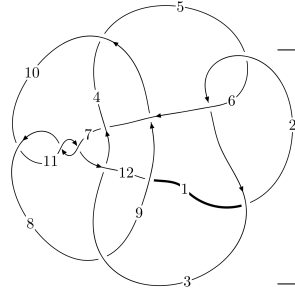
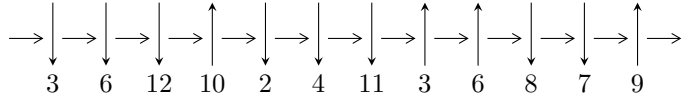


12n₀₄₄₂ (K12n₀₄₄₂)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5,10 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \rightsquigarrow c_3, c_6, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 191026393u^{16} - 1652039068u^{15} + \dots + 64719689b + 1958494945, \\ - 1223765713u^{16} + 10597268099u^{15} + \dots + 1553272536a - 9878621497, \\ u^{17} - 11u^{16} + \dots + 25u - 24 \rangle$$

$$I_2^u = \langle -u^9 - 5u^8 - 6u^7 + 8u^6 + 25u^5 + 16u^4 - 11u^3 - 14u^2 + b + u + 7, \\ - 7u^9 - 51u^8 - 149u^7 - 213u^6 - 119u^5 + 61u^4 + 107u^3 + 8u^2 + 5a - 56u - 27, \\ u^{10} + 8u^9 + 27u^8 + 49u^7 + 47u^6 + 12u^5 - 21u^4 - 19u^3 + 3u^2 + 11u + 5 \rangle$$

$$I_3^u = \langle -u^8a + 2u^8 + \dots - a - 4, -u^8a - u^8 + \dots + a^2 + 4, u^9 + 4u^8 + u^7 - 9u^6 + 12u^4 + 2u^3 + 4u^2 + 1 \rangle$$

$$I_4^u = \langle b^4 - 2b^3 + 3b^2 - 2b + 3, a + 1, u - 1 \rangle$$

$$I_5^u = \langle b^2 + b + 1, a - 1, u - 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 51 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.91 \times 10^8 u^{16} - 1.65 \times 10^9 u^{15} + \dots + 6.47 \times 10^7 b + 1.96 \times 10^9, -1.22 \times 10^9 u^{16} + 1.06 \times 10^{10} u^{15} + \dots + 1.55 \times 10^9 a - 9.88 \times 10^9, u^{17} - 11u^{16} + \dots + 25u - 24 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.787863u^{16} - 6.82254u^{15} + \dots - 4.19484u + 6.35988 \\ -2.95160u^{16} + 25.5261u^{15} + \dots + 20.2471u - 30.2612 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.502780u^{16} + 4.36822u^{15} + \dots + 2.45724u - 4.87506 \\ 1.68304u^{16} - 14.9279u^{15} + \dots - 10.7408u + 18.8611 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.787863u^{16} - 6.82254u^{15} + \dots - 4.19484u + 6.35988 \\ 1.37093u^{16} - 11.8653u^{15} + \dots - 6.94294u + 13.9936 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.583066u^{16} + 5.04279u^{15} + \dots + 2.74810u - 7.63370 \\ 1.37093u^{16} - 11.8653u^{15} + \dots - 6.94294u + 13.9936 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.149136u^{16} + 1.25050u^{15} + \dots + 3.19107u - 2.49878 \\ -0.717661u^{16} + 6.21375u^{15} + \dots + 5.68076u - 7.77323 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.785878u^{16} + 6.96162u^{15} + \dots + 3.90013u - 8.90611 \\ -0.0529908u^{16} + 0.408128u^{15} + \dots + 0.448137u - 0.173332 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.659584u^{16} - 