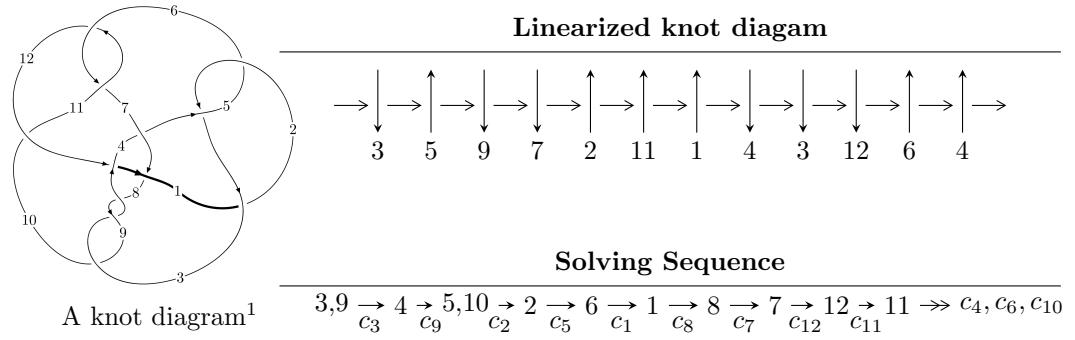


$12n_{0525}$  ( $K12n_{0525}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 730697u^{21} + 8724191u^{20} + \dots + 1495432b + 38274232, \\
 &\quad - 1973739u^{21} - 26703501u^{20} + \dots + 5981728a - 159009976, u^{22} + 11u^{21} + \dots + 232u + 32 \rangle \\
 I_2^u &= \langle -10u^{29} + 31u^{28} + \dots + 8b - 6, -54u^{29}a + 37u^{29} + \dots + 104a - 100, u^{30} - 5u^{29} + \dots - 2u + 1 \rangle \\
 I_3^u &= \langle u^{11} + 2u^{10} + 7u^9 + 10u^8 + 18u^7 + 15u^6 + 19u^5 + 5u^4 + 7u^3 - 2u^2 + b + 2u, \\
 &\quad - u^{11} - u^{10} - 5u^9 - 3u^8 - 8u^7 + 3u^6 - 4u^5 + 14u^4 - 2u^3 + 8u^2 + a - 4u + 1, \\
 &\quad u^{12} + 2u^{11} + 7u^{10} + 10u^9 + 19u^8 + 17u^7 + 24u^6 + 11u^5 + 15u^4 + 2u^3 + 6u^2 + 1 \rangle \\
 I_4^u &= \langle -u^2a + u^3 - u^2 + b + u, u^5a - 2u^4a - 4u^5 + 5u^3a + 5u^4 - 6u^2a - 11u^3 + a^2 + 5au + 9u^2 - 2a - 10u, \\
 &\quad u^6 - u^5 + 3u^4 - 2u^3 + 3u^2 + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 106 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \\ \langle 7.31 \times 10^5 u^{21} + 8.72 \times 10^6 u^{20} + \dots + 1.50 \times 10^6 b + 3.83 \times 10^7, -1.97 \times 10^6 u^{21} - 2.67 \times 10^7 u^{20} + \dots + 5.98 \times 10^6 a - 1.59 \times 10^8, u^{22} + 11u^{21} + \dots + 232u + 32 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.329961u^{21} + 4.46418u^{20} + \dots + 167.160u + 26.5826 \\ -0.488619u^{21} - 5.83389u^{20} + \dots - 164.041u - 25.5941 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.678659u^{21} - 6.54536u^{20} + \dots - 66.3494u - 8.74650 \\ 0.549186u^{21} + 5.23031u^{20} + \dots + 73.2841u + 11.2249 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.309352u^{21} - 2.39786u^{20} + \dots + 59.0207u + 10.7541 \\ -0.730680u^{21} - 8.31181u^{20} + \dots - 218.761u - 33.2810 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.129473u^{21} - 1.31505u^{20} + \dots + 6.93466u + 2.47838 \\ 0.549186u^{21} + 5.23031u^{20} + \dots + 73.2841u + 11.2249 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.770630u^{21} + 8.00468u^{20} + \dots + 111.293u + 15.5266 \\ 0.580458u^{21} + 6.16373u^{20} + \dots + 148.964u + 22.7178 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.459930u^{21} - 4.72878u^{20} + \dots - 87.5298u - 12.2394 \\ 0.109153u^{21} + 1.41941u^{20} + \dots + 32.5161u + 4.14313 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.709930u^{21} - 7.22878u^{20} + \dots - 117.030u - 16.7394 \\ 0.359153u^{21} + 3.66941u^{20} + \dots + 37.0161u + 4.14313 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-\frac{297700}{186929}u^{21} - \frac{2758587}{186929}u^{20} + \dots - \frac{6073132}{186929}u - \frac{1067206}{186929}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^{22} + 13u^{21} + \cdots + 6u + 1$
$c_2, c_5, c_6$ $c_{11}$	$u^{22} + u^{21} + \cdots - 2u + 1$
$c_3, c_8, c_9$	$u^{22} + 11u^{21} + \cdots + 232u + 32$
