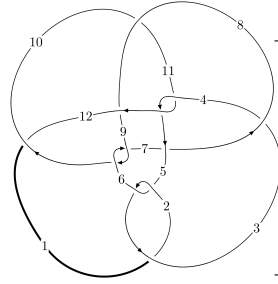
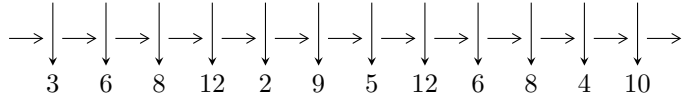


12n<sub>0426</sub> (K12n<sub>0426</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$8,12 \xrightarrow{c_8} 5,9 \xrightarrow{c_4} 4 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \xrightarrow{c_{11}} 11 \xrightarrow{c_{10}} 10 \xrightarrow{c_{12}} 1 \rightsquigarrow c_1, c_5, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^6 + 2u^5 - u^4 - u^3 - u^2 + 3b + u - 1, 5u^6 - 16u^5 + 11u^4 + 20u^3 - 19u^2 + 6a - 14u + 14, u^7 - 4u^6 + 5u^5 + 2u^4 - 7u^3 + 6u - 2 \rangle$$

$$I_2^u = \langle -u^5 - 2u^4 + u^3 + 3u^2 + b + u - 1, 3u^5 + 4u^4 - 10u^3 - 11u^2 + 2a + 5u + 12, u^6 + 2u^5 - 2u^4 - 5u^3 - u^2 + 4u + 2 \rangle$$

