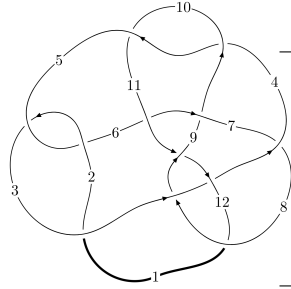
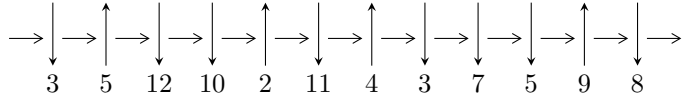


12n<sub>0464</sub> (K12n<sub>0464</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_4} 4,7 \xrightarrow{c_6} 6 \xrightarrow{c_9} 9 \xrightarrow{c_{11}} 12 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_8} 8 \rightsquigarrow c_5, c_7, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -9u^{10} + 50u^9 - 110u^8 + 84u^7 + 135u^6 - 318u^5 + 249u^4 + 140u^3 + 64u^2 + 356b - 268u + 100, \\ 209u^{10} - 1438u^9 + \dots + 712a + 1396, \\ u^{11} - 8u^{10} + 28u^9 - 48u^8 + 21u^7 + 72u^6 - 147u^5 + 118u^4 - 46u^3 + 12u^2 + 4u - 8 \rangle$$

$$I_2^u = \langle -u^{13} - 2u^{12} + 7u^{11} + 14u^{10} - 18u^9 - 37u^8 + 18u^7 + 40u^6 - 3u^4 - 11u^3 - 27u^2 + 2b + 6u + 16, \\ -16u^{13} + 125u^{11} + \dots + 38a - 152, u^{14} - 9u^{12} + 33u^{10} - 60u^8 + 48u^6 + 6u^4 - 37u^2 + 19 \rangle$$

$$I_3^u = \langle -u^2a + au + u^2 + b - u, u^5a - 3u^4a + 2u^5 + 4u^3a - 9u^4 + 13u^3 + 4a^2 + au - 4u^2 - 8a - 6u - 7, \\ u^6 - 5u^5 + 10u^4 - 8u^3 + u^2 - 2u + 4 \rangle$$

$$I_1^v = \langle a, b^2 + b + 1, v + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 39 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -9u^{10} + 50u^9 + \dots + 356b + 100, 209u^{10} - 1438u^9 + \dots + 712a + 1396, u^{11} - 8u^{10} + \dots + 4u - 8 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.293539u^{10} + 2.01966u^9 + \dots - 1.18539u - 1.96067 \\ 0.0252809u^{10} - 0.140449u^9 + \dots + 0.752809u - 0.280899 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0351124u^{10} - 0.306180u^9 + \dots + 0.601124u + 0.387640 \\ 0.266854u^{10} - 1.92697u^9 + \dots + 2.16854u + 2.14607 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.144663u^{10} + 0.831461u^9 + \dots - 0.696629u + 0.162921 \\ -0.325843u^{10} + 1.92135u^9 + \dots + 0.741573u - 1.15730 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.293539u^{10} - 2.01966u^9 + \dots + 0.185393u + 2.96067 \\ 0.328652u^{10} - 2.32584u^9 + \dots + 0.786517u + 2.34831 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.181180u^{10} + 1.08989u^9 + \dots + 1.43820u - 1.32022 \\ -0.325843u^{10} + 1.92135u^9 + \dots + 0.741573u - 1.15730 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.181180u^{10} + 1.08989u^9 + \dots + 1.43820u - 1.32022 \\ -0.926966u^{10} + 5.98315u^9 + \dots + 0.730337u - 4.03371 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.0561798u^{10} - 0.410112u^9 + \dots + 1.93820u + 0.179775 \\ -0.426966u^{10} + 1.98315u^9 + \dots + 0.730337u - 1.03371 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.105337u^{10} - 0.918539u^9 + \dots - 0.196629u + 1.16292 \\ 0.424157u^{10} - 3.07865u^9 + \dots + 1.74157u + 2.84270 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = -\frac{925}{178}u^{10} + \frac{3143}{89}u^9 - \frac{9104}{89}u^8 + \frac{10784}{89}u^7 + \frac{9247}{178}u^6 - \frac{29395}{89}u^5 + \frac{64099}{178}u^4 - \frac{11812}{89}u^3 + \frac{2211}{89}u^2 - \frac{620}{89}u - \frac{3326}{89}$$

(iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing                                     |
|--------------------|--|
| $c_1$              | $u^{11} - 23u^{10} + \dots + 21u - 1$                              |
| $c_2, c_5, c_{11}$ | $u^{11} + u^{10} + \dots - u - 1$                                  |
| $c_3, c_9$         | $u^{11} - u^{10} + 2u^8 + 2u^7 - 2u^5 + 4u^4 + 3u^3 + u^2 - u - 1$ |
| $c_4, c_{10}$      | $u^{11} - 8u^{10} + \dots + 4u - 8$                                |
| $c_6$              | $u^{11} + u^{10} + \dots - 145u - 67$                              |
| $c_7$              | $u^{11} + u^{10} + \dots + 56u + 8$                                |
| $c_8$              | $u^{11} - 4u^{10} + \dots - 17u - 8$                               |
| $c_{12}$           | $u^{11} + 5u^{10} + \dots - 76u - 52$                              |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing          |
|--------------------|---|
| $c_1$              | $y^{11} + 13y^{10} + \dots + 49y - 1$       |
| $c_2, c_5, c_{11}$ | $y^{11} - 23y^{10} + \dots + 21y - 1$       |
| $c_3, c_9$         | $y^{11} - y^{10} + \dots + 3y - 1$          |
| $c_4, c_{10}$      | $y^{11} - 8y^{10} + \dots + 208y - 64$      |
| $c_6$              | $y^{11} + 31y^{10} + \dots - 35389y - 4489$ |
| $c_7$              | $y^{11} - 7y^{10} + \dots + 1792y - 64$     |
| $c_8$              | $y^{11} + 12y^{10} + \dots + 961y - 64$     |
| $c_{12}$           | $y^{11} + 11y^{10} + \dots + 13056y - 2704$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 1.272490 + 0.288412I$<br>$a = -1.145090 + 0.161696I$<br>$b = -0.637420 - 0.913219I$ | $-2.97208 - 5.10948I$                 | $-3.26197 + 5.94709I$ |
| $u = 1.272490 - 0.288412I$<br>$a = -1.145090 - 0.161696I$<br>$b = -0.637420 + 0.913219I$ | $-2.97208 + 5.10948I$                 | $-3.26197 - 5.94709I$ |
| $u = 1.31836$<br>$a = -1.74186$<br>$b = -1.15079$  | $-6.32228$                            | $-14.5780$            |
| $u = -0.006189 + 0.618185I$<br>$a = 0.454297 - 0.805039I$<br>$b = -0.298680 + 0.644156I$ | $0.98614 + 1.71648I$                  | $1.51156 - 4.88656I$  |
| $u = -0.006189 - 0.618185I$<br>$a = 0.454297 + 0.805039I$<br>$b = -0.298680 - 0.644156I$ | $0.98614 - 1.71648I$                  | $1.51156 + 4.88656I$  |
| $u = -1.43000$<br>$a = 1.17850$<br>$b = 0.620255$  | $-3.22805$                            | $-2.67390$            |
| $u = -0.399863$<br>$a = -0.0959405$<br>$b = -0.613457$                                   | $-1.24652$                            | $-9.60770$            |
| $u = 1.42673 + 1.37332I$<br>$a = 0.555878 - 0.153340I$<br>$b = 0.957539 - 0.934630I$     | $9.21923 + 1.76238I$                  | $-4.63285 - 2.25341I$ |
| $u = 1.42673 - 1.37332I$<br>$a = 0.555878 + 0.153340I$<br>$b = 0.957539 + 0.934630I$     | $9.21923 - 1.76238I$                  | $-4.63285 + 2.25341I$ |
| $u = 1.56272 + 1.31035I$<br>$a = 1.214570 - 0.441747I$<br>$b = 1.05056 + 0.96763I$       | $8.8572 - 12.5090I$                   | $-5.18674 + 5.91274I$ |

|       | Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-------|------------------------|---------------------------------------|-----------------------|
| $u =$ | $1.56272 - 1.31035I$   |                                       |                       |
| $a =$ | $1.214570 + 0.441747I$ | $8.8572 + 12.5090I$                   | $-5.18674 - 5.91274I$ |
| $b =$ | $1.05056 - 0.96763I$   |                                       |                       |

