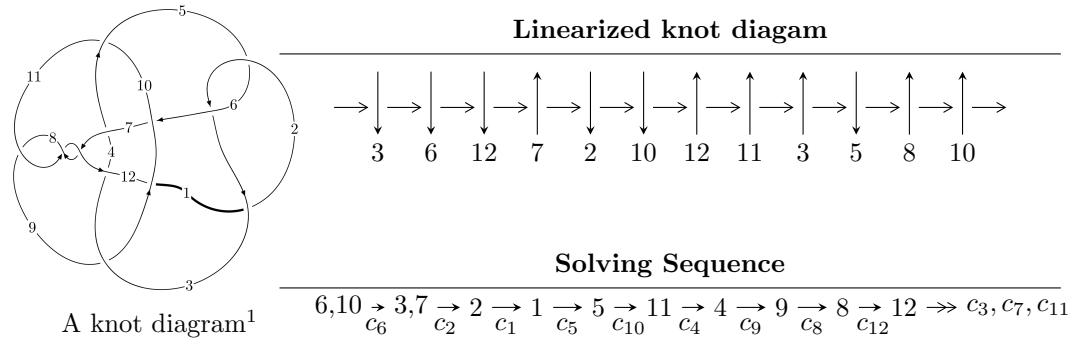


$12n_{0444}$ ($K12n_{0444}$)



Ideals for irreducible components² of X_{par}

$$\begin{aligned}
 I_1^u &= \langle 5.32469 \times 10^{28}u^{19} - 1.94113 \times 10^{29}u^{18} + \dots + 2.78354 \times 10^{30}b - 8.37086 \times 10^{31}, \\
 &\quad - 3.59288 \times 10^{32}u^{19} + 1.29989 \times 10^{33}u^{18} + \dots + 6.03193 \times 10^{33}a + 5.69917 \times 10^{35}, \\
 &\quad u^{20} - 5u^{19} + \dots - 5504u + 2167 \rangle \\
 I_2^u &= \langle -39167u^9 + 24055u^8 + \dots + 90803b + 150893, 39167u^9 - 24055u^8 + \dots + 90803a - 241696, \\
 &\quad u^{10} - 6u^8 + 27u^6 + 30u^5 + 30u^4 + 14u^3 + 10u^2 + 2u + 1 \rangle \\
 I_3^u &= \langle b + 1, a - u + 1, u^3 - 2u^2 + u + 1 \rangle
 \end{aligned}$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 33 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 5.32 \times 10^{28}u^{19} - 1.94 \times 10^{29}u^{18} + \cdots + 2.78 \times 10^{30}b - 8.37 \times 10^{31}, -3.59 \times 10^{32}u^{19} + 1.30 \times 10^{33}u^{18} + \cdots + 6.03 \times 10^{33}a + 5.70 \times 10^{35}, u^{20} - 5u^{19} + \cdots - 5504u + 2167 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0595644u^{19} - 0.215502u^{18} + \cdots + 169.749u - 94.4834 \\ -0.0191292u^{19} + 0.0697361u^{18} + \cdots - 55.2312u + 30.0727 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0404352u^{19} - 0.145766u^{18} + \cdots + 114.518u - 64.4106 \\ -0.0191292u^{19} + 0.0697361u^{18} + \cdots - 55.2312u + 30.0727 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0614601u^{19} + 0.224116u^{18} + \cdots - 176.369u + 97.1863 \\ 0.0732431u^{19} - 0.266224u^{18} + \cdots + 209.407u - 116.188 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0367341u^{19} + 0.133131u^{18} + \cdots - 104.597u + 56.9934 \\ 0.0484428u^{19} - 0.177657u^{18} + \cdots + 141.186u - 79.6977 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.109966u^{19} + 0.400168u^{18} + \cdots - 316.982u + 175.815 \\ -0.00769082u^{19} + 0.0267093u^{18} + \cdots - 20.2609u + 10.6953 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.153606u^{19} + 0.560090u^{18} + \cdots - 444.350u + 246.211 \\ -0.164874u^{19} + 0.598489u^{18} + \cdots - 471.899u + 261.395 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.0266987u^{19} - 0.0960595u^{18} + \cdots + 75.9779u - 40.6092 \\ -0.115096u^{19} + 0.419259u^{18} + \cdots - 332.122u + 184.578 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0291891u^{19} - 0.106960u^{18} + \cdots + 85.6547u - 46.9664 \\ 0.0785887u^{19} - 0.287166u^{18} + \cdots + 225.983u - 125.342 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0614601u^{19} + 0.224116u^{18} + \cdots - 176.369u + 97.1863 \\ -0.0400440u^{19} + 0.146686u^{18} + \cdots - 115.256u + 64.0732 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** = $-0.0313654u^{19} + 0.114631u^{18} + \cdots - 89.3865u + 39.1345$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{20} + 12u^{19} + \cdots - 19u + 4$
