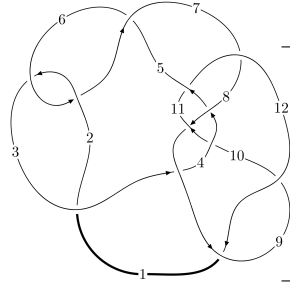
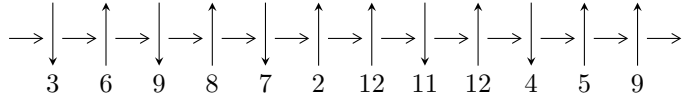


12n₀₄₆₀ (K12n₀₄₆₀)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$8, 11 \xrightarrow{c_8} 5, 9 \xrightarrow{c_{11}} 12 \xrightarrow{c_{12}} 1 \xrightarrow{c_4} 4 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_5} 6 \xrightarrow{c_2} 2 \xrightarrow{c_{10}} 10 \rightsquigarrow c_1, c_6, c_9$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -1248355972972u^{23} - 21816995305526u^{22} + \dots + 1521391151543b - 18832007879252, \\ -18832007879252u^{23} - 332734361961676u^{22} + \dots + 7606955757715a - 305928879409436, \\ u^{24} + 18u^{23} + \dots + 63u + 5 \rangle$$

$$I_2^u = \langle -u^{13} + 3u^{12} - 2u^{11} - 9u^{10} + 22u^9 - 16u^8 - 20u^7 + 55u^6 - 50u^5 - u^4 + 46u^3 - 53u^2 + b + 28u - 8, \\ 8u^{13} - 69u^{12} + \dots + 13a - 164, u^{14} - 7u^{13} + \dots - 66u + 13 \rangle$$

$$I_3^u = \langle u^{11} - 3u^{10} + 5u^9 - 4u^8 + 4u^7 - 5u^6 + 7u^5 - 4u^4 + 3u^3 - 2au - 3u^2 + 2b + 5u - 4, \\ -4u^{11}a + u^{11} + \dots + 4a + 24, \\ u^{12} - 3u^{11} + 7u^{10} - 10u^9 + 16u^8 - 19u^7 + 25u^6 - 22u^5 + 23u^4 - 15u^3 + 15u^2 - 6u + 4 \rangle$$

$$I_1^v = \langle a, v^2 + b - 2v + 2, v^4 - 3v^3 + 5v^2 - 3v + 1 \rangle$$

$$I_2^v = \langle a, b + 1, v - 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 67 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.25 \times 10^{12}u^{23} - 2.18 \times 10^{13}u^{22} + \dots + 1.52 \times 10^{12}b - 1.88 \times 10^{13}, -1.88 \times 10^{13}u^{23} - 3.33 \times 10^{14}u^{22} + \dots + 7.61 \times 10^{12}a - 3.06 \times 10^{14}, u^{24} + 18u^{23} + \dots + 63u + 5 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 2.47563u^{23} + 43.7408u^{22} + \dots + 399.917u + 40.2170 \\ 0.820536u^{23} + 14.3402u^{22} + \dots + 115.748u + 12.3781 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.136050u^{23} + 2.29322u^{22} + \dots + 6.95177u + 1.65823 \\ 0.155672u^{23} + 2.68503u^{22} + \dots + 7.91289u + 0.680248 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.174665u^{23} + 2.79784u^{22} + \dots + 5.73760u + 1.56012 \\ 0.452229u^{23} + 7.79322u^{22} + \dots + 19.7188u + 1.63255 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1.65509u^{23} + 29.4006u^{22} + \dots + 284.170u + 27.8388 \\ 0.820536u^{23} + 14.3402u^{22} + \dots + 115.748u + 12.3781 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 2.38937u^{23} + 42.1061u^{22} + \dots + 383.557u + 38.2617 \\ 1.17675u^{23} + 20.7176u^{22} + \dots + 144.303u + 14.9358 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.812939u^{23} - 13.6447u^{22} + \dots - 40.9787u - 2.36243 \\ -1.10529u^{23} - 18.9019u^{22} + \dots - 56.9798u - 4.84305 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.822628u^{23} + 13.5628u^{22} + \dots + 65.4774u + 5.93289 \\ 2.10151u^{23} + 36.5939u^{22} + \dots + 173.676u + 16.6453 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.778150u^{23} + 