$c_4$	$u^{22} - 15u^{21} + \cdots - 480u + 64$
$c_7, c_{12}$	$u^{22} + 13u^{20} + \cdots - u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{22} + y^{21} + \cdots + 34y + 1$
$c_2, c_5, c_6$ $c_{11}$	$y^{22} + 13y^{21} + \cdots + 6y + 1$
$c_3, c_8, c_9$	$y^{22} + 11y^{21} + \cdots + 3264y + 1024$
$c_4$	$y^{22} + 7y^{21} + \cdots + 39936y + 4096$
$c_7, c_{12}$	$y^{22} + 26y^{21} + \cdots + 17y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.767910 + 0.699836I$		
$a = 0.888145 - 0.307129I$	$-0.286662 + 0.737446I$	$3.26178 - 2.36364I$
$b = -0.688888 - 0.277789I$		
$u = -0.767910 - 0.699836I$		
$a = 0.888145 + 0.307129I$	$-0.286662 - 0.737446I$	$3.26178 + 2.36364I$
$b = -0.688888 + 0.277789I$		
$u = -0.350255 + 1.075900I$		
$a = 0.81263 - 1.53152I$	$-2.88260 + 1.01233I$	$-4.09792 + 3.96823I$
$b = -0.240178 + 0.810554I$		
$u = -0.350255 - 1.075900I$		
$a = 0.81263 + 1.53152I$	$-2.88260 - 1.01233I$	$-4.09792 - 3.96823I$
$b = -0.240178 - 0.810554I$		
$u = -1.033280 + 0.527627I$		
$a = -0.721729 - 0.194727I$	$-8.25550 - 1.54810I$	$-5.19018 + 2.03970I$
$b = 0.417851 - 1.163520I$		
$u = -1.033280 - 0.527627I$		
$a = -0.721729 + 0.194727I$	$-8.25550 + 1.54810I$	$-5.19018 - 2.03970I$
$b = 0.417851 + 1.163520I$		
$u = 0.755708 + 0.364616I$		
$a = 0.685218 + 0.575896I$	$-4.85462 - 1.77876I$	$-4.79807 + 3.91708I$
$b = -0.063685 + 1.154200I$		
$u = 0.755708 - 0.364616I$		
$a = 0.685218 - 0.575896I$	$-4.85462 + 1.77876I$	$-4.79807 - 3.91708I$
$b = -0.063685 - 1.154200I$		
$u = -0.774895 + 1.020220I$		
$a = -0.766277 + 0.769605I$	$0.61034 + 5.16314I$	$3.96974 - 2.90756I$
$b = 0.885411 - 0.402143I$		
$u = -0.774895 - 1.020220I$		
$a = -0.766277 - 0.769605I$	$0.61034 - 5.16314I$	$3.96974 + 2.90756I$
$b = 0.885411 + 0.402143I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.221500 + 0.677927I$		
$a = 0.567702 - 0.117730I$	$-6.12965 - 9.37239I$	$-3.35170 + 5.78555I$
$b = -0.558982 + 1.253320I$		
$u = -1.221500 - 0.677927I$		
$a = 0.567702 + 0.117730I$	$-6.12965 + 9.37239I$	$-3.35170 - 5.78555I$
$b = -0.558982 - 1.253320I$		
$u = -0.127935 + 1.398640I$		
$a = -1.71401 - 0.32772I$	$6.04024 + 2.92164I$	$4.28614 + 0.75325I$
$b = 0.565971 + 0.644936I$		
$u = -0.127935 - 1.398640I$		
$a = -1.71401 + 0.32772I$	$6.04024 - 2.92164I$	$4.28614 - 0.75325I$
$b = 0.565971 - 0.644936I$		
$u = -0.304981 + 0.451421I$		
$a = 0.960223 - 0.185150I$	$0.090652 + 0.977959I$	$1.72728 - 6.82657I$
$b = -0.310004 - 0.375864I$		
$u = -0.304981 - 0.451421I$		
$a = 0.960223 + 0.185150I$	$0.090652 - 0.977959I$	$1.72728 + 6.82657I$
$b = -0.310004 + 0.375864I$		
$u = -0.76091 + 1.25738I$		
$a = 1.92912 + 0.01305I$	$-5.97217 + 8.17735I$	$-2.07600 - 6.92513I$
$b = -0.557890 - 1.095380I$		
$u = -0.76091 - 1.25738I$		
$a = 1.92912 - 0.01305I$	$-5.97217 - 8.17735I$	$-2.07600 + 6.92513I$
$b = -0.557890 + 1.095380I$		
$u = -0.89339 + 1.20903I$		
$a = -1.79322 + 0.05043I$	$-4.4232 + 16.8853I$	$-1.04656 - 9.40882I$