c_2, c_5	$u^{20} - 2u^{19} + \cdots - 5u + 2$
c_3	$u^{20} - 5u^{19} + \cdots - 4312u + 581$
c_4	$u^{20} - u^{19} + \cdots - 622u + 97$
c_6	$u^{20} + 5u^{19} + \cdots + 5504u + 2167$
c_7, c_8, c_{11}	$u^{20} + 3u^{19} + \cdots - 71u + 62$
c_9	$u^{20} - u^{19} + \cdots - 78u + 17$
c_{10}	$u^{20} - u^{19} + \cdots - 52u + 17$
c_{12}	$u^{20} + u^{19} + \cdots - 294u + 151$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{20} - 8y^{19} + \cdots - 417y + 16$
c_2, c_5	$y^{20} - 12y^{19} + \cdots + 19y + 4$
c_3	$y^{20} - 75y^{19} + \cdots + 153632486y + 337561$
c_4	$y^{20} + 63y^{19} + \cdots - 66784y + 9409$
c_6	$y^{20} - 35y^{19} + \cdots - 16056826y + 4695889$
c_7, c_8, c_{11}	$y^{20} + 37y^{19} + \cdots + 27075y + 3844$
c_9	$y^{20} + 39y^{19} + \cdots + 6088y + 289$
c_{10}	$y^{20} - 5y^{19} + \cdots - 120y + 289$
c_{12}	$y^{20} + 47y^{19} + \cdots + 412468y + 22801$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.703317 + 0.600603I$		
$a = -0.437463 - 0.884492I$	$-2.03672 + 1.24145I$	$-6.74073 - 2.13278I$
$b = -0.924571 + 0.362873I$		
$u = 0.703317 - 0.600603I$		
$a = -0.437463 + 0.884492I$	$-2.03672 - 1.24145I$	$-6.74073 + 2.13278I$
$b = -0.924571 - 0.362873I$		
$u = 0.459645 + 0.743049I$		
$a = 0.260880 + 0.613052I$	$0.254769 - 1.344490I$	$2.10960 + 5.34511I$
$b = 0.118127 - 0.454177I$		
$u = 0.459645 - 0.743049I$		
$a = 0.260880 - 0.613052I$	$0.254769 + 1.344490I$	$2.10960 - 5.34511I$
$b = 0.118127 + 0.454177I$		
$u = -0.971034 + 0.814910I$		
$a = 0.177512 - 0.054619I$	$1.28418 - 1.69463I$	$6.51624 + 5.12886I$
$b = 0.759811 + 0.367137I$		
$u = -0.971034 - 0.814910I$		
$a = 0.177512 + 0.054619I$	$1.28418 + 1.69463I$	$6.51624 - 5.12886I$
$b = 0.759811 - 0.367137I$		
$u = 1.358840 + 0.009534I$		
$a = -0.18107 + 1.59414I$	$16.5713 + 0.1764I$	$-5.92523 - 0.80143I$
$b = 1.34261 - 0.46139I$		
$u = 1.358840 - 0.009534I$		
$a = -0.18107 - 1.59414I$	$16.5713 - 0.1764I$	$-5.92523 + 0.80143I$
$b = 1.34261 + 0.46139I$		
$u = -1.39927 + 0.25928I$		
$a = -0.153915 - 1.075640I$	$-5.96211 - 0.50208I$	$-3.53348 + 0.08568I$
$b = -0.150857 + 0.864815I$		
$u = -1.39927 - 0.25928I$		
$a = -0.153915 + 1.075640I$	$-5.96211 + 0.50208I$	$-3.53348 - 0.08568I$
$b = -0.150857 - 0.864815I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.35298 + 0.59131I$		
$a = 0.282108 - 0.480951I$	$-2.42744 - 4.72916I$	$-3.24036 + 7.15543I$
$b = 1.105280 + 0.366189I$		
$u = 1.35298 - 0.59131I$		
