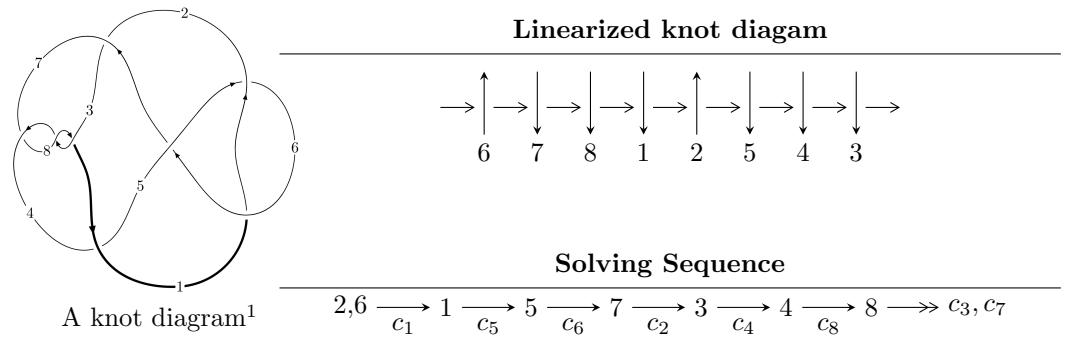


## 8<sub>11</sub> (K8a<sub>9</sub>)



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle u^{10} - u^9 + 3u^8 - 3u^7 + 5u^6 - 5u^5 + 4u^4 - 4u^3 + 3u^2 - 2u + 1 \rangle$$

$$I_2^u = \langle u^3 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 13 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{10} - u^9 + 3u^8 - 3u^7 + 5u^6 - 5u^5 + 4u^4 - 4u^3 + 3u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^5 - 2u^3 + u^2 - u + 1 \\ -u^9 - 3u^7 - 4u^5 + u^4 - u^3 + 2u^2 + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^9 + 4u^8 - 8u^7 + 8u^6 - 8u^5 + 12u^4 + 4u^2 - 4u - 2$

**(iv) u-Polynomials at the component**

| Crossings       | u-Polynomials at each crossing  |
|-----------------|---|
| $c_1, c_5$      | $u^{10} - u^9 + 3u^8 - 3u^7 + 5u^6 - 5u^5 + 4u^4 - 4u^3 + 3u^2 - 2u + 1$  |
| $c_2, c_4$      | $u^{10} - 2u^9 - u^8 + 5u^7 - 3u^6 - 4u^5 + 12u^4 - 13u^3 + 5u^2 - u + 2$ |
| $c_3, c_7, c_8$ | $u^{10} - u^9 + 5u^8 - 5u^7 + 9u^6 - 9u^5 + 6u^4 - 6u^3 + u^2 + 1$        |
| $c_6$           | $u^{10} + 5u^9 + 13u^8 + 19u^7 + 17u^6 + 7u^5 - 2u^3 + u^2 + 2u + 1$      |

**(v) Riley Polynomials at the component**

| Crossings       | Riley Polynomials at each crossing  |
|-----------------|---|
| $c_1, c_5$      | $y^{10} + 5y^9 + 13y^8 + 19y^7 + 17y^6 + 7y^5 - 2y^3 + y^2 + 2y + 1$            |
| $c_2, c_4$      | $y^{10} - 6y^9 + \dots + 19y + 4$   |
| $c_3, c_7, c_8$ | $y^{10} + 9y^9 + 33y^8 + 59y^7 + 41y^6 - 21y^5 - 44y^4 - 6y^3 + 13y^2 + 2y + 1$ |
| $c_6$           | $y^{10} + y^9 + 13y^8 + 11y^7 + 45y^6 + 35y^5 + 12y^4 + 2y^3 + 9y^2 - 2y + 1$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.584958 + 0.771492I$ | $4.93719 - 2.31006I$                  | $0.86369 + 3.52133I$  |
| $u = -0.584958 - 0.771492I$ | $4.93719 + 2.31006I$                  | $0.86369 - 3.52133I$  |
| $u = 0.248527 + 0.782547I$  | $-0.448055 + 1.231690I$               | $-4.90177 - 5.44908I$ |
| $u = 0.248527 - 0.782547I$  | $-0.448055 - 1.231690I$               | $-4.90177 + 5.44908I$ |
| $u = 0.761643 + 0.208049I$  | $2.41360 - 3.47839I$                  | $-0.80497 + 2.79515I$ |
| $u = 0.761643 - 0.208049I$  | $2.41360 + 3.47839I$                  | $-0.80497 - 2.79515I$ |
| $u = -0.449566 + 1.164790I$ | $-4.87665 - 4.14585I$                 | $-8.98134 + 3.97600I$ |
| $u = -0.449566 - 1.164790I$ | $-4.87665 + 4.14585I$                 | $-8.98134 - 3.97600I$ |
| $u = 0.524355 + 1.163410I$  | $-0.38115 + 8.28632I$                 | $-4.17560 - 6.14881I$ |
| $u = 0.524355 - 1.163410I$  | $-0.38115 - 8.28632I$                 | $-4.17560 + 6.14881I$ |