13.1980u^{22} + \dots + 46.3607u + 3.84960 \\ 1.56119u^{23} + 26.8336u^{22} + \dots + 93.3811u + 7.91527 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0582376u^{23} - 0.896432u^{22} + \dots + 2.25306u + 1.07610 \\ 0.0386155u^{23} + 0.504620u^{22} + \dots - 1.21417u - 0.0981103 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{12998513265738}{1521391151543}u^{23} + \frac{228690626935746}{1521391151543}u^{22} + \dots + \frac{1512678087445189}{1521391151543}u + \frac{140722368482773}{1521391151543}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1, c_5 | $u^{24} + 5u^{23} + \dots + 4u + 25$ |
| c_2, c_6 | $u^{24} - 5u^{23} + \dots - 24u + 5$ |
| c_3 | $u^{24} + 32u^{22} + \dots + 3u + 1$ |
| c_4, c_{11} | $u^{24} + u^{23} + \dots + 4u + 1$ |
| c_7 | $u^{24} - 27u^{23} + \dots - 6144u + 1024$ |
| c_8 | $u^{24} - 18u^{23} + \dots - 63u + 5$ |
| c_9, c_{12} | $u^{24} - 26u^{22} + \dots + 17u + 1$ |
| c_{10} | $u^{24} + 12u^{22} + \dots + 19u + 16$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $y^{24} + 33y^{23} + \dots - 7216y + 625$ |
| c_2, c_6 | $y^{24} + 5y^{23} + \dots + 4y + 25$ |
| c_3 | $y^{24} + 64y^{23} + \dots + 7y + 1$ |
| c_4, c_{11} | $y^{24} - 9y^{23} + \dots - 16y + 1$ |
| c_7 | $y^{24} - 15y^{23} + \dots + 29884416y^2 + 1048576$ |
| c_8 | $y^{24} + 50y^{22} + \dots + 101y + 25$ |
| c_9, c_{12} | $y^{24} - 52y^{23} + \dots - 117y + 1$ |
| c_{10} | $y^{24} + 24y^{23} + \dots + 4311y + 256$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.401173 + 1.000390I$ $a = 0.287799 - 1.279530I$ $b = -1.164570 - 0.801223I$ | $4.97730 + 3.76182I$ | $7.47515 - 2.42928I$ |
| $u = -0.401173 - 1.000390I$ $a = 0.287799 + 1.279530I$ $b = -1.164570 + 0.801223I$ | $4.97730 - 3.76182I$ | $7.47515 + 2.42928I$ |
| $u = -0.895129 + 0.707186I$ $a = -0.642012 - 0.323894I$ $b = -0.803737 + 0.164096I$ | $3.40541 + 0.54338I$ | $9.96762 + 0.I$ |
| $u = -0.895129 - 0.707186I$ $a = -0.642012 + 0.323894I$ $b = -0.803737 - 0.164096I$ | $3.40541 - 0.54338I$ | $9.96762 + 0.I$ |
| $u = -0.634153 + 0.969164I$ $a = -0.099094 + 1.257220I$ $b = 1.15561 + 0.89330I$ | $3.19488 + 9.64059I$ | $5.12102 - 7.65493I$ |
| $u = -0.634153 - 0.969164I$ $a = -0.099094 - 1.257220I$ $b = 1.15561 - 0.89330I$ | $3.19488 - 9.64059I$ | $5.12102 + 7.65493I$ |
| $u = -0.388319 + 0.539618I$ $a = -0.22109 + 1.74704I$ $b = 0.856878 + 0.797713I$ | $-1.96075 + 3.03649I$ | $1.72656 - 2.94326I$ |
| $u = -0.388319 - 0.539618I$ $a = -0.22109 - 1.74704I$ $b = 0.856878 - 0.797713I$ | $-1.96075 - 3.03649I$ | $1.72656 + 2.94326I$ |
| $u = 0.264551 + 0.575187I$ $a = -0.414815 + 0.746478I$ $b = 0.539104 + 0.041115I$ | $-0.61911 - 1.60676I$ | $-1.07516 + 5.36024I$ |
| $u = 0.264551 - 0.575187I$ $a = -0.414815 - 0.746478I$ $b = 0.539104 - 0.041115I$ | $-0.61911 + 1.60676I$ | $-1.07516 - 5.36024I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.666916 + 1.239860I$ $a = 0.329991 + 0.358310I$ $b = 0.664331 - 0.170181I$ | $3.42032 - 4.04799I$ | $0. + 7.82789I$ |