$a = 0.282108 + 0.480951I$	$-2.42744 + 4.72916I$	$-3.24036 - 7.15543I$
$b = 1.105280 - 0.366189I$		
$u = -1.33962 + 0.86373I$		
$a = -0.145047 + 1.067730I$	$-10.43980 + 3.82524I$	$-6.93583 - 2.76644I$
$b = 1.296470 - 0.378610I$		
$u = -1.33962 - 0.86373I$		
$a = -0.145047 - 1.067730I$	$-10.43980 - 3.82524I$	$-6.93583 + 2.76644I$
$b = 1.296470 + 0.378610I$		
$u = 1.73280 + 0.79935I$		
$a = -0.300874 - 1.047990I$	$-18.5073 - 4.9976I$	$-2.68482 + 1.85210I$
$b = -0.057341 + 0.997519I$		
$u = 1.73280 - 0.79935I$		
$a = -0.300874 + 1.047990I$	$-18.5073 + 4.9976I$	$-2.68482 - 1.85210I$
$b = -0.057341 - 0.997519I$		
$u = -1.90586 + 0.34611I$		
$a = 0.024972 + 0.827392I$	$-9.03300 - 5.58421I$	$-6.18314 + 4.04952I$
$b = -1.189400 - 0.543552I$		
$u = -1.90586 - 0.34611I$		
$a = 0.024972 - 0.827392I$	$-9.03300 + 5.58421I$	$-6.18314 - 4.04952I$
$b = -1.189400 + 0.543552I$		
$u = 2.50819 + 1.00282I$		
$a = 0.136951 + 0.755014I$	$17.1367 - 10.4420I$	$-5.38225 + 4.71177I$
$b = -1.300140 - 0.529897I$		
$u = 2.50819 - 1.00282I$		
$a = 0.136951 - 0.755014I$	$17.1367 + 10.4420I$	$-5.38225 - 4.71177I$
$b = -1.300140 + 0.529897I$		

$$\text{II. } I_2^u = \langle -39167u^9 + 24055u^8 + \dots + 90803b + 150893, 39167u^9 - 24055u^8 + \dots + 90803a - 241696, u^{10} - 6u^8 + \dots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.431340u^9 + 0.264914u^8 + \dots - 1.16678u + 2.66176 \\ 0.431340u^9 - 0.264914u^8 + \dots + 1.16678u - 1.66176 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ 0.431340u^9 - 0.264914u^8 + \dots + 1.16678u - 1.66176 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 2.92164u^9 - 0.926676u^8 + \dots + 10.7123u - 1.76757 \\ -1.35298u^9 + 0.191591u^8 + \dots - 5.87905u - 0.570664 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.431340u^9 + 0.264914u^8 + \dots - 1.16678u + 2.66176 \\ 1.13732u^9 - 0.470172u^8 + \dots + 3.66644u - 1.67648 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^9 + 6u^7 - 27u^5 - 30u^4 - 30u^3 - 14u^2 - 10u - 2 \\ 0.926676u^9 + 0.384426u^8 + \dots + 9.61086u + 2.92164 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -1.61557u^9 + 0.780393u^8 + \dots - 4.93171u + 4.07332 \\ 1.20899u^9 - 0.543143u^8 + \dots + 3.81972u - 2.19195 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^9 + 6u^7 - 27u^5 - 30u^4 - 30u^3 - 14u^2 - 10u - 2 \\ 0.735086u^9 + 0.0469147u^8 + \dots + 7.47556u + 1.56866 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.429336u^9 - 1.35298u^8 + \dots - 12.2006u - 6.73772 \\ -0.234717u^9 + 0.913527u^8 + \dots + 4.86712u + 4.70396 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 2.92164u^9 - 0.926676u^8 + \dots + 10.7123u - 1.76757 \\ -1.73741u^9 + 0.411198u^8 + \dots - 6.94734u + 0.356012 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

