	$16.4890 - 3.6045I$
$u = 0.10747 + 1.43757I$ $a = -0.231658 + 0.116000I$ $b = -2.40283 - 0.09567I$	$-1.12918 + 2.68232I$	0
$u = 0.10747 - 1.43757I$ $a = -0.231658 - 0.116000I$ $b = -2.40283 + 0.09567I$	$-1.12918 - 2.68232I$	0
$u = -0.00780 + 1.45535I$ $a = -0.234240 - 0.821894I$ $b = -0.634589 + 0.224881I$	$-3.51163 - 1.45830I$	0
$u = -0.00780 - 1.45535I$ $a = -0.234240 + 0.821894I$ $b = -0.634589 - 0.224881I$	$-3.51163 + 1.45830I$	0
$u = 0.19633 + 1.47266I$ $a = -0.180761 + 0.764063I$ $b = -0.450752 - 0.458790I$	$-2.64331 + 7.12189I$	0
$u = 0.19633 - 1.47266I$ $a = -0.180761 - 0.764063I$ $b = -0.450752 + 0.458790I$	$-2.64331 - 7.12189I$	0
$u = -0.04819 + 1.51041I$ $a = 0.39189 - 1.67295I$ $b = 0.87803 - 2.40931I$	$-5.05765 - 2.00436I$	0
$u = -0.04819 - 1.51041I$ $a = 0.39189 + 1.67295I$ $b = 0.87803 + 2.40931I$	$-5.05765 + 2.00436I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.14469 + 1.50993I$ $a = 0.47360 + 1.91984I$ $b = 1.53856 + 2.59401I$	$-4.66611 - 3.99543I$	0
$u = -0.14469 - 1.50993I$ $a = 0.47360 - 1.91984I$ $b = 1.53856 - 2.59401I$	$-4.66611 + 3.99543I$	0
$u = 0.416507 + 0.239610I$ $a = 0.373760 - 0.682809I$ $b = 1.212780 - 0.597298I$	$4.35238 + 0.88122I$	$11.36984 - 2.33709I$
$u = 0.416507 - 0.239610I$ $a = 0.373760 + 0.682809I$ $b = 1.212780 + 0.597298I$	$4.35238 - 0.88122I$	$11.36984 + 2.33709I$
$u = 0.076348 + 0.449359I$ $a = 1.54451 - 2.17798I$ $b = 0.371098 - 0.688121I$	$7.12845 + 4.50045I$	$11.43251 - 4.54345I$
$u = 0.076348 - 0.449359I$ $a = 1.54451 + 2.17798I$ $b = 0.371098 + 0.688121I$	$7.12845 - 4.50045I$	$11.43251 + 4.54345I$
$u = -0.40434 + 1.49345I$ $a = 0.473577 + 0.252036I$ $b = 1.54220 - 0.04301I$	$-5.61605 - 9.26553I$	0
$u = -0.40434 - 1.49345I$ $a = 0.473577 - 0.252036I$ $b = 1.54220 + 0.04301I$	$-5.61605 + 9.26553I$	0
$u = 0.30238 + 1.53005I$ $a = 0.508036 - 0.093774I$ $b = 1.60740 + 0.32922I$	$-8.31392 + 2.90879I$	0
$u = 0.30238 - 1.53005I$ $a = 0.508036 + 0.093774I$ $b = 1.60740 - 0.32922I$	$-8.31392 - 2.90879I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.27909 + 1.54859I$		
$a = 0.761075 - 0.328934I$	$-8.47521 + 9.84153I$	0
$b = 2.56556 - 0.27826I$		
$u = 0.27909 - 1.54859I$		
$a = 0.761075 + 0.328934I$	$-8.47521 - 9.84153I$	0
$b = 2.56556 + 0.27826I$		
$u = 0.39619 + 1.53466I$		
$a = -0.989911 + 0.661170I$	$-4.7262 + 17.0140I$	0
$b = -2.69175 + 0.38369I$		
$u = 0.39619 - 1.53466I$		
$a = -0.989911 - 0.661170I$	$-4.7262 - 17.0140I$	0
$b = -2.69175 - 0.38369I$		
$u = -0.13238 + 1.58588I$		
$a = 0.710747 + 0.251585I$	$-10.02230 - 3.29278I$	0
$b = 2.39257 + 0.46175I$		
$u = -0.13238 - 1.58588I$		
$a = 0.710747 - 0.251585I$	$-10.02230 + 3.29278I$	0
$b = 2.39257 - 0.46175I$		
$u = -0.23845 + 1.60519I$		
$a = -1.019030 - 0.001725I$	$-8.27340 - 4.54754I$	0
$b = -2.17248 + 0.26878I$		
$u = -0.23845 - 1.60519I$		
$a = -1.019030 + 0.001725I$	$-8.27340 + 4.54754I$	0
$b = -2.17248 - 0.26878I$		
$u = -0.30330 + 1.60247I$		
$a = -0.977488 - 0.584250I$	$-7.29392 - 10.27410I$	0
$b = -2.55816 - 0.50781I$		
$u = -0.30330 - 1.60247I$		
$a = -0.977488 + 0.584250I$	$-7.29392 + 10.27410I$	0