5.85549u^{15} + \dots - 6.23720u + 8.19166 \\ 1.16236u^{16} - 10.2237u^{15} + \dots - 7.69444u + 12.0667 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{258679440}{64719689} u^{16} - \frac{2255352174}{64719689} u^{15} + \dots - \frac{1298645313}{64719689} u + \frac{2660816310}{64719689}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|---|
| c_1 | $u^{17} + 33u^{16} + \dots - 5039u + 576$ |
| c_2, c_5 | $u^{17} + 11u^{16} + \dots + 25u + 24$ |
| c_3, c_6 | $u^{17} - u^{16} + \dots + 4u + 1$ |
| c_4, c_8 | $u^{17} + 14u^{15} + \dots - 6u^2 + 1$ |
| c_7, c_{10}, c_{11} | $u^{17} - 6u^{16} + \dots + 19u - 2$ |
| c_9, c_{12} | $u^{17} + u^{16} + \dots + 33u + 3$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------|---|
| c_1 | $y^{17} - 117y^{16} + \dots + 20649889y - 331776$ |
| c_2, c_5 | $y^{17} - 33y^{16} + \dots - 5039y - 576$ |
| c_3, c_6 | $y^{17} + 13y^{16} + \dots - 22y - 1$ |
| c_4, c_8 | $y^{17} + 28y^{16} + \dots + 12y - 1$ |
| c_7, c_{10}, c_{11} | $y^{17} + 14y^{16} + \dots + 93y - 4$ |
| c_9, c_{12} | $y^{17} + 35y^{16} + \dots + 1875y - 9$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.942057 + 0.494267I$ $a = -0.753350 - 0.421156I$ $b = 0.435867 - 0.555452I$ | $1.96186 + 2.24541I$ | $1.44074 - 2.23530I$ |
| $u = -0.942057 - 0.494267I$ $a = -0.753350 + 0.421156I$ $b = 0.435867 + 0.555452I$ | $1.96186 - 2.24541I$ | $1.44074 + 2.23530I$ |
| $u = 1.095620 + 0.300147I$ $a = 0.131673 - 0.311290I$ $b = -1.033950 - 0.750497I$ | $2.79366 + 0.08444I$ | $-4.63288 + 0.68709I$ |
| $u = 1.095620 - 0.300147I$ $a = 0.131673 + 0.311290I$ $b = -1.033950 + 0.750497I$ | $2.79366 - 0.08444I$ | $-4.63288 - 0.68709I$ |
| $u = 0.836685$ $a = -0.0818231$ $b = 0.476471$ | -1.37068 | -8.35980 |
| $u = -0.320479 + 0.572318I$ $a = 0.08297 + 1.68332I$ $b = -0.103629 + 0.996127I$ | $7.44498 + 0.11919I$ | $3.63980 - 1.93920I$ |
| $u = -0.320479 - 0.572318I$ $a = 0.08297 - 1.68332I$ $b = -0.103629 - 0.996127I$ | $7.44498 - 0.11919I$ | $3.63980 + 1.93920I$ |
| $u = -1.25347 + 0.91415I$ $a = 0.916560 - 0.265291I$ $b = 0.46012 + 1.98973I$ | $5.01538 + 5.62718I$ | $-1.75252 - 3.01899I$ |
| $u = -1.25347 - 0.91415I$ $a = 0.916560 + 0.265291I$ $b = 0.46012 - 1.98973I$ | $5.01538 - 5.62718I$ | $-1.75252 + 3.01899I$ |
| $u = -0.032060 + 0.412278I$ $a = -1.57998 - 0.21566I$ $b = -0.592975 + 0.413733I$ | $0.026615 - 1.286250I$ | $0.68462 + 4.17584I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.032060 - 0.412278I$ | | |
