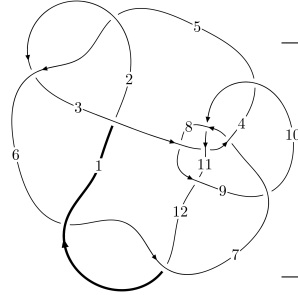
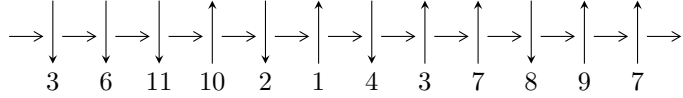


12n₀₄₅₈ (K12n₀₄₅₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3, 11 \xrightarrow{c_3} 4, 9 \xrightarrow{c_{11}} 12 \xrightarrow{c_8} 8 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 1 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \rightsquigarrow c_1, c_4, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 5.47880 \times 10^{25} u^{40} + 7.88111 \times 10^{25} u^{39} + \dots + 1.50975 \times 10^{24} b + 6.96929 \times 10^{25}, \\ -1.08127 \times 10^{26} u^{40} - 1.53797 \times 10^{26} u^{39} + \dots + 1.50975 \times 10^{24} a - 1.21442 \times 10^{26}, u^{41} + u^{40} + \dots + 2u + \dots \rangle$$

$$I_2^u = \langle -2.49556 \times 10^{86} u^{43} - 8.35365 \times 10^{86} u^{42} + \dots + 3.43675 \times 10^{87} b + 3.73757 \times 10^{87}, \\ 2.75946 \times 10^{87} u^{43} + 1.12653 \times 10^{88} u^{42} + \dots + 5.84247 \times 10^{88} a + 3.07830 \times 10^{89}, u^{44} + 4u^{43} + \dots + 77u + \dots \rangle$$

$$I_3^u = \langle -u^{18} + u^{17} + \dots + b + 4u, -4u^{18} + 4u^{17} + \dots + a - 1, u^{19} - u^{18} + \dots - 4u^2 + 1 \rangle$$

$$I_4^u = \langle b - u - 1, a - u - 1, u^2 + u + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 106 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 5.48 \times 10^{25} u^{40} + 7.88 \times 10^{25} u^{39} + \dots + 1.51 \times 10^{24} b + 6.97 \times 10^{25}, -1.08 \times 10^{26} u^{40} - 1.54 \times 10^{26} u^{39} + \dots + 1.51 \times 10^{24} a - 1.21 \times 10^{26}, u^{41} + u^{40} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 71.6189u^{40} + 101.869u^{39} + \dots + 340.999u + 80.4384 \\ -36.2894u^{40} - 52.2014u^{39} + \dots - 199.232u - 46.1618 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -64.2074u^{40} - 87.5660u^{39} + \dots - 425.889u - 95.1075 \\ -18.2487u^{40} - 25.7511u^{39} + \dots - 53.4475u - 14.3937 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 107.908u^{40} + 154.070u^{39} + \dots + 540.231u + 126.600 \\ -36.2894u^{40} - 52.2014u^{39} + \dots - 199.232u - 46.1618 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 107.908u^{40} + 154.070u^{39} + \dots + 541.231u + 126.600 \\ -36.2894u^{40} - 52.2014u^{39} + \dots - 199.232u - 46.1618 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -197.492u^{40} - 281.182u^{39} + \dots - 1214.12u - 264.909 \\ -0.0153376u^{40} - 1.23868u^{39} + \dots + 111.193u + 23.1345 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 74.2253u^{40} + 243.405u^{39} + \dots + 1398.14u + 562.092 \\ 39.9044u^{40} + 24.6029u^{39} + \dots - 18.7145u - 94.6713 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -197.477u^{40} - 279.943u^{39} + \dots - 1325.31u - 288.043 \\ -0.0153376u^{40} - 1.23868u^{39} + \dots + 111.193u + 23.1345 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -64.8577u^{40} - 25.7158u^{39} + \dots + 90.6679u + 163.055 \\ -22.8032u^{40} - 1.56551u^{39} + \dots + 55.9091u + 43.7009 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.594704u^{40} + 4.62146u^{39} + \dots - 162.562u - 30.5253 \\ -46.5535u^{40} - 66.4364u^{39} + \dots - 207.880u - 50.1886 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= \frac{46609776655609602573804741}{1509752124425304287631895} u^{40} - \frac{555844712353330908256438968}{1509752124425304287631895} u^{39} + \\ &\dots - \frac{4270771601823530319752574608}{1509752124425304287631895} u - \frac{2076142798565092784971764701}{1509752124425304287631895} \end{aligned}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $u^{41} + 19u^{40} + \dots + 89u + 16$ |
