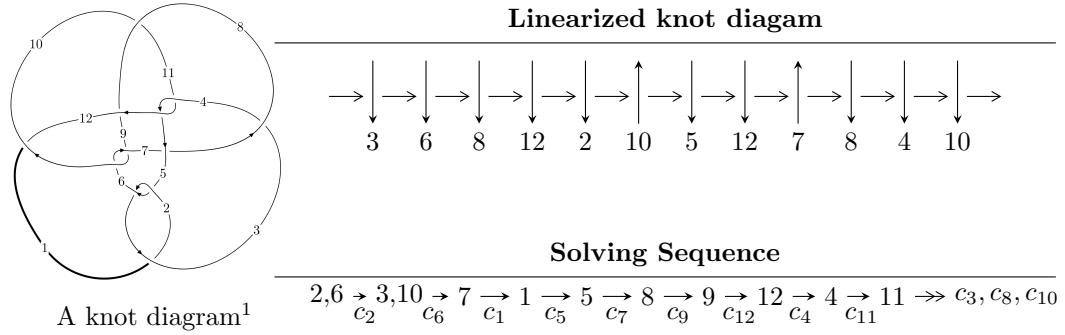


$12n_{0428}$ ($K12n_{0428}$)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 3309761832986841u^{28} - 484169443496906u^{27} + \dots + 2728407209023967b + 10346261032522342, \\ 6.12347 \times 10^{15}u^{28} - 3.65447 \times 10^{15}u^{27} + \dots + 2.72841 \times 10^{15}a + 3.93244 \times 10^{16}, u^{29} - u^{28} + \dots + 11u - 1 \rangle$$

$$I_2^u = \langle 13u^{13} + 7u^{12} + \dots + b - 29, 224u^{13} + 105u^{12} + \dots + a - 480, \\ u^{14} - 5u^{12} + u^{11} + 11u^{10} - 4u^9 - 13u^8 + 7u^7 + 8u^6 - 10u^5 - u^4 + 10u^3 - 2u^2 - 3u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 43 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 3.31 \times 10^{15} u^{28} - 4.84 \times 10^{14} u^{27} + \dots + 2.73 \times 10^{15} b + 1.03 \times 10^{16}, 6.12 \times 10^{15} u^{28} - 3.65 \times 10^{15} u^{27} + \dots + 2.73 \times 10^{15} a + 3.93 \times 10^{16}, u^{29} - u^{28} + \dots + 11u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2.24434u^{28} + 1.33942u^{27} + \dots + 45.0118u - 14.4130 \\ -1.21307u^{28} + 0.177455u^{27} + \dots + 17.9088u - 3.79205 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3.72446u^{28} - 1.92791u^{27} + \dots - 66.8278u + 18.8763 \\ 1.69382u^{28} - 0.176481u^{27} + \dots - 18.8053u + 4.46366 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 3.69627u^{28} - 1.96435u^{27} + \dots - 67.8684u + 19.1555 \\ 1.66563u^{28} - 0.212920u^{27} + \dots - 19.8460u + 4.74286 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -8.80217u^{28} + 2.99230u^{27} + \dots + 150.634u - 40.2378 \\ -5.79123u^{28} - 0.238662u^{27} + \dots + 64.3246u - 11.6085 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -5.43646u^{28} + 2.41208u^{27} + \dots + 107.030u - 28.7016 \\ -2.54933u^{28} - 0.164013u^{27} + \dots + 33.7253u - 7.14216 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2.50984u^{28} - 6.17071u^{27} + \dots - 123.703u + 44.9330 \\ -2.45081u^{28} - 2.07795u^{27} + \dots - 2.61459u + 7.33026 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 11.3793u^{28} - 5.86912u^{27} + \dots - 218.129u + 62.4454 \\ 6.01027u^{28} - 0.499882u^{27} + \dots - 76.2473u + 16.4335 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{29606274479465}{94083007207723}u^{28} - \frac{112181565603524}{94083007207723}u^{27} + \dots - \frac{79763733552791}{94083007207723}u - \frac{508359165202078}{94083007207723}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{29} + 23u^{28} + \cdots + 57u + 1$
c_2, c_5	$u^{29} + u^{28} + \cdots + 11u + 1$
c_3	$u^{29} + 2u^{28} + \cdots - 512u - 181$
