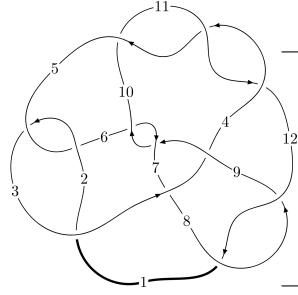
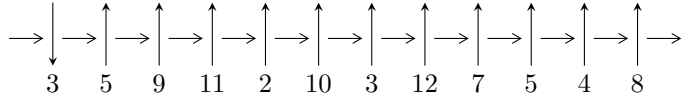


12n₀₄₃₂ (K12n₀₄₃₂)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$4,9 \xrightarrow{c_3} 3,12 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 1 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_4} 5 \xrightarrow{c_2} 2 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 10 \twoheadrightarrow c_1, c_6, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 74u^{12} - 692u^{11} + \dots + 2529b + 2355, 785u^{12} - 3703u^{11} + \dots + 7587a + 387, \\ u^{13} - 5u^{12} + 15u^{11} - 29u^{10} + 44u^9 - 54u^8 + 61u^7 - 62u^6 + 65u^5 - 67u^4 + 72u^3 - 57u^2 + 36u - 9 \rangle$$

$$I_2^u = \langle b + u - 1, u^4 - 4u^3 + 8u^2 + a - 7u + 3, u^5 - 4u^4 + 8u^3 - 7u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle a^3 - a^2u - a^2 + 3au + b + 2u + 3, a^4 - a^3u + 2a^2u - a^2 + 4au + 3a + 2, u^2 + u + 1 \rangle$$

$$I_4^u = \langle -a^3 - a^2u - a^2 + au + b + 2u + 1, a^4 + a^3u - 2a^2u - a^2 - 2au - a + 2u, u^2 + u + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 34 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 74u^{12} - 692u^{11} + \dots + 2529b + 2355, 785u^{12} - 3703u^{11} + \dots + 7587a + 387, u^{13} - 5u^{12} + \dots + 36u - 9 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.103466u^{12} + 0.488072u^{11} + \dots + 2.94108u - 0.0510083 \\ -0.0292606u^{12} + 0.273626u^{11} + \dots + 3.67378u - 0.931198 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0726242u^{12} + 0.196652u^{11} + \dots - 1.94029u + 0.651246 \\ -0.166469u^{12} + 0.622776u^{11} + \dots + 4.26572u - 0.653618 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.168051u^{12} - 0.640569u^{11} + \dots - 3.47331u + 1.42467 \\ 0.0723606u^{12} - 0.397390u^{11} + \dots - 4.74733u + 1.77580 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.115724u^{12} + 0.320417u^{11} + \dots - 0.866746u - 0.193357 \\ -0.148675u^{12} + 1.00593u^{11} + \dots + 7.18031u - 1.47924 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0742059u^{12} + 0.214446u^{11} + \dots - 0.732701u + 0.880190 \\ -0.0292606u^{12} + 0.273626u^{11} + \dots + 3.67378u - 0.931198 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0938447u^{12} - 0.426124u^{11} + \dots - 5.20601u + 2.30486 \\ -0.166469u^{12} + 0.622776u^{11} + \dots + 3.26572u - 0.653618 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.319889u^{12} - 1.34875u^{11} + \dots - 4.40214u + 1.44603 \\ -0.329775u^{12} + 0.876631u^{11} + \dots - 5.21708u + 2.23488 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.628312u^{12} - 2.59628u^{11} + \dots - 11.5492u + 3.46856 \\ -0.758798u^{12} + 2.67537u^{11} + \dots + 5.17556u - 0.747331 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.00237248u^{12} - 0.139976u^{11} + \dots - 2.52195u + 0.843416 \\ 0.199684u^{12} - 0.774219u^{11} + \dots - 4.62515u + 1.51246 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{3325}{2529}u^{12} - \frac{17666}{2529}u^{11} + \frac{17227}{843}u^{10} - \frac{96773}{2529}u^9 + \frac{137357}{2529}u^8 - \frac{17822}{281}u^7 + \frac{173059}{2529}u^6 - \frac{170021}{2529}u^5 + \frac{175199}{2529}u^4 - \frac{187657}{2529}u^3 + \frac{67681}{843}u^2 - \frac{48875}{843}u + \frac{9022}{281}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--|--------------------------------------|