| c_2, c_5 | $u^{41} + 5u^{40} + \dots + 7u + 4$ |
| c_3, c_7 | $u^{41} + u^{40} + \dots + 2u + 1$ |
| c_4, c_8 | $u^{41} - 9u^{39} + \dots - 69u + 17$ |
| c_6, c_{12} | $u^{41} + 15u^{40} + \dots + 87u + 4$ |
| c_9, c_{11} | $u^{41} - 4u^{40} + \dots + 27u + 1$ |
| c_{10} | $u^{41} - 26u^{40} + \dots + 23u - 2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1 | $y^{41} + 9y^{40} + \dots - 3311y - 256$ |
| c_2, c_5 | $y^{41} - 19y^{40} + \dots + 89y - 16$ |
| c_3, c_7 | $y^{41} + 17y^{40} + \dots - 36y - 1$ |
| c_4, c_8 | $y^{41} - 18y^{40} + \dots + 5577y - 289$ |
| c_6, c_{12} | $y^{41} + y^{40} + \dots + 633y - 16$ |
| c_9, c_{11} | $y^{41} - 58y^{40} + \dots + 333y - 1$ |
| c_{10} | $y^{41} + 68y^{39} + \dots + 81y - 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 0.347021 + 1.021800I$ $a = 0.446471 + 0.717252I$ $b = 0.856068 + 0.901582I$ | $2.01077 + 1.97128I$ | 0 |
| $u = 0.347021 - 1.021800I$ $a = 0.446471 - 0.717252I$ $b = 0.856068 - 0.901582I$ | $2.01077 - 1.97128I$ | 0 |
| $u = -0.517326 + 0.952123I$ $a = -0.494773 + 0.392816I$ $b = -1.002680 + 0.556094I$ | $2.33608 + 2.70211I$ | 0 |
| $u = -0.517326 - 0.952123I$ $a = -0.494773 - 0.392816I$ $b = -1.002680 - 0.556094I$ | $2.33608 - 2.70211I$ | 0 |
| $u = -0.380066 + 0.811067I$ $a = 0.82614 + 1.79073I$ $b = 0.853726 - 0.187521I$ | $4.94484 - 5.32421I$ | $4.21074 + 0.90918I$ |
| $u = -0.380066 - 0.811067I$ $a = 0.82614 - 1.79073I$ $b = 0.853726 + 0.187521I$ | $4.94484 + 5.32421I$ | $4.21074 - 0.90918I$ |
| $u = 0.054668 + 1.145580I$ $a = 0.106091 + 1.208380I$ $b = 0.17829 + 1.44060I$ | $1.57207 - 1.96637I$ | 0 |
| $u = 0.054668 - 1.145580I$ $a = 0.106091 - 1.208380I$ $b = 0.17829 - 1.44060I$ | $1.57207 + 1.96637I$ | 0 |
| $u = 0.358415 + 0.770361I$ $a = -0.68843 + 2.01808I$ $b = -0.906548 - 0.088949I$ | $6.85307 + 0.06384I$ | $7.45973 + 4.03926I$ |
| $u = 0.358415 - 0.770361I$ $a = -0.68843 - 2.01808I$ $b = -0.906548 + 0.088949I$ | $6.85307 - 0.06384I$ | $7.45973 - 4.03926I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.045169 + 0.822753I$ $a = -0.154528 + 1.094100I$ $b = 0.346455 + 0.374027I$ | $1.46454 + 1.46331I$ | $5.06919 - 4.70044I$ |
| $u = -0.045169 - 0.822753I$ $a = -0.154528 - 1.094100I$ $b = 0.346455 - 0.374027I$ | $1.46454 - 1.46331I$ | $5.06919 + 4.70044I$ |
| $u = -0.229168 + 0.751258I$ $a = -0.04740 + 1.82480I$ $b = 0.739876 + 0.180844I$ | $1.64581 + 1.65716I$ | $2.62674 - 4.29220I$ |
| $u = -0.229168 - 0.751258I$ $a = -0.04740 - 1.82480I$ $b = 0.739876 - 0.180844I$ | $1.64581 - 1.65716I$ | $2.62674 + 4.29220I$ |
| $u = 0.325313 + 0.680386I$ $a = -0.29563 + 2.60667I$ $b = -1.039970 + 0.122963I$ | $7.08787 - 2.96529I$ | $8.51449 + 5.47804I$ |
| $u = 0.325313 - 0.680386I$ $a = -0.29563 - 2.60667I$ $b = -1.039970 - 0.122963I$ | $7.08787 + 2.96529I$ | $8.51449 - 5.47804I$ |
| $u = -0.314460 + 0.648327I$ $a = 0.08581 + 2.85549I$ $b = 1.088460 + 0.205257I$ | $5.38587 + 8.24752I$ | $6.33209 - 10.48383I$ |
| $u = -0.314460 - 0.648327I$ $a = 0.08581 - 2.85549I$ $b = 1.088460 - 0.205257I$ | $5.38587 - 8.24752I$ | $6.33209 + 10.48383I$ |