$$\text{(iii) Cusp Shapes} = -\frac{418432}{90803}u^9 - \frac{85648}{90803}u^8 + \frac{2619224}{90803}u^7 + \frac{532096}{90803}u^6 - \frac{11982728}{90803}u^5 - \frac{14963376}{90803}u^4 - \frac{12033384}{90803}u^3 - \frac{4718044}{90803}u^2 - \frac{2327168}{90803}u - \frac{672892}{90803}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2$
c_2, c_5	$u^{10} - 3u^8 + 4u^6 - u^4 - u^2 + 1$
c_3	$u^{10} + 4u^9 + \dots + 10u + 1$
c_4	$u^{10} - 2u^9 + u^8 - 4u^7 + 7u^6 + 10u^5 - 8u^4 + 14u^3 + 53u^2 + 25$
c_6	$u^{10} - 6u^8 + 27u^6 + 30u^5 + 30u^4 + 14u^3 + 10u^2 + 2u + 1$
c_7, c_8, c_{11}	$u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1$
c_9, c_{10}	$(u^2 + 1)^5$
c_{12}	$u^{10} + u^8 - 10u^7 - u^6 + 10u^5 + 40u^4 + 4u^3 - 3u^2 - 50u + 25$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$
c_2, c_5	$(y^5 - 3y^4 + 4y^3 - y^2 - y + 1)^2$
c_3	$y^{10} + 12y^9 + \dots - 16y + 1$
c_4	$y^{10} - 2y^9 + \dots + 2650y + 625$
c_6	$y^{10} - 12y^9 + \dots + 16y + 1$
c_7, c_8, c_{11}	$(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$
c_9, c_{10}	$(y + 1)^{10}$
c_{12}	$y^{10} + 2y^9 + \dots - 2650y + 625$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.482881 + 0.629714I$		
$a = 1.000000 - 0.766826I$	-2.40108	$-1.48114 + 0.I$
$b = 0.766826I$		
$u = -0.482881 - 0.629714I$		
$a = 1.000000 + 0.766826I$	-2.40108	$-1.48114 + 0.I$
$b = -0.766826I$		
$u = 0.098692 + 0.530370I$		
$a = 1.82238 + 0.339111I$	-0.32910 - 1.53058I	$-0.51511 + 4.43065I$
$b = -0.822375 - 0.339110I$		
$u = 0.098692 - 0.530370I$		
$a = 1.82238 - 0.339111I$	-0.32910 + 1.53058I	$-0.51511 - 4.43065I$
$b = -0.822375 + 0.339110I$		
$u = -0.090267 + 0.435818I$		
$a = 2.20015 - 0.45570I$	-5.87256 + 4.40083I	$-4.74431 - 3.49859I$
$b = -1.200150 + 0.455697I$		
$u = -0.090267 - 0.435818I$		
$a = 2.20015 + 0.45570I$	-5.87256 - 4.40083I	$-4.74431 + 3.49859I$
$b = -1.200150 - 0.455697I$		
$u = -1.83956 + 0.80797I$		
$a = -0.200152 + 0.455697I$	-5.87256 + 4.40083I	$-4.74431 - 3.49859I$
$b = 1.200150 - 0.455697I$		
$u = -1.83956 - 0.80797I$		
$a = -0.200152 - 0.455697I$	-5.87256 - 4.40083I	$-4.74431 + 3.49859I$
$b = 1.200150 + 0.455697I$		
$u = 2.31402 + 1.21207I$		
$a = 0.177625 + 0.339110I$	-0.32910 + 1.53058I	$-0.51511 - 4.43065I$
$b = 0.822375 - 0.339110I$		
$u = 2.31402 - 1.21207I$		
$a = 0.177625 - 0.339110I$	-0.32910 - 1.53058I	$-0.51511 + 4.43065I$
$b = 0.822375 + 0.339110I$		

$$\text{III. } I_3^u = \langle b+1, a-u+1, u^3 - 2u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u-1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u-2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u-1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2-1 \\ u^2-2u-2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_5	$(u + 1)^3$