$b = -2.55816 + 0.50781I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.09043 + 1.66784I$ $a = -0.977056 - 0.182021I$ $b = -2.14804 - 0.39830I$	$-9.44818 - 2.46020I$	0
$u = 0.09043 - 1.66784I$ $a = -0.977056 + 0.182021I$ $b = -2.14804 + 0.39830I$	$-9.44818 + 2.46020I$	0
$u = 0.060670 + 0.183744I$ $a = 0.36004 + 5.05217I$ $b = -0.395346 - 1.125760I$	$1.88776 - 1.50114I$	$7.21238 + 4.30156I$
$u = 0.060670 - 0.183744I$ $a = 0.36004 - 5.05217I$ $b = -0.395346 + 1.125760I$	$1.88776 + 1.50114I$	$7.21238 - 4.30156I$

$$\text{II. } I_2^u = \langle -44u^{17} + 4u^{16} + \dots + 69b + 127u, -44u^{17} - 264u^{15} + \dots + 69a - 224, u^{18} + 6u^{16} + \dots + 3u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.637681u^{17} + 3.82609u^{15} + \dots + 2.66667u + 3.24638 \\ 0.637681u^{17} - 0.0579710u^{16} + \dots + 3.91304u^2 - 1.84058u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.637681u^{17} + 3.82609u^{15} + \dots + 2.66667u + 3.24638 \\ 0.637681u^{17} + 0.173913u^{16} + \dots + 5.24638u^2 - 2.47826u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.594203u^{17} + 3.56522u^{15} + \dots + 3.66667u + 0.115942 \\ 0.594203u^{17} - 0.594203u^{16} + \dots - 3.55072u^2 - 0.115942u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.840580u^{17} + 5.04348u^{15} + \dots + 4.33333u + 3.18841 \\ 0.840580u^{17} - 0.0579710u^{16} + \dots + 3.85507u^2 - 1.84058u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 - u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{20}{23}u^{15} + \frac{100}{23}u^{13} + \frac{44}{23}u^{12} + \frac{200}{23}u^{11} + \frac{176}{23}u^{10} + \frac{316}{23}u^9 + \frac{264}{23}u^8 + \frac{448}{23}u^7 + \frac{260}{23}u^6 + 16u^5 + \frac{212}{23}u^4 + \frac{208}{23}u^3 + \frac{84}{23}u^2 + 4u + \frac{106}{23}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} + 12u^{17} + \dots + 3u + 1$
$c_2, c_3, c_5$ $c_7$	$u^{18} + 6u^{16} + \dots - 3u + 1$
$c_4$	$(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^3$
$c_6$	$u^{18} - 12u^{17} + \dots - 3u + 1$
$c_8, c_{11}$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$
$c_9$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^3$
$c_{10}, c_{12}$	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{18} - 12y^{17} + \dots + 95y + 1$
$c_2, c_3, c_5$ $c_7$	$y^{18} + 12y^{17} + \dots + 3y + 1$
$c_4, c_9$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^3$
$c_8, c_{10}, c_{11}$ $c_{12}$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.577722 + 0.852843I$ $a = -0.598036 + 0.102351I$ $b = -0.488236 - 0.375359I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = -0.577722 - 0.852843I$ $a = -0.598036 - 0.102351I$ $b = -0.488236 + 0.375359I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 0.196160 + 0.885066I$ $a = 0.419078 + 1.129010I$ $b = -2.92263 - 1.35280I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 0.196160 - 0.885066I$ $a = 0.419078 - 1.129010I$ $b = -2.92263 + 1.35280I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.945163 + 0.610473I$ $a = 1.206700 - 0.490377I$ $b = 0.819070 - 0.094621I$	$-5.69302I$	$0. + 5.51057I$