| $u = 1.054420 + 0.767365I$ $a = 0.225727 - 0.075550I$ $b = 0.757531 - 0.087155I$ | $-5.03812 + 0.55979I$ | 0 |
| $u = 1.054420 - 0.767365I$ $a = 0.225727 + 0.075550I$ $b = 0.757531 + 0.087155I$ | $-5.03812 - 0.55979I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.954640 + 0.895605I$ $a = -0.323203 - 0.114281I$ $b = -0.907475 - 0.104542I$ | $-1.12434 + 3.55718I$ | 0 |
| $u = -0.954640 - 0.895605I$ $a = -0.323203 + 0.114281I$ $b = -0.907475 + 0.104542I$ | $-1.12434 - 3.55718I$ | 0 |
| $u = -0.652653$ $a = -0.0877425$ $b = -0.483905$ | -1.46612 | -7.06880 |
| $u = -0.001515 + 0.601854I$ $a = -0.852039 + 0.542047I$ $b = 0.481262 + 0.639634I$ | $0.81408 + 1.37351I$ | $2.99559 - 3.76838I$ |
| $u = -0.001515 - 0.601854I$ $a = -0.852039 - 0.542047I$ $b = 0.481262 - 0.639634I$ | $0.81408 - 1.37351I$ | $2.99559 + 3.76838I$ |
| $u = 1.03621 + 0.97465I$ $a = 0.272897 - 0.206391I$ $b = 0.879946 - 0.246548I$ | $-4.42034 - 8.30464I$ | 0 |
| $u = 1.03621 - 0.97465I$ $a = 0.272897 + 0.206391I$ $b = 0.879946 + 0.246548I$ | $-4.42034 + 8.30464I$ | 0 |
| $u = 0.051342 + 0.543114I$ $a = 1.57833 + 0.32834I$ $b = -0.542371 + 0.798966I$ | $-1.14789 - 5.43637I$ | $-0.71682 + 6.54388I$ |
| $u = 0.051342 - 0.543114I$ $a = 1.57833 - 0.32834I$ $b = -0.542371 - 0.798966I$ | $-1.14789 + 5.43637I$ | $-0.71682 - 6.54388I$ |
| $u = -0.005268 + 0.490051I$ $a = 0.720841 - 0.530154I$ $b = -0.243798 + 0.805884I$ | $-2.19779 + 1.00862I$ | $-5.99392 - 1.40222I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.005268 - 0.490051I$ $a = 0.720841 + 0.530154I$ $b = -0.243798 - 0.805884I$ | $-2.19779 - 1.00862I$ | $-5.99392 + 1.40222I$ |
| $u = -0.92388 + 1.21329I$ $a = -0.693432 - 0.848976I$ $b = -1.60443 - 0.79675I$ | $7.22406 + 2.19782I$ | 0 |
| $u = -0.92388 - 1.21329I$ $a = -0.693432 + 0.848976I$ $b = -1.60443 + 0.79675I$ | $7.22406 - 2.19782I$ | 0 |
| $u = 0.93985 + 1.21945I$ $a = 0.624751 - 0.961319I$ $b = 1.57161 - 0.93510I$ | $8.66754 - 7.90114I$ | 0 |
| $u = 0.93985 - 1.21945I$ $a = 0.624751 + 0.961319I$ $b = 1.57161 + 0.93510I$ | $8.66754 + 7.90114I$ | 0 |
| $u = -0.96302 + 1.20795I$ $a = -0.367468 - 0.971278I$ $b = -1.31719 - 1.03611I$ | $1.99155 + 9.34995I$ | 0 |
| $u = -0.96302 - 1.20795I$ $a = -0.367468 + 0.971278I$ $b = -1.31719 + 1.03611I$ | $1.99155 - 9.34995I$ | 0 |
| $u = 0.96655 + 1.22224I$ $a = 0.421833 - 1.155040I$ $b = 1.43574 - 1.19661I$ | $7.8645 - 11.8540I$ | 0 |
| $u = 0.96655 - 1.22224I$ $a = 0.421833 + 1.155040I$ $b = 1.43574 + 1.19661I$ | $7.8645 + 11.8540I$ | 0 |
| $u = -0.97295 + 1.22134I$ $a = -0.348119 - 1.207570I$ $b = -1.38255 - 1.27245I$ | $5.7918 + 17.4569I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.97295 - 1.22134I$ | | |
| $a = -0.348119 + 1.207570I$ | $5.7918 - 17.4569I$ | 0 |
| $b = -1.38255 + 1.27245I$ | | |

$$\text{II. } I_2^u = \langle -2.50 \times 10^{86} u^{43} - 8.35 \times 10^{86} u^{42} + \dots + 3.44 \times 10^{87} b + 3.74 \times 10^{87}, 2.76 \times 10^{87} u^{43} + 1.13 \times 10^{88} u^{42} + \dots + 5.84 \times 10^{88} a + 3.08 \times 10^{89}, u^{44} + 4u^{43} + \dots + 77u + 17 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0472311u^{43} - 0.192817u^{42} + \dots - 14.3118u - 5.26884 \\ 0.0726141u^{43} + 0.243068u^{42} + \dots - 1.78608u - 1.08753 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0360992u^{43} - 0.157605u^{42} + \dots - 15.0581u - 5.83261 \\ 0.0702088u^{43} + 