| $u = -0.666916 - 1.239860I$ $a = 0.329991 - 0.358310I$ $b = 0.664331 + 0.170181I$ | $3.42032 + 4.04799I$ | $0. - 7.82789I$ |
| $u = -0.053583 + 0.452097I$ $a = 0.55903 - 2.05204I$ $b = -0.897767 - 0.362690I$ | $1.51247 + 0.42081I$ | $8.19848 - 1.31600I$ |
| $u = -0.053583 - 0.452097I$ $a = 0.55903 + 2.05204I$ $b = -0.897767 + 0.362690I$ | $1.51247 - 0.42081I$ | $8.19848 + 1.31600I$ |
| $u = -0.359542 + 0.101893I$ $a = -0.10927 + 2.29685I$ $b = 0.194744 + 0.836947I$ | $0.17995 - 2.31205I$ | $-1.12278 + 4.62522I$ |
| $u = -0.359542 - 0.101893I$ $a = -0.10927 - 2.29685I$ $b = 0.194744 - 0.836947I$ | $0.17995 + 2.31205I$ | $-1.12278 - 4.62522I$ |
| $u = -0.93950 + 1.42997I$ $a = 0.065784 - 0.924691I$ $b = -1.26048 - 0.96281I$ | $15.4724 + 7.4151I$ | 0 |
| $u = -0.93950 - 1.42997I$ $a = 0.065784 + 0.924691I$ $b = -1.26048 + 0.96281I$ | $15.4724 - 7.4151I$ | 0 |
| $u = -1.02696 + 1.40305I$ $a = -0.027606 + 0.911387I$ $b = 1.25037 + 0.97469I$ | $15.0388 + 14.5096I$ | 0 |
| $u = -1.02696 - 1.40305I$ $a = -0.027606 - 0.911387I$ $b = 1.25037 - 0.97469I$ | $15.0388 - 14.5096I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.96069 + 1.10463I$ | | |
| $a = -0.366729 + 0.020741I$ | $12.99680 + 2.23230I$ | 0 |
| $b = -0.696132 + 0.445764I$ | | |
| $u = -1.96069 - 1.10463I$ | | |
| $a = -0.366729 - 0.020741I$ | $12.99680 - 2.23230I$ | 0 |
| $b = -0.696132 - 0.445764I$ | | |
| $u = -1.93859 + 1.28607I$ | | |
| $a = 0.338018 + 0.004948I$ | $13.11360 - 4.55126I$ | 0 |
| $b = 0.661642 - 0.425123I$ | | |
| $u = -1.93859 - 1.28607I$ | | |
| $a = 0.338018 - 0.004948I$ | $13.11360 + 4.55126I$ | 0 |
| $b = 0.661642 + 0.425123I$ | | |

$$\text{II. } I_2^u = \langle -u^{13} + 3u^{12} + \dots + b - 8, 8u^{13} - 69u^{12} + \dots + 13a - 164, u^{14} - 7u^{13} + \dots - 66u + 13 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.615385u^{13} + 5.30769u^{12} + \dots - 54.0769u + 12.6154 \\ u^{13} - 3u^{12} + \dots - 28u + 8 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.923077u^{13} + 5.46154u^{12} + \dots - 40.6154u + 6.92308 \\ -u^{13} + 6u^{12} + \dots - 53u + 12 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.923077u^{13} + 5.46154u^{12} + \dots - 39.6154u + 5.92308 \\ -u^{13} + 6u^{12} + \dots - 53u + 12 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -1.61538u^{13} + 8.30769u^{12} + \dots - 26.0769u + 4.61538 \\ u^{13} - 3u^{12} + \dots - 28u + 8 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 3.38462u^{13} - 18.6923u^{12} + \dots + 122.923u - 26.3846 \\ 11u^{13} - 64u^{12} + \dots + 435u - 96 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1.92308u^{13} - 12.4615u^{12} + \dots + 134.615u - 31.9231 \\ -u^{12} + 5u^{11} + \dots + 40u - 12 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -4.38462u^{13} + 20.6923u^{12} + \dots - 6.92308u - 5.61538 \\ -19u^{13} + 