| $a = -1.57998 + 0.21566I$ | $0.026615 + 1.286250I$ | $0.68462 - 4.17584I$ |
| $b = -0.592975 - 0.413733I$ | | |
| $u = 2.13442 + 0.33433I$ | | |
| $a = -0.041538 + 1.111040I$ | $-10.20570 - 0.23808I$ | $-2.00230 - 0.80635I$ |
| $b = 1.96060 - 2.85602I$ | | |
| $u = 2.13442 - 0.33433I$ | | |
| $a = -0.041538 - 1.111040I$ | $-10.20570 + 0.23808I$ | $-2.00230 + 0.80635I$ |
| $b = 1.96060 + 2.85602I$ | | |
| $u = 2.15252 + 0.26857I$ | | |
| $a = 0.260975 - 1.202630I$ | $-7.3294 - 12.2045I$ | $-2.87951 + 5.29191I$ |
| $b = -2.33574 + 2.94126I$ | | |
| $u = 2.15252 - 0.26857I$ | | |
| $a = 0.260975 + 1.202630I$ | $-7.3294 + 12.2045I$ | $-2.87951 - 5.29191I$ |
| $b = -2.33574 - 2.94126I$ | | |
| $u = 2.24717 + 0.01207I$ | | |
| $a = -0.122236 + 1.201380I$ | $-13.0039 - 6.5145I$ | $-5.31806 + 4.17343I$ |
| $b = 0.47148 - 3.89441I$ | | |
| $u = 2.24717 - 0.01207I$ | | |
| $a = -0.122236 - 1.201380I$ | $-13.0039 + 6.5145I$ | $-5.31806 - 4.17343I$ |
| $b = 0.47148 + 3.89441I$ | | |

II.

$$I_2^u = \langle -u^9 - 5u^8 + \dots + b + 7, -7u^9 - 51u^8 + \dots + 5a - 27, u^{10} + 8u^9 + \dots + 11u + 5 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{7}{5}u^9 + \frac{51}{5}u^8 + \dots + \frac{56}{5}u + \frac{27}{5} \\ u^9 + 5u^8 + 6u^7 - 8u^6 - 25u^5 - 16u^4 + 11u^3 + 14u^2 - u - 7 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{4}{5}u^9 + \frac{27}{5}u^8 + \dots + \frac{32}{5}u + \frac{9}{5} \\ -u^9 - 8u^8 - 26u^7 - 43u^6 - 33u^5 + 3u^4 + 24u^3 + 10u^2 - 9u - 9 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{7}{5}u^9 + \frac{51}{5}u^8 + \dots + \frac{56}{5}u + \frac{27}{5} \\ u^9 + 6u^8 + 13u^7 + 10u^6 - 5u^5 - 12u^4 - u^3 + 7u^2 + 3u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{2}{5}u^9 + \frac{21}{5}u^8 + \dots + \frac{41}{5}u + \frac{37}{5} \\ u^9 + 6u^8 + 13u^7 + 10u^6 - 5u^5 - 12u^4 - u^3 + 7u^2 + 3u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{13}{5}u^9 + \frac{89}{5}u^8 + \dots + \frac{84}{5}u + \frac{23}{5} \\ -u^9 - 9u^8 - 33u^7 - 61u^6 - 52u^5 + 2u^4 + 38u^3 + 16u^2 - 15u - 13 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{9}{5}u^9 - \frac{67}{5}u^8 + \dots - \frac{77}{5}u - \frac{54}{5} \\ -2u^9 - 13u^8 - 33u^7 - 39u^6 - 12u^5 + 21u^4 + 18u^3 - 4u^2 - 11u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{5}u^9 + \frac{8}{5}u^8 + \dots + \frac{8}{5}u + \frac{16}{5} \\ u^9 + 7u^8 + 20u^7 + 29u^6 + 18u^5 - 6u^4 - 15u^3 - 4u^2 + 7u + 4 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -8u^9 - 57u^8 - 163u^7 - 230u^6 - 130u^5 + 61u^4 + 115u^3 + 15u^2 - 61u - 34$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $u^{10} - 10u^9 + \dots - 91u + 25$ |