0.234463u^{42} + \dots - 1.55171u - 1.42798 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.119845u^{43} - 0.435885u^{42} + \dots - 12.5257u - 4.18131 \\ 0.0726141u^{43} + 0.243068u^{42} + \dots - 1.78608u - 1.08753 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0588235u^{43} - 0.235294u^{42} + \dots - 13u - 4.52941 \\ 0.0610217u^{43} + 0.200591u^{42} + \dots + 0.525708u - 0.348105 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.101101u^{43} - 0.408588u^{42} + \dots - 18.6194u - 7.52962 \\ 0.00441605u^{43} - 0.0127382u^{42} + \dots - 3.21768u - 1.61521 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0490639u^{43} - 0.254746u^{42} + \dots - 9.79483u - 5.26468 \\ 0.0362894u^{43} + 0.127630u^{42} + \dots - 0.376828u - 1.15074 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.105517u^{43} - 0.395849u^{42} + \dots - 15.4017u - 5.91441 \\ 0.00441605u^{43} - 0.0127382u^{42} + \dots - 3.21768u - 1.61521 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.142243u^{43} + 0.513366u^{42} + \dots + 14.5329u + 3.09094 \\ -0.00902369u^{43} - 0.0430917u^{42} + \dots - 3.30811u - 1.10503 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0606353u^{43} - 0.229405u^{42} + \dots - 7.19891u - 3.39724 \\ -0.0456727u^{43} - 0.162664u^{42} + \dots - 4.30750u - 1.00739 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-0.861289u^{43} - 3.44599u^{42} + \dots - 97.7115u - 26.0425$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $(u^{22} + 10u^{21} + \dots + 6u^2 + 1)^2$ |
| c_2, c_5 | $(u^{22} - 2u^{21} + \dots - 5u^3 + 1)^2$ |
| c_3, c_7 | $u^{44} + 4u^{43} + \dots + 77u + 17$ |
| c_4, c_8 | $u^{44} + 2u^{43} + \dots - 7681u + 1663$ |
| c_6, c_{12} | $(u^{22} - 9u^{21} + \dots - 27u + 8)^2$ |
| c_9, c_{11} | $u^{44} - 3u^{43} + \dots - 5634u + 459$ |
| c_{10} | $(u^{22} + 9u^{21} + \dots + u + 2)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1 | $(y^{22} + 6y^{21} + \dots + 12y + 1)^2$ |
| c_2, c_5 | $(y^{22} - 10y^{21} + \dots + 6y^2 + 1)^2$ |
| c_3, c_7 | $y^{44} - 8y^{43} + \dots + 1585y + 289$ |
| c_4, c_8 | $y^{44} - 20y^{43} + \dots + 60881257y + 2765569$ |
| c_6, c_{12} | $(y^{22} - 5y^{21} + \dots - 137y + 64)^2$ |
| c_9, c_{11} | $y^{44} - 23y^{43} + \dots + 46259586y + 210681$ |
| c_{10} | $(y^{22} + 3y^{21} + \dots + 43y + 4)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.466106 + 0.845310I$ $a = 0.120142 + 0.417834I$ $b = 1.67800 + 0.61371I$ | $-0.49172 + 7.76222I$ | $0.81633 - 10.97056I$ |
| $u = -0.466106 - 0.845310I$ $a = 0.120142 - 0.417834I$ $b = 1.67800 - 0.61371I$ | $-0.49172 - 7.76222I$ | $0.81633 + 10.97056I$ |
| $u = -0.612747 + 0.847167I$ $a = -0.309849 + 0.822684I$ $b = 1.14999 + 1.06245I$ | $-2.01009 + 2.56491I$ | $-5.72976 - 4.00419I$ |
| $u = -0.612747 - 0.847167I$ $a = -0.309849 - 0.822684I$ $b = 1.14999 - 1.06245I$ | $-2.01009 - 2.56491I$ | $-5.72976 + 4.00419I$ |
| $u = 0.899310 + 0.535213I$ $a = 1.22496 + 1.07887I$ $b = -0.208918 + 0.720383I$ | $-2.01009 - 2.56491I$ | $-5.72976 + 4.00419I$ |
| $u = 0.899310 - 0.535213I$ $a = 1.22496 - 1.07887I$ $b = -0.208918 - 0.720383I$ | $-2.01009 + 2.56491I$ | $-5.72976 - 4.00419I$ |
| $u = 0.667133 + 0.876190I$ $a = 0.565670 + 0.915397I$ $b = -0.73275 + 1.28707I$ | $-2.61181 - 5.56778I$ | $-6.67774 + 6.14625I$ |
| $u = 0.667133 - 0.876190I$ $a = 0.565670 - 0.915397I$ $b = -0.73275 - 1.28707I$ | $-2.61181 + 5.56778I$ | $-6.67774 - 6.14625I$ |