111u^{12} + \dots - 752u + 161 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.923077u^{13} - 6.46154u^{12} + \dots + 80.6154u - 20.9231 \\ -2u^{12} + 10u^{11} + \dots + 82u - 25 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.0769231u^{13} - 0.538462u^{12} + \dots + 13.3846u - 4.07692 \\ u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -14u^{13} + 87u^{12} - 228u^{11} + 253u^{10} + 151u^9 - 946u^8 + 1451u^7 - 907u^6 - 571u^5 + 1908u^4 - 2143u^3 + 1430u^2 - 580u + 122$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---------------------------------------|
| c_1, c_5 | $u^{14} - 4u^{13} + \dots - 11u + 1$ |
| c_2 | $u^{14} - 2u^{13} + \dots - u + 1$ |
| c_3 | $u^{14} - u^{13} + \dots - 4u + 1$ |
| c_4, c_{11} | $u^{14} + u^{12} + \dots + u + 1$ |
| c_6 | $u^{14} + 2u^{13} + \dots + u + 1$ |
| c_7 | $u^{14} - 5u^{13} + \dots + 2u + 1$ |
| c_8 | $u^{14} - 7u^{13} + \dots - 66u + 13$ |
| c_9 | $u^{14} + 7u^{13} + \dots + 2u + 1$ |
| c_{10} | $u^{14} - u^{13} + \dots + u^2 + 1$ |
| c_{12} | $u^{14} - 7u^{13} + \dots - 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $y^{14} + 16y^{13} + \dots - 29y + 1$ |
| c_2, c_6 | $y^{14} + 4y^{13} + \dots + 11y + 1$ |
| c_3 | $y^{14} + 7y^{13} + \dots - 2y + 1$ |
| c_4, c_{11} | $y^{14} + 2y^{13} + \dots + 7y + 1$ |
| c_7 | $y^{14} - 15y^{13} + \dots - 6y + 1$ |
| c_8 | $y^{14} - 5y^{13} + \dots + 168y + 169$ |
| c_9, c_{12} | $y^{14} - 5y^{13} + \dots + 14y + 1$ |
| c_{10} | $y^{14} + 7y^{13} + \dots + 2y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.849111 + 0.715901I$ $a = 0.019947 + 1.052460I$ $b = -0.736521 + 0.907937I$ | $-3.07370 - 3.80425I$ | $-5.63446 + 5.71514I$ |
| $u = 0.849111 - 0.715901I$ $a = 0.019947 - 1.052460I$ $b = -0.736521 - 0.907937I$ | $-3.07370 + 3.80425I$ | $-5.63446 - 5.71514I$ |
| $u = 0.313761 + 1.089880I$ $a = -0.549742 - 0.549016I$ $b = 0.425872 - 0.771411I$ | $1.77746 - 4.05505I$ | $3.41727 + 6.24011I$ |
| $u = 0.313761 - 1.089880I$ $a = -0.549742 + 0.549016I$ $b = 0.425872 + 0.771411I$ | $1.77746 + 4.05505I$ | $3.41727 - 6.24011I$ |
| $u = 0.311775 + 0.708424I$ $a = 0.892105 + 0.945635I$ $b = -0.391774 + 0.926814I$ | $0.73793 + 1.30082I$ | $2.62476 + 1.43148I$ |
| $u = 0.311775 - 0.708424I$ $a = 0.892105 - 0.945635I$ $b = -0.391774 - 0.926814I$ | $0.73793 - 1.30082I$ | $2.62476 - 1.43148I$ |
| $u = 1.119030 + 0.593759I$ $a = -0.391744 + 0.935712I$ $b = -0.993957 + 0.814483I$ | $1.54894 - 8.36056I$ | $3.10198 + 6.93573I$ |
| $u = 1.119030 - 0.593759I$ $a = -0.391744 - 0.935712I$ $b = -0.993957 - 0.814483I$ | $1.54894 + 8.36056I$ | $3.10198 - 6.93573I$ |
| $u = 1.189000 + 0.649257I$ $a = 0.371944 - 0.816978I$ $b = 0.972669 - 0.729899I$ | $2.10101 - 2.72257I$ | $4.91037 + 2.51501I$ |
| $u = 1.189000 - 0.649257I$ $a = 0.371944 + 0.816978I$ $b = 0.972669 + 0.729899I$ | $2.10101 + 2.72257I$ | $4.91037 - 2.51501I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.381310 + 0.146372I$ | $12.91060 - 3.47104I$ | $5.96925 + 1.99685I$ |