$$I_3^u = \langle b + u, a + u, u^2 + u - 1 \rangle$$

$$I_4^u = \langle b - a - u - 1, a^2 + au + 2a + 2u + 1, u^2 + u - 1 \rangle$$

$$I_5^u = \langle u^3 - 2u^2 + b + 2u - 1, -u^3 + 2u^2 + a - 3u + 2, u^4 - 2u^3 + 4u^2 - 3u + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 23 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^6 + 2u^5 - u^4 - u^3 - u^2 + 3b + u - 1, 5u^6 - 16u^5 + \dots + 6a + 14, u^7 - 4u^6 + 5u^5 + 2u^4 - 7u^3 + 6u - 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -\frac{5}{6}u^6 + \frac{8}{3}u^5 + \dots + \frac{7}{3}u - \frac{7}{3} \\ \frac{1}{3}u^6 - \frac{2}{3}u^5 + \dots - \frac{1}{3}u + \frac{1}{3} \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{5}{6}u^6 + \frac{8}{3}u^5 + \dots + \frac{7}{3}u - \frac{7}{3} \\ \frac{2}{3}u^6 - \frac{7}{3}u^5 + \dots - \frac{8}{3}u + \frac{5}{3} \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{1}{6}u^6 + \frac{1}{3}u^5 + \dots - \frac{1}{3}u - \frac{2}{3} \\ \frac{2}{3}u^6 - \frac{7}{3}u^5 + \dots - \frac{8}{3}u + \frac{5}{3} \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{6}u^6 - \frac{1}{3}u^5 + \dots - \frac{2}{3}u + \frac{5}{3} \\ \frac{1}{3}u^6 - \frac{2}{3}u^5 + \dots - \frac{4}{3}u + \frac{1}{3} \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{1}{6}u^6 + \frac{1}{3}u^5 + \dots - \frac{1}{3}u + \frac{4}{3} \\ -u^6 + 3u^5 - 2u^4 - 3u^3 + 2u^2 + 2u - 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{2}u^6 + u^5 + \frac{1}{2}u^4 - 3u^3 + \frac{1}{2}u^2 + 2u - 1 \\ -\frac{1}{3}u^6 + \frac{2}{3}u^5 + \dots + \frac{7}{3}u - \frac{1}{3} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -\frac{1}{6}u^6 + \frac{1}{3}u^5 + \dots + \frac{2}{3}u + \frac{1}{3} \\ \frac{1}{3}u^6 - \frac{2}{3}u^5 + \dots - \frac{1}{3}u + \frac{1}{3} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{6}u^6 - \frac{1}{3}u^5 + \dots + \frac{1}{3}u + \frac{2}{3} \\ \frac{1}{3}u^6 - \frac{2}{3}u^5 + \dots - \frac{1}{3}u + \frac{1}{3} \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{1}{6}u^6 - \frac{1}{3}u^5 + \dots + \frac{1}{3}u - \frac{1}{3} \\ u^5 - u^4 - 2u^3 + 2u^2 + 3u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 2u^6 - 6u^5 + 4u^4 + 6u^3 - 10u - 10$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^7 + 6u^6 + 27u^5 + 62u^4 + 93u^3 + 76u^2 + 36u + 4$
$c_2, c_5, c_8$	$u^7 + 4u^6 + 5u^5 - 2u^4 - 7u^3 + 6u + 2$
$c_3, c_4, c_{11}$	$u^7 + 3u^6 - 2u^5 - 8u^4 + 2u^3 + 4u^2 + 3u + 1$
$c_6, c_7, c_9$ $c_{12}$	$u^7 - u^6 + 6u^5 + 6u^4 + 12u^3 + 8u^2 + 5u + 1$
$c_{10}$	$u^7 - 9u^6 + 29u^5 - 47u^4 + 60u^3 - 40u^2 + 12u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^7 + 18y^6 + 171y^5 + 338y^4 + 1121y^3 + 424y^2 + 688y - 16$
$c_2, c_5, c_8$	$y^7 - 6y^6 + 27y^5 - 62y^4 + 93y^3 - 76y^2 + 36y - 4$
$c_3, c_4, c_{11}$	$y^7 - 13y^6 + 56y^5 - 90y^4 + 50y^3 + 12y^2 + y - 1$
$c_6, c_7, c_9$ $c_{12}$	$y^7 + 11y^6 + 72y^5 + 134y^4 + 110y^3 + 44y^2 + 9y - 1$
$c_{10}$	$y^7 - 23y^6 + 115y^5 + 575y^4 + 608y^3 + 216y^2 + 464y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877051 + 0.401438I$ $a = 0.390423 - 0.367676I$ $b = 0.173321 - 0.977693I$	$1.59409 + 3.78166I$	$-7.32325 - 7.33619I$
$u = -0.877051 - 0.401438I$ $a = 0.390423 + 0.367676I$ $b = 0.173321 + 0.977693I$	$1.59409 - 3.78166I$	$-7.32325 + 7.33619I$
$u = 1.140270 + 0.557068I$ $a = 0.742429 - 0.652700I$ $b = 0.353960 + 0.627763I$	$-2.78671 - 4.23450I$	$-16.3139 + 4.7703I$
$u = 1.140270 - 0.557068I$ $a = 0.742429 + 0.652700I$ $b = 0.353960 - 0.627763I$	$-2.78671 + 4.23450I$	$-16.3139 - 4.7703I$
$u = 0.389062$ $a = -1.16362$ $b = 0.276584$	$-0.727542$	$-13.4920$
$u = 1.54225 + 1.02576I$ $a = -1.051040 + 0.651247I$ $b = -1.16557 - 2.38792I$	$4.02380 - 9.18258I$	$-12.61674 + 3.92434I$
$u = 1.54225 - 1.02576I$ $a = -1.051040 - 0.651247I$ $b = -1.16557 + 2.38792I$	$4.02380 + 9.18258I$	$-12.61674 - 3.92434I$