$u = -0.945163 - 0.610473I$ $a = 1.206700 + 0.490377I$ $b = 0.819070 + 0.094621I$	$5.69302I$	$0. - 5.51057I$
$u = 0.090472 + 1.133120I$ $a = -0.583686 + 0.762709I$ $b = -3.11733 - 0.76503I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = 0.090472 - 1.133120I$ $a = -0.583686 - 0.762709I$ $b = -3.11733 + 0.76503I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 0.686633 + 0.502578I$ $a = -0.150201 - 0.718978I$ $b = -0.530542 - 0.156218I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 0.686633 - 0.502578I$ $a = -0.150201 + 0.718978I$ $b = -0.530542 + 0.156218I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.824262 + 0.925280I$ $a = 0.271648 + 1.151080I$ $b = 0.190767 + 0.581448I$	$-5.69302I$	$0. + 5.51057I$
$u = 0.824262 - 0.925280I$ $a = 0.271648 - 1.151080I$ $b = 0.190767 - 0.581448I$	$5.69302I$	$0. - 5.51057I$
$u = -0.108911 + 1.355420I$ $a = 0.402013 - 0.222804I$ $b = 1.71123 - 1.31922I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = -0.108911 - 1.355420I$ $a = 0.402013 + 0.222804I$ $b = 1.71123 + 1.31922I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 0.12090 + 1.53575I$ $a = -0.819509 + 0.483205I$ $b = -2.32751 + 0.84183I$	$5.69302I$	$0. - 5.51057I$
$u = 0.12090 - 1.53575I$ $a = -0.819509 - 0.483205I$ $b = -2.32751 - 0.84183I$	$-5.69302I$	$0. + 5.51057I$
$u = -0.286632 + 0.248050I$ $a = 2.85200 + 0.40141I$ $b = 0.665192 - 0.947661I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = -0.286632 - 0.248050I$ $a = 2.85200 - 0.40141I$ $b = 0.665192 + 0.947661I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$

$$\text{III. } I_3^u = \langle a^4 - a^3u + 2a^2 - au + b - u + 2, a^5 - a^4 + 2a^3 - a^2 + a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -a^4 + a^3u - 2a^2 + au + u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -a^4 + a^3u - 2a^2 + au - a + u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a^2 \\ -a^4u + a^4 - a^2u + a^2 - au + a \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^4u \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^4 \\ -a^4 - 2a^2 + u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a^4 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^4 + u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a^3 + 4a^2 - 4a + 4$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^{10}$
$c_2, c_3, c_5$ $c_7$	$(u^2 + 1)^5$
$c_4$	$u^{10} + u^8 + 8u^6 + 3u^4 + 3u^2 + 1$
$c_6$	$(u + 1)^{10}$
$c_8$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2$
$c_9$	$u^{10} - 3u^8 + 4u^6 - u^4 - u^2 + 1$
$c_{10}$	$u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1$
$c_{11}$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$
$c_{12}$	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y - 1)^{10}$
$c_2, c_3, c_5$ $c_7$	$(y + 1)^{10}$
$c_4$	$(y^5 + y^4 + 8y^3 + 3y^2 + 3y + 1)^2$
$c_8, c_{11}$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$
$c_9$	$(y^5 - 3y^4 + 4y^3 - y^2 - y + 1)^2$
$c_{10}$	$(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$