$$\text{II. } I_2^u = \langle -u^{13} - 2u^{12} + \dots + 2b + 16, -16u^{13} + 125u^{11} + \dots + 38a - 152, u^{14} - 9u^{12} + \dots - 37u^2 + 19 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.421053u^{13} - 3.28947u^{11} + \dots - 7.07895u + 4 \\ \frac{1}{2}u^{13} + u^{12} + \dots - 3u - 8 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{8}{19}u^{13} + \frac{1}{2}u^{12} + \dots - \frac{79}{38}u - 4 \\ u^{13} + \frac{3}{2}u^{12} + \dots - 3u - \frac{35}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{33}{38}u^{13} + \frac{3}{2}u^{12} + \dots - \frac{119}{38}u - 10 \\ \frac{3}{2}u^{13} + 2u^{12} + \dots - 10u - \frac{33}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.421053u^{13} + 3.28947u^{11} + \dots + 6.07895u + 5 \\ -\frac{1}{2}u^{12} + \frac{1}{2}u^{11} + \dots + 4u + 8 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.631579u^{13} - 0.500000u^{12} + \dots - 6.86842u + 6.50000 \\ \frac{3}{2}u^{13} - 2u^{12} + \dots - 10u + \frac{33}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.631579u^{13} - 0.500000u^{12} + \dots - 6.86842u + 6.50000 \\ \frac{5}{2}u^{13} - \frac{5}{2}u^{12} + \dots - 22u + 26 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{30}{19}u^{13} + \frac{1}{2}u^{12} + \dots - \frac{312}{19}u - 7 \\ \frac{5}{2}u^{13} - \frac{3}{2}u^{12} + \dots - \frac{35}{2}u + 8 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{35}{38}u^{13} + \frac{3}{2}u^{12} + \dots - \frac{163}{19}u - 15 \\ u^{13} + \frac{5}{2}u^{12} + \dots - \frac{9}{2}u - 27 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -3u^{12} + 18u^{10} - 37u^8 + 17u^6 + 30u^4 - 24u^2 - 16$$

(iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing                                    |
|---------------|---|
| $c_1$         | $u^{14} - 7u^{13} + \dots + 3u + 1$                               |
| $c_2$         | $u^{14} - 3u^{13} + \dots - 3u + 1$                               |
| $c_3, c_9$    | $u^{14} + 7u^{13} + \dots + 4u + 1$                               |
| $c_4, c_{10}$ | $u^{14} - 9u^{12} + 33u^{10} - 60u^8 + 48u^6 + 6u^4 - 37u^2 + 19$ |
| $c_5, c_{11}$ | $u^{14} + 3u^{13} + \dots + 3u + 1$                               |
| $c_6$         | $u^{14} + 8u^{13} + \dots + 449u + 137$                           |
| $c_7$         | $u^{14} + 5u^{12} + \dots - 8u + 8$                               |
| $c_8$         | $(u^7 - 2u^5 + u^4 + u^3 + u - 1)^2$                              |
| $c_{12}$      | $u^{14} - 4u^{12} + 6u^{10} + 5u^8 - 8u^6 - 15u^4 + 49u^2 + 19$   |