| $u = 0.420458 + 0.759517I$ $a = 0.0506571 + 0.0690852I$ $b = -1.51754 + 0.25724I$ | $0.63374 - 3.32247I$ | $4.93738 + 4.78079I$ |
| $u = 0.420458 - 0.759517I$ $a = 0.0506571 - 0.0690852I$ $b = -1.51754 - 0.25724I$ | $0.63374 + 3.32247I$ | $4.93738 - 4.78079I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.592653 + 0.967467I$ | | |
| $a = 0.548691 + 0.593530I$ | $-2.49866 + 0.61650I$ | $-5.58678 - 1.76375I$ |
| $b = -0.351079 + 1.129330I$ | | |
| $u = 0.592653 - 0.967467I$ | | |
| $a = 0.548691 - 0.593530I$ | $-2.49866 - 0.61650I$ | $-5.58678 + 1.76375I$ |
| $b = -0.351079 - 1.129330I$ | | |
| $u = -0.510707 + 0.679843I$ | | |
| $a = -0.82932 - 1.56718I$ | $4.38951 + 8.87036I$ | $2.10374 - 11.14588I$ |
| $b = -1.70942 - 1.64533I$ | | |
| $u = -0.510707 - 0.679843I$ | | |
| $a = -0.82932 + 1.56718I$ | $4.38951 - 8.87036I$ | $2.10374 + 11.14588I$ |
| $b = -1.70942 + 1.64533I$ | | |
| $u = -0.748334 + 0.350797I$ | | |
| $a = -1.67537 + 0.57034I$ | $-2.61181 + 5.56778I$ | $-6.67774 - 6.14625I$ |
| $b = 0.087323 + 0.207716I$ | | |
| $u = -0.748334 - 0.350797I$ | | |
| $a = -1.67537 - 0.57034I$ | $-2.61181 - 5.56778I$ | $-6.67774 + 6.14625I$ |
| $b = 0.087323 - 0.207716I$ | | |
| $u = 0.438421 + 0.674226I$ | | |
| $a = 0.90058 - 1.59216I$ | $6.45761 - 3.23482I$ | $6.36482 + 6.95069I$ |
| $b = 1.81717 - 1.62217I$ | | |
| $u = 0.438421 - 0.674226I$ | | |
| $a = 0.90058 + 1.59216I$ | $6.45761 + 3.23482I$ | $6.36482 - 6.95069I$ |
| $b = 1.81717 + 1.62217I$ | | |
| $u = -0.784806 + 0.951389I$ | | |
| $a = -0.431263 + 0.864629I$ | $-0.29493 + 2.91734I$ | $2.41857 - 2.23849I$ |
| $b = 0.541102 + 0.996237I$ | | |
| $u = -0.784806 - 0.951389I$ | | |
| $a = -0.431263 - 0.864629I$ | $-0.29493 - 2.91734I$ | $2.41857 + 2.23849I$ |
| $b = 0.541102 - 0.996237I$ | | |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = -0.149975 + 0.738011I$ $a = -0.89919 - 1.49365I$ $b = -2.06203 - 1.36914I$ | $5.86334 - 6.33920I$ | $7.62789 + 3.75640I$ |
| $u = -0.149975 - 0.738011I$ $a = -0.89919 + 1.49365I$ $b = -2.06203 + 1.36914I$ | $5.86334 + 6.33920I$ | $7.62789 - 3.75640I$ |
| $u = 0.229621 + 0.711467I$ $a = 0.93052 - 1.58410I$ $b = 2.01034 - 1.49221I$ | $7.29150 + 0.70655I$ | $9.80660 + 2.74214I$ |
| $u = 0.229621 - 0.711467I$ $a = 0.93052 + 1.58410I$ $b = 2.01034 + 1.49221I$ | $7.29150 - 0.70655I$ | $9.80660 - 2.74214I$ |
| $u = 1.057640 + 0.711303I$ $a = 0.72238 + 1.49263I$ $b = -0.394766 + 1.085170I$ | $-0.49172 - 7.76222I$ | $0. + 10.97056I$ |
| $u = 1.057640 - 0.711303I$ $a = 0.72238 - 1.49263I$ $b = -0.394766 - 1.085170I$ | $-0.49172 + 7.76222I$ | $0. - 10.97056I$ |
| $u = -1.010300 + 0.819633I$ $a = -0.496055 + 1.296710I$ $b = 0.521329 + 1.021470I$ | $0.63374 + 3.32247I$ | $4.93738 - 4.78079I$ |
| $u = -1.010300 - 0.819633I$ $a = -0.496055 - 1.296710I$ $b = 0.521329 - 1.021470I$ | $0.63374 - 3.32247I$ | $4.93738 + 4.78079I$ |
| $u = 0.456405 + 0.493869I$ $a = 1.008840 - 0.278321I$ $b = -0.785235 - 0.137592I$ | $-0.29493 - 2.91734I$ | $2.41857 + 2.23849I$ |
| $u = 0.456405 - 0.493869I$ $a = 1.008840 + 0.278321I$ $b = -0.785235 + 0.137592I$ | $-0.29493 + 2.91734I$ | $2.41857 - 2.23849I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.352482 + 0.507121I$ $a = -1.07753 - 1.61193I$ $b = -1.91155 - 1.49298I$ | $0.543309 + 0.646462I$ | $7.41895 - 11.49115I$ |
