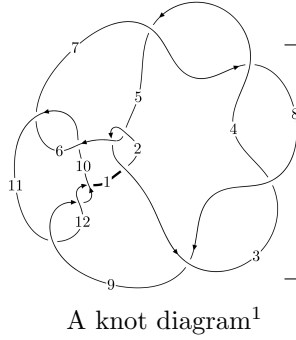
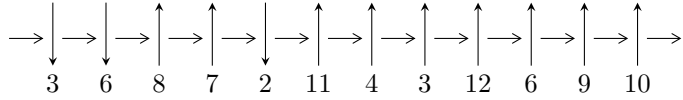


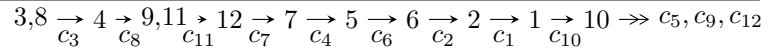
12n₀₄₅₄ (K12n₀₄₅₄)



Linearized knot diagram



Solving Sequence



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -5.34392 \times 10^{24}u^{30} + 1.20403 \times 10^{25}u^{29} + \dots + 2.13898 \times 10^{24}b - 8.19442 \times 10^{25}, \\ - 5.24612 \times 10^{24}u^{30} + 1.21449 \times 10^{25}u^{29} + \dots + 2.13898 \times 10^{24}a - 6.53057 \times 10^{25}, \\ u^{31} - 2u^{30} + \dots + 28u + 4 \rangle$$