| c_1 | $u^{13} - u^{12} + \dots + 4u - 1$ |
| c_2, c_5, c_6 c_9 | $u^{13} + u^{12} + \dots + 2u - 1$ |
| c_3 | $u^{13} - 5u^{12} + \dots + 36u - 9$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $u^{13} + 8u^{11} + \dots - u - 1$ |
| c_7 | $u^{13} - u^{12} + \dots + 90u - 25$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|--|
| c_1 | $y^{13} + 35y^{12} + \dots + 212y - 1$ |
| c_2, c_5, c_6 c_9 | $y^{13} - y^{12} + \dots + 4y - 1$ |
| c_3 | $y^{13} + 5y^{12} + \dots + 270y - 81$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $y^{13} + 16y^{12} + \dots - 5y - 1$ |
| c_7 | $y^{13} - 7y^{12} + \dots + 3150y - 625$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-------------------------|
| $u = 0.377421 + 0.995561I$ | | |
| $a = 1.42395 + 0.27192I$ | $-13.25130 + 1.59234I$ | $-1.196156 - 0.103558I$ |
| $b = 0.26672 + 1.52025I$ | | |
| $u = 0.377421 - 0.995561I$ | | |
| $a = 1.42395 - 0.27192I$ | $-13.25130 - 1.59234I$ | $-1.196156 + 0.103558I$ |
| $b = 0.26672 - 1.52025I$ | | |
| $u = -0.826366 + 0.684268I$ | | |
| $a = -0.040776 + 0.277567I$ | $-1.74296 - 2.47632I$ | $11.79558 + 3.97407I$ |
| $b = -0.156234 - 0.257273I$ | | |
| $u = -0.826366 - 0.684268I$ | | |
| $a = -0.040776 - 0.277567I$ | $-1.74296 + 2.47632I$ | $11.79558 - 3.97407I$ |
| $b = -0.156234 + 0.257273I$ | | |
| $u = -0.261323 + 1.190470I$ | | |
| $a = -0.753030 + 0.372533I$ | $-5.78672 - 1.79985I$ | $0.24328 + 2.30841I$ |
| $b = -0.246705 - 0.993811I$ | | |
| $u = -0.261323 - 1.190470I$ | | |
| $a = -0.753030 - 0.372533I$ | $-5.78672 + 1.79985I$ | $0.24328 - 2.30841I$ |
| $b = -0.246705 + 0.993811I$ | | |
| $u = 1.197260 + 0.637614I$ | | |
| $a = 0.000701 + 1.040290I$ | $3.92798 - 4.17113I$ | $7.23672 + 2.38066I$ |
| $b = -0.662461 + 1.245930I$ | | |
| $u = 1.197260 - 0.637614I$ | | |
| $a = 0.000701 - 1.040290I$ | $3.92798 + 4.17113I$ | $7.23672 - 2.38066I$ |
| $b = -0.662461 - 1.245930I$ | | |
| $u = 0.80433 + 1.22011I$ | | |
| $a = 1.250130 + 0.103984I$ | $1.94166 + 11.33090I$ | $6.29855 - 5.31818I$ |
| $b = 0.87865 + 1.60894I$ | | |
| $u = 0.80433 - 1.22011I$ | | |
| $a = 1.250130 - 0.103984I$ | $1.94166 - 11.33090I$ | $6.29855 + 5.31818I$ |
| $b = 0.87865 - 1.60894I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = 0.425591$ $a = 0.763681$ $b = 0.325016$ | 0.561978 | 17.8790 |
| $u = 0.99588 + 1.33587I$ $a = -0.762815 - 0.387161I$ $b = -0.24248 - 1.40459I$ | $-8.39874 + 4.39673I$ | $4.68261 + 1.52874I$ |
| $u = 0.99588 - 1.33587I$ $a = -0.762815 + 0.387161I$ $b = -0.24248 + 1.40459I$ | $-8.39874 - 4.39673I$ | $4.68261 - 1.52874I$ |

II.