c_3, c_4, c_9 c_{10}	$u^3 + u + 1$
c_6	$u^3 + 2u^2 + u - 1$
c_7, c_8, c_{11}	u^3
c_{12}	$u^3 - 2u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^3$
c_3, c_4, c_9 c_{10}	$y^3 + 2y^2 + y - 1$
c_6, c_{12}	$y^3 - 2y^2 + 5y - 1$
c_7, c_8, c_{11}	y^3

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.23279 + 0.79255I$		
$a = 0.232786 + 0.792552I$	-1.64493	-6.00000
$b = -1.00000$		
$u = 1.23279 - 0.79255I$		
$a = 0.232786 - 0.792552I$	-1.64493	-6.00000
$b = -1.00000$		
$u = -0.465571$		
$a = -1.46557$	-1.64493	-6.00000
$b = -1.00000$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u + 1)^3)(u^5 - 3u^4 + \dots - u + 1)^2(u^{20} + 12u^{19} + \dots - 19u + 4)$
c_2, c_5	$((u + 1)^3)(u^{10} - 3u^8 + \dots - u^2 + 1)(u^{20} - 2u^{19} + \dots - 5u + 2)$
c_3	$(u^3 + u + 1)(u^{10} + 4u^9 + \dots + 10u + 1)(u^{20} - 5u^{19} + \dots - 4312u + 581)$
c_4	$(u^3 + u + 1)(u^{10} - 2u^9 + \dots + 53u^2 + 25)$ $\cdot (u^{20} - u^{19} + \dots - 622u + 97)$
c_6	$(u^3 + 2u^2 + u - 1)$ $\cdot (u^{10} - 6u^8 + 27u^6 + 30u^5 + 30u^4 + 14u^3 + 10u^2 + 2u + 1)$ $\cdot (u^{20} + 5u^{19} + \dots + 5504u + 2167)$
c_7, c_8, c_{11}	$u^3(u^{10} + 5u^8 + \dots - u^2 + 1)(u^{20} + 3u^{19} + \dots - 71u + 62)$
c_9	$((u^2 + 1)^5)(u^3 + u + 1)(u^{20} - u^{19} + \dots - 78u + 17)$
c_{10}	$((u^2 + 1)^5)(u^3 + u + 1)(u^{20} - u^{19} + \dots - 52u + 17)$
c_{12}	$(u^3 - 2u^2 + u + 1)$ $\cdot (u^{10} + u^8 - 10u^7 - u^6 + 10u^5 + 40u^4 + 4u^3 - 3u^2 - 50u + 25)$ $\cdot (u^{20} + u^{19} + \dots - 294u + 151)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y - 1)^3(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2 \\ \cdot (y^{20} - 8y^{19} + \dots - 417y + 16)$
c_2, c_5	$((y - 1)^3)(y^5 - 3y^4 + \dots - y + 1)^2(y^{20} - 12y^{19} + \dots + 19y + 4)$
c_3	$(y^3 + 2y^2 + y - 1)(y^{10} + 12y^9 + \dots - 16y + 1) \\ \cdot (y^{20} - 75y^{19} + \dots + 153632486y + 337561)$
c_4	$(y^3 + 2y^2 + y - 1)(y^{10} - 2y^9 + \dots + 2650y + 625) \\ \cdot (y^{20} + 63y^{19} + \dots - 66784y + 9409)$
c_6	$(y^3 - 2y^2 + 5y - 1)(y^{10} - 12y^9 + \dots + 16y + 1) \\ \cdot (y^{20} - 35y^{19} + \dots - 16056826y + 4695889)$
c_7, c_8, c_{11}	$y^3(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2 \\ \cdot (y^{20} + 37y^{19} + \dots + 27075y + 3844)$
c_9	$((y + 1)^{10})(y^3 + 2y^2 + y - 1)(y^{20} + 39y^{19} + \dots + 6088y + 289)$
c_{10}	$((y + 1)^{10})(y^3 + 2y^2 + y - 1)(y^{20} - 5y^{19} + \dots - 120y + 289)$
c_{12}	$(y^3 - 2y^2 + 5y - 1)(y^{10} + 2y^9 + \dots - 2650y + 625) \\ \cdot (y^{20} + 47y^{19} + \dots + 412468y + 22801)$