c_4, c_{11}	$u^{29} + 3u^{28} + \cdots + 52u + 17$
c_6, c_9	$u^{29} + 6u^{28} + \cdots - 3u - 1$
c_7	$u^{29} - 3u^{28} + \cdots - 343u - 73$
c_8	$u^{29} + 3u^{28} + \cdots - 802u - 61$
c_{10}	$u^{29} - 2u^{28} + \cdots + 306u + 17$
c_{12}	$u^{29} - 13u^{28} + \cdots - 419u - 617$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{29} - 27y^{28} + \cdots + 3781y - 1$
c_2, c_5	$y^{29} - 23y^{28} + \cdots + 57y - 1$
c_3	$y^{29} - 66y^{28} + \cdots + 773288y - 32761$
c_4, c_{11}	$y^{29} - 47y^{28} + \cdots + 3350y - 289$
c_6, c_9	$y^{29} + 30y^{28} + \cdots + 5y - 1$
c_7	$y^{29} - 9y^{28} + \cdots + 108013y - 5329$
c_8	$y^{29} - 53y^{28} + \cdots + 159352y - 3721$
c_{10}	$y^{29} - 74y^{28} + \cdots + 76942y - 289$
c_{12}	$y^{29} - 79y^{28} + \cdots - 73773123y - 380689$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.847490 + 0.607947I$		
$a = -0.422315 - 0.373511I$	$1.85694 + 2.41024I$	$-0.38198 - 1.83000I$
$b = -0.453967 - 0.141290I$		
$u = -0.847490 - 0.607947I$		
$a = -0.422315 + 0.373511I$	$1.85694 - 2.41024I$	$-0.38198 + 1.83000I$
$b = -0.453967 + 0.141290I$		
$u = 0.071949 + 0.929488I$		
$a = 1.55015 + 0.37840I$	$-5.90516 - 1.34940I$	$-11.77988 + 1.16724I$
$b = -0.033988 + 0.404715I$		
$u = 0.071949 - 0.929488I$		
$a = 1.55015 - 0.37840I$	$-5.90516 + 1.34940I$	$-11.77988 - 1.16724I$
$b = -0.033988 - 0.404715I$		
$u = 1.099740 + 0.372987I$		
$a = 0.429259 - 0.314350I$	$-2.13143 - 3.61670I$	$-10.87499 + 4.53147I$
$b = -0.496131 + 0.172360I$		
$u = 1.099740 - 0.372987I$		
$a = 0.429259 + 0.314350I$	$-2.13143 + 3.61670I$	$-10.87499 - 4.53147I$
$b = -0.496131 - 0.172360I$		
$u = -0.071629 + 1.166630I$		
$a = -1.42014 + 0.38258I$	$-17.8156 + 5.4788I$	$-11.43005 - 2.27554I$
$b = 0.0590394 - 0.0700190I$		
$u = -0.071629 - 1.166630I$		
$a = -1.42014 - 0.38258I$	$-17.8156 - 5.4788I$	$-11.43005 + 2.27554I$
$b = 0.0590394 + 0.0700190I$		
$u = -1.20779$		
$a = 1.06012$	-5.45443	-17.0500
$b = 0.608535$		
$u = -1.241400 + 0.177721I$		
$a = 0.09350 - 1.46108I$	$-4.23135 + 3.90349I$	$-13.5060 - 7.1974I$
$b = -0.13368 - 2.49732I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.241400 - 0.177721I$		
$a = 0.09350 + 1.46108I$	$-4.23135 - 3.90349I$	$-13.5060 + 7.1974I$
$b = -0.13368 + 2.49732I$		
$u = 0.607700 + 0.416192I$		
$a = 0.030334 + 0.170685I$	$-0.645013 + 0.114015I$	$-8.30235 - 0.44217I$
$b = 0.768475 - 0.109674I$		
$u = 0.607700 - 0.416192I$		
$a = 0.030334 - 0.170685I$	$-0.645013 - 0.114015I$	$-8.30235 + 0.44217I$
$b = 0.768475 + 0.109674I$		
$u = 1.264620 + 0.097173I$		
$a = 0.126127 + 0.975567I$	$-4.42915 + 0.22712I$	$-13.77800 + 0.54237I$
