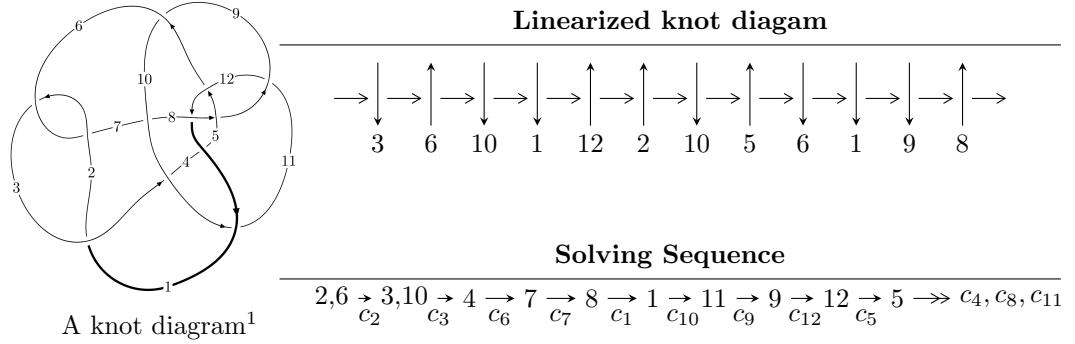


## $12n_{0521}$ ( $K12n_{0521}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 432917u^{27} + 3841573u^{26} + \dots + 262964b + 2783376, \\
 &\quad 413130u^{27} + 3479001u^{26} + \dots + 262964a + 1217429, u^{28} + 9u^{27} + \dots + 124u + 16 \rangle \\
 I_2^u &= \langle -87u^{16} + 385u^{15} + \dots + 77b - 41, -190u^{16} + 693u^{15} + \dots + 231a - 163, u^{17} - 4u^{16} + \dots - 6u^2 - 1 \rangle \\
 I_3^u &= \langle 343u^{10}a^3 + 5345u^{10}a^2 + \dots + 5127a + 18129, u^{10}a^3 - 3u^{10}a^2 + \dots + 26a + 1, \\
 &\quad u^{11} - 2u^{10} + 6u^9 - 8u^8 + 12u^7 - 13u^6 + 12u^5 - 13u^4 + 9u^3 - 8u^2 + 4u - 1 \rangle \\
 I_4^u &= \langle b - a + u, a^2 + a - u - 1, u^2 + u + 1 \rangle \\
 I_5^u &= \langle b - a + 1, a^2 - au - a + 1, u^2 + u + 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 97 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 4.33 \times 10^5 u^{27} + 3.84 \times 10^6 u^{26} + \dots + 2.63 \times 10^5 b + 2.78 \times 10^6, 4.13 \times 10^5 u^{27} + 3.48 \times 10^6 u^{26} + \dots + 2.63 \times 10^5 a + 1.22 \times 10^6, u^{28} + 9u^{27} + \dots + 124u + 16 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1.57105u^{27} - 13.2300u^{26} + \dots - 55.0012u - 4.62964 \\ -1.64630u^{27} - 14.6087u^{26} + \dots - 102.538u - 10.5846 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.956809u^{27} + 9.01001u^{26} + \dots + 2.45249u - 3.84208 \\ 1.67232u^{27} + 15.4625u^{26} + \dots + 188.238u + 21.6886 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.715515u^{27} - 6.45245u^{26} + \dots - 184.785u - 26.5307 \\ 0.687566u^{27} + 5.41127u^{26} + \dots - 74.2301u - 11.6532 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.693057u^{27} - 6.09592u^{26} + \dots + 30.7434u + 7.11420 \\ -2.14571u^{27} - 18.5603u^{26} + \dots - 94.5924u - 9.92361 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1.57105u^{27} - 13.2300u^{26} + \dots - 55.0012u - 4.62964 \\ -2.38308u^{27} - 20.2951u^{26} + \dots - 14.8953u + 3.96757 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.33446u^{27} - 10.2494u^{26} + \dots - 6.34518u + 1.73776 \\ 1.02850u^{27} + 9.08118u^{26} + \dots + 212.265u + 31.6255 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2.39557u^{27} + 20.4749u^{26} + \dots + 148.520u + 18.4022 \\ 1.49590u^{27} + 15.8334u^{26} + \dots + 111.117u + 8.74080 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-\frac{394167}{65741}u^{27} - \frac{3195674}{65741}u^{26} + \dots - \frac{10576918}{65741}u - \frac{485930}{65741}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{28} + 17u^{27} + \cdots + 1360u + 256$
$c_2, c_6$	$u^{28} - 9u^{27} + \cdots - 124u + 16$
$c_3, c_9$	$u^{28} + u^{27} + \cdots + u + 1$
$c_4$	$u^{28} - 2u^{27} + \cdots - 45u + 25$
$c_5, c_8$	$u^{28} + u^{26} + \cdots + 3u + 1$
$c_7, c_{10}$	$u^{28} + u^{27} + \cdots + 21u + 1$
$c_{11}$	$u^{28} - 28u^{27} + \cdots - 50u + 4$
$c_{12}$	$u^{28} - 26u^{27} + \cdots - 5120u + 512$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{28} - 11y^{27} + \cdots + 264448y + 65536$
$c_2, c_6$	$y^{28} + 17y^{27} + \cdots + 1360y + 256$
$c_3, c_9$	$y^{28} - 31y^{27} + \cdots - 7y + 1$
$c_4$	$y^{28} - 16y^{27} + \cdots - 10575y + 625$