| $u = -0.352482 - 0.507121I$ $a = -1.07753 + 1.61193I$ $b = -1.91155 + 1.49298I$ | $0.543309 - 0.646462I$ | $7.41895 + 11.49115I$ |
| $u = -0.439360 + 0.215788I$ $a = -2.17643 - 0.43074I$ $b = 0.249933 - 0.497594I$ | $-2.49866 - 0.61650I$ | $-5.58678 + 1.76375I$ |
| $u = -0.439360 - 0.215788I$ $a = -2.17643 + 0.43074I$ $b = 0.249933 + 0.497594I$ | $-2.49866 + 0.61650I$ | $-5.58678 - 1.76375I$ |
| $u = -1.42727 + 1.17674I$ $a = 0.732491 + 0.810544I$ $b = 0.999624 + 0.416425I$ | $5.86334 + 6.33920I$ | 0 |
| $u = -1.42727 - 1.17674I$ $a = 0.732491 - 0.810544I$ $b = 0.999624 - 0.416425I$ | $5.86334 - 6.33920I$ | 0 |
| $u = -1.58647 + 1.01845I$ $a = 0.919715 + 0.087483I$ $b = 0.855383 - 0.305806I$ | $4.38951 - 8.87036I$ | 0 |
| $u = -1.58647 - 1.01845I$ $a = 0.919715 - 0.087483I$ $b = 0.855383 + 0.305806I$ | $4.38951 + 8.87036I$ | 0 |
| $u = 1.49066 + 1.18106I$ $a = -0.792313 + 0.634501I$ $b = -0.974820 + 0.249567I$ | $7.29150 - 0.70655I$ | 0 |
| $u = 1.49066 - 1.18106I$ $a = -0.792313 - 0.634501I$ $b = -0.974820 - 0.249567I$ | $7.29150 + 0.70655I$ | 0 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.59443 + 1.07242I$ $a = -0.889783 + 0.221269I$ $b = -0.883190 - 0.162509I$ | $6.45761 + 3.23482I$ | 0 |
| $u = 1.59443 - 1.07242I$ $a = -0.889783 - 0.221269I$ $b = -0.883190 + 0.162509I$ | $6.45761 - 3.23482I$ | 0 |
| $u = -1.75816 + 1.21062I$ $a = 0.587756 + 0.268789I$ $b = 0.621112 + 0.027345I$ | $0.543309 - 0.646462I$ | 0 |
| $u = -1.75816 - 1.21062I$ $a = 0.587756 - 0.268789I$ $b = 0.621112 - 0.027345I$ | $0.543309 + 0.646462I$ | 0 |

III.

$$I_3^u = \langle -u^{18} + u^{17} + \dots + b + 4u, -4u^{18} + 4u^{17} + \dots + a - 1, u^{19} - u^{18} + \dots - 4u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 4u^{18} - 4u^{17} + \dots - 8u + 1 \\ u^{18} - u^{17} + \dots + u^2 - 4u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -8u^{18} + 9u^{17} + \dots + 14u - 4 \\ -4u^{18} + 4u^{17} + \dots + 9u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 3u^{18} - 3u^{17} + \dots - 4u + 1 \\ u^{18} - u^{17} + \dots + u^2 - 4u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 3u^{18} - 3u^{17} + \dots - 5u + 1 \\ u^{18} - u^{17} + \dots + u^2 - 4u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^{18} + 2u^{16} + \dots + 5u^2 - 2 \\ 2u^{18} - 3u^{17} + \dots - 3u + 2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -4u^{18} + 5u^{17} + \dots - 6u^2 + 8u \\ 3u^{18} - 3u^{17} + \dots + 9u^3 - 3u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -3u^{18} + 3u^{17} + \dots + 3u - 4 \\ 2u^{18} - 3u^{17} + \dots - 3u + 2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2u^{18} + 3u^{17} + \dots - 3u^3 - 1 \\ -u^{18} + 4u^{17} + \dots + 3u - 5 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^{18} + 2u^{17} + \dots + 2u - 2 \\ -3u^{18} + 3u^{17} + \dots + 5u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -7u^{18} + 12u^{17} + u^{16} - 22u^{15} - 16u^{14} + 59u^{13} - 18u^{12} - 76u^{11} + 20u^{10} + 87u^9 - 54u^8 - 93u^7 + 68u^6 + 56u^5 - 50u^4 - 29u^3 + 45u^2 + 11u - 15$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--------------------------------------|
| c_1 | $u^{19} - 10u^{18} + \dots + 4u - 1$ |
| c_2 | $u^{19} + 2u^{18} + \dots - 2u - 1$ |
| c_3, c_7 | $u^{19} - u^{18} + \dots - 4u^2 + 1$ |
| c_4, c_8 | $u^{19} - 4u^{17} + \dots - u + 1$ |
| c_5 | $u^{19} - 2u^{18} + \dots - 2u + 1$ |