$b = 0.45216 + 2.48013I$		
$u = 1.264620 - 0.097173I$		
$a = 0.126127 - 0.975567I$	$-4.42915 - 0.22712I$	$-13.77800 - 0.54237I$
$b = 0.45216 - 2.48013I$		
$u = 1.27084$		
$a = -2.54450$	-14.6938	-21.3900
$b = -2.41619$		
$u = -1.35314$		
$a = -0.122473$	-15.8953	-17.3790
$b = 1.92297$		
$u = 1.288070 + 0.432233I$		
$a = -0.52667 - 1.40404I$	$-9.72617 - 3.55628I$	$-15.1648 + 2.5004I$
$b = -0.52972 - 2.41614I$		
$u = 1.288070 - 0.432233I$		
$a = -0.52667 + 1.40404I$	$-9.72617 + 3.55628I$	$-15.1648 - 2.5004I$
$b = -0.52972 + 2.41614I$		
$u = -1.36698 + 0.39083I$		
$a = 0.056520 + 1.082730I$	$-10.50180 + 6.08146I$	$-14.9405 - 3.9753I$
$b = -0.25816 + 2.57538I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.36698 - 0.39083I$		
$a = 0.056520 - 1.082730I$	$-10.50180 - 6.08146I$	$-14.9405 + 3.9753I$
$b = -0.25816 - 2.57538I$		
$u = 0.529556$		
$a = -0.279573$	-0.808015	-11.9270
$b = 0.469661$		
$u = 1.43624 + 0.53316I$		
$a = 0.045983 + 1.342010I$	$16.8944 - 11.5066I$	$-13.6242 + 4.6544I$
$b = -0.02188 + 2.71357I$		
$u = 1.43624 - 0.53316I$		
$a = 0.045983 - 1.342010I$	$16.8944 + 11.5066I$	$-13.6242 - 4.6544I$
$b = -0.02188 - 2.71357I$		
$u = -1.40063 + 0.62143I$		
$a = 0.391966 - 0.973746I$	$17.5554 + 0.8894I$	$-13.74018 - 0.79352I$
$b = 0.84600 - 2.06054I$		
$u = -1.40063 - 0.62143I$		
$a = 0.391966 + 0.973746I$	$17.5554 - 0.8894I$	$-13.74018 + 0.79352I$
$b = 0.84600 + 2.06054I$		
$u = -0.024136 + 0.378698I$		
$a = -2.54654 - 0.61175I$	$-0.56395 - 1.71430I$	$-3.16058 + 4.19709I$
$b = -0.009603 + 0.352025I$		
$u = -0.024136 - 0.378698I$		
$a = -2.54654 + 0.61175I$	$-0.56395 + 1.71430I$	$-3.16058 - 4.19709I$
$b = -0.009603 - 0.352025I$		
$u = 0.128440$		
$a = -9.72992$	-11.0443	-5.88640
$b = -1.96207$		

$$\text{II. } I_2^u = \langle 13u^{13} + 7u^{12} + \cdots + b - 29, 224u^{13} + 105u^{12} + \cdots + a - 480, u^{14} - 5u^{12} + \cdots - 3u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -224u^{13} - 105u^{12} + \cdots - 415u + 480 \\ -13u^{13} - 7u^{12} + \cdots - 29u + 29 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -143u^{13} - 67u^{12} + \cdots - 263u + 304 \\ 67u^{13} + 32u^{12} + \cdots + 129u - 145 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -189u^{13} - 89u^{12} + \cdots - 350u + 403 \\ 21u^{13} + 10u^{12} + \cdots + 42u - 46 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -143u^{13} - 67u^{12} + \cdots - 268u + 306 \\ -8u^{13} - 5u^{12} + \cdots - 25u + 21 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -98u^{13} - 46u^{12} + \cdots - 178u + 210 \\ -22u^{13} - 10u^{12} + \cdots - 35u + 44 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -130u^{13} - 63u^{12} + \cdots - 249u + 284 \\ -2u^{13} - 4u^{12} + \cdots - 20u + 12 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 62u^{13} + 30u^{12} + \cdots + 114u - 133 \\ -13u^{13} - 7u^{12} + \cdots - 35u + 31 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