$c_5, c_8$	$y^{28} + 2y^{27} + \cdots + y + 1$
$c_7, c_{10}$	$y^{28} - 39y^{27} + \cdots - 197y + 1$
$c_{11}$	$y^{28} - 22y^{27} + \cdots - 188y + 16$
$c_{12}$	$y^{28} - 6y^{27} + \cdots - 1310720y + 262144$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.029760 + 1.024060I$		
$a = -0.76705 + 1.20618I$	$-1.70801 + 1.93955I$	$-4.01504 - 3.31370I$
$b = 0.33513 + 2.03849I$		
$u = -0.029760 - 1.024060I$		
$a = -0.76705 - 1.20618I$	$-1.70801 - 1.93955I$	$-4.01504 + 3.31370I$
$b = 0.33513 - 2.03849I$		
$u = -0.205800 + 0.952470I$		
$a = -0.890270 - 0.134444I$	$-1.87676 - 2.57239I$	$-5.76873 + 3.90772I$
$b = -1.028510 + 0.354995I$		
$u = -0.205800 - 0.952470I$		
$a = -0.890270 + 0.134444I$	$-1.87676 + 2.57239I$	$-5.76873 - 3.90772I$
$b = -1.028510 - 0.354995I$		
$u = 0.703844 + 0.651022I$		
$a = 0.364061 + 0.072255I$	$2.58954 - 1.93444I$	$4.44360 + 1.82417I$
$b = -0.169040 - 0.626677I$		
$u = 0.703844 - 0.651022I$		
$a = 0.364061 - 0.072255I$	$2.58954 + 1.93444I$	$4.44360 - 1.82417I$
$b = -0.169040 + 0.626677I$		
$u = -0.233119 + 1.022850I$		
$a = 0.432125 - 0.884732I$	$-0.84729 - 2.02401I$	$-1.05491 + 4.41629I$
$b = 0.046325 - 1.319720I$		
$u = -0.233119 - 1.022850I$		
$a = 0.432125 + 0.884732I$	$-0.84729 + 2.02401I$	$-1.05491 - 4.41629I$
$b = 0.046325 + 1.319720I$		
$u = -0.592728 + 0.886067I$		
$a = 0.419564 - 0.328119I$	$0.19636 - 2.32367I$	$1.59759 + 0.30167I$
$b = 0.484607 - 0.267874I$		
$u = -0.592728 - 0.886067I$		
$a = 0.419564 + 0.328119I$	$0.19636 + 2.32367I$	$1.59759 - 0.30167I$
$b = 0.484607 + 0.267874I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.126080 + 0.017717I$		
$a = 1.48097 - 0.28232I$	$-9.14619 + 10.60730I$	$-4.00237 - 5.50977I$
$b = -0.203539 + 0.072850I$		
$u = -1.126080 - 0.017717I$		
$a = 1.48097 + 0.28232I$	$-9.14619 - 10.60730I$	$-4.00237 + 5.50977I$
$b = -0.203539 - 0.072850I$		
$u = -1.213710 + 0.122756I$		
$a = -1.169300 - 0.161303I$	$-6.88343 + 0.76194I$	$-9.63760 - 8.88824I$
$b = 0.313944 - 0.165481I$		
$u = -1.213710 - 0.122756I$		
$a = -1.169300 + 0.161303I$	$-6.88343 - 0.76194I$	$-9.63760 + 8.88824I$
$b = 0.313944 + 0.165481I$		
$u = 0.134895 + 0.764791I$		
$a = 0.249686 - 0.929537I$	$-1.33224 - 1.70353I$	$-4.58528 + 4.79833I$
$b = -0.794879 - 0.643863I$		
$u = 0.134895 - 0.764791I$		
$a = 0.249686 + 0.929537I$	$-1.33224 + 1.70353I$	$-4.58528 - 4.79833I$
$b = -0.794879 + 0.643863I$		
$u = 0.679542 + 1.054720I$		
$a = -0.182005 + 0.228644I$	$1.38884 + 7.31481I$	$-0.62097 - 4.93244I$
$b = 0.574163 + 0.446259I$		
$u = 0.679542 - 1.054720I$		
$a = -0.182005 - 0.228644I$	$1.38884 - 7.31481I$	$-0.62097 + 4.93244I$
$b = 0.574163 - 0.446259I$		
$u = -0.460065 + 0.249682I$		
$a = 0.997340 - 0.899044I$	$1.23290 - 0.94981I$	$4.62875 + 1.98787I$
$b = 0.291991 - 0.299264I$		
$u = -0.460065 - 0.249682I$		
$a = 0.997340 + 0.899044I$	$1.23290 + 0.94981I$	$4.62875 - 1.98787I$
$b = 0.291991 + 0.299264I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.55190 + 1.37856I$		
$a = -0.123948 - 1.306340I$	$-13.4242 - 16.5538I$	$0. + 7.97631I$
$b = -0.07928 - 2.82342I$		
$u = -0.55190 - 1.37856I$		
$a = -0.123948 + 1.306340I$	$-13.4242 + 16.5538I$	$0. - 7.97631I$
$b = -0.07928 + 2.82342I$		
$u = -0.52857 + 1.41990I$		
$a = -0.376449 - 1.012200I$	$-13.6922 + 4.6715I$	0