$$I_2^u = \langle b + u - 1, u^4 - 4u^3 + 8u^2 + a - 7u + 3, u^5 - 4u^4 + 8u^3 - 7u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^4 + 4u^3 - 8u^2 + 7u - 3 \\ -u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - 4u^3 + 8u^2 - 8u + 4 \\ -u^2 + 3u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2u^4 + 8u^3 - 17u^2 + 17u - 8 \\ -u^3 + 4u^2 - 5u + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^4 - 5u^3 + 11u^2 - 12u + 5 \\ -u^4 + 4u^3 - 7u^2 + 5u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^4 + 4u^3 - 8u^2 + 8u - 4 \\ -u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4 - 4u^3 + 9u^2 - 10u + 6 \\ -u^2 + 2u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u^4 + 12u^3 - 25u^2 + 24u - 10 \\ -u^3 + 4u^2 - 4u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 6u^4 - 26u^3 + 56u^2 - 58u + 27 \\ -2u^4 + 8u^3 - 15u^2 + 13u - 4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2u^4 + 9u^3 - 20u^2 + 22u - 11 \\ -u^3 + 3u^2 - 4u + 2 \end{pmatrix}$$

(ii) Obstruction class = 1

$$(iii) \text{ Cusp Shapes} = u^4 - 3u^3 + 4u^2 - 8u + 5$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|-------------------------------------|
| c_1 | $u^5 + 2u^4 - 7u^3 + 8u^2 - 4u + 1$ |
| c_2, c_6 | $u^5 + 2u^4 + u^3 + 2u^2 + 1$ |
| c_3 | $u^5 - 4u^4 + 8u^3 - 7u^2 + 2u + 1$ |
| c_4, c_{12} | $u^5 - u^4 + 2u^3 - 3u^2 + u - 1$ |
| c_5, c_9 | $u^5 - 2u^4 + u^3 - 2u^2 - 1$ |
| c_7 | $u^5 - 2u^3 - 3u^2 - 4u - 3$ |
| c_8, c_{10}, c_{11} | $u^5 + u^4 + 2u^3 + 3u^2 + u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|-------------------------------------|
| c_1 | $y^5 - 18y^4 + 9y^3 - 12y^2 - 1$ |
| c_2, c_5, c_6 c_9 | $y^5 - 2y^4 - 7y^3 - 8y^2 - 4y - 1$ |
| c_3 | $y^5 + 12y^3 - 9y^2 + 18y - 1$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $y^5 + 3y^4 - 7y^2 - 5y - 1$ |
| c_7 | $y^5 - 4y^4 - 4y^3 + 7y^2 - 2y - 9$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = 0.917062 + 0.638199I$ $a = -0.265352 - 0.511254I$ $b = 0.082938 - 0.638199I$ | $-2.41512 + 2.46056I$ | $-0.73583 - 3.45885I$ |
| $u = 0.917062 - 0.638199I$ $a = -0.265352 + 0.511254I$ $b = 0.082938 + 0.638199I$ | $-2.41512 - 2.46056I$ | $-0.73583 + 3.45885I$ |
| $u = -0.238871$ $a = -5.18635$ $b = 1.23887$ | 5.64999 | 7.18340 |
| $u = 1.20237 + 1.38128I$ $a = -0.641472 - 0.411875I$ $b = -0.202374 - 1.381280I$ | $-8.63454 + 4.90423I$ | $-1.85585 - 10.90056I$ |
| $u = 1.20237 - 1.38128I$ $a = -0.641472 + 0.411875I$ $b = -0.202374 + 1.381280I$ | $-8.63454 - 4.90423I$ | $-1.85585 + 10.90056I$ |

