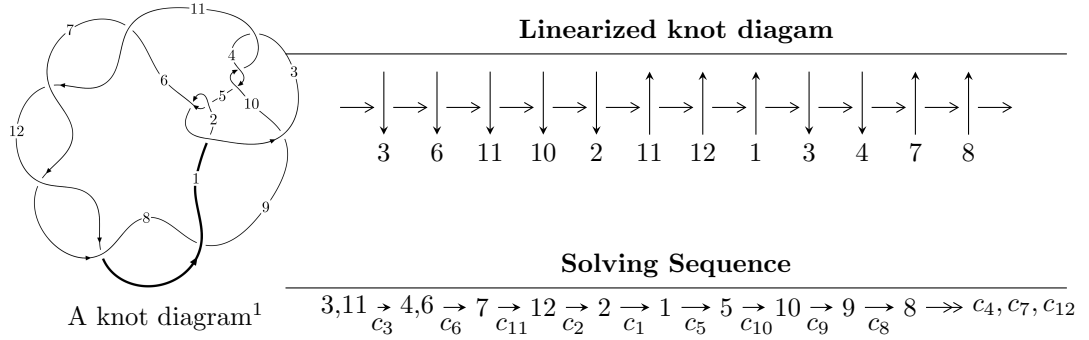


12n₀₄₇₅ (K12n₀₄₇₅)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^7 - u^6 + 6u^5 - 3u^4 + 8u^3 - 6u^2 + 2b + 2u - 2, -u^7 + 2u^6 - 7u^5 + 7u^4 - 9u^3 + 4u^2 + 4a - 6u - 2, u^9 - u^8 + 10u^7 - 3u^6 + 30u^5 + 4u^4 + 36u^3 + 8u - 4 \rangle$$

$$I_2^u = \langle b + 1, 2a^2 - au + 1, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - 1, v^2 + v - 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 15 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^7 - u^6 + 6u^5 - 3u^4 + 8u^3 - 6u^2 + 2b + 2u - 2, -u^7 + 2u^6 + \dots + 4a - 2, u^9 - u^8 + \dots + 8u - 4 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{4}u^7 - \frac{1}{2}u^6 + \dots + \frac{3}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^7 + \frac{1}{2}u^6 + \dots - u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{4}u^7 - \frac{1}{2}u^6 + \dots + \frac{3}{2}u + \frac{1}{2} \\ \frac{1}{4}u^8 + \frac{1}{4}u^7 + \dots + \frac{5}{2}u^2 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{4}u^7 + \frac{7}{4}u^5 + \dots + \frac{3}{2}u - \frac{1}{2} \\ \frac{1}{4}u^7 - \frac{1}{4}u^6 + \dots + 2u^3 + \frac{3}{2}u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{4}u^8 - 2u^6 + \dots + \frac{1}{2}u + \frac{1}{2} \\ u^7 + 5u^5 + 3u^4 + 6u^3 - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{4}u^8 + u^7 + \dots + \frac{1}{2}u - \frac{1}{2} \\ u^7 + 5u^5 + 3u^4 + 6u^3 - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{4}u^8 - \frac{3}{2}u^6 + \dots + \frac{3}{2}u + \frac{1}{2} \\ -\frac{1}{4}u^8 - \frac{5}{4}u^6 + \dots + \frac{1}{2}u^2 + \frac{3}{2}u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-u^8 + u^7 - 10u^6 + 4u^5 - 31u^4 - 37u^2 - 2u - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^9 - 5u^8 + \dots + 20u + 121$
c_2, c_5	$u^9 + 3u^8 + 7u^7 + 8u^6 + 9u^5 - 14u^4 + 29u^3 + 8u^2 - 14u + 11$
c_3, c_4, c_{10}	$u^9 + u^8 + 10u^7 + 3u^6 + 30u^5 - 4u^4 + 36u^3 + 8u + 4$
c_6, c_7, c_8 c_{11}, c_{12}	$u^9 + 2u^8 - 7u^7 - 14u^6 + 16u^5 + 33u^4 - 5u^3 - 13u^2 + 7u + 3$
c_9	$u^9 - 19u^8 + \dots + 1064u + 212$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^9 + 13y^8 + \dots - 137056y - 14641$
c_2, c_5	$y^9 + 5y^8 + \dots + 20y - 121$
c_3, c_4, c_{10}	$y^9 + 19y^8 + \dots + 64y - 16$
c_6, c_7, c_8 c_{11}, c_{12}	$y^9 - 18y^8 + \dots + 127y - 9$
c_9	$y^9 + 7y^8 + \dots + 50048y - 44944$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.356661 + 1.085780I$ $a = -0.402756 - 1.012080I$ $b = -0.703349 + 0.767146I$	$6.51508 + 2.26295I$	$5.26586 - 3.19513I$
$u = -0.356661 - 1.085780I$ $a = -0.402756 + 1.012080I$ $b = -0.703349 - 0.767146I$	$6.51508 - 2.26295I$	$5.26586 + 3.19513I$
$u = -0.218744 + 0.648601I$ $a = 0.771686 + 0.526493I$ $b = -0.432002 - 0.509023I$	$1.07917 - 0.96089I$	$3.53169 + 3.58492I$
$u = -0.218744 - 0.648601I$ $a = 0.771686 - 0.526493I$ $b = -0.432002 + 0.509023I$	$1.07917 + 0.96089I$	$3.53169 - 3.58492I$
$u = 0.325488$ $a = 0.946130$ $b = 0.860684$	-1.12741	-12.9160
$u = 0.47728 + 2.04979I$ $a = -0.410722 + 0.825671I$ $b = 0.27104 - 2.15157I$	$17.8250 + 0.9503I$	$4.58159 - 0.40162I$
$u = 0.47728 - 2.04979I$ $a = -0.410722 - 0.825671I$ $b = 0.27104 + 2.15157I$	$17.8250 - 0.9503I$	$4.58159 + 0.40162I$
$u = 0.43538 + 2.08426I$ $a = 0.068727 - 0.946296I$ $b = 1.93397 + 1.37424I$	$-7.58379 - 6.45137I$	$4.07876 + 2.00413I$
$u = 0.43538 - 2.08426I$ $a = 0.068727 + 0.946296I$ $b = 1.93397 - 1.37424I$	$-7.58379 + 6.45137I$	$4.07876 - 2.00413I$