$b = -0.77064 - 2.32349I$		
$u = -0.52857 - 1.41990I$		
$a = -0.376449 + 1.012200I$	$-13.6922 - 4.6715I$	0
$b = -0.77064 + 2.32349I$		
$u = -0.61460 + 1.40685I$		
$a = 0.274785 + 0.995117I$	$-10.96370 - 7.28590I$	0
$b = 0.28808 + 2.29388I$		
$u = -0.61460 - 1.40685I$		
$a = 0.274785 - 0.995117I$	$-10.96370 + 7.28590I$	0
$b = 0.28808 - 2.29388I$		
$u = -0.46195 + 1.47320I$		
$a = 0.040494 + 1.014100I$	$-12.15350 - 5.19576I$	$-13.77473 + 0.I$
$b = 0.21165 + 2.44842I$		
$u = -0.46195 - 1.47320I$		
$a = 0.040494 - 1.014100I$	$-12.15350 + 5.19576I$	$-13.77473 + 0.I$
$b = 0.21165 - 2.44842I$		

$$\text{II. } I_2^u = \langle -87u^{16} + 385u^{15} + \cdots + 77b - 41, -190u^{16} + 693u^{15} + \cdots + 231a - 163, u^{17} - 4u^{16} + \cdots - 6u^2 - 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.822511u^{16} - 3u^{15} + \cdots + 1.92641u + 0.705628 \\ \frac{87}{77}u^{16} - 5u^{15} + \cdots - \frac{9}{77}u + \frac{41}{77} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.307359u^{16} - 3u^{15} + \cdots - 2.04329u + 2.82684 \\ -1.68831u^{16} + 5u^{15} + \cdots + 1.51948u + 2.07792 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1.99567u^{16} + 8u^{15} + \cdots + 4.56277u + 0.251082 \\ -1.05195u^{16} + 5u^{15} + \cdots + 3.24675u - 2.01299 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.722944u^{16} - 2u^{15} + \cdots + 0.982684u + 0.930736 \\ \frac{46}{33}u^{16} - 5u^{15} + \cdots - \frac{26}{33}u - \frac{5}{33} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.822511u^{16} - 3u^{15} + \cdots + 1.92641u + 0.705628 \\ \frac{65}{33}u^{16} - 8u^{15} + \cdots - \frac{31}{33}u + \frac{8}{33} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.995671u^{16} - 3u^{15} + \cdots + 0.437229u - 2.25108 \\ 0.757576u^{16} - 3u^{15} + \cdots - 4.51515u - 0.0606061 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.601732u^{16} - 4u^{15} + \cdots - 1.77489u + 1.90043 \\ -1.12121u^{16} + 2u^{15} + \cdots + 1.24242u + 2.96970 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-\frac{733}{231}u^{16} + 12u^{15} + \cdots - \frac{1504}{231}u - \frac{2089}{231}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{17} - 10u^{16} + \cdots - 12u + 1$
$c_2$	$u^{17} - 4u^{16} + \cdots - 6u^2 - 1$
$c_3, c_9$	$u^{17} - u^{16} + \cdots + 3u + 1$
$c_4$	$u^{17} + 2u^{16} + \cdots + 9u + 3$
$c_5, c_8$	$u^{17} + 3u^{15} + \cdots - u + 1$
$c_6$	$u^{17} + 4u^{16} + \cdots + 6u^2 + 1$
$c_7, c_{10}$	$u^{17} - 7u^{16} + \cdots + 3u - 1$
$c_{11}$	$u^{17} + 11u^{16} + \cdots - 3066u - 441$
$c_{12}$	$u^{17} + 5u^{16} + \cdots - 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{17} - 2y^{16} + \cdots - 72y - 1$
$c_2, c_6$	$y^{17} + 10y^{16} + \cdots - 12y - 1$
$c_3, c_9$	$y^{17} - 15y^{16} + \cdots - 5y - 1$
$c_4$	$y^{17} - 8y^{16} + \cdots - 69y - 9$
$c_5, c_8$	$y^{17} + 6y^{16} + \cdots - y - 1$
$c_7, c_{10}$	$y^{17} - 15y^{16} + \cdots - 7y - 1$
$c_{11}$	$y^{17} - 17y^{16} + \cdots + 1120140y - 194481$
$c_{12}$	$y^{17} - 7y^{16} + \cdots + 10y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.681671 + 0.839345I$		
$a = -0.122858 + 0.250052I$	$-0.38004 - 2.63462I$	$-9.27234 + 5.42347I$
$b = -0.441734 - 0.354193I$		
$u = -0.681671 - 0.839345I$		
$a = -0.122858 - 0.250052I$	$-0.38004 + 2.63462I$	$-9.27234 - 5.42347I$