$$\text{II. } I_2^u = \langle -u^5 - 2u^4 + u^3 + 3u^2 + b + u - 1, 3u^5 + 4u^4 - 10u^3 - 11u^2 + 2a + 5u + 12, u^6 + 2u^5 - 2u^4 - 5u^3 - u^2 + 4u + 2 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{3}{2}u^5 - 2u^4 + 5u^3 + \frac{11}{2}u^2 - \frac{5}{2}u - 6 \\ u^5 + 2u^4 - u^3 - 3u^2 - u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{3}{2}u^5 - 2u^4 + 5u^3 + \frac{11}{2}u^2 - \frac{5}{2}u - 6 \\ u^5 + 2u^4 - 2u^3 - 4u^2 + 3 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{2}u^5 + 3u^3 + \frac{3}{2}u^2 - \frac{5}{2}u - 3 \\ u^5 + 2u^4 - 2u^3 - 4u^2 + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{3}{2}u^5 + 2u^4 - 4u^3 - \frac{9}{2}u^2 + \frac{3}{2}u + 6 \\ u^3 + u^2 - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^5 + u^4 - u^3 - \frac{5}{2}u^2 + \frac{1}{2}u + 3 \\ -u^5 - u^4 + 4u^3 + 3u^2 - 2u - 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{3}{2}u^5 + 2u^4 - 4u^3 - \frac{7}{2}u^2 + \frac{3}{2}u + 4 \\ u^2 + u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{7}{2}u^5 - 5u^4 + 10u^3 + \frac{23}{2}u^2 - \frac{7}{2}u - 12 \\ 2u^5 + 3u^4 - 6u^3 - 7u^2 + 3u + 7 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{3}{2}u^5 - 2u^4 + 4u^3 + \frac{9}{2}u^2 - \frac{1}{2}u - 5 \\ 2u^5 + 3u^4 - 6u^3 - 7u^2 + 3u + 7 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{9}{2}u^5 + 6u^4 - 13u^3 - \frac{27}{2}u^2 + \frac{9}{2}u + 14 \\ -4u^5 - 6u^4 + 11u^3 + 15u^2 - 3u - 15 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^4 - 2u^3 + u^2 + 2u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^6 - 8u^5 + 22u^4 - 33u^3 + 33u^2 - 20u + 4$
$c_2, c_8$	$u^6 + 2u^5 - 2u^4 - 5u^3 - u^2 + 4u + 2$
$c_3, c_{11}$	$(u^3 + 2u^2 + 1)^2$
$c_4$	$(u^3 - 2u^2 - 1)^2$
$c_5$	$u^6 - 2u^5 - 2u^4 + 5u^3 - u^2 - 4u + 2$
$c_6$	$u^6 - 3u^5 + 3u^4 - 3u^3 - 3u^2 + 4u - 1$
$c_7, c_9, c_{12}$	$u^6 + 3u^5 + 3u^4 + 3u^3 - 3u^2 - 4u - 1$
$c_{10}$	$u^6 + 6u^5 + 3u^4 - 21u^3 - 5u^2 + 25u + 13$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^6 - 20y^5 + 22y^4 + 51y^3 - 55y^2 - 136y + 16$
$c_2, c_5, c_8$	$y^6 - 8y^5 + 22y^4 - 33y^3 + 33y^2 - 20y + 4$
$c_3, c_4, c_{11}$	$(y^3 - 4y^2 - 4y - 1)^2$
$c_6, c_7, c_9$ $c_{12}$	$y^6 - 3y^5 - 15y^4 - 5y^3 + 27y^2 - 10y + 1$
$c_{10}$	$y^6 - 30y^5 + 251y^4 - 745y^3 + 1153y^2 - 755y + 169$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.853859 + 0.662904I$ $a = 0.452623 - 0.427953I$ $b = -0.456155 + 0.029114I$	$1.03690 + 2.56897I$	$-11.22670 - 1.46771I$
$u = -0.853859 - 0.662904I$ $a = 0.452623 + 0.427953I$ $b = -0.456155 - 0.029114I$	$1.03690 - 2.56897I$	$-11.22670 + 1.46771I$
$u = 1.183340 + 0.139351I$ $a = -0.020355 + 0.564750I$ $b = -0.31715 + 1.43860I$	$1.03690 + 2.56897I$	$-11.22670 - 1.46771I$
$u = 1.183340 - 0.139351I$ $a = -0.020355 - 0.564750I$ $b = -0.31715 - 1.43860I$	$1.03690 - 2.56897I$	$-11.22670 + 1.46771I$
$u = -0.579846$ $a = -3.80372$ $b = 0.926680$	$-13.5883$	$-10.5470$
$u = -2.07912$ $a = -1.06082$ $b = -2.38008$	$-13.5883$	$-10.5470$

$$\text{III. } \Gamma_3^u = \langle b + u, a + u, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u - 1 \\ -2u + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -2u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -3u + 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -20

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_{11}$	$u^2 - 3u + 1$
$c_2, c_6, c_8$	$u^2 + u - 1$
$c_4$	$u^2 + 3u + 1$
$c_5, c_7, c_9$ $c_{12}$	$u^2 - u - 1$
$c_{10}$	$u^2 + 6u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_{11}$	$y^2 - 7y + 1$
$c_2, c_5, c_6$ $c_7, c_8, c_9$ $c_{12}$	$y^2 - 3y + 1$
$c_{10}$	$y^2 - 28y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -0.618034$ $b = -0.618034$	-1.97392	-20.0000
$u = -1.61803$ $a = 1.61803$ $b = 1.61803$	-17.7653	-20.0000

$$\text{IV. } I_4^u = \langle b - a - u - 1, a^2 + au + 2a + 2u + 1, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ a + u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ au + u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} au + a + u + 1 \\ au + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a + 2u + 2 \\ -au + u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u + 1 \\ -a - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} au + a + u + 2 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -au - a + u - 2 \\ -2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -au - a - u - 1 \\ -2u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a + 2 \\ -2au + a - u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -14