| c_2 | $u^{10} + 8u^9 + \dots + 11u + 5$ |
| c_3, c_6 | $u^{10} + u^9 + 3u^8 + u^6 - 3u^5 - 2u^4 - u^3 + 2u + 1$ |
| c_4, c_8 | $u^{10} + 6u^8 + 7u^6 - 2u^5 + 5u^4 + 2u^3 + 5u^2 + 2u + 1$ |
| c_5 | $u^{10} - 8u^9 + \dots - 11u + 5$ |
| c_7 | $u^{10} - 3u^9 + \dots - 10u + 3$ |
| c_9, c_{12} | $u^{10} - u^9 + 6u^8 - 10u^7 + 10u^6 - 6u^5 + 2u^4 - u^3 + 2u^2 - u + 1$ |
| c_{10}, c_{11} | $u^{10} + 3u^9 + \dots + 10u + 3$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--|
| c_1 | $y^{10} - 22y^9 + \dots + 2569y + 625$ |
| c_2, c_5 | $y^{10} - 10y^9 + \dots - 91y + 25$ |
| c_3, c_6 | $y^{10} + 5y^9 + 11y^8 + 8y^7 - 9y^6 - 15y^5 + 4y^4 + 13y^3 - 4y + 1$ |
| c_4, c_8 | $y^{10} + 12y^9 + \dots + 6y + 1$ |
| c_7, c_{10}, c_{11} | $y^{10} + 9y^9 + \dots + 20y + 9$ |
| c_9, c_{12} | $y^{10} + 11y^9 + 36y^8 + 12y^7 + 6y^6 + 8y^5 + 24y^4 + 15y^3 + 6y^2 + 3y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-------------------------|
| $u = -0.698244 + 0.611679I$ $a = -0.594983 + 0.452728I$ $b = -1.12357 - 1.18282I$ | $6.61177 + 7.24611I$ | $1.48024 - 6.55546I$ |
| $u = -0.698244 - 0.611679I$ $a = -0.594983 - 0.452728I$ $b = -1.12357 + 1.18282I$ | $6.61177 - 7.24611I$ | $1.48024 + 6.55546I$ |
| $u = -0.765895 + 0.862612I$ $a = 0.577252 + 0.100829I$ $b = 0.25692 + 1.47319I$ | $1.12408 + 3.31101I$ | $-1.94210 - 5.90631I$ |
| $u = -0.765895 - 0.862612I$ $a = 0.577252 - 0.100829I$ $b = 0.25692 - 1.47319I$ | $1.12408 - 3.31101I$ | $-1.94210 + 5.90631I$ |
| $u = 0.649524 + 0.270637I$ $a = 0.986717 + 0.863844I$ $b = 0.280240 - 0.198619I$ | $-0.88058 + 1.43796I$ | $-7.95798 - 4.23415I$ |
| $u = 0.649524 - 0.270637I$ $a = 0.986717 - 0.863844I$ $b = 0.280240 + 0.198619I$ | $-0.88058 - 1.43796I$ | $-7.95798 + 4.23415I$ |
| $u = -1.11228 + 0.88745I$ $a = -0.346880 - 0.585052I$ $b = 1.56427 - 1.47362I$ | $5.04002 - 1.56785I$ | $-0.680979 + 1.239329I$ |
| $u = -1.11228 - 0.88745I$ $a = -0.346880 + 0.585052I$ $b = 1.56427 + 1.47362I$ | $5.04002 + 1.56785I$ | $-0.680979 - 1.239329I$ |
| $u = -2.07310 + 0.22780I$ $a = 0.077895 + 1.141750I$ $b = -1.47786 - 2.59954I$ | $-11.89530 + 1.62532I$ | $-4.89918 - 0.65986I$ |
| $u = -2.07310 - 0.22780I$ $a = 0.077895 - 1.141750I$ $b = -1.47786 + 2.59954I$ | $-11.89530 - 1.62532I$ | $-4.89918 + 0.65986I$ |