$$\text{III. } I_3^u = \langle a^3 - a^2u - a^2 + 3au + b + 2u + 3, a^4 - a^3u + 2a^2u - a^2 + 4au + 3a + 2, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ -a^3 + a^2u + a^2 - 3au - 2u - 3 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a^2u \\ -a^3u - a^2 + 2au + 2a - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -a^3u - a^3 + a \\ a^3u - au - 2a - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^3u - a^2u - 2au - 2a + u \\ -a^3u + a^3 - a^2 + 4au + 2a - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3 - a^2u - a^2 + 3au + a + 2u + 3 \\ -a^3 + a^2u + a^2 - 3au - 2u - 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a^3u + a^2u + 2au + 2a \\ a^3u - a^3 + a^2 - 4au - 2a - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -a^3u - a^3 + 2a + 1 \\ a^3u - 2au - 3a - u - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a^3u - a^3 + a^2u - au + 2a - 2u - 1 \\ 2a^3u + a^3 - a^2u + a^2 - 3au - 6a + 3u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^3u + a^2 - 3au - 3a + 2u - 1 \\ a^3u + a^3 - 2a^2u - a^2 + au - 2a + 2u + 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u + 9$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|--|
| c_1 | $u^8 - 7u^7 + 18u^6 - 20u^5 + 11u^4 - 5u^3 + 3u^2 + 2u + 1$ |
| c_2, c_6 | $u^8 - u^7 + 4u^6 - 2u^5 + 3u^4 - u^3 + u^2 - 2u + 1$ |
| c_3 | $(u^2 + u + 1)^4$ |
| c_4, c_{12} | $u^8 + u^7 + 6u^6 + 6u^5 + 12u^4 + 13u^3 + 11u^2 + 10u + 4$ |
| c_5, c_9 | $u^8 + u^7 + 4u^6 + 2u^5 + 3u^4 + u^3 + u^2 + 2u + 1$ |
| c_7 | $u^8 - 5u^7 + 19u^6 - 45u^5 + 76u^4 - 100u^3 + 99u^2 - 60u + 16$ |
| c_8, c_{10}, c_{11} | $u^8 - u^7 + 6u^6 - 6u^5 + 12u^4 - 13u^3 + 11u^2 - 10u + 4$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|--|
| c_1 | $y^8 - 13y^7 + 66y^6 - 68y^5 + 59y^4 + 157y^3 + 51y^2 + 2y + 1$ |
| c_2, c_5, c_6 c_9 | $y^8 + 7y^7 + 18y^6 + 20y^5 + 11y^4 + 5y^3 + 3y^2 - 2y + 1$ |
| c_3 | $(y^2 + y + 1)^4$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $y^8 + 11y^7 + 48y^6 + 104y^5 + 108y^4 + 23y^3 - 43y^2 - 12y + 16$ |
| c_7 | $y^8 + 13y^7 + 63y^6 + 61y^5 - 30y^4 + 256y^3 + 233y^2 - 432y + 256$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.500000 + 0.866025I$ $a = -1.008180 + 0.726793I$ $b = -0.683684 - 0.164757I$ | $-4.27683 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 + 0.866025I$ $a = -1.271040 + 0.252871I$ $b = -0.10751 + 1.76242I$ | $-12.17250 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 + 0.866025I$ $a = 0.199158 + 0.674466I$ $b = -0.125333 - 1.236500I$ | $-4.27683 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 + 0.866025I$ $a = 1.58005 - 0.78810I$ $b = 0.416526 - 1.227190I$ | $-12.17250 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = -1.008180 - 0.726793I$ $b = -0.683684 + 0.164757I$ | $-4.27683 + 2.02988I$ | $7.00000 - 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = -1.271040 - 0.252871I$ $b = -0.10751 - 1.76242I$ | $-12.17250 + 2.02988I$ | $7.00000 - 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = 0.199158 - 0.674466I$ $b = -0.125333 + 1.236500I$ | $-4.27683 + 2.02988I$ | $7.00000 - 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = 1.58005 + 0.78810I$ $b = 0.416526 + 1.227190I$ | $-12.17250 + 2.02988I$ | $7.00000 - 3.46410I$ |