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + 3u + 1)^2$
$c_2, c_5, c_8$	$(u^2 - u - 1)^2$
$c_3, c_4, c_{11}$	$u^4 + u^3 - 6u^2 - 10u - 5$
$c_6, c_7, c_9$ $c_{12}$	$u^4 - u^3 - 2u^2 - 2u - 1$
$c_{10}$	$(u^2 + 4u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 - 7y + 1)^2$
$c_2, c_5, c_8$	$(y^2 - 3y + 1)^2$
$c_3, c_4, c_{11}$	$y^4 - 13y^3 + 46y^2 - 40y + 25$
$c_6, c_7, c_9$ $c_{12}$	$y^4 - 5y^3 - 2y^2 + 1$
$c_{10}$	$(y^2 - 18y + 1)^2$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -1.30902 + 0.72287I$ $b = 0.309017 + 0.722871I$	-0.328987	-14.0000
$u = 0.618034$ $a = -1.30902 - 0.72287I$ $b = 0.309017 - 0.722871I$	-0.328987	-14.0000
$u = -1.61803$ $a = 1.31651$ $b = 0.698478$	-16.1204	-14.0000
$u = -1.61803$ $a = -1.69848$ $b = -2.31651$	-16.1204	-14.0000

$$I_5^u = \langle u^3 - 2u^2 + b + 2u - 1, -u^3 + 2u^2 + a - 3u + 2, u^4 - 2u^3 + 4u^2 - 3u + 1 \rangle$$

V.