| c_6 | $u^{19} - 6u^{18} + \dots + 14u - 3$ |
| c_9, c_{11} | $u^{19} - 8u^{18} + \dots + 5u - 1$ |
| c_{10} | $u^{19} + 11u^{18} + \dots + u - 3$ |
| c_{12} | $u^{19} + 6u^{18} + \dots + 14u + 3$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|--|
| c_1 | $y^{19} + 2y^{18} + \dots + 74y^3 - 1$ |
| c_2, c_5 | $y^{19} - 10y^{18} + \dots + 4y - 1$ |
| c_3, c_7 | $y^{19} - 5y^{18} + \dots + 8y - 1$ |
| c_4, c_8 | $y^{19} - 8y^{18} + \dots + 5y - 1$ |
| c_6, c_{12} | $y^{19} + 6y^{18} + \dots + 88y - 9$ |
| c_9, c_{11} | $y^{19} - 16y^{17} + \dots - 19y - 1$ |
| c_{10} | $y^{19} - 3y^{18} + \dots + 217y - 9$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = 0.571670 + 0.772339I$ $a = 1.062330 + 0.376696I$ $b = -0.619150 + 0.836486I$ | $-1.93329 - 0.79135I$ | $-1.90450 + 1.96423I$ |
| $u = 0.571670 - 0.772339I$ $a = 1.062330 - 0.376696I$ $b = -0.619150 - 0.836486I$ | $-1.93329 + 0.79135I$ | $-1.90450 - 1.96423I$ |
| $u = -0.691700 + 0.817412I$ $a = -0.700220 + 0.415999I$ $b = 0.603256 + 0.712894I$ | $-0.67906 + 4.36107I$ | $0.50991 - 7.74806I$ |
| $u = -0.691700 - 0.817412I$ $a = -0.700220 - 0.415999I$ $b = 0.603256 - 0.712894I$ | $-0.67906 - 4.36107I$ | $0.50991 + 7.74806I$ |
| $u = -0.694686 + 0.594925I$ $a = -0.687377 + 1.111670I$ $b = 0.830443 + 0.711186I$ | $-0.66120 + 2.86463I$ | $-0.58084 - 3.68051I$ |
| $u = -0.694686 - 0.594925I$ $a = -0.687377 - 1.111670I$ $b = 0.830443 - 0.711186I$ | $-0.66120 - 2.86463I$ | $-0.58084 + 3.68051I$ |
| $u = -0.901419$ $a = 1.36528$ $b = 1.10936$ | 0.308220 | -0.909270 |
| $u = 0.590402 + 0.625214I$ $a = 1.20330 + 1.01252I$ $b = -0.798416 + 0.845493I$ | $-1.76829 - 6.62156I$ | $-2.87860 + 10.87292I$ |
| $u = 0.590402 - 0.625214I$ $a = 1.20330 - 1.01252I$ $b = -0.798416 - 0.845493I$ | $-1.76829 + 6.62156I$ | $-2.87860 - 10.87292I$ |
| $u = 0.769919 + 0.066620I$ $a = -2.09450 + 0.55481I$ $b = -1.289190 + 0.111552I$ | $6.31789 - 1.80381I$ | $3.64499 + 0.37370I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.769919 - 0.066620I$ $a = -2.09450 - 0.55481I$ $b = -1.289190 - 0.111552I$ | $6.31789 + 1.80381I$ | $3.64499 - 0.37370I$ |
| $u = -0.756714 + 0.118401I$ $a = 1.98867 + 0.99926I$ $b = 1.289920 + 0.201830I$ | $4.58239 + 7.30195I$ | $0.96040 - 5.11591I$ |
| $u = -0.756714 - 0.118401I$ $a = 1.98867 - 0.99926I$ $b = 1.289920 - 0.201830I$ | $4.58239 - 7.30195I$ | $0.96040 + 5.11591I$ |
| $u = -0.966965 + 0.774347I$ $a = -0.231110 + 0.472518I$ $b = 0.630095 + 0.504581I$ | $-2.00054 + 3.89777I$ | $-3.98253 - 5.34580I$ |
| $u = -0.966965 - 0.774347I$ $a = -0.231110 - 0.472518I$ $b = 0.630095 - 0.504581I$ | $-2.00054 - 3.89777I$ | $-3.98253 + 5.34580I$ |
| $u = 1.100580 + 0.706359I$ $a = 0.062826 + 0.442679I$ $b = -0.643531 + 0.413021I$ | $-5.47313 + 0.16274I$ | $-9.10286 + 4.27042I$ |
| $u = 1.100580 - 0.706359I$ $a = 0.062826 - 0.442679I$ $b = -0.643531 - 0.413021I$ | $-5.47313 - 0.16274I$ | $-9.10286 - 4.27042I$ |
| $u = 1.028200 + 0.886045I$ $a = 0.213453 + 0.338188I$ $b = -0.558115 + 0.480952I$ | $-5.11861 - 8.27352I$ | $-8.71133 + 6.81608I$ |
| $u = 1.028200 - 0.886045I$ $a = 0.213453 - 0.338188I$ $b = -0.558115 - 0.480952I$ | $-5.11861 + 8.27352I$ | $-8.71133 - 6.81608I$ |