$c_{12}$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = -0.339110 + 0.822375I$ $b = -1.43128 + 1.79928I$	$0.32910 + 1.53058I$	$0.51511 - 4.43065I$
$u = 1.000000I$ $a = -0.339110 - 0.822375I$ $b = -0.331455 + 0.820551I$	$0.32910 - 1.53058I$	$0.51511 + 4.43065I$
$u = 1.000000I$ $a = 0.766826$ $b = -3.52181 + 2.21774I$	$2.40108$	$1.48110$
$u = 1.000000I$ $a = 0.455697 + 1.200150I$ $b = -0.0768928 + 0.0902877I$	$5.87256 - 4.40083I$	$4.74431 + 3.49859I$
$u = 1.000000I$ $a = 0.455697 - 1.200150I$ $b = 0.361438 - 0.927855I$	$5.87256 + 4.40083I$	$4.74431 - 3.49859I$
$u = -1.000000I$ $a = -0.339110 + 0.822375I$ $b = -0.331455 - 0.820551I$	$0.32910 + 1.53058I$	$0.51511 - 4.43065I$
$u = -1.000000I$ $a = -0.339110 - 0.822375I$ $b = -1.43128 - 1.79928I$	$0.32910 - 1.53058I$	$0.51511 + 4.43065I$
$u = -1.000000I$ $a = 0.766826$ $b = -3.52181 - 2.21774I$	$2.40108$	$1.48110$
$u = -1.000000I$ $a = 0.455697 + 1.200150I$ $b = 0.361438 + 0.927855I$	$5.87256 - 4.40083I$	$4.74431 + 3.49859I$
$u = -1.000000I$ $a = 0.455697 - 1.200150I$ $b = -0.0768928 - 0.0902877I$	$5.87256 + 4.40083I$	$4.74431 - 3.49859I$

$$\text{IV. } I_4^u = \langle -3u^3 + 6u^2 + 4b - 5u + 1, u^3 + 2a - u + 3, u^4 - u^3 + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u - \frac{3}{2} \\ \frac{3}{4}u^3 - \frac{3}{2}u^2 + \frac{5}{4}u - \frac{1}{4} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u - \frac{3}{2} \\ \frac{5}{4}u^3 - \frac{5}{2}u^2 + \frac{7}{4}u + \frac{1}{4} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u^3 - u^2 - 1 \\ u^3 - u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}u^3 + u^2 + \frac{1}{2}u - \frac{1}{2} \\ \frac{5}{4}u^3 - \frac{3}{2}u^2 + \frac{7}{4}u + \frac{1}{4} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = \frac{71}{16}u^3 + \frac{7}{8}u^2 + \frac{241}{16}u + \frac{147}{16}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_2$	$u^4 - u^3 + u^2 + 1$
$c_4$	$u^4 - u^3 + 5u^2 + u + 2$
$c_5$	$u^4 + u^3 + u^2 + 1$
$c_6$	$u^4 + 5u^3 + 7u^2 + 2u + 1$
$c_7$	$u^4 + u^3 + 3u^2 + 2u + 1$
$c_8$	$(u + 1)^4$
$c_9, c_{10}$	$2(2u^4 - u^3 + 5u^2 + u + 1)$
$c_{11}$	$(u - 1)^4$
$c_{12}$	$u^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_7$	$y^4 + 5y^3 + 7y^2 + 2y + 1$
$c_2, c_5$	$y^4 + y^3 + 3y^2 + 2y + 1$
$c_4$	$y^4 + 9y^3 + 31y^2 + 19y + 4$
$c_6$	$y^4 - 11y^3 + 31y^2 + 10y + 1$
$c_8, c_{11}$	$(y - 1)^4$
$c_9, c_{10}$	$4(4y^4 + 19y^3 + 31y^2 + 9y + 1)$
$c_{12}$	$y^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.351808 + 0.720342I$ $a = -1.92796 + 0.41333I$ $b = 0.28101 + 1.58096I$	$1.43393 - 1.41510I$	$5.77964 + 9.93490I$
$u = -0.351808 - 0.720342I$ $a = -1.92796 - 0.41333I$ $b = 0.28101 - 1.58096I$	$1.43393 + 1.41510I$	$5.77964 - 9.93490I$
$u = 0.851808 + 0.911292I$ $a = -0.322042 - 0.157780I$ $b = -0.156006 - 0.269484I$	$8.43568 + 3.16396I$	$15.2516 + 20.5289I$
$u = 0.851808 - 0.911292I$ $a = -0.322042 + 0.157780I$ $b = -0.156006 + 0.269484I$	$8.43568 - 3.16396I$	$15.2516 - 20.5289I$

### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^{10})(u^4 - u^3 + 3u^2 - 2u + 1)(u^{18} + 12u^{17} + \dots + 3u + 1) \cdot (u^{54} + 60u^{53} + \dots + 17614u + 289)$