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u^2 + 3u - 2 \\ -u^3 + 2u^2 - 2u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - 2u^2 + 3u - 2 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - u^2 + 2u - 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 - 2u + 2 \\ -u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u^2 - 3u + 2 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 - u + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 - u^2 \\ u^3 + u^2 - u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-u^2 + u - 13$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^4 - 4u^3 + 6u^2 + u + 1$
$c_2, c_5, c_8$	$u^4 + 2u^3 + 4u^2 + 3u + 1$
$c_3, c_4, c_{11}$	$(u^2 - u - 1)^2$
$c_6, c_7, c_9$ $c_{12}$	$u^4 - u^3 + 6u^2 + 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^4 - 4y^3 + 46y^2 + 11y + 1$
$c_2, c_5, c_8$	$y^4 + 4y^3 + 6y^2 - y + 1$
$c_3, c_4, c_{11}$	$(y^2 - 3y + 1)^2$
$c_6, c_7, c_9$ $c_{12}$	$y^4 + 11y^3 + 46y^2 - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.363271I$	-0.657974	$-12.61803 + 0.I$
$a = -0.809017 + 0.587785I$		
$b = 0.309017 - 0.224514I$		
$u = 0.500000 - 0.363271I$	-0.657974	$-12.61803 + 0.I$
$a = -0.809017 - 0.587785I$		
$b = 0.309017 + 0.224514I$		
$u = 0.500000 + 1.53884I$	7.23771	$-10.38197 + 0.I$
$a = 0.309017 - 0.951057I$		
$b = -0.80902 + 2.48990I$		
$u = 0.500000 - 1.53884I$	7.23771	$-10.38197 + 0.I$
$a = 0.309017 + 0.951057I$		
$b = -0.80902 - 2.48990I$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - 3u + 1)(u^2 + 3u + 1)^2(u^4 - 4u^3 + 6u^2 + u + 1)$ $\cdot (u^6 - 8u^5 + 22u^4 - 33u^3 + 33u^2 - 20u + 4)$ $\cdot (u^7 + 6u^6 + 27u^5 + 62u^4 + 93u^3 + 76u^2 + 36u + 4)$
$c_2, c_8$	$(u^2 - u - 1)^2(u^2 + u - 1)(u^4 + 2u^3 + 4u^2 + 3u + 1)$ $\cdot (u^6 + 2u^5 - 2u^4 - 5u^3 - u^2 + 4u + 2)$ $\cdot (u^7 + 4u^6 + 5u^5 - 2u^4 - 7u^3 + 6u + 2)$
$c_3, c_{11}$	$(u^2 - 3u + 1)(u^2 - u - 1)^2(u^3 + 2u^2 + 1)^2(u^4 + u^3 + \dots - 10u - 5)$ $\cdot (u^7 + 3u^6 - 2u^5 - 8u^4 + 2u^3 + 4u^2 + 3u + 1)$
$c_4$	$((u^2 - u - 1)^2)(u^2 + 3u + 1)(u^3 - 2u^2 - 1)^2(u^4 + u^3 + \dots - 10u - 5)$ $\cdot (u^7 + 3u^6 - 2u^5 - 8u^4 + 2u^3 + 4u^2 + 3u + 1)$
$c_5$	$(u^2 - u - 1)^3(u^4 + 2u^3 + 4u^2 + 3u + 1)$ $\cdot (u^6 - 2u^5 - 2u^4 + 5u^3 - u^2 - 4u + 2)$ $\cdot (u^7 + 4u^6 + 5u^5 - 2u^4 - 7u^3 + 6u + 2)$
$c_6$	$(u^2 + u - 1)(u^4 - u^3 - 2u^2 - 2u - 1)(u^4 - u^3 + 6u^2 + 4u + 1)$ $\cdot (u^6 - 3u^5 + 3u^4 - 3u^3 - 3u^2 + 4u - 1)$ $\cdot (u^7 - u^6 + 6u^5 + 6u^4 + 12u^3 + 8u^2 + 5u + 1)$
$c_7, c_9, c_{12}$	$(u^2 - u - 1)(u^4 - u^3 - 2u^2 - 2u - 1)(u^4 - u^3 + 6u^2 + 4u + 1)$ $\cdot (u^6 + 3u^5 + 3u^4 + 3u^3 - 3u^2 - 4u - 1)$ $\cdot (u^7 - u^6 + 6u^5 + 6u^4 + 12u^3 + 8u^2 + 5u + 1)$
$c_{10}$	$(u^2 + 4u - 1)^2(u^2 + 6u + 4)(u^4 - 4u^3 + 6u^2 + u + 1)$ $\cdot (u^6 + 6u^5 + 3u^4 - 21u^3 - 5u^2 + 25u + 13)$ $\cdot (u^7 - 9u^6 + 29u^5 - 47u^4 + 60u^3 - 40u^2 + 12u + 4)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 - 7y + 1)^3(y^4 - 4y^3 + 46y^2 + 11y + 1)$ $\cdot (y^6 - 20y^5 + 22y^4 + 51y^3 - 55y^2 - 136y + 16)$ $\cdot (y^7 + 18y^6 + 171y^5 + 338y^4 + 1121y^3 + 424y^2 + 688y - 16)$
$c_2, c_5, c_8$	$(y^2 - 3y + 1)^3(y^4 + 4y^3 + 6y^2 - y + 1)$ $\cdot (y^6 - 8y^5 + 22y^4 - 33y^3 + 33y^2 - 20y + 4)$ $\cdot (y^7 - 6y^6 + 27y^5 - 62y^4 + 93y^3 - 76y^2 + 36y - 4)$
$c_3, c_4, c_{11}$	$(y^2 - 7y + 1)(y^2 - 3y + 1)^2(y^3 - 4y^2 - 4y - 1)^2$ $\cdot (y^4 - 13y^3 + 46y^2 - 40y + 25)$ $\cdot (y^7 - 13y^6 + 56y^5 - 90y^4 + 50y^3 + 12y^2 + y - 1)$
$c_6, c_7, c_9$ $c_{12}$	$(y^2 - 3y + 1)(y^4 - 5y^3 - 2y^2 + 1)(y^4 + 11y^3 + 46y^2 - 4y + 1)$ $\cdot (y^6 - 3y^5 - 15y^4 - 5y^3 + 27y^2 - 10y + 1)$ $\cdot (y^7 + 11y^6 + 72y^5 + 134y^4 + 110y^3 + 44y^2 + 9y - 1)$
$c_{10}$	$(y^2 - 28y + 16)(y^2 - 18y + 1)^2(y^4 - 4y^3 + 46y^2 + 11y + 1)$ $\cdot (y^6 - 30y^5 + 251y^4 - 745y^3 + 1153y^2 - 755y + 169)$ $\cdot (y^7 - 23y^6 + 115y^5 + 575y^4 + 608y^3 + 216y^2 + 464y - 16)$