$$(iii) \text{ Cusp Shapes} = 254u^{13} + 120u^{12} - 1214u^{11} - 319u^{10} + 2647u^9 + 232u^8 - 3201u^7 + 272u^6 + 2171u^5 - 1523u^4 - 980u^3 + 2088u^2 + 476u - 559$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{14} - 10u^{13} + \cdots - 13u + 1$
c_2	$u^{14} - 5u^{12} + \cdots - 3u + 1$
c_3	$u^{14} + u^{13} + \cdots + 50u - 25$
c_4	$u^{14} - 2u^{13} + \cdots - 2u - 1$
c_5	$u^{14} - 5u^{12} + \cdots + 3u + 1$
c_6	$u^{14} - u^{13} + \cdots + 7u + 1$
c_7	$u^{14} + 2u^{13} + \cdots + u - 1$
c_8	$u^{14} + 4u^{13} + \cdots + 2u + 1$
c_9	$u^{14} + u^{13} + \cdots - 7u + 1$
c_{10}	$u^{14} + 15u^{13} + \cdots + 1248u + 169$
c_{11}	$u^{14} + 2u^{13} + \cdots + 2u - 1$
c_{12}	$u^{14} + 6u^{13} + \cdots + 215u + 25$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{14} - 6y^{13} + \cdots - 45y + 1$
c_2, c_5	$y^{14} - 10y^{13} + \cdots - 13y + 1$
c_3	$y^{14} - 13y^{13} + \cdots + 4600y + 625$
c_4, c_{11}	$y^{14} - 18y^{13} + \cdots + 2y + 1$
c_6, c_9	$y^{14} + 7y^{13} + \cdots - 17y + 1$
c_7	$y^{14} + 8y^{13} + \cdots + 7y + 1$
c_8	$y^{14} - 16y^{13} + \cdots - 8y + 1$
c_{10}	$y^{14} - 9y^{13} + \cdots - 67938y + 28561$
c_{12}	$y^{14} - 22y^{13} + \cdots - 5325y + 625$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.835923 + 0.681048I$		
$a = -0.125313 - 0.206996I$	$1.26701 + 2.62945I$	$-13.2524 - 5.2108I$
$b = -0.446348 + 0.397563I$		
$u = -0.835923 - 0.681048I$		
$a = -0.125313 + 0.206996I$	$1.26701 - 2.62945I$	$-13.2524 + 5.2108I$
$b = -0.446348 - 0.397563I$		
$u = 0.345551 + 0.838709I$		
$a = -1.020240 - 0.715351I$	$-2.18681 - 1.21939I$	$-11.09554 + 1.93458I$
$b = -0.243705 - 0.098495I$		
$u = 0.345551 - 0.838709I$		
$a = -1.020240 + 0.715351I$	$-2.18681 + 1.21939I$	$-11.09554 - 1.93458I$
$b = -0.243705 + 0.098495I$		
$u = -1.22266$		
$a = 1.67303$	-13.8048	-11.3860
$b = 0.728923$		
$u = 1.244710 + 0.138183I$		
$a = -0.311608 - 0.937054I$	$-4.37404 - 2.52484I$	$-15.1413 + 2.0385I$
$b = 0.34348 - 2.09289I$		
$u = 1.244710 - 0.138183I$		
$a = -0.311608 + 0.937054I$	$-4.37404 + 2.52484I$	$-15.1413 - 2.0385I$
$b = 0.34348 + 2.09289I$		
$u = -0.727304$		
$a = 1.73201$	-11.7805	-17.4240
$b = 2.70193$		
$u = 1.124850 + 0.672854I$		
$a = 0.314703 + 0.747799I$	$-4.34890 - 4.36927I$	$-12.83000 + 4.03520I$
$b = 0.580657 + 1.233750I$		