$b = -0.441734 + 0.354193I$		
$u = 0.140165 + 1.110590I$		
$a = 0.71958 + 1.33512I$	$-4.67353 + 6.46548I$	$-8.36385 - 4.08762I$
$b = -0.09285 + 2.38278I$		
$u = 0.140165 - 1.110590I$		
$a = 0.71958 - 1.33512I$	$-4.67353 - 6.46548I$	$-8.36385 + 4.08762I$
$b = -0.09285 - 2.38278I$		
$u = 0.826686 + 0.794603I$		
$a = -0.711849 + 0.393093I$	$1.46643 - 2.44849I$	$-3.63614 + 3.80526I$
$b = -0.347366 + 0.674089I$		
$u = 0.826686 - 0.794603I$		
$a = -0.711849 - 0.393093I$	$1.46643 + 2.44849I$	$-3.63614 - 3.80526I$
$b = -0.347366 - 0.674089I$		
$u = 1.16029$		
$a = -1.30387$	$-6.83994$	$-5.94510$
$b = 0.242504$		
$u = 0.760360 + 0.946681I$		
$a = 0.216684 - 0.748655I$	$0.99165 + 8.38015I$	$-2.49309 - 10.10429I$
$b = -0.135378 - 0.914178I$		
$u = 0.760360 - 0.946681I$		
$a = 0.216684 + 0.748655I$	$0.99165 - 8.38015I$	$-2.49309 + 10.10429I$
$b = -0.135378 + 0.914178I$		
$u = 0.123423 + 0.767586I$		
$a = 1.31748 - 1.02145I$	$-3.32631 - 5.28974I$	$-7.90203 + 5.12286I$
$b = 1.50929 + 0.04931I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.123423 - 0.767586I$		
$a = 1.31748 + 1.02145I$	$-3.32631 + 5.28974I$	$-7.90203 - 5.12286I$
$b = 1.50929 - 0.04931I$		
$u = -0.063406 + 1.278620I$		
$a = -0.358068 - 0.728040I$	$-6.36689 - 2.53679I$	$-10.96403 + 3.03478I$
$b = 0.48768 - 1.65706I$		
$u = -0.063406 - 1.278620I$		
$a = -0.358068 + 0.728040I$	$-6.36689 + 2.53679I$	$-10.96403 - 3.03478I$
$b = 0.48768 + 1.65706I$		
$u = 0.52000 + 1.40243I$		
$a = 0.163383 - 1.128450I$	$-11.37900 + 5.95622I$	$-6.44408 - 3.49025I$
$b = 0.29881 - 2.51025I$		
$u = 0.52000 - 1.40243I$		
$a = 0.163383 + 1.128450I$	$-11.37900 - 5.95622I$	$-6.44408 + 3.49025I$
$b = 0.29881 + 2.51025I$		
$u = -0.205705 + 0.307610I$		
$a = 1.42758 + 1.56792I$	$-2.52117 + 1.45550I$	$-12.95189 - 5.06302I$
$b = -0.899718 + 0.379291I$		
$u = -0.205705 - 0.307610I$		
$a = 1.42758 - 1.56792I$	$-2.52117 - 1.45550I$	$-12.95189 + 5.06302I$
$b = -0.899718 - 0.379291I$		

$$\text{III. } I_3^u = \langle 343u^{10}a^3 + 5345u^{10}a^2 + \cdots + 5127a + 18129, u^{10}a^3 - 3u^{10}a^2 + \cdots + 26a + 1, u^{11} - 2u^{10} + \cdots + 4u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ -0.0262373a^3u^{10} - 0.408858a^2u^{10} + \cdots - 0.392182a - 1.38675 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.318825a^3u^{10} - 0.142507a^2u^{10} + \cdots - 0.164385a + 1.37895 \\ 1.32211a^3u^{10} + 0.701752a^2u^{10} + \cdots - 0.826589a + 0.354548 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.360514a^3u^{10} - 0.000152987a^2u^{10} + \cdots - 0.115582a + 0.209210 \\ 1.27721a^3u^{10} + 1.06035a^2u^{10} + \cdots + 1.09699a - 0.0332747 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.156276a^3u^{10} + 0.274918a^2u^{10} + \cdots + 0.700375a + 0.0499503 \\ 0.639180a^3u^{10} + 0.619292a^2u^{10} + \cdots - 0.125143a - 1.88136 \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ -0.0262373a^3u^{10} - 0.408858a^2u^{10} + \cdots - 0.392182a - 1.38675 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.156276a^3u^{10} + 0.274918a^2u^{10} + \cdots + 0.700375a + 0.0499503 \\ 0.890691a^3u^{10} + 1.68729a^2u^{10} + \cdots - 0.249063a - 2.37512 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.538591a^3u^{10} - 0.338866a^2u^{10} + \cdots - 0.0135394a + 1.39976 \\ 1.48596a^3u^{10} + 1.15299a^2u^{10} + \cdots - 0.418267a - 0.209822 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = \frac{18852}{13073}u^{10}a^3 - \frac{8}{13073}u^{10}a^2 + \cdots - \frac{6044}{13073}a + \frac{50159}{13073}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{11} + 8u^{10} + \cdots - 18u^2 - 1)^4$