$$\text{III. } I_3^u = \langle -u^8 a + 2u^8 + \cdots - a - 4, -u^8 a - u^8 + \cdots + a^2 + 4, u^9 + 4u^8 + u^7 - 9u^6 + 12u^4 + 2u^3 + 4u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ \frac{1}{8}u^8 a - \frac{1}{4}u^8 + \cdots + \frac{1}{8}a + \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{4}u^8 a + \frac{7}{8}u^8 + \cdots + \frac{1}{2}a + \frac{15}{8} \\ \frac{1}{4}u^8 a + \frac{3}{8}u^8 + \cdots + \frac{1}{2}a - \frac{5}{8} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ \frac{1}{8}u^8 a - \frac{1}{4}u^8 + \cdots + \frac{1}{8}a + \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{8}u^8 a + \frac{1}{4}u^8 + \cdots + \frac{7}{8}a - \frac{1}{2} \\ \frac{1}{8}u^8 a - \frac{1}{4}u^8 + \cdots + \frac{1}{8}a + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{4}u^8 a + \frac{1}{2}u^8 + \cdots + \frac{1}{2}a + \frac{5}{4} \\ \frac{1}{8}u^8 a - \frac{3}{4}u^8 + \cdots + \frac{3}{8}a - \frac{3}{4} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u^8 a - \frac{7}{8}u^8 + \cdots - \frac{1}{4}a - \frac{7}{8} \\ \frac{1}{4}u^8 a + \frac{3}{8}u^8 + \cdots + \frac{3}{4}a - \frac{3}{8} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^8 - 4u^7 - u^6 + 9u^5 - 12u^3 - 2u^2 - 4u \\ \frac{1}{2}u^8 a + \frac{1}{8}u^8 + \cdots + \frac{1}{4}a - \frac{7}{8} \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{5}{4}u^8 + \frac{25}{4}u^7 + \frac{7}{2}u^6 - \frac{63}{4}u^5 - \frac{15}{4}u^4 + \frac{93}{4}u^3 + \frac{7}{4}u^2 + \frac{27}{4}u - \frac{13}{4}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|--|
| c_1 | $(u^9 + 14u^8 + 73u^7 + 173u^6 + 188u^5 + 80u^4 - 74u^3 + 40u^2 - 8u + 1)^2$ |
| c_2, c_5 | $(u^9 - 4u^8 + u^7 + 9u^6 - 12u^4 + 2u^3 - 4u^2 - 1)^2$ |
| c_3, c_6 | $u^{18} - 4u^{17} + \dots - 19u + 7$ |
| c_4, c_8 | $u^{18} + 17u^{16} + \dots - 33u + 61$ |
| c_7, c_{10}, c_{11} | $(u^9 + u^8 + 5u^7 + 4u^6 + 8u^5 + 5u^4 + 3u^3 - 2u - 2)^2$ |
| c_9, c_{12} | $u^{18} - 3u^{17} + \dots - 38u + 787$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--|
| c_1 | $(y^9 - 50y^8 + \dots - 16y - 1)^2$ |
| c_2, c_5 | $(y^9 - 14y^8 + 73y^7 - 173y^6 + 188y^5 - 80y^4 - 74y^3 - 40y^2 - 8y - 1)^2$ |
| c_3, c_6 | $y^{18} + 2y^{17} + \dots + 451y + 49$ |
| c_4, c_8 | $y^{18} + 34y^{17} + \dots + 4279y + 3721$ |
| c_7, c_{10}, c_{11} | $(y^9 + 9y^8 + 33y^7 + 60y^6 + 50y^5 + 7y^4 - 7y^3 + 8y^2 + 4y - 4)^2$ |
