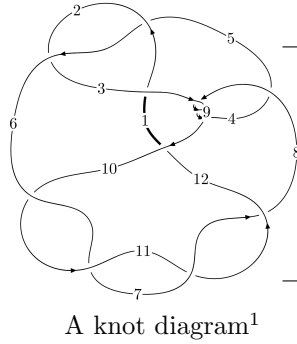
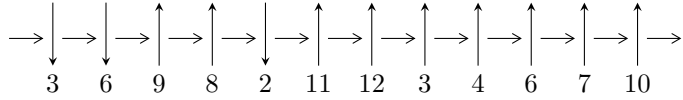


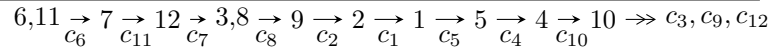
12n<sub>0466</sub> (K12n<sub>0466</sub>)



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -296878516u^{31} - 276724358u^{30} + \dots + 441171721b - 537239537, \\ - 397220095u^{31} - 1740337107u^{30} + \dots + 882343442a - 7870777298, u^{32} + 2u^{31} + \dots + 6u + 1 \rangle$$

$$I_2^u = \langle b - 1, a^2 + 2a - 2u - 3, u^2 + u - 1 \rangle$$

$$I_3^u = \langle b + 1, a - 1, u^2 - u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 38 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2.97 \times 10^8 u^{31} - 2.77 \times 10^8 u^{30} + \dots + 4.41 \times 10^8 b - 5.37 \times 10^8, -3.97 \times 10^8 u^{31} - 1.74 \times 10^9 u^{30} + \dots + 8.82 \times 10^8 a - 7.87 \times 10^9, u^{32} + 2u^{31} + \dots + 6u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.450188u^{31} + 1.97240u^{30} + \dots - 8.67806u + 8.92031 \\ 0.672932u^{31} + 0.627249u^{30} + \dots + 0.391427u + 1.21776 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2.40634u^{31} - 3.60527u^{30} + \dots + 10.8122u - 12.0712 \\ 0.218460u^{31} - 0.291561u^{30} + \dots + 2.47123u - 1.19894 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.12312u^{31} + 2.59965u^{30} + \dots - 8.28663u + 10.1381 \\ 0.672932u^{31} + 0.627249u^{30} + \dots + 0.391427u + 1.21776 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^5 + 2u^3 + u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.26155u^{31} - 2.69290u^{30} + \dots + 10.8624u - 9.38644 \\ -1.03259u^{31} - 0.976097u^{30} + \dots - 1.09592u - 1.51802 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.145728u^{31} - 1.66532u^{30} + \dots + 12.4977u - 7.36530 \\ -1.43787u^{31} - 1.24356u^{30} + \dots - 2.16974u - 1.82405 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{619975605}{441171721}u^{31} - \frac{1193144219}{441171721}u^{30} + \dots + \frac{5092498689}{441171721}u + \frac{1186500205}{441171721}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{32} + 37u^{31} + \dots + 305u + 1$
$c_2, c_5$	$u^{32} + 3u^{31} + \dots - 7u - 1$
$c_3, c_8, c_9$	$u^{32} + u^{31} + \dots - 4u + 4$
$c_4$	$u^{32} - 3u^{31} + \dots + 12u - 4$
$c_6, c_7, c_{10}$ $c_{11}$	$u^{32} + 2u^{31} + \dots + 6u + 1$
$c_{12}$	$u^{32} + 4u^{31} + \dots - 20u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{32} - 77y^{31} + \dots - 68569y + 1$
$c_2, c_5$	$y^{32} - 37y^{31} + \dots - 305y + 1$
$c_3, c_8, c_9$	$y^{32} - 27y^{31} + \dots - 208y + 16$
$c_4$	$y^{32} + 33y^{31} + \dots - 336y + 16$
$c_6, c_7, c_{10}$ $c_{11}$	$y^{32} - 36y^{31} + \dots - 56y + 1$
$c_{12}$	$y^{32} + 36y^{31} + \dots - 568y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.647923 + 0.702860I$ $a = -0.11556 - 1.50516I$ $b = -1.60683 + 0.23584I$	$-5.40621 + 7.69916I$	$6.58632 - 5.74078I$
$u = 0.647923 - 0.702860I$ $a = -0.11556 + 1.50516I$ $b = -1.60683 - 0.23584I$	$-5.40621 - 7.69916I$	$6.58632 + 5.74078I$
$u = -0.934535$ $a = 0.920748$ $b = -1.27591$	0.214319	11.1130
$u = -0.528252 + 0.752905I$ $a = 0.219575 - 1.040740I$ $b = 1.65258 + 0.07144I$	$-9.84928 - 2.50165I$	$2.86477 + 2.84418I$