$c_2, c_6$	$(u^{11} + 2u^{10} + \cdots + 4u + 1)^4$
$c_3, c_9$	$u^{44} - 25u^{42} + \cdots + 193u + 1$
$c_4$	$u^{44} - 6u^{43} + \cdots - 351984u + 130591$
$c_5, c_8$	$u^{44} - 2u^{43} + \cdots + 95u + 25$
$c_7, c_{10}$	$u^{44} + 5u^{43} + \cdots + 281670u + 28225$
$c_{11}$	$(u^{11} + 5u^{10} + \cdots - 10u - 4)^4$
$c_{12}$	$(u^2 + u + 1)^{22}$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{11} - 8y^{10} + \cdots - 36y - 1)^4$
$c_2, c_6$	$(y^{11} + 8y^{10} + \cdots - 18y^2 - 1)^4$
$c_3, c_9$	$y^{44} - 50y^{43} + \cdots + 33239y + 1$
$c_4$	$y^{44} - 44y^{43} + \cdots + 412133171800y + 17054009281$
$c_5, c_8$	$y^{44} + 10y^{43} + \cdots + 21775y + 625$
$c_7, c_{10}$	$y^{44} - 53y^{43} + \cdots - 30404080600y + 796650625$
$c_{11}$	$(y^{11} - 5y^{10} + \cdots + 108y - 16)^4$
$c_{12}$	$(y^2 + y + 1)^{22}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.617799 + 0.778228I$		
$a = 0.589454 + 0.528793I$	$-0.43565 - 4.46673I$	$-8.45208 + 10.60791I$
$b = 0.540084 - 0.380969I$		
$u = -0.617799 + 0.778228I$		
$a = -0.056046 - 0.700162I$	$-0.435652 - 0.406964I$	$-8.45208 + 3.67970I$
$b = -0.643608 - 0.688149I$		
$u = -0.617799 + 0.778228I$		
$a = -0.439822 - 1.326850I$	$-0.435652 - 0.406964I$	$-8.45208 + 3.67970I$
$b = 0.597857 - 1.109030I$		
$u = -0.617799 + 0.778228I$		
$a = 1.41393 + 0.05528I$	$-0.43565 - 4.46673I$	$-8.45208 + 10.60791I$
$b = 1.03920 + 1.23994I$		
$u = -0.617799 - 0.778228I$		
$a = 0.589454 - 0.528793I$	$-0.43565 + 4.46673I$	$-8.45208 - 10.60791I$
$b = 0.540084 + 0.380969I$		
$u = -0.617799 - 0.778228I$		
$a = -0.056046 + 0.700162I$	$-0.435652 + 0.406964I$	$-8.45208 - 3.67970I$
$b = -0.643608 + 0.688149I$		
$u = -0.617799 - 0.778228I$		
$a = -0.439822 + 1.326850I$	$-0.435652 + 0.406964I$	$-8.45208 - 3.67970I$
$b = 0.597857 + 1.109030I$		
$u = -0.617799 - 0.778228I$		
$a = 1.41393 - 0.05528I$	$-0.43565 + 4.46673I$	$-8.45208 - 10.60791I$
$b = 1.03920 - 1.23994I$		
$u = 1.06351$		
$a = -1.49958 + 0.14846I$	$-7.98334 + 2.02988I$	$-7.16744 - 3.46410I$
$b = -0.022831 + 0.204938I$		
$u = 1.06351$		
$a = -1.49958 - 0.14846I$	$-7.98334 - 2.02988I$	$-7.16744 + 3.46410I$
$b = -0.022831 - 0.204938I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.06351$		
$a = 1.61628 + 0.35059I$	$-7.98334 - 2.02988I$	$-7.16744 + 3.46410I$
$b = -0.233271 - 0.238643I$		
$u = 1.06351$		
$a = 1.61628 - 0.35059I$	$-7.98334 + 2.02988I$	$-7.16744 - 3.46410I$
$b = -0.233271 + 0.238643I$		
$u = 0.221199 + 1.131890I$		
$a = -0.282121 - 1.073420I$	$-4.38744 + 7.66724I$	$-6.48609 - 11.64165I$
$b = 0.52445 - 3.15670I$		
$u = 0.221199 + 1.131890I$		
$a = -0.722841 - 0.452983I$	$-4.38744 + 3.60747I$	$-6.48609 - 4.71344I$
$b = 0.335223 - 0.182775I$		
$u = 0.221199 + 1.131890I$		
$a = -0.253046 + 1.234040I$	$-4.38744 + 3.60747I$	$-6.48609 - 4.71344I$
$b = -0.04671 + 2.56573I$		
$u = 0.221199 + 1.131890I$		