| $a = -0.063316 + 0.461767I$ | | |
| $b = 0.019869 - 0.647110I$ | | |
| $u = -1.381310 - 0.146372I$ | $12.91060 + 3.47104I$ | $5.96925 - 1.99685I$ |
| $a = -0.063316 - 0.461767I$ | | |
| $b = 0.019869 + 0.647110I$ | | |
| $u = 1.09864 + 1.09539I$ | $-1.19786 - 3.68086I$ | $-0.88917 + 6.15653I$ |
| $a = 0.028499 - 0.613967I$ | | |
| $b = 0.703842 - 0.643310I$ | | |
| $u = 1.09864 - 1.09539I$ | $-1.19786 + 3.68086I$ | $-0.88917 - 6.15653I$ |
| $a = 0.028499 + 0.613967I$ | | |
| $b = 0.703842 + 0.643310I$ | | |

$$\text{III. } I_3^u = \langle u^{11} - 3u^{10} + \dots + 2b - 4, -4u^{11}a + u^{11} + \dots + 4a + 24, u^{12} - 3u^{11} + \dots - 6u + 4 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} a \\ -\frac{1}{2}u^{11} + \frac{3}{2}u^{10} + \dots - \frac{5}{2}u + 2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} \frac{1}{2}u^{11}a - \frac{1}{4}u^{11} + \dots - 2a + \frac{1}{2} \\ 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{3}{2}u^{11}a - \frac{1}{4}u^{11} + \dots - 2a + \frac{3}{2} \\ -u^{11}a + 3u^{10}a + \dots - 4au + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{1}{2}u^{11} - \frac{3}{2}u^{10} + \dots + a - 2 \\ -\frac{1}{2}u^{11} + \frac{3}{2}u^{10} + \dots - \frac{5}{2}u + 2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^{11} - 3u^{10} + \dots + a + 2u \\ -\frac{1}{2}u^{11} + \frac{3}{2}u^{10} + \dots - \frac{9}{2}u + 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{2}u^{11}a - \frac{1}{4}u^{11} + \dots - 2a + \frac{3}{2} \\ 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{1}{2}u^{11}a + \frac{1}{2}u^{11} + \dots + 2a - \frac{1}{2} \\ au \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^{10}a - \frac{1}{4}u^{11} + \dots - 4a + \frac{3}{2} \\ -\frac{1}{2}u^{11} + \frac{3}{2}u^{10} + \dots + 2a + 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{3}{2}u^{11}a - \frac{1}{4}u^{11} + \dots - 2a + \frac{1}{2} \\ -u^{11}a + 3u^{10}a + \dots + u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{1}{2}u^{11} + \frac{5}{2}u^{10} - \frac{5}{2}u^9 + 4u^8 - 2u^7 + \frac{19}{2}u^6 - \frac{7}{2}u^5 + 12u^4 - \frac{3}{2}u^3 + \frac{29}{2}u^2 - \frac{5}{2}u + 16$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $(u^{12} + 2u^{11} + \dots + 6u + 1)^2$ |
| c_2, c_6 | $(u^{12} + 2u^{11} + \dots + 2u + 1)^2$ |
| c_3 | $u^{24} + 20u^{22} + \dots - 1035u + 22$ |
| c_4, c_{11} | $u^{24} + 2u^{23} + \dots - 7u + 16$ |
| c_7 | $(u + 1)^{24}$ |
| c_8 | $(u^{12} + 3u^{11} + \dots + 6u + 4)^2$ |
| c_9, c_{12} | $u^{24} - 5u^{23} + \dots + 8613u + 4448$ |
| c_{10} | $u^{24} + 2u^{23} + \dots + 1443u + 5011$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $(y^{12} + 18y^{11} + \dots + 6y + 1)^2$ |
| c_2, c_6 | $(y^{12} + 2y^{11} + \dots + 6y + 1)^2$ |
| c_3 | $y^{24} + 40y^{23} + \dots - 489721y + 484$ |
| c_4, c_{11} | $y^{24} + 38y^{22} + \dots - 2737y + 256$ |