$b = 0.663517 + 1.230310I$		
$u = -0.89339 - 1.20903I$		
$a = -1.79322 - 0.05043I$	$-4.4232 - 16.8853I$	$-1.04656 + 9.40882I$
$b = 0.663517 - 1.230310I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.02066 + 1.63363I$		
$a = -0.972799 + 0.791268I$	$3.03407 - 4.86939I$	$-4.68451 + 3.83035I$
$b = 0.386878 - 1.096150I$		
$u = -0.02066 - 1.63363I$		
$a = -0.972799 - 0.791268I$	$3.03407 + 4.86939I$	$-4.68451 - 3.83035I$
$b = 0.386878 + 1.096150I$		

$$\text{II. } I_2^u = \langle -10u^{29} + 31u^{28} + \cdots + 8b - 6, -54u^{29}a + 37u^{29} + \cdots + 104a - 100, u^{30} - 5u^{29} + \cdots - 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} a \\ \frac{5}{4}u^{29} - \frac{31}{8}u^{28} + \cdots + \frac{25}{8}u + \frac{3}{4} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{3}{2}u^{29}a + \frac{5}{4}u^{29} + \cdots - \frac{7}{8}a + \frac{3}{8} \\ \frac{7}{8}u^{29}a - \frac{1}{8}u^{29} + \cdots - \frac{3}{4}a - \frac{29}{8} \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.500000au^{29} + 2.12500u^{29} + \cdots - 1.62500a - 2.75000 \\ -\frac{3}{2}u^{29}a - \frac{11}{2}u^{29} + \cdots + 2a + \frac{69}{8} \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{5}{8}u^{29}a + \frac{9}{8}u^{29} + \cdots - \frac{13}{8}a - \frac{13}{8} \\ \frac{7}{8}u^{29}a - \frac{1}{8}u^{29} + \cdots - \frac{3}{4}a - \frac{29}{8} \end{pmatrix} \\ a_8 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -4u^{29}a + 4u^{29} + \cdots + \frac{19}{4}a - \frac{19}{4} \\ u^{29}a + \frac{9}{4}u^{29} + \cdots + \frac{3}{4}a - \frac{9}{8} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -2u^{29}a - \frac{5}{8}u^{29} + \cdots + \frac{3}{8}a + \frac{15}{8} \\ \frac{5}{4}u^{29}a + \frac{13}{4}u^{29} + \cdots - \frac{5}{8}a - \frac{49}{8} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -3u^{29}a + \frac{15}{4}u^{29} + \cdots + \frac{11}{2}a - \frac{5}{2} \\ \frac{3}{4}u^{29}a - \frac{13}{4}u^{29} + \cdots - \frac{5}{4}a - \frac{1}{8} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $19u^{29} - \frac{169}{2}u^{28} + \cdots + 26u - \frac{5}{2}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^{60} + 30u^{59} + \cdots + 31603u + 2209$
$c_2, c_5, c_6$ $c_{11}$	$u^{60} - 2u^{59} + \cdots + 81u + 47$
$c_3, c_8, c_9$	$(u^{30} - 5u^{29} + \cdots - 2u + 1)^2$
$c_4$	$(u^{30} + 6u^{29} + \cdots + 9u + 1)^2$
$c_7, c_{12}$	$u^{60} + 5u^{59} + \cdots - 18u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{60} + 6y^{59} + \cdots - 90081877y + 4879681$
$c_2, c_5, c_6$ $c_{11}$	$y^{60} + 30y^{59} + \cdots + 31603y + 2209$
$c_3, c_8, c_9$	$(y^{30} + 9y^{29} + \cdots + 14y + 1)^2$
$c_4$	$(y^{30} + 10y^{29} + \cdots - 9y + 1)^2$
$c_7, c_{12}$	$y^{60} + 39y^{59} + \cdots - 40y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.408738 + 0.809128I$		
$a = 1.47348 + 0.03228I$	$1.95297 + 0.83755I$	$3.80919 - 0.73546I$
$b = -0.881093 - 0.652728I$		
$u = -0.408738 + 0.809128I$		