$a = 1.44648 + 1.52804I$	$-4.38744 + 7.66724I$	$-6.48609 - 11.64165I$
$b = 1.39498 + 1.71537I$		
$u = 0.221199 - 1.131890I$		
$a = -0.282121 + 1.073420I$	$-4.38744 - 7.66724I$	$-6.48609 + 11.64165I$
$b = 0.52445 + 3.15670I$		
$u = 0.221199 - 1.131890I$		
$a = -0.722841 + 0.452983I$	$-4.38744 - 3.60747I$	$-6.48609 + 4.71344I$
$b = 0.335223 + 0.182775I$		
$u = 0.221199 - 1.131890I$		
$a = -0.253046 - 1.234040I$	$-4.38744 - 3.60747I$	$-6.48609 + 4.71344I$
$b = -0.04671 - 2.56573I$		
$u = 0.221199 - 1.131890I$		
$a = 1.44648 - 1.52804I$	$-4.38744 - 7.66724I$	$-6.48609 + 11.64165I$
$b = 1.39498 - 1.71537I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.029838 + 1.264780I$		
$a = -0.177967 + 0.946487I$	$-6.65088 - 0.57787I$	$-11.49826 - 1.42165I$
$b = -0.42614 + 2.84232I$		
$u = -0.029838 + 1.264780I$		
$a = -1.062190 - 0.030421I$	$-6.65088 - 0.57787I$	$-11.49826 - 1.42165I$
$b = -0.504118 + 0.124524I$		
$u = -0.029838 + 1.264780I$		
$a = -0.11469 - 1.68739I$	$-6.65088 - 4.63764I$	$-11.49826 + 5.50656I$
$b = 0.13874 - 2.62771I$		
$u = -0.029838 + 1.264780I$		
$a = -0.058572 + 0.155353I$	$-6.65088 - 4.63764I$	$-11.49826 + 5.50656I$
$b = -2.24297 + 0.33866I$		
$u = -0.029838 - 1.264780I$		
$a = -0.177967 - 0.946487I$	$-6.65088 + 0.57787I$	$-11.49826 + 1.42165I$
$b = -0.42614 - 2.84232I$		
$u = -0.029838 - 1.264780I$		
$a = -1.062190 + 0.030421I$	$-6.65088 + 0.57787I$	$-11.49826 + 1.42165I$
$b = -0.504118 - 0.124524I$		
$u = -0.029838 - 1.264780I$		
$a = -0.11469 + 1.68739I$	$-6.65088 + 4.63764I$	$-11.49826 - 5.50656I$
$b = 0.13874 + 2.62771I$		
$u = -0.029838 - 1.264780I$		
$a = -0.058572 - 0.155353I$	$-6.65088 + 4.63764I$	$-11.49826 - 5.50656I$
$b = -2.24297 - 0.33866I$		
$u = 0.52365 + 1.35993I$		
$a = -0.440908 + 1.028850I$	$-12.23950 + 3.61593I$	$-9.10897 - 0.19933I$
$b = -1.08236 + 2.43446I$		
$u = 0.52365 + 1.35993I$		
$a = 0.052366 - 1.202380I$	$-12.2395 + 7.6757I$	$-9.10897 - 7.12753I$
$b = 0.35777 - 2.45711I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.52365 + 1.35993I$		
$a = 0.337952 - 1.232570I$	$-12.23950 + 3.61593I$	$-9.10897 - 0.19933I$
$b = 0.40689 - 2.36204I$		
$u = 0.52365 + 1.35993I$		
$a = -0.177318 + 1.393410I$	$-12.2395 + 7.6757I$	$-9.10897 - 7.12753I$
$b = 0.04268 + 3.00587I$		
$u = 0.52365 - 1.35993I$		
$a = -0.440908 - 1.028850I$	$-12.23950 - 3.61593I$	$-9.10897 + 0.19933I$
$b = -1.08236 - 2.43446I$		
$u = 0.52365 - 1.35993I$		
$a = 0.052366 + 1.202380I$	$-12.2395 - 7.6757I$	$-9.10897 + 7.12753I$
$b = 0.35777 + 2.45711I$		
$u = 0.52365 - 1.35993I$		
$a = 0.337952 + 1.232570I$	$-12.23950 - 3.61593I$	$-9.10897 + 0.19933I$
$b = 0.40689 + 2.36204I$		
$u = 0.52365 - 1.35993I$		
$a = -0.177318 - 1.393410I$	$-12.2395 - 7.6757I$	$-9.10897 + 7.12753I$
$b = 0.04268 - 3.00587I$		
$u = 0.371033 + 0.270161I$		
$a = 0.01049750 + 0.00431977I$	$-1.90371 - 1.10694I$	$-0.37088 - 1.58915I$
$b = -1.009870 - 0.210773I$		
$u = 0.371033 + 0.270161I$		
$a = 2.04632 - 0.92835I$	$-1.90371 - 1.10694I$	$-0.37088 - 1.58915I$
$b = -0.321194 - 0.354636I$		
$u = 0.371033 + 0.270161I$		
$a = -2.71130 + 0.68471I$	$-1.90371 - 5.16670I$	$-0.37088 + 5.33905I$
$b = -0.187627 - 0.749850I$		
$u = 0.371033 + 0.270161I$		
$a = 2.48312 + 1.55855I$	$-1.90371 - 5.16670I$	$-0.37088 + 5.33905I$