| c_9, c_{12} | $y^{18} + 29y^{17} + \dots + 1731530y + 619369$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.149930 + 0.591217I$ $a = -0.601255 - 0.402054I$ $b = -0.395481 + 0.118419I$ | $1.86176 + 1.02570I$ | $-2.63382 - 1.45009I$ |
| $u = 1.149930 + 0.591217I$ $a = 1.283380 - 0.095795I$ $b = -0.77918 - 2.34414I$ | $1.86176 + 1.02570I$ | $-2.63382 - 1.45009I$ |
| $u = 1.149930 - 0.591217I$ $a = -0.601255 + 0.402054I$ $b = -0.395481 - 0.118419I$ | $1.86176 - 1.02570I$ | $-2.63382 + 1.45009I$ |
| $u = 1.149930 - 0.591217I$ $a = 1.283380 + 0.095795I$ $b = -0.77918 + 2.34414I$ | $1.86176 - 1.02570I$ | $-2.63382 + 1.45009I$ |
| $u = -0.256958 + 0.481474I$ $a = 2.09172 + 0.18082I$ $b = -0.347105 + 0.467672I$ | $5.86635 - 5.34937I$ | $-0.84423 + 2.78056I$ |
| $u = -0.256958 + 0.481474I$ $a = 0.39890 - 2.37095I$ $b = 1.48260 - 1.54705I$ | $5.86635 - 5.34937I$ | $-0.84423 + 2.78056I$ |
| $u = -0.256958 - 0.481474I$ $a = 2.09172 - 0.18082I$ $b = -0.347105 - 0.467672I$ | $5.86635 + 5.34937I$ | $-0.84423 - 2.78056I$ |
| $u = -0.256958 - 0.481474I$ $a = 0.39890 + 2.37095I$ $b = 1.48260 + 1.54705I$ | $5.86635 + 5.34937I$ | $-0.84423 - 2.78056I$ |
| $u = 0.202323 + 0.429977I$ $a = -1.06958 - 1.32915I$ $b = -0.028684 + 0.501202I$ | $-0.08117 - 1.83340I$ | $-4.79553 + 3.05314I$ |
| $u = 0.202323 + 0.429977I$ $a = -1.78447 + 1.20971I$ $b = -0.54712 + 1.46919I$ | $-0.08117 - 1.83340I$ | $-4.79553 + 3.05314I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.202323 - 0.429977I$ $a = -1.06958 + 1.32915I$ $b = -0.028684 - 0.501202I$ | $-0.08117 + 1.83340I$ | $-4.79553 - 3.05314I$ |
| $u = 0.202323 - 0.429977I$ $a = -1.78447 - 1.20971I$ $b = -0.54712 - 1.46919I$ | $-0.08117 + 1.83340I$ | $-4.79553 - 3.05314I$ |
| $u = -2.04009 + 0.22792I$ $a = -0.374086 - 0.921422I$ $b = 2.26253 + 1.38756I$ | $-10.25890 + 3.35426I$ | $-1.96692 - 2.76177I$ |
| $u = -2.04009 + 0.22792I$ $a = -0.189467 + 1.360530I$ $b = -0.72311 - 3.40708I$ | $-10.25890 + 3.35426I$ | $-1.96692 - 2.76177I$ |
| $u = -2.04009 - 0.22792I$ $a = -0.374086 + 0.921422I$ $b = 2.26253 - 1.38756I$ | $-10.25890 - 3.35426I$ | $-1.96692 + 2.76177I$ |
| $u = -2.04009 - 0.22792I$ $a = -0.189467 - 1.360530I$ $b = -0.72311 + 3.40708I$ | $-10.25890 - 3.35426I$ | $-1.96692 + 2.76177I$ |
| $u = -2.11041$ $a = 0.244866 + 1.162790I$ $b = -0.92445 - 2.96892I$ | -14.5153 | -7.51900 |
| $u = -2.11041$ $a = 0.244866 - 1.162790I$ $b = -0.92445 + 2.96892I$ | -14.5153 | -7.51900 |