$$\text{II. } I_2^u = \langle b + 1, 2a^2 - au + 1, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ 2a - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a - \frac{1}{2}u \\ -au - 2a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a - \frac{1}{2}u \\ -au - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$(u - 1)^4$
c_2	$(u + 1)^4$
c_3, c_4, c_9 c_{10}	$(u^2 + 2)^2$
c_6, c_7, c_8	$(u^2 + u - 1)^2$
c_{11}, c_{12}	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^4$
c_3, c_4, c_9 c_{10}	$(y + 2)^4$
c_6, c_7, c_8 c_{11}, c_{12}	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.414210I$	12.1725	4.00000
$a =$	$1.144120I$		
$b =$	-1.00000		
$u =$	$1.414210I$	4.27683	4.00000
$a =$	$-0.437016I$		
$b =$	-1.00000		
$u =$	$-1.414210I$	12.1725	4.00000
$a =$	$-1.144120I$		
$b =$	-1.00000		
$u =$	$-1.414210I$	4.27683	4.00000
$a =$	$0.437016I$		
$b =$	-1.00000		

$$\text{III. } I_1^v = \langle a, b - 1, v^2 + v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -v + 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -v + 1 \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ v \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^2$
c_3, c_4, c_9 c_{10}	u^2
c_5	$(u + 1)^2$
c_6, c_7, c_8	$u^2 - u - 1$
c_{11}, c_{12}	$u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^2$
c_3, c_4, c_9 c_{10}	y^2
c_6, c_7, c_8 c_{11}, c_{12}	$y^2 - 3y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.618034$ $a = 0$ $b = 1.00000$	-0.657974	6.00000
$v = -1.61803$ $a = 0$ $b = 1.00000$	7.23771	6.00000

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^6)(u^9 - 5u^8 + \dots + 20u + 121)$
c_2	$(u-1)^2(u+1)^4$ $\cdot (u^9 + 3u^8 + 7u^7 + 8u^6 + 9u^5 - 14u^4 + 29u^3 + 8u^2 - 14u + 11)$
c_3, c_4, c_{10}	$u^2(u^2+2)^2(u^9 + u^8 + 10u^7 + 3u^6 + 30u^5 - 4u^4 + 36u^3 + 8u + 4)$
c_5	$(u-1)^4(u+1)^2$ $\cdot (u^9 + 3u^8 + 7u^7 + 8u^6 + 9u^5 - 14u^4 + 29u^3 + 8u^2 - 14u + 11)$
c_6, c_7, c_8	$(u^2 - u - 1)(u^2 + u - 1)^2$ $\cdot (u^9 + 2u^8 - 7u^7 - 14u^6 + 16u^5 + 33u^4 - 5u^3 - 13u^2 + 7u + 3)$
c_9	$u^2(u^2+2)^2(u^9 - 19u^8 + \dots + 1064u + 212)$
c_{11}, c_{12}	$(u^2 - u - 1)^2(u^2 + u - 1)$ $\cdot (u^9 + 2u^8 - 7u^7 - 14u^6 + 16u^5 + 33u^4 - 5u^3 - 13u^2 + 7u + 3)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^6)(y^9 + 13y^8 + \dots - 137056y - 14641)$
c_2, c_5	$((y - 1)^6)(y^9 + 5y^8 + \dots + 20y - 121)$
c_3, c_4, c_{10}	$y^2(y + 2)^4(y^9 + 19y^8 + \dots + 64y - 16)$
c_6, c_7, c_8 c_{11}, c_{12}	$((y^2 - 3y + 1)^3)(y^9 - 18y^8 + \dots + 127y - 9)$
c_9	$y^2(y + 2)^4(y^9 + 7y^8 + \dots + 50048y - 44944)$