$$I_2^u = \langle 3b - u - 2, 3a + 2u + 1, u^2 + u + 1 \rangle$$

$$I_3^u = \langle au + 3b - 4a + 2u + 1, 2a^2 - 3au + 2a + u - 3, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - v + 2, v^2 - 3v + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 39 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -5.34 \times 10^{24} u^{30} + 1.20 \times 10^{25} u^{29} + \cdots + 2.14 \times 10^{24} b - 8.19 \times 10^{25}, -5.25 \times 10^{24} u^{30} + 1.21 \times 10^{25} u^{29} + \cdots + 2.14 \times 10^{24} a - 6.53 \times 10^{25}, u^{31} - 2u^{30} + \cdots + 28u + 4 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 2.45262u^{30} - 5.67789u^{29} + \cdots + 112.994u + 30.5312 \\ 2.49834u^{30} - 5.62900u^{29} + \cdots + 123.421u + 38.3098 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 2.40875u^{30} - 5.56826u^{29} + \cdots + 108.882u + 29.9698 \\ 2.45447u^{30} - 5.51937u^{29} + \cdots + 119.309u + 37.7485 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.185869u^{30} - 0.506326u^{29} + \cdots + 8.73363u - 0.480369 \\ 0.954311u^{30} - 2.13631u^{29} + \cdots + 45.6943u + 14.8328 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1.20265u^{30} - 2.80559u^{29} + \cdots + 57.4529u + 14.8908 \\ -1.14984u^{30} + 2.60951u^{29} + \cdots - 55.1167u - 16.9723 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0528171u^{30} - 0.196085u^{29} + \cdots + 2.33621u - 2.08152 \\ -1.14984u^{30} + 2.60951u^{29} + \cdots - 55.1167u - 16.9723 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.871927u^{30} + 2.04345u^{29} + \cdots - 48.9524u - 11.3712 \\ 2.44025u^{30} - 5.52900u^{29} + \cdots + 118.778u + 35.8466 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = \frac{40150014847740772034704846}{1604238713781269697683811} u^{30} - \frac{30333063294678849729282082}{534746237927089899227937} u^{29} + \cdots + \frac{642744006791888105510144570}{534746237927089899227937} u + \frac{616846322292496574153802580}{1604238713781269697683811}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{31} + 34u^{30} + \dots + 16249u + 361$
c_2, c_5	$u^{31} + 4u^{30} + \dots - 17u + 19$
c_3, c_4, c_7 c_8	$u^{31} + 2u^{30} + \dots + 28u - 4$
c_6, c_{10}	$u^{31} + 2u^{30} + \dots - 36u - 36$
c_9, c_{11}, c_{12}	$u^{31} + 6u^{30} + \dots + 5u + 9$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{31} - 74y^{30} + \dots + 131918441y - 130321$
c_2, c_5	$y^{31} - 34y^{30} + \dots + 16249y - 361$
c_3, c_4, c_7 c_8	$y^{31} + 40y^{30} + \dots + 272y - 16$
c_6, c_{10}	$y^{31} + 6y^{30} + \dots + 2232y - 1296$
c_9, c_{11}, c_{12}	$y^{31} - 20y^{30} + \dots + 223y - 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.150087 + 0.994909I$ $a = 0.49984 - 1.89088I$ $b = 1.130920 - 0.806791I$	$-3.71035 - 1.41787I$	$3.38804 + 1.32048I$
$u = -0.150087 - 0.994909I$ $a = 0.49984 + 1.89088I$ $b = 1.130920 + 0.806791I$	$-3.71035 + 1.41787I$	$3.38804 - 1.32048I$
$u = 0.949025 + 0.259341I$ $a = -0.072682 + 0.704869I$ $b = 0.582494 - 0.117627I$	$-3.71574 - 2.40842I$	$3.33618 + 2.66984I$