$c_2$	$((u^2 + 1)^5)(u^4 - u^3 + u^2 + 1)(u^{18} + 6u^{16} + \dots - 3u + 1) \cdot (u^{54} + 2u^{53} + \dots + 112u + 17)$
$c_3$	$((u^2 + 1)^5)(u^4 - u^3 + 3u^2 - 2u + 1)(u^{18} + 6u^{16} + \dots - 3u + 1) \cdot (u^{54} + 2u^{53} + \dots + 20u + 17)$
$c_4$	$(u^4 - u^3 + 5u^2 + u + 2)(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^3 \cdot (u^{10} + u^8 + 8u^6 + 3u^4 + 3u^2 + 1)(u^{54} - 7u^{53} + \dots - 8u + 4)$
$c_5$	$((u^2 + 1)^5)(u^4 + u^3 + u^2 + 1)(u^{18} + 6u^{16} + \dots - 3u + 1) \cdot (u^{54} + 2u^{53} + \dots + 112u + 17)$
$c_6$	$((u+1)^{10})(u^4 + 5u^3 + \dots + 2u + 1)(u^{18} - 12u^{17} + \dots - 3u + 1) \cdot (u^{54} - 20u^{53} + \dots - 15886u + 289)$
$c_7$	$((u^2 + 1)^5)(u^4 + u^3 + 3u^2 + 2u + 1)(u^{18} + 6u^{16} + \dots - 3u + 1) \cdot (u^{54} + 2u^{53} + \dots + 20u + 17)$
$c_8$	$(u+1)^4(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3 \cdot (u^{54} + 4u^{53} + \dots + 481u + 16)$
$c_9$	$4(2u^4 - u^3 + 5u^2 + u + 1)(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^3 \cdot (u^{10} - 3u^8 + 4u^6 - u^4 - u^2 + 1)(2u^{54} + 11u^{53} + \dots + 27633u + 3982)$
$c_{10}$	$4(2u^4 - u^3 + 5u^2 + u + 1)(u^6 - u^5 - u^4 + 2u^3 - u + 1)^3 \cdot (u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1)(2u^{54} + 3u^{53} + \dots - 26787u + 17894)$
$c_{11}$	$(u-1)^4(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3 \cdot (u^{54} + 4u^{53} + \dots + 481u + 16)$
$c_{12}$	$u^4(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)^3 \cdot (u^{54} - 8u^{53} + \dots - 2976u + 256)$



## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^{10})(y^4 + 5y^3 + \dots + 2y + 1)(y^{18} - 12y^{17} + \dots + 95y + 1)$ $\cdot (y^{54} - 120y^{53} + \dots - 34842354y + 83521)$
$c_2, c_5$	$((y+1)^{10})(y^4 + y^3 + 3y^2 + 2y + 1)(y^{18} + 12y^{17} + \dots + 3y + 1)$ $\cdot (y^{54} + 60y^{53} + \dots + 17614y + 289)$
$c_3, c_7$	$((y+1)^{10})(y^4 + 5y^3 + \dots + 2y + 1)(y^{18} + 12y^{17} + \dots + 3y + 1)$ $\cdot (y^{54} + 20y^{53} + \dots + 15886y + 289)$
$c_4$	$(y^4 + 9y^3 + 31y^2 + 19y + 4)(y^5 + y^4 + 8y^3 + 3y^2 + 3y + 1)^2$ $\cdot ((y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^3)(y^{54} + 17y^{53} + \dots + 152y + 16)$
$c_6$	$((y-1)^{10})(y^4 - 11y^3 + \dots + 10y + 1)(y^{18} - 12y^{17} + \dots + 95y + 1)$ $\cdot (y^{54} + 40y^{53} + \dots - 35600546y + 83521)$
$c_8, c_{11}$	$(y-1)^4(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ $\cdot (y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^3$ $\cdot (y^{54} - 32y^{53} + \dots - 95457y + 256)$
$c_9$	$16(4y^4 + 19y^3 + 31y^2 + 9y + 1)(y^5 - 3y^4 + 4y^3 - y^2 - y + 1)^2$ $\cdot (y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^3$ $\cdot (4y^{54} - 173y^{53} + \dots + 170212239y + 15856324)$
$c_{10}$	$16(4y^4 + 19y^3 + 31y^2 + 9y + 1)(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$ $\cdot (y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^3$ $\cdot (4y^{54} - 205y^{53} + \dots + 5530254095y + 320195236)$
$c_{12}$	$y^4(y^5 + 3y^4 + \dots - y - 1)^2(y^6 - 3y^5 + \dots - y + 1)^3$ $\cdot (y^{54} - 12y^{53} + \dots - 1545216y + 65536)$