$u = 1.124850 - 0.672854I$		
$a = 0.314703 - 0.747799I$	$-4.34890 + 4.36927I$	$-12.83000 - 4.03520I$
$b = 0.580657 - 1.233750I$		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.372300 + 0.328498I$		
$a = -0.239034 - 1.275240I$	$-7.44862 + 5.20740I$	$-13.30820 - 4.11576I$
$b = -0.26688 - 2.25518I$		
$u = -1.372300 - 0.328498I$		
$a = -0.239034 + 1.275240I$	$-7.44862 - 5.20740I$	$-13.30820 + 4.11576I$
$b = -0.26688 + 2.25518I$		
$u = 0.468087 + 0.001290I$		
$a = 0.67897 - 1.74706I$	$-1.36973 - 1.50897I$	$-13.46764 + 1.98399I$
$b = -0.682627 - 0.104415I$		
$u = 0.468087 - 0.001290I$		
$a = 0.67897 + 1.74706I$	$-1.36973 + 1.50897I$	$-13.46764 - 1.98399I$
$b = -0.682627 + 0.104415I$		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u^{14} - 10u^{13} + \dots - 13u + 1)(u^{29} + 23u^{28} + \dots + 57u + 1)$
c_2	$(u^{14} - 5u^{12} + \dots - 3u + 1)(u^{29} + u^{28} + \dots + 11u + 1)$
c_3	$(u^{14} + u^{13} + \dots + 50u - 25)(u^{29} + 2u^{28} + \dots - 512u - 181)$
c_4	$(u^{14} - 2u^{13} + \dots - 2u - 1)(u^{29} + 3u^{28} + \dots + 52u + 17)$
c_5	$(u^{14} - 5u^{12} + \dots + 3u + 1)(u^{29} + u^{28} + \dots + 11u + 1)$
c_6	$(u^{14} - u^{13} + \dots + 7u + 1)(u^{29} + 6u^{28} + \dots - 3u - 1)$
c_7	$(u^{14} + 2u^{13} + \dots + u - 1)(u^{29} - 3u^{28} + \dots - 343u - 73)$
c_8	$(u^{14} + 4u^{13} + \dots + 2u + 1)(u^{29} + 3u^{28} + \dots - 802u - 61)$
c_9	$(u^{14} + u^{13} + \dots - 7u + 1)(u^{29} + 6u^{28} + \dots - 3u - 1)$
c_{10}	$(u^{14} + 15u^{13} + \dots + 1248u + 169)(u^{29} - 2u^{28} + \dots + 306u + 17)$
c_{11}	$(u^{14} + 2u^{13} + \dots + 2u - 1)(u^{29} + 3u^{28} + \dots + 52u + 17)$
c_{12}	$(u^{14} + 6u^{13} + \dots + 215u + 25)(u^{29} - 13u^{28} + \dots - 419u - 617)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y^{14} - 6y^{13} + \dots - 45y + 1)(y^{29} - 27y^{28} + \dots + 3781y - 1)$
c_2, c_5	$(y^{14} - 10y^{13} + \dots - 13y + 1)(y^{29} - 23y^{28} + \dots + 57y - 1)$
c_3	$(y^{14} - 13y^{13} + \dots + 4600y + 625) \cdot (y^{29} - 66y^{28} + \dots + 773288y - 32761)$
c_4, c_{11}	$(y^{14} - 18y^{13} + \dots + 2y + 1)(y^{29} - 47y^{28} + \dots + 3350y - 289)$
c_6, c_9	$(y^{14} + 7y^{13} + \dots - 17y + 1)(y^{29} + 30y^{28} + \dots + 5y - 1)$
c_7	$(y^{14} + 8y^{13} + \dots + 7y + 1)(y^{29} - 9y^{28} + \dots + 108013y - 5329)$
c_8	$(y^{14} - 16y^{13} + \dots - 8y + 1)(y^{29} - 53y^{28} + \dots + 159352y - 3721)$
c_{10}	$(y^{14} - 9y^{13} + \dots - 67938y + 28561) \cdot (y^{29} - 74y^{28} + \dots + 76942y - 289)$
c_{12}	$(y^{14} - 22y^{13} + \dots - 5325y + 625) \cdot (y^{29} - 79y^{28} + \dots - 73773123y - 380689)$