$u = 0.949025 - 0.259341I$ $a = -0.072682 - 0.704869I$ $b = 0.582494 + 0.117627I$	$-3.71574 + 2.40842I$	$3.33618 - 2.66984I$
$u = -0.761649 + 0.761026I$ $a = -0.101228 + 0.295647I$ $b = -0.778145 - 0.069572I$	$1.17088 - 2.70519I$	$1.34730 + 7.26275I$
$u = -0.761649 - 0.761026I$ $a = -0.101228 - 0.295647I$ $b = -0.778145 + 0.069572I$	$1.17088 + 2.70519I$	$1.34730 - 7.26275I$
$u = 0.801880 + 0.845490I$ $a = 0.192710 + 0.190905I$ $b = 1.308920 - 0.176651I$	$-5.44830 + 8.20678I$	$3.96431 - 6.25123I$
$u = 0.801880 - 0.845490I$ $a = 0.192710 - 0.190905I$ $b = 1.308920 + 0.176651I$	$-5.44830 - 8.20678I$	$3.96431 + 6.25123I$
$u = 0.518296 + 1.138380I$ $a = 0.075776 + 0.484959I$ $b = -0.478186 - 0.043766I$	$-8.10871 + 2.46499I$	0
$u = 0.518296 - 1.138380I$ $a = 0.075776 - 0.484959I$ $b = -0.478186 + 0.043766I$	$-8.10871 - 2.46499I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.239573 + 1.258650I$ $a = -0.049051 + 0.239996I$ $b = -0.174354 - 0.870729I$	$3.35227 - 2.03069I$	$6.00000 + 0.I$
$u = -0.239573 - 1.258650I$ $a = -0.049051 - 0.239996I$ $b = -0.174354 + 0.870729I$	$3.35227 + 2.03069I$	$6.00000 + 0.I$
$u = -0.049257 + 0.651330I$ $a = 0.031163 + 0.438228I$ $b = 0.636530 + 0.528351I$	$-1.02719 - 1.35876I$	$0.38562 + 5.54408I$
$u = -0.049257 - 0.651330I$ $a = 0.031163 - 0.438228I$ $b = 0.636530 - 0.528351I$	$-1.02719 + 1.35876I$	$0.38562 - 5.54408I$
$u = -0.01769 + 1.49068I$ $a = -1.84020 + 1.15884I$ $b = -2.05375 + 1.80415I$	$-4.97013 + 0.88940I$	0
$u = -0.01769 - 1.49068I$ $a = -1.84020 - 1.15884I$ $b = -2.05375 - 1.80415I$	$-4.97013 - 0.88940I$	0
$u = 0.146387 + 0.409089I$ $a = 0.10548 - 1.80116I$ $b = -1.016560 + 0.397771I$	$1.43804 + 0.67860I$	$5.66172 + 1.82882I$
$u = 0.146387 - 0.409089I$ $a = 0.10548 + 1.80116I$ $b = -1.016560 - 0.397771I$	$1.43804 - 0.67860I$	$5.66172 - 1.82882I$
$u = -0.333653$ $a = 4.41543$ $b = -0.313107$	7.50433	24.5590
$u = 0.06381 + 1.68753I$ $a = 1.345990 + 0.237815I$ $b = 1.82999 - 0.04669I$	$-9.31296 - 0.73241I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.06381 - 1.68753I$ $a = 1.345990 - 0.237815I$ $b = 1.82999 + 0.04669I$	$-9.31296 + 0.73241I$	0
$u = 0.26352 + 1.68744I$ $a = 1.67424 + 0.15516I$ $b = 2.20381 - 0.62844I$	$-13.9459 + 12.3803I$	0
$u = 0.26352 - 1.68744I$ $a = 1.67424 - 0.15516I$ $b = 2.20381 + 0.62844I$	$-13.9459 - 12.3803I$	0
$u = -0.18187 + 1.70595I$ $a = -1.372120 - 0.010334I$ $b = -1.81881 - 0.60789I$	$-7.53329 - 6.21670I$	0
$u = -0.18187 - 1.70595I$ $a = -1.372120 + 0.010334I$ $b = -1.81881 + 0.60789I$	$-7.53329 + 6.21670I$	0
$u = -0.283237$ $a = -1.71193$ $b = -0.227764$	0.766548	14.0280
$u = -0.03812 + 1.72844I$ $a = 1.237920 - 0.134015I$ $b = 1.67073 + 0.76279I$	$-13.51010 - 2.18010I$	0
$u = -0.03812 - 1.72844I$ $a = 1.237920 + 0.134015I$ $b = 1.67073 - 0.76279I$	$-13.51010 + 2.18010I$	0
$u = -0.260390$ $a = -0.560132$ $b = 2.58879$	-0.450742	39.0360
$u = 0.13397 + 1.76472I$ $a = -1.46619 - 0.05769I$ $b = -2.23420 - 0.13354I$	$-18.3679 + 5.2164I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.13397 - 1.76472I$		
$a = -1.46619 + 0.05769I$	$-18.3679 - 5.2164I$	0
$b = -2.23420 + 0.13354I$		