$$\text{IV. } J_4^u = \langle -a^3 - a^2u - a^2 + au + b + 2u + 1, a^4 + a^3u - 2a^2u - a^2 - 2au - a + 2u, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ a^3 + a^2u + a^2 - au - 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a^2u \\ -a^3u + a^2 - u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -a^3u - a^3 + a \\ -a^3u + 2a^2 - au - 2u - 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^3u - a^2u - 2a^2 + u + 2 \\ -a^3u + a^3 + 2a^2u + 3a^2 - 3u - 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^3 - a^2u - a^2 + au + a + 2u + 1 \\ a^3 + a^2u + a^2 - au - 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a^3u + a^2u + 2a^2 - 2u - 2 \\ a^3u - a^3 - 2a^2u - 3a^2 + 4u + 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^3u - a^3 - 2a^2 + 2u + 3 \\ -a^3u + 2a^3 + 2a^2u + 4a^2 + a - 5u - 4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3a^3u + a^3 + 5a^2u + 8a^2 - au + 2a - 8u - 7 \\ 4a^3u - 5a^3 - 9a^2u - 13a^2 + au - 2a + 15u + 11 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^3u - 2a^3 - 2a^2u - 3a^2 + au + a + 4u + 3 \\ -a^3u + 3a^3 + 4a^2u + 5a^2 - au - 6u - 4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u + 9$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--|--|
| c_1 | $u^8 - 17u^7 + 102u^6 - 212u^5 - 177u^4 + 949u^3 + 83u^2 - 594u + 361$ |
| c_2, c_5, c_6 c_9 | $u^8 + u^7 - 8u^6 - 12u^5 + 7u^4 + 23u^3 + 45u^2 + 48u + 19$ |
| c_3 | $(u^2 + u + 1)^4$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $u^8 - u^7 - 2u^6 + 4u^4 + u^3 + 3u^2 + 6u + 4$ |
| c_7 | $u^8 - 3u^7 - 3u^6 + 5u^5 + 34u^4 - 12u^3 + 7u^2 - 8u + 4$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|--|
| c_1 | $y^8 - 85y^7 + \dots - 292910y + 130321$ |
| c_2, c_5, c_6 c_9 | $y^8 - 17y^7 + 102y^6 - 212y^5 - 177y^4 + 949y^3 + 83y^2 - 594y + 361$ |
| c_3 | $(y^2 + y + 1)^4$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $y^8 - 5y^7 + 12y^6 - 8y^5 + 24y^4 + 7y^3 + 29y^2 - 12y + 16$ |
| c_7 | $y^8 - 15y^7 + 107y^6 - 287y^5 + 1194y^4 + 388y^3 + 129y^2 - 8y + 16$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.500000 + 0.866025I$ $a = -1.038240 + 0.127249I$ $b = -0.717935 + 0.427530I$ | $-2.30291 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 + 0.866025I$ $a = 0.729219 + 0.407985I$ $b = 0.408918 - 0.962763I$ | $-2.30291 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 + 0.866025I$ $a = 1.172410 + 0.406591I$ $b = 1.74734 + 0.58922I$ | $5.59278 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 + 0.866025I$ $a = -0.36339 - 1.80785I$ $b = -0.938321 + 0.812037I$ | $5.59278 - 2.02988I$ | $7.00000 + 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = -1.038240 - 0.127249I$ $b = -0.717935 - 0.427530I$ | $-2.30291 + 2.02988I$ | $7.00000 - 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = 0.729219 - 0.407985I$ $b = 0.408918 + 0.962763I$ | $-2.30291 + 2.02988I$ | $7.00000 - 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = 1.172410 - 0.406591I$ $b = 1.74734 - 0.58922I$ | $5.59278 + 2.02988I$ | $7.00000 - 3.46410I$ |