| c_7 | $(y - 1)^{24}$ |
| c_8 | $(y^{12} + 5y^{11} + \dots + 84y + 16)^2$ |
| c_9, c_{12} | $y^{24} - 37y^{23} + \dots + 4661479y + 19784704$ |
| c_{10} | $y^{24} + 20y^{23} + \dots + 194809963y + 25110121$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.595557 + 0.863954I$ $a = -0.141148 - 0.929948I$ $b = 1.07056 - 1.49446I$ | $13.6814 + 5.8161I$ | $7.09681 - 5.45294I$ |
| $u = -0.595557 + 0.863954I$ $a = 1.75162 + 0.03168I$ $b = -0.887493 - 0.431892I$ | $13.6814 + 5.8161I$ | $7.09681 - 5.45294I$ |
| $u = -0.595557 - 0.863954I$ $a = -0.141148 + 0.929948I$ $b = 1.07056 + 1.49446I$ | $13.6814 - 5.8161I$ | $7.09681 + 5.45294I$ |
| $u = -0.595557 - 0.863954I$ $a = 1.75162 - 0.03168I$ $b = -0.887493 + 0.431892I$ | $13.6814 - 5.8161I$ | $7.09681 + 5.45294I$ |
| $u = -0.521857 + 0.963930I$ $a = 0.105818 + 0.886399I$ $b = -1.08284 + 1.48890I$ | $14.05920 - 1.29677I$ | $8.02075 - 0.64369I$ |
| $u = -0.521857 + 0.963930I$ $a = -1.66482 - 0.22205I$ $b = 0.909648 + 0.360572I$ | $14.05920 - 1.29677I$ | $8.02075 - 0.64369I$ |
| $u = -0.521857 - 0.963930I$ $a = 0.105818 - 0.886399I$ $b = -1.08284 - 1.48890I$ | $14.05920 + 1.29677I$ | $8.02075 + 0.64369I$ |
| $u = -0.521857 - 0.963930I$ $a = -1.66482 + 0.22205I$ $b = 0.909648 - 0.360572I$ | $14.05920 + 1.29677I$ | $8.02075 + 0.64369I$ |
| $u = 0.380152 + 1.069420I$ $a = -0.102983 + 0.676971I$ $b = -1.04377 + 1.20002I$ | $3.57471 - 4.01356I$ | $9.35409 + 5.50726I$ |
| $u = 0.380152 + 1.069420I$ $a = -0.688213 - 1.220660I$ $b = 0.763114 - 0.147220I$ | $3.57471 - 4.01356I$ | $9.35409 + 5.50726I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.380152 - 1.069420I$ $a = -0.102983 - 0.676971I$ $b = -1.04377 - 1.20002I$ | $3.57471 + 4.01356I$ | $9.35409 - 5.50726I$ |
| $u = 0.380152 - 1.069420I$ $a = -0.688213 + 1.220660I$ $b = 0.763114 + 0.147220I$ | $3.57471 + 4.01356I$ | $9.35409 - 5.50726I$ |
| $u = 0.246665 + 0.748766I$ $a = 0.218149 - 0.727778I$ $b = 1.29103 - 1.21568I$ | $2.20338 + 1.32744I$ | $9.73221 + 1.32386I$ |
| $u = 0.246665 + 0.748766I$ $a = 0.95223 + 2.03791I$ $b = -0.598745 + 0.016175I$ | $2.20338 + 1.32744I$ | $9.73221 + 1.32386I$ |
| $u = 0.246665 - 0.748766I$ $a = 0.218149 + 0.727778I$ $b = 1.29103 + 1.21568I$ | $2.20338 - 1.32744I$ | $9.73221 - 1.32386I$ |
| $u = 0.246665 - 0.748766I$ $a = 0.95223 - 2.03791I$ $b = -0.598745 - 0.016175I$ | $2.20338 - 1.32744I$ | $9.73221 - 1.32386I$ |
| $u = 1.005850 + 0.842159I$ $a = -0.170941 + 0.863353I$ $b = -0.453719 + 0.571135I$ | $-1.51202 - 2.72726I$ | $-2.43929 - 0.47681I$ |
| $u = 1.005850 + 0.842159I$ $a = -0.014301 - 0.555838I$ $b = 0.899022 - 0.724448I$ | $-1.51202 - 2.72726I$ | $-2.43929 - 0.47681I$ |
| $u = 1.005850 - 0.842159I$ $a = -0.170941 - 0.863353I$ $b = -0.453719 - 0.571135I$ | $-1.51202 + 2.72726I$ | $-2.43929 + 0.47681I$ |
| $u = 1.005850 - 0.842159I$ $a = -0.014301 + 0.555838I$ $b = 0.899022 + 0.724448I$ | $-1.51202 + 2.72726I$ | $-2.43929 + 0.47681I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.98474 + 1.10667I$ | | |