$$\text{II. } I_2^u = \langle 3b - u - 2, 3a + 2u + 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{2}{3}u - \frac{1}{3} \\ \frac{1}{3}u + \frac{2}{3} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{5}{3}u - \frac{1}{3} \\ -\frac{2}{3}u + \frac{2}{3} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{2}{3}u - \frac{1}{3} \\ \frac{1}{3}u + \frac{2}{3} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $\frac{4}{3}u + 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_4 c_5	$u^2 + u + 1$
c_2, c_7, c_8	$u^2 - u + 1$
c_6, c_{10}	u^2
c_9	$(u + 1)^2$
c_{11}, c_{12}	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_5, c_7 c_8	$y^2 + y + 1$
c_6, c_{10}	y^2
c_9, c_{11}, c_{12}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = -0.577350I$	$1.64493 - 2.02988I$	$6.33333 + 1.15470I$
$b = 0.500000 + 0.288675I$		
$u = -0.500000 - 0.866025I$		
$a = 0.577350I$	$1.64493 + 2.02988I$	$6.33333 - 1.15470I$
$b = 0.500000 - 0.288675I$		

$$\text{III. } I_3^u = \langle au + 3b - 4a + 2u + 1, 2a^2 - 3au + 2a + u - 3, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -\frac{1}{3}au + \frac{4}{3}a - \frac{2}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{2}{3}au + \frac{1}{3}a + \frac{4}{3}u + \frac{2}{3} \\ \frac{1}{3}au + \frac{2}{3}a + \frac{2}{3}u + \frac{1}{3} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{3}au + \frac{1}{3}a - \frac{7}{6}u - \frac{4}{3} \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{3}au + \frac{1}{3}a - \frac{7}{6}u - \frac{1}{3} \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{3}au + \frac{1}{3}a - \frac{7}{6}u - \frac{4}{3} \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -au + a - \frac{3}{2}u - 2 \\ -\frac{2}{3}au + \frac{2}{3}a - \frac{1}{3}u - \frac{5}{3} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$(u - 1)^4$
c_2	$(u + 1)^4$
c_3, c_4, c_7 c_8	$(u^2 + 2)^2$
c_6, c_{11}, c_{12}	$(u^2 + u - 1)^2$
c_9, c_{10}	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^4$
c_3, c_4, c_7 c_8	$(y + 2)^4$
c_6, c_9, c_{10} c_{11}, c_{12}	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.414210I$		
$a = 0.618034 + 0.270091I$	2.30291	4.00000
$b = 0.618034 - 0.874032I$		
$u = 1.414210I$		
$a = -1.61803 + 1.85123I$	-5.59278	4.00000
$b = -1.61803 + 2.28825I$		
$u = -1.414210I$		
$a = 0.618034 - 0.270091I$	2.30291	4.00000
$b = 0.618034 + 0.874032I$		
$u = -1.414210I$		
$a = -1.61803 - 1.85123I$	-5.59278	4.00000
$b = -1.61803 - 2.28825I$		

$$\text{IV. } I_1^v = \langle a, b - v + 2, v^2 - 3v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ v - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2v - 1 \\ v - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -v + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -v \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2v + 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^2$
c_3, c_4, c_7 c_8	u^2
c_5	$(u + 1)^2$
c_6, c_9	$u^2 - u - 1$
c_{10}, c_{11}, c_{12}	$u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^2$
c_3, c_4, c_7 c_8	y^2
c_6, c_9, c_{10} c_{11}, c_{12}	$y^2 - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.381966$ $a = 0$ $b = -1.61803$	-0.657974	-6.00000
$v = 2.61803$ $a = 0$ $b = 0.618034$	7.23771	-6.00000

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^6)(u^2 + u + 1)(u^{31} + 34u^{30} + \dots + 16249u + 361)$
c_2	$((u - 1)^2)(u + 1)^4(u^2 - u + 1)(u^{31} + 4u^{30} + \dots - 17u + 19)$
c_3, c_4	$u^2(u^2 + 2)^2(u^2 + u + 1)(u^{31} + 2u^{30} + \dots + 28u - 4)$
c_5	$((u - 1)^4)(u + 1)^2(u^2 + u + 1)(u^{31} + 4u^{30} + \dots - 17u + 19)$
c_6	$u^2(u^2 - u - 1)(u^2 + u - 1)^2(u^{31} + 2u^{30} + \dots - 36u - 36)$
c_7, c_8	$u^2(u^2 + 2)^2(u^2 - u + 1)(u^{31} + 2u^{30} + \dots + 28u - 4)$
c_9	$((u + 1)^2)(u^2 - u - 1)^3(u^{31} + 6u^{30} + \dots + 5u + 9)$
c_{10}	$u^2(u^2 - u - 1)^2(u^2 + u - 1)(u^{31} + 2u^{30} + \dots - 36u - 36)$
c_{11}, c_{12}	$((u - 1)^2)(u^2 + u - 1)^3(u^{31} + 6u^{30} + \dots + 5u + 9)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^6)(y^2 + y + 1)(y^{31} - 74y^{30} + \dots + 1.31918 \times 10^8 y - 130321)$
c_2, c_5	$((y - 1)^6)(y^2 + y + 1)(y^{31} - 34y^{30} + \dots + 16249y - 361)$
c_3, c_4, c_7 c_8	$y^2(y + 2)^4(y^2 + y + 1)(y^{31} + 40y^{30} + \dots + 272y - 16)$
c_6, c_{10}	$y^2(y^2 - 3y + 1)^3(y^{31} + 6y^{30} + \dots + 2232y - 1296)$
c_9, c_{11}, c_{12}	$((y - 1)^2)(y^2 - 3y + 1)^3(y^{31} - 20y^{30} + \dots + 223y - 81)$