$b = 1.342820 - 0.120180I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.371033 - 0.270161I$		
$a = 0.01049750 - 0.00431977I$	$-1.90371 + 1.10694I$	$-0.37088 + 1.58915I$
$b = -1.009870 + 0.210773I$		
$u = 0.371033 - 0.270161I$		
$a = 2.04632 + 0.92835I$	$-1.90371 + 1.10694I$	$-0.37088 + 1.58915I$
$b = -0.321194 + 0.354636I$		
$u = 0.371033 - 0.270161I$		
$a = -2.71130 - 0.68471I$	$-1.90371 + 5.16670I$	$-0.37088 - 5.33905I$
$b = -0.187627 + 0.749850I$		
$u = 0.371033 - 0.270161I$		
$a = 2.48312 - 1.55855I$	$-1.90371 + 5.16670I$	$-0.37088 - 5.33905I$
$b = 1.342820 + 0.120180I$		

$$\text{IV. } I_4^u = \langle b - a + u, a^2 + a - u - 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ a - u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 2 \\ -au - a + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} au + a + u \\ au + a + u + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ -u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a + 1 \\ a - u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ au + 2a - u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} a + 1 \\ a - u + 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -au - u + 1 \\ -2au - a - u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $3u + 3$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$ $c_{10}, c_{12}$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_3, c_5, c_8$ $c_9$	$u^4 - u^3 + 2u + 1$
$c_4$	$u^4 - 3u + 3$
$c_{11}$	$u^4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{10}, c_{12}$	$(y^2 + y + 1)^2$
$c_3, c_5, c_8$ $c_9$	$y^4 - y^3 + 6y^2 - 4y + 1$
$c_4$	$y^4 + 6y^2 - 9y + 9$
$c_{11}$	$y^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0.473561 + 0.444772I$	$- 4.05977I$	$1.50000 + 2.59808I$
$b = 0.973561 - 0.421254I$		
$u = -0.500000 + 0.866025I$		
$a = -1.47356 - 0.44477I$	$- 4.05977I$	$1.50000 + 2.59808I$
$b = -0.97356 - 1.31080I$		
$u = -0.500000 - 0.866025I$		
$a = 0.473561 - 0.444772I$	$4.05977I$	$1.50000 - 2.59808I$
$b = 0.973561 + 0.421254I$		
$u = -0.500000 - 0.866025I$		
$a = -1.47356 + 0.44477I$	$4.05977I$	$1.50000 - 2.59808I$
$b = -0.97356 + 1.31080I$		

$$\mathbf{V. } I_5^u = \langle b - a + 1, a^2 - au - a + 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} a \\ a - 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u + 1 \\ au + 2u + 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -au + u \\ -au + 2u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ -u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a - u - 1 \\ a - u - 2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} a \\ au + 2a - 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} a - u - 1 \\ a - u - 2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -a + 2u + 1 \\ au - a + 3u + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u - 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$ $c_{10}, c_{12}$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_3, c_5, c_8$ $c_9$	$u^4 + 2u^3 - u + 1$
$c_4$	$u^4 + 3u^3 + 3u^2 + 3u + 3$
$c_{11}$	$u^4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{10}, c_{12}$	$(y^2 + y + 1)^2$
$c_3, c_5, c_8$ $c_9$	$y^4 - 4y^3 + 6y^2 - y + 1$
$c_4$	$y^4 - 3y^3 - 3y^2 + 9y + 9$
$c_{11}$	$y^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0.148403 - 0.632502I$	0	$1.50000 - 4.33013I$