$$\text{IV. } I_4^u = \langle b - u - 1, a - u - 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u + 1 \\ u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u - 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u + 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u - 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u + 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -3

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| c_1, c_2, c_9 c_{11} | $(u - 1)^2$ |
| c_3, c_4, c_7 c_8 | $u^2 + u + 1$ |
| c_5 | $(u + 1)^2$ |
| c_6, c_{10}, c_{12} | u^2 |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|----------------------------------|------------------------------------|
| c_1, c_2, c_5 c_9, c_{11} | $(y - 1)^2$ |
| c_3, c_4, c_7 c_8 | $y^2 + y + 1$ |
| c_6, c_{10}, c_{12} | y^2 |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.500000 + 0.866025I$ | 0 | -3.00000 |
| $a = 0.500000 + 0.866025I$ | | |
| $b = 0.500000 + 0.866025I$ | | |
| $u = -0.500000 - 0.866025I$ | 0 | -3.00000 |
| $a = 0.500000 - 0.866025I$ | | |
| $b = 0.500000 - 0.866025I$ | | |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $((u-1)^2)(u^{19} - 10u^{18} + \dots + 4u - 1)(u^{22} + 10u^{21} + \dots + 6u^2 + 1)^2 \cdot (u^{41} + 19u^{40} + \dots + 89u + 16)$ |
| c_2 | $((u-1)^2)(u^{19} + 2u^{18} + \dots - 2u - 1)(u^{22} - 2u^{21} + \dots - 5u^3 + 1)^2 \cdot (u^{41} + 5u^{40} + \dots + 7u + 4)$ |
| c_3, c_7 | $(u^2 + u + 1)(u^{19} - u^{18} + \dots - 4u^2 + 1)(u^{41} + u^{40} + \dots + 2u + 1) \cdot (u^{44} + 4u^{43} + \dots + 77u + 17)$ |
| c_4, c_8 | $(u^2 + u + 1)(u^{19} - 4u^{17} + \dots - u + 1)(u^{41} - 9u^{39} + \dots - 69u + 17) \cdot (u^{44} + 2u^{43} + \dots - 7681u + 1663)$ |
| c_5 | $((u+1)^2)(u^{19} - 2u^{18} + \dots - 2u + 1)(u^{22} - 2u^{21} + \dots - 5u^3 + 1)^2 \cdot (u^{41} + 5u^{40} + \dots + 7u + 4)$ |
| c_6 | $u^2(u^{19} - 6u^{18} + \dots + 14u - 3)(u^{22} - 9u^{21} + \dots - 27u + 8)^2 \cdot (u^{41} + 15u^{40} + \dots + 87u + 4)$ |
| c_9, c_{11} | $((u-1)^2)(u^{19} - 8u^{18} + \dots + 5u - 1)(u^{41} - 4u^{40} + \dots + 27u + 1) \cdot (u^{44} - 3u^{43} + \dots - 5634u + 459)$ |
| c_{10} | $u^2(u^{19} + 11u^{18} + \dots + u - 3)(u^{22} + 9u^{21} + \dots + u + 2)^2 \cdot (u^{41} - 26u^{40} + \dots + 23u - 2)$ |
| c_{12} | $u^2(u^{19} + 6u^{18} + \dots + 14u + 3)(u^{22} - 9u^{21} + \dots - 27u + 8)^2 \cdot (u^{41} + 15u^{40} + \dots + 87u + 4)$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1 | $((y-1)^2)(y^{19} + 2y^{18} + \dots + 74y^3 - 1)(y^{22} + 6y^{21} + \dots + 12y + 1)^2 \cdot (y^{41} + 9y^{40} + \dots - 3311y - 256)$ |
| c_2, c_5 | $((y-1)^2)(y^{19} - 10y^{18} + \dots + 4y - 1)(y^{22} - 10y^{21} + \dots + 6y^2 + 1)^2 \cdot (y^{41} - 19y^{40} + \dots + 89y - 16)$ |
| c_3, c_7 | $(y^2 + y + 1)(y^{19} - 5y^{18} + \dots + 8y - 1)(y^{41} + 17y^{40} + \dots - 36y - 1) \cdot (y^{44} - 8y^{43} + \dots + 1585y + 289)$ |
| c_4, c_8 | $(y^2 + y + 1)(y^{19} - 8y^{18} + \dots + 5y - 1)(y^{41} - 18y^{40} + \dots + 5577y - 289) \cdot (y^{44} - 20y^{43} + \dots + 60881257y + 2765569)$ |
| c_6, c_{12} | $y^2(y^{19} + 6y^{18} + \dots + 88y - 9)(y^{22} - 5y^{21} + \dots - 137y + 64)^2 \cdot (y^{41} + y^{40} + \dots + 633y - 16)$ |
| c_9, c_{11} | $((y-1)^2)(y^{19} - 16y^{17} + \dots - 19y - 1)(y^{41} - 58y^{40} + \dots + 333y - 1) \cdot (y^{44} - 23y^{43} + \dots + 46259586y + 210681)$ |
| c_{10} | $y^2(y^{19} - 3y^{18} + \dots + 217y - 9)(y^{22} + 3y^{21} + \dots + 43y + 4)^2 \cdot (y^{41} + 68y^{39} + \dots + 81y - 4)$ |