(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing                         |
|--------------------|--|
| $c_1$              | $y^{14} - y^{13} + \dots + 5y + 1$                         |
| $c_2, c_5, c_{11}$ | $y^{14} + 7y^{13} + \dots - 3y + 1$                        |
| $c_3, c_9$         | $y^{14} - 3y^{13} + \dots - 10y + 1$                       |
| $c_4, c_{10}$      | $(y^7 - 9y^6 + 33y^5 - 60y^4 + 48y^3 + 6y^2 - 37y + 19)^2$ |
| $c_6$              | $y^{14} - 20y^{13} + \dots - 90357y + 18769$               |
| $c_7$              | $y^{14} + 10y^{13} + \dots + 448y + 64$                    |
| $c_8$              | $(y^7 - 4y^6 + 6y^5 - 3y^4 - 3y^3 + 4y^2 + y - 1)^2$       |
| $c_{12}$           | $(y^7 - 4y^6 + 6y^5 + 5y^4 - 8y^3 - 15y^2 + 49y + 19)^2$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|-----------------------------|---------------------------------------|---------------------|
| $u = 0.869734I$             |                                       |                     |
| $a = -0.225055 + 0.152531I$ | -1.32199                              | -5.17190            |
| $b = -0.718860 + 0.558616I$ |                                       |                     |
| $u = -0.869734I$            |                                       |                     |
| $a = -0.225055 - 0.152531I$ | -1.32199                              | -5.17190            |
| $b = -0.718860 - 0.558616I$ |                                       |                     |
| $u = -1.100240 + 0.309359I$ |                                       |                     |
| $a = 0.430002 + 1.302590I$  | -4.63494 + 5.44459I                   | -7.69561 - 8.32422I |
| $b = 0.504604 - 0.512077I$  |                                       |                     |
| $u = -1.100240 - 0.309359I$ |                                       |                     |
| $a = 0.430002 - 1.302590I$  | -4.63494 - 5.44459I                   | -7.69561 + 8.32422I |
| $b = 0.504604 + 0.512077I$  |                                       |                     |
| $u = 1.100240 + 0.309359I$  |                                       |                     |
| $a = -1.59402 - 0.26059I$   | -4.63494 - 5.44459I                   | -7.69561 + 8.32422I |
| $b = -1.05779 - 1.16536I$   |                                       |                     |
| $u = 1.100240 - 0.309359I$  |                                       |                     |
| $a = -1.59402 + 0.26059I$   | -4.63494 + 5.44459I                   | -7.69561 - 8.32422I |
| $b = -1.05779 + 1.16536I$   |                                       |                     |
| $u = -1.266100 + 0.207453I$ |                                       |                     |
| $a = 0.621317 + 0.689999I$  | -5.47716 - 2.46971I                   | -8.53877 + 0.63512I |
| $b = 0.695772 - 0.312580I$  |                                       |                     |
| $u = -1.266100 - 0.207453I$ |                                       |                     |
| $a = 0.621317 - 0.689999I$  | -5.47716 + 2.46971I                   | -8.53877 - 0.63512I |
| $b = 0.695772 + 0.312580I$  |                                       |                     |
| $u = 1.266100 + 0.207453I$  |                                       |                     |
| $a = -1.294320 + 0.392263I$ | -5.47716 + 2.46971I                   | -8.53877 - 0.63512I |
| $b = -1.11920 + 0.89289I$   |                                       |                     |
| $u = 1.266100 - 0.207453I$  |                                       |                     |
| $a = -1.294320 - 0.392263I$ | -5.47716 - 2.46971I                   | -8.53877 + 0.63512I |
| $b = -1.11920 - 0.89289I$   |                                       |                     |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -1.50572 + 0.25250I$   |                                       |                      |
| $a = -1.53985 - 0.28019I$   | $-6.49871 + 4.55112I$                 | $0.32033 + 2.72283I$ |
| $b = -0.518967 + 0.078684I$ |                                       |                      |
| $u = -1.50572 - 0.25250I$   |                                       |                      |
| $a = -1.53985 + 0.28019I$   | $-6.49871 - 4.55112I$                 | $0.32033 - 2.72283I$ |
| $b = -0.518967 - 0.078684I$ |                                       |                      |
| $u = 1.50572 + 0.25250I$    |                                       |                      |
| $a = -1.398080 - 0.188533I$ | $-6.49871 - 4.55112I$                 | $0.32033 - 2.72283I$ |
| $b = -1.28556 - 1.10250I$   |                                       |                      |
| $u = 1.50572 - 0.25250I$    |                                       |                      |
| $a = -1.398080 + 0.188533I$ | $-6.49871 + 4.55112I$                 | $0.32033 + 2.72283I$ |
| $b = -1.28556 + 1.10250I$   |                                       |                      |

$$\text{III. } I_3^u = \langle -u^2a + au + u^2 + b - u, u^5a + 2u^5 + \dots - 8a - 7, u^6 - 5u^5 + 10u^4 - 8u^3 + u^2 - 2u + 4 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ u^2a - au - u^2 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -au - u^2 + a + u \\ -u^3a - u^4 + u^2a + u^3 - au - u^2 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^5a - \frac{3}{4}u^5 + \dots - a + 2 \\ u^5a - \frac{3}{2}u^5 + \dots - 2a + 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{4}u^5 - \frac{3}{4}u^4 + u^3 + a - \frac{3}{4}u - 1 \\ \frac{1}{2}u^5 - \frac{3}{2}u^4 + 2u^3 + au - \frac{3}{2}u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{2}u^5a - \frac{1}{4}u^5 + \dots + a + \frac{1}{2} \\ -u^5a + 3u^4a - u^5 - 3u^3a + 4u^4 - 6u^3 + u^2 + 2a + u + 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u^5a - \frac{1}{4}u^5 + \dots + a + \frac{1}{2} \\ -2u^5a + 8u^4a - u^5 - 10u^3a + 3u^4 + u^2a - 5u^3 + u^2 + 6a + 2u + 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^5a + \frac{3}{4}u^5 + \dots - 2a + 1 \\ -3u^4a + \frac{1}{2}u^5 + \dots - 4a + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4a - u^3a - u^4 - u^2a + u^3 + a \\ u^4a - u^3a - u^4 + u^3 - au - u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 11u^5 - 41u^4 + 56u^3 - 10u^2 - 12u - 38$$

(iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing                  |
|--------------------|---|
| $c_1$              | $u^{12} - 10u^{11} + \dots + 23u + 1$           |
| $c_2, c_5, c_{11}$ | $u^{12} - 5u^{10} + \dots - 3u + 1$             |
| $c_3, c_9$         | $u^{12} - 2u^{11} + \dots - 6u + 1$             |
| $c_4, c_{10}$      | $(u^6 - 5u^5 + 10u^4 - 8u^3 + u^2 - 2u + 4)^2$  |
| $c_6$              | $u^{12} + 7u^{11} + \dots - 841u + 683$         |
| $c_7$              | $u^{12} - 3u^{11} + \dots + 184u + 83$          |
| $c_8$              | $(u^6 + 2u^5 + 7u^4 + u^3 + 5u^2 + 1)^2$        |
| $c_{12}$           | $(u^6 - 2u^5 + 6u^4 - 2u^3 + 10u^2 - 2u + 5)^2$ |

(v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing                    |
|--------------------|---|
| $c_1$              | $y^{12} + 22y^{11} + \dots + 635y + 1$                |
| $c_2, c_5, c_{11}$ | $y^{12} - 10y^{11} + \dots + 23y + 1$                 |
| $c_3, c_9$         | $y^{12} - 2y^{11} + \dots - 10y + 1$                  |
| $c_4, c_{10}$      | $(y^6 - 5y^5 + 22y^4 - 56y^3 + 49y^2 + 4y + 16)^2$    |
| $c_6$              | $y^{12} + 5y^{11} + \dots + 483871y + 466489$         |
| $c_7$              | $y^{12} - 11y^{11} + \dots - 9288y + 6889$            |
| $c_8$              | $(y^6 + 10y^5 + 55y^4 + 71y^3 + 39y^2 + 10y + 1)^2$   |
| $c_{12}$           | $(y^6 + 8y^5 + 48y^4 + 118y^3 + 152y^2 + 96y + 25)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.416505 + 0.576021I$ |                                       |                       |
| $a = 1.267250 + 0.372963I$  | $-0.82381 + 1.88495I$                 | $-3.85860 - 4.25494I$ |
| $b = 0.462791 - 0.185881I$  |                                       |                       |
| $u = -0.416505 + 0.576021I$ |                                       |                       |
| $a = 0.341182 - 0.466302I$  | $-0.82381 + 1.88495I$                 | $-3.85860 - 4.25494I$ |
| $b = -0.662439 + 0.575225I$ |                                       |                       |
| $u = -0.416505 - 0.576021I$ |                                       |                       |
| $a = 1.267250 - 0.372963I$  | $-0.82381 - 1.88495I$                 | $-3.85860 + 4.25494I$ |
| $b = 0.462791 + 0.185881I$  |                                       |                       |
| $u = -0.416505 - 0.576021I$ |                                       |                       |
| $a = 0.341182 + 0.466302I$  | $-0.82381 - 1.88495I$                 | $-3.85860 + 4.25494I$ |
| $b = -0.662439 - 0.575225I$ |                                       |                       |
| $u = 1.44321 + 0.21109I$    |                                       |                       |
| $a = -1.46241 - 0.27942I$   | $-6.77592 - 4.75667I$                 | $-18.9940 + 11.0912I$ |
| $b = -1.35407 - 1.14684I$   |                                       |                       |
| $u = 1.44321 + 0.21109I$    |                                       |                       |
| $a = 1.89212 - 0.31592I$    | $-6.77592 - 4.75667I$                 | $-18.9940 + 11.0912I$ |
| $b = 0.656685 + 0.167255I$  |                                       |                       |
| $u = 1.44321 - 0.21109I$    |                                       |                       |
| $a = -1.46241 + 0.27942I$   | $-6.77592 + 4.75667I$                 | $-18.9940 - 11.0912I$ |
| $b = -1.35407 + 1.14684I$   |                                       |                       |
| $u = 1.44321 - 0.21109I$    |                                       |                       |
| $a = 1.89212 + 0.31592I$    | $-6.77592 + 4.75667I$                 | $-18.9940 - 11.0912I$ |
| $b = 0.656685 - 0.167255I$  |                                       |                       |
| $u = 1.47330 + 1.24522I$    |                                       |                       |
| $a = 1.222760 - 0.470970I$  | $9.24467 - 5.12766I$                  | $-4.64737 + 2.37505I$ |
| $b = 0.951529 + 0.941807I$  |                                       |                       |
| $u = 1.47330 + 1.24522I$    |                                       |                       |
| $a = 0.489110 - 0.210227I$  | $9.24467 - 5.12766I$                  | $-4.64737 + 2.37505I$ |
| $b = 0.94550 - 1.05898I$    |                                       |                       |