$b = -0.851597 - 0.632502I$		
$u = -0.500000 + 0.866025I$		
$a = 0.35160 + 1.49853I$	0	$1.50000 - 4.33013I$
$b = -0.64840 + 1.49853I$		
$u = -0.500000 - 0.866025I$		
$a = 0.148403 + 0.632502I$	0	$1.50000 + 4.33013I$
$b = -0.851597 + 0.632502I$		
$u = -0.500000 - 0.866025I$		
$a = 0.35160 - 1.49853I$	0	$1.50000 + 4.33013I$
$b = -0.64840 - 1.49853I$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^4)(u^{11} + 8u^{10} + \dots - 18u^2 - 1)^4$ $\cdot (u^{17} - 10u^{16} + \dots - 12u + 1)(u^{28} + 17u^{27} + \dots + 1360u + 256)$
$c_2$	$((u^2 + u + 1)^4)(u^{11} + 2u^{10} + \dots + 4u + 1)^4(u^{17} - 4u^{16} + \dots - 6u^2 - 1)$ $\cdot (u^{28} - 9u^{27} + \dots - 124u + 16)$
$c_3, c_9$	$(u^4 - u^3 + 2u + 1)(u^4 + 2u^3 - u + 1)(u^{17} - u^{16} + \dots + 3u + 1)$ $\cdot (u^{28} + u^{27} + \dots + u + 1)(u^{44} - 25u^{42} + \dots + 193u + 1)$
$c_4$	$(u^4 - 3u + 3)(u^4 + 3u^3 + \dots + 3u + 3)(u^{17} + 2u^{16} + \dots + 9u + 3)$ $\cdot (u^{28} - 2u^{27} + \dots - 45u + 25)(u^{44} - 6u^{43} + \dots - 351984u + 130591)$
$c_5, c_8$	$(u^4 - u^3 + 2u + 1)(u^4 + 2u^3 - u + 1)(u^{17} + 3u^{15} + \dots - u + 1)$ $\cdot (u^{28} + u^{26} + \dots + 3u + 1)(u^{44} - 2u^{43} + \dots + 95u + 25)$
$c_6$	$((u^2 - u + 1)^4)(u^{11} + 2u^{10} + \dots + 4u + 1)^4(u^{17} + 4u^{16} + \dots + 6u^2 + 1)$ $\cdot (u^{28} - 9u^{27} + \dots - 124u + 16)$
$c_7, c_{10}$	$((u^2 - u + 1)^4)(u^{17} - 7u^{16} + \dots + 3u - 1)(u^{28} + u^{27} + \dots + 21u + 1)$ $\cdot (u^{44} + 5u^{43} + \dots + 281670u + 28225)$
$c_{11}$	$u^8(u^{11} + 5u^{10} + \dots - 10u - 4)^4(u^{17} + 11u^{16} + \dots - 3066u - 441)$ $\cdot (u^{28} - 28u^{27} + \dots - 50u + 4)$
$c_{12}$	$((u^2 - u + 1)^4)(u^2 + u + 1)^{22}(u^{17} + 5u^{16} + \dots - 2u - 1)$ $\cdot (u^{28} - 26u^{27} + \dots - 5120u + 512)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^4)(y^{11} - 8y^{10} + \dots - 36y - 1)^4$ $\cdot (y^{17} - 2y^{16} + \dots - 72y - 1)(y^{28} - 11y^{27} + \dots + 264448y + 65536)$
$c_2, c_6$	$((y^2 + y + 1)^4)(y^{11} + 8y^{10} + \dots - 18y^2 - 1)^4$ $\cdot (y^{17} + 10y^{16} + \dots - 12y - 1)(y^{28} + 17y^{27} + \dots + 1360y + 256)$
$c_3, c_9$	$(y^4 - 4y^3 + 6y^2 - y + 1)(y^4 - y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{17} - 15y^{16} + \dots - 5y - 1)(y^{28} - 31y^{27} + \dots - 7y + 1)$ $\cdot (y^{44} - 50y^{43} + \dots + 33239y + 1)$
$c_4$	$(y^4 + 6y^2 - 9y + 9)(y^4 - 3y^3 + \dots + 9y + 9)(y^{17} - 8y^{16} + \dots - 69y - 9)$ $\cdot (y^{28} - 16y^{27} + \dots - 10575y + 625)$ $\cdot (y^{44} - 44y^{43} + \dots + 412133171800y + 17054009281)$
$c_5, c_8$	$(y^4 - 4y^3 + 6y^2 - y + 1)(y^4 - y^3 + 6y^2 - 4y + 1)(y^{17} + 6y^{16} + \dots - y - 1)$ $\cdot (y^{28} + 2y^{27} + \dots + y + 1)(y^{44} + 10y^{43} + \dots + 21775y + 625)$
$c_7, c_{10}$	$((y^2 + y + 1)^4)(y^{17} - 15y^{16} + \dots - 7y - 1)$ $\cdot (y^{28} - 39y^{27} + \dots - 197y + 1)$ $\cdot (y^{44} - 53y^{43} + \dots - 30404080600y + 796650625)$
$c_{11}$	$y^8(y^{11} - 5y^{10} + \dots + 108y - 16)^4$ $\cdot (y^{17} - 17y^{16} + \dots + 1120140y - 194481)$ $\cdot (y^{28} - 22y^{27} + \dots - 188y + 16)$
$c_{12}$	$((y^2 + y + 1)^{26})(y^{17} - 7y^{16} + \dots + 10y - 1)$ $\cdot (y^{28} - 6y^{27} + \dots - 1310720y + 262144)$