$a = 0.65867 + 1.49537I$	$1.95297 + 0.83755I$	$3.80919 - 0.73546I$
$b = 0.483976 - 0.827208I$		
$u = -0.408738 - 0.809128I$		
$a = 1.47348 - 0.03228I$	$1.95297 - 0.83755I$	$3.80919 + 0.73546I$
$b = -0.881093 + 0.652728I$		
$u = -0.408738 - 0.809128I$		
$a = 0.65867 - 1.49537I$	$1.95297 - 0.83755I$	$3.80919 + 0.73546I$
$b = 0.483976 + 0.827208I$		
$u = 0.204797 + 0.865298I$		
$a = 0.913167 + 0.827489I$	$0.86908 + 5.05707I$	$0.52377 - 4.80046I$
$b = -0.717809 - 1.010560I$		
$u = 0.204797 + 0.865298I$		
$a = 0.79610 - 2.03259I$	$0.86908 + 5.05707I$	$0.52377 - 4.80046I$
$b = 0.378609 + 0.969447I$		
$u = 0.204797 - 0.865298I$		
$a = 0.913167 - 0.827489I$	$0.86908 - 5.05707I$	$0.52377 + 4.80046I$
$b = -0.717809 + 1.010560I$		
$u = 0.204797 - 0.865298I$		
$a = 0.79610 + 2.03259I$	$0.86908 - 5.05707I$	$0.52377 + 4.80046I$
$b = 0.378609 - 0.969447I$		
$u = 0.846145 + 0.766192I$		
$a = -0.742838 + 0.117308I$	$-5.03543 - 2.48830I$	$-2.08110 + 3.16963I$
$b = 0.633812 - 0.058357I$		
$u = 0.846145 + 0.766192I$		
$a = 0.161640 + 0.601130I$	$-5.03543 - 2.48830I$	$-2.08110 + 3.16963I$
$b = 0.123075 + 1.176780I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.846145 - 0.766192I$		
$a = -0.742838 - 0.117308I$	$-5.03543 + 2.48830I$	$-2.08110 - 3.16963I$
$b = 0.633812 + 0.058357I$		
$u = 0.846145 - 0.766192I$		
$a = 0.161640 - 0.601130I$	$-5.03543 + 2.48830I$	$-2.08110 - 3.16963I$
$b = 0.123075 - 1.176780I$		
$u = 0.476164 + 0.624124I$		
$a = 1.065700 + 0.769850I$	$-0.16540 - 7.91184I$	$-1.25799 + 13.37489I$
$b = -0.560439 + 1.270490I$		
$u = 0.476164 + 0.624124I$		
$a = -3.03202 - 0.17816I$	$-0.16540 - 7.91184I$	$-1.25799 + 13.37489I$
$b = 0.670131 - 1.010730I$		
$u = 0.476164 - 0.624124I$		
$a = 1.065700 - 0.769850I$	$-0.16540 + 7.91184I$	$-1.25799 - 13.37489I$
$b = -0.560439 - 1.270490I$		
$u = 0.476164 - 0.624124I$		
$a = -3.03202 + 0.17816I$	$-0.16540 + 7.91184I$	$-1.25799 - 13.37489I$
$b = 0.670131 + 1.010730I$		
$u = 0.843824 + 0.910765I$		
$a = 0.922245 + 0.095668I$	$-5.24308 - 3.14036I$	$3.38309 + 6.95597I$
$b = -0.146948 + 1.374310I$		
$u = 0.843824 + 0.910765I$		
$a = 0.418535 + 0.014710I$	$-5.24308 - 3.14036I$	$3.38309 + 6.95597I$
$b = 0.036650 + 0.609588I$		
$u = 0.843824 - 0.910765I$		
$a = 0.922245 - 0.095668I$	$-5.24308 + 3.14036I$	$3.38309 - 6.95597I$
$b = -0.146948 - 1.374310I$		
$u = 0.843824 - 0.910765I$		
$a = 0.418535 - 0.014710I$	$-5.24308 + 3.14036I$	$3.38309 - 6.95597I$
$b = 0.036650 - 0.609588I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.535931 + 0.532997I$		
$a = 1.74162 - 0.15387I$	$1.99448 - 4.75213I$	$1.25920 + 8.38226I$
$b = -0.945912 + 0.839676I$		
$u = 0.535931 + 0.532997I$		
$a = -1.15336 - 2.63260I$	$1.99448 - 4.75213I$	$1.25920 + 8.38226I$
$b = 0.461109 - 0.821998I$		
$u = 0.535931 - 0.532997I$		
$a = 1.74162 + 0.15387I$	$1.99448 + 4.75213I$	$1.25920 - 8.38226I$
$b = -0.945912 - 0.839676I$		
$u = 0.535931 - 0.532997I$		
$a = -1.15336 + 2.63260I$	$1.99448 + 4.75213I$	$1.25920 - 8.38226I$