$u = -0.528252 - 0.752905I$ $a = 0.219575 + 1.040740I$ $b = 1.65258 - 0.07144I$	$-9.84928 + 2.50165I$	$2.86477 - 2.84418I$
$u = 0.383863 + 0.766338I$ $a = -0.382365 - 0.514382I$ $b = -1.62188 - 0.11406I$	$-6.19158 - 2.80814I$	$5.10038 + 0.76938I$
$u = 0.383863 - 0.766338I$ $a = -0.382365 + 0.514382I$ $b = -1.62188 + 0.11406I$	$-6.19158 + 2.80814I$	$5.10038 - 0.76938I$
$u = -0.750792$ $a = -1.84633$ $b = 0.310110$	5.68749	17.7080
$u = 0.505153 + 0.538065I$ $a = 0.446790 + 1.310620I$ $b = 0.571805 - 0.732824I$	$1.93515 + 4.07265I$	$8.92952 - 7.04568I$
$u = 0.505153 - 0.538065I$ $a = 0.446790 - 1.310620I$ $b = 0.571805 + 0.732824I$	$1.93515 - 4.07265I$	$8.92952 + 7.04568I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.395138 + 0.481331I$ $a = -0.551243 - 0.194239I$ $b = 0.642691 + 0.571386I$	$1.68006 - 0.53375I$	$7.96422 - 0.32995I$
$u = 0.395138 - 0.481331I$ $a = -0.551243 + 0.194239I$ $b = 0.642691 - 0.571386I$	$1.68006 + 0.53375I$	$7.96422 + 0.32995I$
$u = -1.40514 + 0.25786I$ $a = 0.848313 + 0.771560I$ $b = -1.59035 - 0.06318I$	$-0.512682 - 0.890588I$	$8.15263 + 0.I$
$u = -1.40514 - 0.25786I$ $a = 0.848313 - 0.771560I$ $b = -1.59035 + 0.06318I$	$-0.512682 + 0.890588I$	$8.15263 + 0.I$
$u = 1.44428 + 0.09174I$ $a = 0.42149 - 1.57076I$ $b = -0.611773 + 0.763659I$	$4.34598 + 2.60375I$	$7.93484 - 3.36675I$
$u = 1.44428 - 0.09174I$ $a = 0.42149 + 1.57076I$ $b = -0.611773 - 0.763659I$	$4.34598 - 2.60375I$	$7.93484 + 3.36675I$
$u = 1.44949$ $a = 0.265813$ $b = 1.38846$	$8.83218$	$9.93110$
$u = -1.45288 + 0.07180I$ $a = -0.88013 + 1.22133I$ $b = 0.795382 - 0.670343I$	$7.57700 - 1.16778I$	$11.36341 + 0.54162I$
$u = -1.45288 - 0.07180I$ $a = -0.88013 - 1.22133I$ $b = 0.795382 + 0.670343I$	$7.57700 + 1.16778I$	$11.36341 - 0.54162I$
$u = -1.51955 + 0.16796I$ $a = -0.08132 - 1.78171I$ $b = 0.464019 + 0.904411I$	$8.62955 - 6.62987I$	$12.50269 + 5.26876I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.51955 - 0.16796I$ $a = -0.08132 + 1.78171I$ $b = 0.464019 - 0.904411I$	$8.62955 + 6.62987I$	$12.50269 - 5.26876I$
$u = -0.299017 + 0.362824I$ $a = -0.106458 + 1.400860I$ $b = -0.751935 - 0.325766I$	$-1.32881 - 1.04587I$	$0.13410 + 4.26985I$
$u = -0.299017 - 0.362824I$ $a = -0.106458 - 1.400860I$ $b = -0.751935 + 0.325766I$	$-1.32881 + 1.04587I$	$0.13410 - 4.26985I$
$u = 1.52451 + 0.26507I$ $a = -0.93070 + 1.22794I$ $b = 1.61492 - 0.22198I$	$-3.16368 + 6.23347I$	$6.00000 - 3.63332I$
$u = 1.52451 - 0.26507I$ $a = -0.93070 - 1.22794I$ $b = 1.61492 + 0.22198I$	$-3.16368 - 6.23347I$	$6.00000 + 3.63332I$
$u = 0.451835$ $a = 0.432993$ $b = 0.202201$	$0.642131$	$15.9520$
$u = -1.58469$ $a = -0.466896$ $b = 0.692717$	$7.78318$	$17.5750$
$u = -1.58841 + 0.23470I$ $a = 0.92703 + 1.56136I$ $b = -1.56211 - 0.33651I$	$2.01653 - 11.20740I$	$0$
$u = -1.58841 - 0.23470I$ $a = 0.92703 - 1.56136I$ $b = -1.56211 + 0.33651I$	$2.01653 + 11.20740I$	$0$
$u = 1.61270$ $a = -0.848466$ $b = -0.0619566$	$13.8091$	$18.0020$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.68667$ $a = 1.46963$ $b = -1.31101$	9.57646	6.00000
$u = -0.145893$ $a = 9.44166$ $b = 1.06237$	3.33910	1.65970