| $u = -0.500000 - 0.866025I$ $a = -0.36339 + 1.80785I$ $b = -0.938321 - 0.812037I$ | $5.59278 + 2.02988I$ | $7.00000 - 3.46410I$ |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|-----------------------|--|
| c_1 | $(u^5 + 2u^4 - 7u^3 + 8u^2 - 4u + 1)$ $\cdot (u^8 - 17u^7 + 102u^6 - 212u^5 - 177u^4 + 949u^3 + 83u^2 - 594u + 361)$ $\cdot (u^8 - 7u^7 + 18u^6 - 20u^5 + 11u^4 - 5u^3 + 3u^2 + 2u + 1)$ $\cdot (u^{13} - u^{12} + \dots + 4u - 1)$ |
| c_2, c_6 | $(u^5 + 2u^4 + u^3 + 2u^2 + 1)(u^8 - u^7 + \dots - 2u + 1)$ $\cdot (u^8 + u^7 - 8u^6 - 12u^5 + 7u^4 + 23u^3 + 45u^2 + 48u + 19)$ $\cdot (u^{13} + u^{12} + \dots + 2u - 1)$ |
| c_3 | $(u^2 + u + 1)^8(u^5 - 4u^4 + 8u^3 - 7u^2 + 2u + 1)$ $\cdot (u^{13} - 5u^{12} + \dots + 36u - 9)$ |
| c_4, c_{12} | $(u^5 - u^4 + 2u^3 - 3u^2 + u - 1)(u^8 - u^7 + \dots + 6u + 4)$ $\cdot (u^8 + u^7 + 6u^6 + 6u^5 + 12u^4 + 13u^3 + 11u^2 + 10u + 4)$ $\cdot (u^{13} + 8u^{11} + \dots - u - 1)$ |
| c_5, c_9 | $(u^5 - 2u^4 + u^3 - 2u^2 - 1)$ $\cdot (u^8 + u^7 - 8u^6 - 12u^5 + 7u^4 + 23u^3 + 45u^2 + 48u + 19)$ $\cdot (u^8 + u^7 + \dots + 2u + 1)(u^{13} + u^{12} + \dots + 2u - 1)$ |
| c_7 | $(u^5 - 2u^3 - 3u^2 - 4u - 3)$ $\cdot (u^8 - 5u^7 + 19u^6 - 45u^5 + 76u^4 - 100u^3 + 99u^2 - 60u + 16)$ $\cdot (u^8 - 3u^7 - 3u^6 + 5u^5 + 34u^4 - 12u^3 + 7u^2 - 8u + 4)$ $\cdot (u^{13} - u^{12} + \dots + 90u - 25)$ |
| c_8, c_{10}, c_{11} | $(u^5 + u^4 + 2u^3 + 3u^2 + u + 1)(u^8 - u^7 + \dots + 6u + 4)$ $\cdot (u^8 - u^7 + 6u^6 - 6u^5 + 12u^4 - 13u^3 + 11u^2 - 10u + 4)$ $\cdot (u^{13} + 8u^{11} + \dots - u - 1)$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--|--|
| c_1 | $(y^5 - 18y^4 + 9y^3 - 12y^2 - 1)(y^8 - 85y^7 + \dots - 292910y + 130321)$ $\cdot (y^8 - 13y^7 + 66y^6 - 68y^5 + 59y^4 + 157y^3 + 51y^2 + 2y + 1)$ $\cdot (y^{13} + 35y^{12} + \dots + 212y - 1)$ |
| c_2, c_5, c_6 c_9 | $(y^5 - 2y^4 - 7y^3 - 8y^2 - 4y - 1)$ $\cdot (y^8 - 17y^7 + 102y^6 - 212y^5 - 177y^4 + 949y^3 + 83y^2 - 594y + 361)$ $\cdot (y^8 + 7y^7 + 18y^6 + 20y^5 + 11y^4 + 5y^3 + 3y^2 - 2y + 1)$ $\cdot (y^{13} - y^{12} + \dots + 4y - 1)$ |
| c_3 | $((y^2 + y + 1)^8)(y^5 + 12y^3 + \dots + 18y - 1)(y^{13} + 5y^{12} + \dots + 270y - 81)$ |
| c_4, c_8, c_{10} c_{11}, c_{12} | $(y^5 + 3y^4 - 7y^2 - 5y - 1)$ $\cdot (y^8 - 5y^7 + 12y^6 - 8y^5 + 24y^4 + 7y^3 + 29y^2 - 12y + 16)$ $\cdot (y^8 + 11y^7 + 48y^6 + 104y^5 + 108y^4 + 23y^3 - 43y^2 - 12y + 16)$ $\cdot (y^{13} + 16y^{12} + \dots - 5y - 1)$ |
| c_7 | $(y^5 - 4y^4 - 4y^3 + 7y^2 - 2y - 9)$ $\cdot (y^8 - 15y^7 + 107y^6 - 287y^5 + 1194y^4 + 388y^3 + 129y^2 - 8y + 16)$ $\cdot (y^8 + 13y^7 + 63y^6 + 61y^5 - 30y^4 + 256y^3 + 233y^2 - 432y + 256)$ $\cdot (y^{13} - 7y^{12} + \dots + 3150y - 625)$ |