$b = 0.461109 + 0.821998I$		
$u = -0.009746 + 0.748854I$		
$a = 0.263930 - 0.170722I$	$3.73099 + 2.66963I$	$10.94282 - 2.46654I$
$b = -0.891285 - 0.086936I$		
$u = -0.009746 + 0.748854I$		
$a = -2.60774 - 1.78017I$	$3.73099 + 2.66963I$	$10.94282 - 2.46654I$
$b = 0.695330 + 0.857378I$		
$u = -0.009746 - 0.748854I$		
$a = 0.263930 + 0.170722I$	$3.73099 - 2.66963I$	$10.94282 + 2.46654I$
$b = -0.891285 + 0.086936I$		
$u = -0.009746 - 0.748854I$		
$a = -2.60774 + 1.78017I$	$3.73099 - 2.66963I$	$10.94282 + 2.46654I$
$b = 0.695330 - 0.857378I$		
$u = 1.008520 + 0.761169I$		
$a = 1.152310 + 0.354766I$	$-2.70377 + 3.89986I$	$-0.32016 - 2.93300I$
$b = -0.976428 + 0.128566I$		
$u = 1.008520 + 0.761169I$		
$a = 0.479203 - 0.132479I$	$-2.70377 + 3.89986I$	$-0.32016 - 2.93300I$
$b = -0.523001 - 1.118150I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.008520 - 0.761169I$		
$a = 1.152310 - 0.354766I$	$-2.70377 - 3.89986I$	$-0.32016 + 2.93300I$
$b = -0.976428 - 0.128566I$		
$u = 1.008520 - 0.761169I$		
$a = 0.479203 + 0.132479I$	$-2.70377 - 3.89986I$	$-0.32016 + 2.93300I$
$b = -0.523001 + 1.118150I$		
$u = 0.716463 + 1.086870I$		
$a = 0.985703 + 0.963170I$	$-4.00624 - 3.41764I$	$-0.54348 + 2.60438I$
$b = -0.637549 - 0.440747I$		
$u = 0.716463 + 1.086870I$		
$a = 1.73164 + 0.46125I$	$-4.00624 - 3.41764I$	$-0.54348 + 2.60438I$
$b = -0.354117 + 1.056240I$		
$u = 0.716463 - 1.086870I$		
$a = 0.985703 - 0.963170I$	$-4.00624 + 3.41764I$	$-0.54348 - 2.60438I$
$b = -0.637549 + 0.440747I$		
$u = 0.716463 - 1.086870I$		
$a = 1.73164 - 0.46125I$	$-4.00624 + 3.41764I$	$-0.54348 - 2.60438I$
$b = -0.354117 - 1.056240I$		
$u = -0.464563 + 0.517217I$		
$a = 0.810151 - 0.727418I$	$0.97854 + 2.53138I$	$-0.41612 - 5.99517I$
$b = -0.576786 - 1.098220I$		
$u = -0.464563 + 0.517217I$		
$a = -0.46286 + 1.86979I$	$0.97854 + 2.53138I$	$-0.41612 - 5.99517I$
$b = 0.737137 - 0.620730I$		
$u = -0.464563 - 0.517217I$		
$a = 0.810151 + 0.727418I$	$0.97854 - 2.53138I$	$-0.41612 + 5.99517I$
$b = -0.576786 + 1.098220I$		
$u = -0.464563 - 0.517217I$		
$a = -0.46286 - 1.86979I$	$0.97854 - 2.53138I$	$-0.41612 + 5.99517I$
$b = 0.737137 + 0.620730I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.037400 + 0.901379I$	$-7.97522 + 6.40080I$	$-3.44445 - 6.75759I$
$a = -1.183640 + 0.552154I$		
$b = 0.465103 + 1.121610I$		
$u = -1.037400 + 0.901379I$	$-7.97522 + 6.40080I$	$-3.44445 - 6.75759I$
$a = 0.145261 + 0.219918I$		
$b = 0.19421 - 1.45130I$		
$u = -1.037400 - 0.901379I$	$-7.97522 - 6.40080I$	$-3.44445 + 6.75759I$
$a = -1.183640 - 0.552154I$		
$b = 0.465103 - 1.121610I$		
$u = -1.037400 - 0.901379I$	$-7.97522 - 6.40080I$	$-3.44445 + 6.75759I$
$a = 0.145261 - 0.219918I$		
$b = 0.19421 + 1.45130I$		
$u = 0.862751 + 1.092420I$	$-1.66664 - 10.74240I$	$0. + 6.67563I$
$a = -1.077000 - 0.739852I$		
$b = 1.047710 + 0.340566I$		
$u = 0.862751 + 1.092420I$	$-1.66664 - 10.74240I$	$0. + 6.67563I$