|       | Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-------|------------------------|---------------------------------------|-----------------------|
| $u =$ | $1.47330 - 1.24522I$   |                                       |                       |
| $a =$ | $1.222760 + 0.470970I$ | $9.24467 + 5.12766I$                  | $-4.64737 - 2.37505I$ |
| $b =$ | $0.951529 - 0.941807I$ |                                       |                       |
| $u =$ | $1.47330 - 1.24522I$   |                                       |                       |
| $a =$ | $0.489110 + 0.210227I$ | $9.24467 + 5.12766I$                  | $-4.64737 - 2.37505I$ |
| $b =$ | $0.94550 + 1.05898I$   |                                       |                       |



$$\text{IV. } I_1^v = \langle a, b^2 + b + 1, v + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ b + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -b \\ -b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -b - 2 \\ -b - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -b - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -b \\ -b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b \\ b \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-8b - 4$

(iv) u-Polynomials at the component

| Crossings                     | u-Polynomials at each crossing |
|-------------------------------|--------------------------------|
| $c_1, c_5, c_6$<br>$c_{11}$   | $u^2 - u + 1$                  |
| $c_2, c_3, c_7$<br>$c_8, c_9$ | $u^2 + u + 1$                  |
| $c_4, c_{10}, c_{12}$         | $u^2$                          |

(v) Riley Polynomials at the component

| Crossings  | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_3$<br>$c_5, c_6, c_7$<br>$c_8, c_9, c_{11}$ | $y^2 + y + 1$                      |
| $c_4, c_{10}, c_{12}$                                    | $y^2$                              |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$                                     | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape      |
|--|---------------------------------------|-----------------|
| $v = -1.00000$<br>$a = 0$<br>$b = -0.500000 + 0.866025I$ | $4.05977I$                            | $0. - 6.92820I$ |
| $v = -1.00000$<br>$a = 0$<br>$b = -0.500000 - 0.866025I$ | $- 4.05977I$                          | $0. + 6.92820I$ |