$$\text{IV. } I_4^u = \langle b^4 - 2b^3 + 3b^2 - 2b + 3, a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -b + 1 \\ b^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ b - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -b \\ b - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -b^3 + b^2 - b - 1 \\ b^3 - 2b^2 + 3b - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -b^2 + 2b - 1 \\ b^3 - b^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -b \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|--------------------------------|
| c_1, c_2 | $(u - 1)^4$ |
| c_3, c_6 | $u^4 + 2u^3 + 3u^2 + 2u + 3$ |
| c_4, c_8 | $u^4 - 2u^3 + 3u^2 - 2u + 3$ |
| c_5, c_9, c_{12} | $(u + 1)^4$ |
| c_7, c_{10}, c_{11} | $(u^2 + 2)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|----------------------------------|------------------------------------|
| c_1, c_2, c_5 c_9, c_{12} | $(y - 1)^4$ |
| c_3, c_4, c_6 c_8 | $y^4 + 2y^3 + 7y^2 + 14y + 9$ |
| c_7, c_{10}, c_{11} | $(y + 2)^4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.00000$ $a = -1.00000$ $b = -0.152220 + 1.084150I$ | 4.93480 | 0 |
| $u = 1.00000$ $a = -1.00000$ $b = -0.152220 - 1.084150I$ | 4.93480 | 0 |
| $u = 1.00000$ $a = -1.00000$ $b = 1.15222 + 1.08415I$ | 4.93480 | 0 |
| $u = 1.00000$ $a = -1.00000$ $b = 1.15222 - 1.08415I$ | 4.93480 | 0 |

$$\mathbf{V. } I_5^u = \langle b^2 + b + 1, a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b + 1 \\ -b - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ b + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -b \\ b + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -b \\ b + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| c_1, c_2, c_9 c_{12} | $(u - 1)^2$ |
| c_3, c_4, c_6 c_8 | $u^2 + u + 1$ |
| c_5 | $(u + 1)^2$ |
| c_7, c_{10}, c_{11} | u^2 |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|----------------------------------|------------------------------------|
| c_1, c_2, c_5 c_9, c_{12} | $(y - 1)^2$ |
| c_3, c_4, c_6 c_8 | $y^2 + y + 1$ |
| c_7, c_{10}, c_{11} | y^2 |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 1.00000$ $a = 1.00000$ $b = -0.500000 + 0.866025I$ | 0 | -6.00000 |
| $u = 1.00000$ $a = 1.00000$ $b = -0.500000 - 0.866025I$ | 0 | -6.00000 |

VI. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|--|
| c_1 | $(u - 1)^6$ $\cdot (u^9 + 14u^8 + 73u^7 + 173u^6 + 188u^5 + 80u^4 - 74u^3 + 40u^2 - 8u + 1)^2$ $\cdot (u^{10} - 10u^9 + \dots - 91u + 25)(u^{17} + 33u^{16} + \dots - 5039u + 576)$ |