| $a = -0.168174 - 0.749804I$ | $-0.75285 - 4.59014I$ | $2.73542 + 11.41867I$ |
| $b = 0.797372 - 0.556358I$ | | |
| $u = 0.98474 + 1.10667I$ | | |
| $a = -0.077239 + 0.651782I$ | $-0.75285 - 4.59014I$ | $2.73542 + 11.41867I$ |
| $b = -0.664181 + 0.924478I$ | | |
| $u = 0.98474 - 1.10667I$ | | |
| $a = -0.168174 + 0.749804I$ | $-0.75285 + 4.59014I$ | $2.73542 - 11.41867I$ |
| $b = 0.797372 + 0.556358I$ | | |
| $u = 0.98474 - 1.10667I$ | | |
| $a = -0.077239 - 0.651782I$ | $-0.75285 + 4.59014I$ | $2.73542 - 11.41867I$ |
| $b = -0.664181 - 0.924478I$ | | |

$$\text{IV. } I_1^v = \langle a, v^2 + b - 2v + 2, v^4 - 3v^3 + 5v^2 - 3v + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -v^2 + 2v - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v - 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v^2 - 2v + 2 \\ -v^2 + 2v - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -v^2 + 2v - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -v + 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -v^3 + 2v^2 - 3v + 1 \\ -v^3 + 2v^2 - 2v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v - 1 \\ v^3 - 3v^2 + 5v - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v + 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-7v^3 + 21v^2 - 28v + 14$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--------------------------------|
| c_1, c_5, c_6 | $(u^2 - u + 1)^2$ |
| c_2 | $(u^2 + u + 1)^2$ |
| c_3, c_4, c_{10} c_{11} | $u^4 - u^3 - u^2 + u + 1$ |
| c_7, c_9 | $(u + 1)^4$ |
| c_8 | u^4 |
| c_{12} | $(u - 1)^4$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| c_1, c_2, c_5 c_6 | $(y^2 + y + 1)^2$ |
| c_3, c_4, c_{10} c_{11} | $y^4 - 3y^3 + 5y^2 - 3y + 1$ |
| c_7, c_9, c_{12} | $(y - 1)^4$ |
| c_8 | y^4 |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $v = 0.378256 + 0.440597I$ $a = 0$ $b = -1.192440 + 0.547877I$ | $1.64493 + 2.02988I$ | $3.50000 - 6.06218I$ |
| $v = 0.378256 - 0.440597I$ $a = 0$ $b = -1.192440 - 0.547877I$ | $1.64493 - 2.02988I$ | $3.50000 + 6.06218I$ |
| $v = 1.12174 + 1.30662I$ $a = 0$ $b = 0.692440 - 0.318148I$ | $1.64493 - 2.02988I$ | $3.50000 + 6.06218I$ |
| $v = 1.12174 - 1.30662I$ $a = 0$ $b = 0.692440 + 0.318148I$ | $1.64493 + 2.02988I$ | $3.50000 - 6.06218I$ |

$$\mathbf{V. } I_2^v = \langle a, b + 1, v - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) **u**-Polynomials at the component

| Crossings | u -Polynomials at each crossing |
|--|--|
| c_1, c_2, c_5 c_6, c_8 | u |
| c_3, c_4, c_7 c_9, c_{10}, c_{11} c_{12} | $u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|------------------------------------|
| c_1, c_2, c_5 c_6, c_8 | y |
| c_3, c_4, c_7 c_9, c_{10}, c_{11} c_{12} | $y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $v = 1.00000$ | | |
| $a = 0$ | 1.64493 | 6.00000 |
| $b = -1.00000$ | | |