$a = -1.77506 - 0.35041I$		
$b = 0.627078 - 1.150130I$		
$u = 0.862751 - 1.092420I$	$-1.66664 + 10.74240I$	$0. - 6.67563I$
$a = -1.077000 + 0.739852I$		
$b = 1.047710 - 0.340566I$		
$u = 0.862751 - 1.092420I$	$-1.66664 + 10.74240I$	$0. - 6.67563I$
$a = -1.77506 + 0.35041I$		
$b = 0.627078 + 1.150130I$		
$u = 0.173166 + 1.400750I$	$4.99765 + 1.93280I$	$0. - 5.83991I$
$a = -1.367910 - 0.170007I$		
$b = 0.212711 - 0.577463I$		
$u = 0.173166 + 1.400750I$	$4.99765 + 1.93280I$	$0. - 5.83991I$
$a = -1.38631 - 0.99061I$		
$b = 0.646364 + 0.999117I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.173166 - 1.400750I$		
$a = -1.367910 + 0.170007I$	$4.99765 - 1.93280I$	$0. + 5.83991I$
$b = 0.212711 + 0.577463I$		
$u = 0.173166 - 1.400750I$		
$a = -1.38631 + 0.99061I$	$4.99765 - 1.93280I$	$0. + 5.83991I$
$b = 0.646364 - 0.999117I$		
$u = -1.00992 + 1.06850I$		
$a = 1.291960 + 0.152355I$	$-7.50048 + 1.00444I$	$0$
$b = -0.39965 - 1.37579I$		
$u = -1.00992 + 1.06850I$		
$a = 0.154134 + 0.113540I$	$-7.50048 + 1.00444I$	$0$
$b = -0.344881 + 1.084600I$		
$u = -1.00992 - 1.06850I$		
$a = 1.291960 - 0.152355I$	$-7.50048 - 1.00444I$	$0$
$b = -0.39965 + 1.37579I$		
$u = -1.00992 - 1.06850I$		
$a = 0.154134 - 0.113540I$	$-7.50048 - 1.00444I$	$0$
$b = -0.344881 - 1.084600I$		
$u = -0.237396 + 0.363229I$		
$a = 0.87244 - 1.36981I$	$1.67828 - 1.77422I$	$-0.88602 - 3.46618I$
$b = -0.849393 + 0.936354I$		
$u = -0.237396 + 0.363229I$		
$a = -0.74915 + 5.11939I$	$1.67828 - 1.77422I$	$-0.88602 - 3.46618I$
$b = 0.392284 + 0.725566I$		
$u = -0.237396 - 0.363229I$		
$a = 0.87244 + 1.36981I$	$1.67828 + 1.77422I$	$-0.88602 + 3.46618I$
$b = -0.849393 - 0.936354I$		
$u = -0.237396 - 0.363229I$		
$a = -0.74915 - 5.11939I$	$1.67828 + 1.77422I$	$-0.88602 + 3.46618I$
$b = 0.392284 - 0.725566I$		

### III.

$$I_3^u = \langle u^{11} + 2u^{10} + \dots + b + 2u, -u^{11} - u^{10} + \dots + a + 1, u^{12} + 2u^{11} + \dots + 6u^2 + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{11} + u^{10} + 5u^9 + 3u^8 + 8u^7 - 3u^6 + 4u^5 - 14u^4 + 2u^3 - 8u^2 + 4u - 1 \\ -u^{11} - 2u^{10} + \dots + 2u^2 - 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^{11} - 2u^{10} + \dots - u + 6 \\ 2u^{11} + 4u^{10} + \dots + 4u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{11} + 3u^9 - 4u^8 - 2u^7 - 22u^6 - 13u^5 - 38u^4 - 10u^3 - 24u^2 + u - 7 \\ -2u^{11} - 4u^{10} + \dots - 6u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2u^{10} + 5u^9 + \dots + 3u + 5 \\ 2u^{11} + 4u^{10} + \dots + 4u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{11} - 3u^{10} + \dots - 2u - 3 \\ u^{10} + 2u^9 + 6u^8 + 8u^7 + 13u^6 + 9u^5 + 11u^4 + 2u^3 + 3u^2 - u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{11} - u^{10} + \dots - u + 4 \\ 2u^{11} + 5u^{10} + \dots + 3u^2 + 5u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{11} - 2u^{10} + \dots - 4u - 2 \\ u^{11} + 3u^{10} + 8u^9 + 14u^8 + 21u^7 + 22u^6 + 20u^5 + 12u^4 + 4u^3 + u^2 + 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes**