## V. u-Polynomials

| Crossings     | u-Polynomials at each crossing   |
|---------------|--|
| $c_1$         | $(u^2 - u + 1)(u^{11} - 23u^{10} + \dots + 21u - 1)(u^{12} - 10u^{11} + \dots + 23u + 1)$ $\cdot (u^{14} - 7u^{13} + \dots + 3u + 1)$                                    |
| $c_2$         | $(u^2 + u + 1)(u^{11} + u^{10} + \dots - u - 1)(u^{12} - 5u^{10} + \dots - 3u + 1)$ $\cdot (u^{14} - 3u^{13} + \dots - 3u + 1)$  |
| $c_3, c_9$    | $(u^2 + u + 1)(u^{11} - u^{10} + 2u^8 + 2u^7 - 2u^5 + 4u^4 + 3u^3 + u^2 - u - 1)$ $\cdot (u^{12} - 2u^{11} + \dots - 6u + 1)(u^{14} + 7u^{13} + \dots + 4u + 1)$         |
| $c_4, c_{10}$ | $u^2(u^6 - 5u^5 + \dots - 2u + 4)^2(u^{11} - 8u^{10} + \dots + 4u - 8)$ $\cdot (u^{14} - 9u^{12} + 33u^{10} - 60u^8 + 48u^6 + 6u^4 - 37u^2 + 19)$                        |
| $c_5, c_{11}$ | $(u^2 - u + 1)(u^{11} + u^{10} + \dots - u - 1)(u^{12} - 5u^{10} + \dots - 3u + 1)$ $\cdot (u^{14} + 3u^{13} + \dots + 3u + 1)$  |
| $c_6$         | $(u^2 - u + 1)(u^{11} + u^{10} + \dots - 145u - 67)(u^{12} + 7u^{11} + \dots - 841u + 683)$ $\cdot (u^{14} + 8u^{13} + \dots + 449u + 137)$                              |
| $c_7$         | $(u^2 + u + 1)(u^{11} + u^{10} + \dots + 56u + 8)(u^{12} - 3u^{11} + \dots + 184u + 83)$ $\cdot (u^{14} + 5u^{12} + \dots - 8u + 8)$                                     |
| $c_8$         | $(u^2 + u + 1)(u^6 + 2u^5 + 7u^4 + u^3 + 5u^2 + 1)^2$ $\cdot ((u^7 - 2u^5 + u^4 + u^3 + u - 1)^2)(u^{11} - 4u^{10} + \dots - 17u - 8)$                                   |
| $c_{12}$      | $u^2(u^6 - 2u^5 + 6u^4 - 2u^3 + 10u^2 - 2u + 5)^2$ $\cdot (u^{11} + 5u^{10} + \dots - 76u - 52)$ $\cdot (u^{14} - 4u^{12} + 6u^{10} + 5u^8 - 8u^6 - 15u^4 + 49u^2 + 19)$ |

## VI. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing  |
|--------------------|---|
| $c_1$              | $(y^2 + y + 1)(y^{11} + 13y^{10} + \dots + 49y - 1)(y^{12} + 22y^{11} + \dots + 635y + 1)$ $\cdot (y^{14} - y^{13} + \dots + 5y + 1)$                                       |
| $c_2, c_5, c_{11}$ | $(y^2 + y + 1)(y^{11} - 23y^{10} + \dots + 21y - 1)(y^{12} - 10y^{11} + \dots + 23y + 1)$ $\cdot (y^{14} + 7y^{13} + \dots - 3y + 1)$                                       |
| $c_3, c_9$         | $(y^2 + y + 1)(y^{11} - y^{10} + \dots + 3y - 1)(y^{12} - 2y^{11} + \dots - 10y + 1)$ $\cdot (y^{14} - 3y^{13} + \dots - 10y + 1)$  |
| $c_4, c_{10}$      | $y^2(y^6 - 5y^5 + 22y^4 - 56y^3 + 49y^2 + 4y + 16)^2$ $\cdot (y^7 - 9y^6 + 33y^5 - 60y^4 + 48y^3 + 6y^2 - 37y + 19)^2$ $\cdot (y^{11} - 8y^{10} + \dots + 208y - 64)$       |
| $c_6$              | $(y^2 + y + 1)(y^{11} + 31y^{10} + \dots - 35389y - 4489)$ $\cdot (y^{12} + 5y^{11} + \dots + 483871y + 466489)$ $\cdot (y^{14} - 20y^{13} + \dots - 90357y + 18769)$       |
| $c_7$              | $(y^2 + y + 1)(y^{11} - 7y^{10} + \dots + 1792y - 64)$ $\cdot (y^{12} - 11y^{11} + \dots - 9288y + 6889)(y^{14} + 10y^{13} + \dots + 448y + 64)$                            |
| $c_8$              | $(y^2 + y + 1)(y^6 + 10y^5 + 55y^4 + 71y^3 + 39y^2 + 10y + 1)^2$ $\cdot (y^7 - 4y^6 + 6y^5 - 3y^4 - 3y^3 + 4y^2 + y - 1)^2$ $\cdot (y^{11} + 12y^{10} + \dots + 961y - 64)$ |
| $c_{12}$           | $y^2(y^6 + 8y^5 + 48y^4 + 118y^3 + 152y^2 + 96y + 25)^2$ $\cdot (y^7 - 4y^6 + 6y^5 + 5y^4 - 8y^3 - 15y^2 + 49y + 19)^2$ $\cdot (y^{11} + 11y^{10} + \dots + 13056y - 2704)$ |