VI. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $u(u^2 - u + 1)^2(u^{12} + 2u^{11} + \dots + 6u + 1)^2$ $\cdot (u^{14} - 4u^{13} + \dots - 11u + 1)(u^{24} + 5u^{23} + \dots + 4u + 25)$ |
| c_2 | $u(u^2 + u + 1)^2(u^{12} + 2u^{11} + \dots + 2u + 1)^2(u^{14} - 2u^{13} + \dots - u + 1)$ $\cdot (u^{24} - 5u^{23} + \dots - 24u + 5)$ |
| c_3 | $(u - 1)(u^4 - u^3 - u^2 + u + 1)(u^{14} - u^{13} + \dots - 4u + 1)$ $\cdot (u^{24} + 20u^{22} + \dots - 1035u + 22)(u^{24} + 32u^{22} + \dots + 3u + 1)$ |
| c_4, c_{11} | $(u - 1)(u^4 - u^3 - u^2 + u + 1)(u^{14} + u^{12} + \dots + u + 1)$ $\cdot (u^{24} + u^{23} + \dots + 4u + 1)(u^{24} + 2u^{23} + \dots - 7u + 16)$ |
| c_6 | $u(u^2 - u + 1)^2(u^{12} + 2u^{11} + \dots + 2u + 1)^2(u^{14} + 2u^{13} + \dots + u + 1)$ $\cdot (u^{24} - 5u^{23} + \dots - 24u + 5)$ |
| c_7 | $(u - 1)(u + 1)^{28}(u^{14} - 5u^{13} + \dots + 2u + 1)$ $\cdot (u^{24} - 27u^{23} + \dots - 6144u + 1024)$ |
| c_8 | $u^5(u^{12} + 3u^{11} + \dots + 6u + 4)^2(u^{14} - 7u^{13} + \dots - 66u + 13)$ $\cdot (u^{24} - 18u^{23} + \dots - 63u + 5)$ |
| c_9 | $(u - 1)(u + 1)^4(u^{14} + 7u^{13} + \dots + 2u + 1)(u^{24} - 26u^{22} + \dots + 17u + 1)$ $\cdot (u^{24} - 5u^{23} + \dots + 8613u + 4448)$ |
| c_{10} | $(u - 1)(u^4 - u^3 - u^2 + u + 1)(u^{14} - u^{13} + \dots + u^2 + 1)$ $\cdot (u^{24} + 12u^{22} + \dots + 19u + 16)(u^{24} + 2u^{23} + \dots + 1443u + 5011)$ |
| c_{12} | $((u - 1)^5)(u^{14} - 7u^{13} + \dots - 2u + 1)(u^{24} - 26u^{22} + \dots + 17u + 1)$ $\cdot (u^{24} - 5u^{23} + \dots + 8613u + 4448)$ |

VII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---------------|---|
| c_1, c_5 | $y(y^2 + y + 1)^2(y^{12} + 18y^{11} + \dots + 6y + 1)^2$ $\cdot (y^{14} + 16y^{13} + \dots - 29y + 1)(y^{24} + 33y^{23} + \dots - 7216y + 625)$ |
| c_2, c_6 | $y(y^2 + y + 1)^2(y^{12} + 2y^{11} + \dots + 6y + 1)^2$ $\cdot (y^{14} + 4y^{13} + \dots + 11y + 1)(y^{24} + 5y^{23} + \dots + 4y + 25)$ |
| c_3 | $(y - 1)(y^4 - 3y^3 + \dots - 3y + 1)(y^{14} + 7y^{13} + \dots - 2y + 1)$ $\cdot (y^{24} + 40y^{23} + \dots - 489721y + 484)(y^{24} + 64y^{23} + \dots + 7y + 1)$ |
| c_4, c_{11} | $(y - 1)(y^4 - 3y^3 + \dots - 3y + 1)(y^{14} + 2y^{13} + \dots + 7y + 1)$ $\cdot (y^{24} + 38y^{22} + \dots - 2737y + 256)(y^{24} - 9y^{23} + \dots - 16y + 1)$ |
| c_7 | $((y - 1)^{29})(y^{14} - 15y^{13} + \dots - 6y + 1)$ $\cdot (y^{24} - 15y^{23} + \dots + 29884416y^2 + 1048576)$ |
| c_8 | $y^5(y^{12} + 5y^{11} + \dots + 84y + 16)^2(y^{14} - 5y^{13} + \dots + 168y + 169)$ $\cdot (y^{24} + 50y^{22} + \dots + 101y + 25)$ |
| c_9, c_{12} | $((y - 1)^5)(y^{14} - 5y^{13} + \dots + 14y + 1)(y^{24} - 52y^{23} + \dots - 117y + 1)$ $\cdot (y^{24} - 37y^{23} + \dots + 4661479y + 19784704)$ |
| c_{10} | $(y - 1)(y^4 - 3y^3 + \dots - 3y + 1)(y^{14} + 7y^{13} + \dots + 2y + 1)$ $\cdot (y^{24} + 20y^{23} + \dots + 194809963y + 25110121)$ $\cdot (y^{24} + 24y^{23} + \dots + 4311y + 256)$ |