$$\text{II. } I_2^u = \langle b - 1, a^2 + 2a - 2u - 3, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} au - 2 \\ -au - 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -au - u + 1 \\ au - a + u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u - 1)^4$
$c_2$	$(u + 1)^4$
$c_3, c_4, c_8$ $c_9$	$(u^2 - 2)^2$
$c_6, c_7, c_{12}$	$(u^2 + u - 1)^2$
$c_{10}, c_{11}$	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^4$
$c_3, c_4, c_8$ $c_9$	$(y - 2)^4$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = 1.28825$ $b = 1.00000$	4.27683	12.0000
$u = 0.618034$ $a = -3.28825$ $b = 1.00000$	4.27683	12.0000
$u = -1.61803$ $a = -0.125968$ $b = 1.00000$	12.1725	12.0000
$u = -1.61803$ $a = -1.87403$ $b = 1.00000$	12.1725	12.0000

$$\text{III. } I_3^u = \langle b + 1, a - 1, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 2

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_4, c_8$ $c_9$	$u^2$
$c_5$	$(u + 1)^2$
$c_6, c_7$	$u^2 - u - 1$
$c_{10}, c_{11}, c_{12}$	$u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^2$
$c_3, c_4, c_8$ $c_9$	$y^2$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y^2 - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = 1.00000$ $b = -1.00000$	-0.657974	2.00000
$u = 1.61803$ $a = 1.00000$ $b = -1.00000$	7.23771	2.00000



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^6)(u^{32} + 37u^{31} + \dots + 305u + 1)$
$c_2$	$((u-1)^2)(u+1)^4(u^{32} + 3u^{31} + \dots - 7u - 1)$
$c_3, c_8, c_9$	$u^2(u^2 - 2)^2(u^{32} + u^{31} + \dots - 4u + 4)$
$c_4$	$u^2(u^2 - 2)^2(u^{32} - 3u^{31} + \dots + 12u - 4)$
$c_5$	$((u-1)^4)(u+1)^2(u^{32} + 3u^{31} + \dots - 7u - 1)$
$c_6, c_7$	$(u^2 - u - 1)(u^2 + u - 1)^2(u^{32} + 2u^{31} + \dots + 6u + 1)$
$c_{10}, c_{11}$	$((u^2 - u - 1)^2)(u^2 + u - 1)(u^{32} + 2u^{31} + \dots + 6u + 1)$
$c_{12}$	$((u^2 + u - 1)^3)(u^{32} + 4u^{31} + \dots - 20u + 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^6)(y^{32} - 77y^{31} + \dots - 68569y + 1)$
$c_2, c_5$	$((y - 1)^6)(y^{32} - 37y^{31} + \dots - 305y + 1)$
$c_3, c_8, c_9$	$y^2(y - 2)^4(y^{32} - 27y^{31} + \dots - 208y + 16)$
$c_4$	$y^2(y - 2)^4(y^{32} + 33y^{31} + \dots - 336y + 16)$
$c_6, c_7, c_{10}$ $c_{11}$	$((y^2 - 3y + 1)^3)(y^{32} - 36y^{31} + \dots - 56y + 1)$
$c_{12}$	$((y^2 - 3y + 1)^3)(y^{32} + 36y^{31} + \dots - 568y + 1)$