$$\text{II. } I_2^u = \langle u^3 + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u+1 \\ -1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u-1 \\ -u^2+u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^2+1 \\ u^2+u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

**(iv) u-Polynomials at the component**

| Crossings                     | u-Polynomials at each crossing |
|-------------------------------|--------------------------------|
| $c_1, c_3, c_5$<br>$c_7, c_8$ | $u^3 + u + 1$                  |
| $c_2, c_4$                    | $(u + 1)^3$                    |
| $c_6$                         | $u^3 + 2u^2 + u - 1$           |

**(v) Riley Polynomials at the component**

| Crossings                     | Riley Polynomials at each crossing |
|-------------------------------|------------------------------------|
| $c_1, c_3, c_5$<br>$c_7, c_8$ | $y^3 + 2y^2 + y - 1$               |
| $c_2, c_4$                    | $(y - 1)^3$                        |
| $c_6$                         | $y^3 - 2y^2 + 5y - 1$              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_2^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|------------|
| $u = 0.341164 + 1.161540I$ | -1.64493                              | -6.00000   |
| $u = 0.341164 - 1.161540I$ | -1.64493                              | -6.00000   |
| $u = -0.682328$            | -1.64493                              | -6.00000   |

### III. u-Polynomials

| Crossings       | u-Polynomials at each crossing  |
|-----------------|---|
| $c_1, c_5$      | $(u^3 + u + 1)(u^{10} - u^9 + \cdots - 2u + 1)$   |
| $c_2, c_4$      | $((u + 1)^3)(u^{10} - 2u^9 + \cdots - u + 2)$   |
| $c_3, c_7, c_8$ | $(u^3 + u + 1)(u^{10} - u^9 + 5u^8 - 5u^7 + 9u^6 - 9u^5 + 6u^4 - 6u^3 + u^2 + 1)$                   |
| $c_6$           | $(u^3 + 2u^2 + u - 1)$ $\cdot (u^{10} + 5u^9 + 13u^8 + 19u^7 + 17u^6 + 7u^5 - 2u^3 + u^2 + 2u + 1)$ |

#### IV. Riley Polynomials

| Crossings       | Riley Polynomials at each crossing   |
|-----------------|--|
| $c_1, c_5$      | $(y^3 + 2y^2 + y - 1) \cdot (y^{10} + 5y^9 + 13y^8 + 19y^7 + 17y^6 + 7y^5 - 2y^3 + y^2 + 2y + 1)$            |
| $c_2, c_4$      | $((y - 1)^3)(y^{10} - 6y^9 + \cdots + 19y + 4)$  |
| $c_3, c_7, c_8$ | $(y^3 + 2y^2 + y - 1) \cdot (y^{10} + 9y^9 + 33y^8 + 59y^7 + 41y^6 - 21y^5 - 44y^4 - 6y^3 + 13y^2 + 2y + 1)$ |
| $c_6$           | $(y^3 - 2y^2 + 5y - 1) \cdot (y^{10} + y^9 + 13y^8 + 11y^7 + 45y^6 + 35y^5 + 12y^4 + 2y^3 + 9y^2 - 2y + 1)$  |