| c_2 | $(u - 1)^6(u^9 - 4u^8 + u^7 + 9u^6 - 12u^4 + 2u^3 - 4u^2 - 1)^2$ $\cdot (u^{10} + 8u^9 + \dots + 11u + 5)(u^{17} + 11u^{16} + \dots + 25u + 24)$ |
| c_3, c_6 | $(u^2 + u + 1)(u^4 + 2u^3 + 3u^2 + 2u + 3)$ $\cdot (u^{10} + u^9 + \dots + 2u + 1)(u^{17} - u^{16} + \dots + 4u + 1)$ $\cdot (u^{18} - 4u^{17} + \dots - 19u + 7)$ |
| c_4, c_8 | $(u^2 + u + 1)(u^4 - 2u^3 + 3u^2 - 2u + 3)$ $\cdot (u^{10} + 6u^8 + 7u^6 - 2u^5 + 5u^4 + 2u^3 + 5u^2 + 2u + 1)$ $\cdot (u^{17} + 14u^{15} + \dots - 6u^2 + 1)(u^{18} + 17u^{16} + \dots - 33u + 61)$ |
| c_5 | $(u + 1)^6(u^9 - 4u^8 + u^7 + 9u^6 - 12u^4 + 2u^3 - 4u^2 - 1)^2$ $\cdot (u^{10} - 8u^9 + \dots - 11u + 5)(u^{17} + 11u^{16} + \dots + 25u + 24)$ |
| c_7 | $u^2(u^2 + 2)^2(u^9 + u^8 + 5u^7 + 4u^6 + 8u^5 + 5u^4 + 3u^3 - 2u - 2)^2$ $\cdot (u^{10} - 3u^9 + \dots - 10u + 3)(u^{17} - 6u^{16} + \dots + 19u - 2)$ |
| c_9, c_{12} | $(u - 1)^2(u + 1)^4$ $\cdot (u^{10} - u^9 + 6u^8 - 10u^7 + 10u^6 - 6u^5 + 2u^4 - u^3 + 2u^2 - u + 1)$ $\cdot (u^{17} + u^{16} + \dots + 33u + 3)(u^{18} - 3u^{17} + \dots - 38u + 787)$ |
| c_{10}, c_{11} | $u^2(u^2 + 2)^2(u^9 + u^8 + 5u^7 + 4u^6 + 8u^5 + 5u^4 + 3u^3 - 2u - 2)^2$ $\cdot (u^{10} + 3u^9 + \dots + 10u + 3)(u^{17} - 6u^{16} + \dots + 19u - 2)$ |

VII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--|
| c_1 | $((y-1)^6)(y^9 - 50y^8 + \dots - 16y - 1)^2$ $\cdot (y^{10} - 22y^9 + \dots + 2569y + 625)$ $\cdot (y^{17} - 117y^{16} + \dots + 20649889y - 331776)$ |
| c_2, c_5 | $(y-1)^6$ $\cdot (y^9 - 14y^8 + 73y^7 - 173y^6 + 188y^5 - 80y^4 - 74y^3 - 40y^2 - 8y - 1)^2$ $\cdot (y^{10} - 10y^9 + \dots - 91y + 25)(y^{17} - 33y^{16} + \dots - 5039y - 576)$ |
| c_3, c_6 | $(y^2 + y + 1)(y^4 + 2y^3 + 7y^2 + 14y + 9)$ $\cdot (y^{10} + 5y^9 + 11y^8 + 8y^7 - 9y^6 - 15y^5 + 4y^4 + 13y^3 - 4y + 1)$ $\cdot (y^{17} + 13y^{16} + \dots - 22y - 1)(y^{18} + 2y^{17} + \dots + 451y + 49)$ |
| c_4, c_8 | $(y^2 + y + 1)(y^4 + 2y^3 + \dots + 14y + 9)(y^{10} + 12y^9 + \dots + 6y + 1)$ $\cdot (y^{17} + 28y^{16} + \dots + 12y - 1)(y^{18} + 34y^{17} + \dots + 4279y + 3721)$ |
| c_7, c_{10}, c_{11} | $y^2(y+2)^4$ $\cdot (y^9 + 9y^8 + 33y^7 + 60y^6 + 50y^5 + 7y^4 - 7y^3 + 8y^2 + 4y - 4)^2$ $\cdot (y^{10} + 9y^9 + \dots + 20y + 9)(y^{17} + 14y^{16} + \dots + 93y - 4)$ |
| c_9, c_{12} | $(y-1)^6$ $\cdot (y^{10} + 11y^9 + 36y^8 + 12y^7 + 6y^6 + 8y^5 + 24y^4 + 15y^3 + 6y^2 + 3y + 1)$ $\cdot (y^{17} + 35y^{16} + \dots + 1875y - 9)$ $\cdot (y^{18} + 29y^{17} + \dots + 1731530y + 619369)$ |