$$= -7u^{11} - 13u^{10} - 41u^9 - 49u^8 - 86u^7 - 47u^6 - 71u^5 + 13u^4 - 26u^3 + 32u^2 - 13u + 14$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^{12} - 7u^{11} + \cdots - 9u + 1$
$c_2, c_6$	$u^{12} + u^{11} + \cdots + u + 1$
$c_3$	$u^{12} + 2u^{11} + \cdots + 6u^2 + 1$
$c_4$	$u^{12} - 2u^{11} + \cdots - 2u + 1$
$c_5, c_{11}$	$u^{12} - u^{11} + \cdots - u + 1$
$c_7, c_{12}$	$u^{12} + 2u^{10} - u^9 + u^8 - 2u^7 + u^6 + 4u^4 + 3u^3 - 2u^2 + 1$
$c_8, c_9$	$u^{12} - 2u^{11} + \cdots + 6u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{12} + 3y^{11} + \cdots - 11y + 1$
$c_2, c_5, c_6$ $c_{11}$	$y^{12} + 7y^{11} + \cdots + 9y + 1$
$c_3, c_8, c_9$	$y^{12} + 10y^{11} + \cdots + 12y + 1$
$c_4$	$y^{12} + 6y^{11} + \cdots - 2y + 1$
$c_7, c_{12}$	$y^{12} + 4y^{11} + \cdots - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.398201 + 0.944382I$		
$a = 0.90750 - 1.42868I$	$-2.45692 + 1.58415I$	$2.68356 - 4.01575I$
$b = -0.101632 + 0.556849I$		
$u = -0.398201 - 0.944382I$		
$a = 0.90750 + 1.42868I$	$-2.45692 - 1.58415I$	$2.68356 + 4.01575I$
$b = -0.101632 - 0.556849I$		
$u = 0.009554 + 1.336590I$		
$a = -1.96403 + 0.31123I$	$6.04841 - 3.70923I$	$4.35790 + 9.04746I$
$b = 0.618206 - 0.752212I$		
$u = 0.009554 - 1.336590I$		
$a = -1.96403 - 0.31123I$	$6.04841 + 3.70923I$	$4.35790 - 9.04746I$
$b = 0.618206 + 0.752212I$		
$u = 0.321162 + 0.526918I$		
$a = 2.45149 + 1.05480I$	$0.26042 - 7.07580I$	$3.22594 + 4.98075I$
$b = -0.642424 + 1.102360I$		
$u = 0.321162 - 0.526918I$		
$a = 2.45149 - 1.05480I$	$0.26042 + 7.07580I$	$3.22594 - 4.98075I$
$b = -0.642424 - 1.102360I$		
$u = -0.008480 + 0.565991I$		
$a = 0.23065 + 2.01576I$	$2.91227 + 3.67114I$	$6.22425 - 5.54178I$
$b = -0.746714 - 0.688145I$		
$u = -0.008480 - 0.565991I$		
$a = 0.23065 - 2.01576I$	$2.91227 - 3.67114I$	$6.22425 + 5.54178I$
$b = -0.746714 + 0.688145I$		
$u = -1.04086 + 1.00123I$		
$a = 0.678256 - 0.226364I$	$-7.51749 + 3.74982I$	$-4.74315 - 3.41984I$
$b = -0.116334 - 1.202190I$		
$u = -1.04086 - 1.00123I$		
$a = 0.678256 + 0.226364I$	$-7.51749 - 3.74982I$	$-4.74315 + 3.41984I$
$b = -0.116334 + 1.202190I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.11683 + 1.44227I$		
$a = -0.803868 - 0.992511I$	$4.04318 + 5.16032I$	$4.25149 - 6.22222I$
$b = 0.488896 + 1.051410I$		
$u = 0.11683 - 1.44227I$		
$a = -0.803868 + 0.992511I$	$4.04318 - 5.16032I$	$4.25149 + 6.22222I$
$b = 0.488896 - 1.051410I$		

$$\text{IV. } I_4^u = \langle -u^2a + u^3 - u^2 + b + u, u^5a - 4u^5 + \dots + a^2 - 2a, u^6 - u^5 + 3u^4 - 2u^3 + 3u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ u^2a - u^3 + u^2 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^5a + u^4a - 2u^5 - u^3a + 2u^4 - 4u^3 + 3u^2 - a - 4u + 2 \\ u^5a - u^4a + u^5 + 2u^3a - u^4 - u^2a + 2u^3 + au - u^2 + 2u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3a - 2u^4 + 3u^3 - 5u^2 + a + 3u - 3 \\ u^5 - u^3a + u^2a - au + 2u^2 - u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^5 + u^3a + u^4 - u^2a - 2u^3 + au + 2u^2 - a - 2u + 1 \\ u^5a - u^4a + u^5 + 2u^3a - u^4 - u^2a + 2u^3 + au - u^2 + 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^5a - u^4a - u^5 + 3u^3a + u^4 - 2u^2a - 3u^3 + 2au + 2u^2 - 2u \\ -u^3a + u^4 - au + 2u^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^5 + 2u^4 - u^2a - 3u^3 + 4u^2 - a - 3u + 2 \\ -u^4a + u^5 + u^3a - 2u^4 - u^2a + 3u^3 + au - 3u^2 + 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^5a - u^4a - u^5 + 2u^3a + 2u^4 - 2u^2a - 3u^3 + au + 4u^2 - 3u + 1 \\ -u^5a - u^3a - u^4 + u^3 - 2u^2 - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^5 + 5u^4 - u^3 + 11u^2 - 9u + 9$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^{12} - 7u^{11} + \cdots - 7u + 1$
$c_2, c_6$	$u^{12} + u^{11} + \cdots + u + 1$
$c_3$	$(u^6 - u^5 + 3u^4 - 2u^3 + 3u^2 + 1)^2$
$c_4$	$(u^6 + 2u^4 + 2u^3 + u + 1)^2$
$c_5, c_{11}$	$u^{12} - u^{11} + \cdots - u + 1$
$c_7, c_{12}$	$u^{12} + 4u^{10} + 5u^9 + 6u^8 + 11u^7 + 9u^6 + 6u^5 + 2u^4 - 2u^3 - 2u^2 + 1$
$c_8, c_9$	$(u^6 + u^5 + 3u^4 + 2u^3 + 3u^2 + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{12} + 3y^{11} + \cdots + 3y + 1$
$c_2, c_5, c_6$ $c_{11}$	$y^{12} + 7y^{11} + \cdots + 7y + 1$
$c_3, c_8, c_9$	$(y^6 + 5y^5 + 11y^4 + 16y^3 + 15y^2 + 6y + 1)^2$
$c_4$	$(y^6 + 4y^5 + 4y^4 - 2y^3 - y + 1)^2$
$c_7, c_{12}$	$y^{12} + 8y^{11} + \cdots - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.751720 + 0.952459I$		
$a = 1.161910 + 0.208933I$	$-5.66414 - 2.84527I$	$-10.09526 - 1.04786I$
$b = -0.169435 + 1.321240I$		
$u = 0.751720 + 0.952459I$		
$a = -0.214542 + 0.486127I$	$-5.66414 - 2.84527I$	$-10.09526 - 1.04786I$
$b = -0.095489 - 0.744618I$		
$u = 0.751720 - 0.952459I$		
$a = 1.161910 - 0.208933I$	$-5.66414 + 2.84527I$	$-10.09526 + 1.04786I$
$b = -0.169435 - 1.321240I$		
$u = 0.751720 - 0.952459I$		
$a = -0.214542 - 0.486127I$	$-5.66414 + 2.84527I$	$-10.09526 + 1.04786I$
$b = -0.095489 + 0.744618I$		
$u = -0.081708 + 1.363140I$		
$a = -1.41421 + 0.28398I$	$5.25930 - 1.24964I$	$4.40551 - 3.55084I$
$b = 0.456929 + 0.708982I$		
$u = -0.081708 + 1.363140I$		
$a = -1.40363 + 1.20387I$	$5.25930 - 1.24964I$	$4.40551 - 3.55084I$
$b = 0.642260 - 0.996545I$		
$u = -0.081708 - 1.363140I$		
$a = -1.41421 - 0.28398I$	$5.25930 + 1.24964I$	$4.40551 + 3.55084I$
$b = 0.456929 - 0.708982I$		
$u = -0.081708 - 1.363140I$		
$a = -1.40363 - 1.20387I$	$5.25930 + 1.24964I$	$4.40551 + 3.55084I$
$b = 0.642260 + 0.996545I$		
$u = -0.170012 + 0.579072I$		
$a = 1.72240 + 0.01156I$	$2.04978 + 2.32699I$	$7.18975 - 6.61882I$
$b = -0.828025 - 0.974687I$		
$u = -0.170012 + 0.579072I$		
$a = -1.35194 - 3.13856I$	$2.04978 + 2.32699I$	$7.18975 - 6.61882I$
$b = -0.506239 + 0.595906I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.170012 - 0.579072I$		
$a = 1.72240 - 0.01156I$	$2.04978 - 2.32699I$	$7.18975 + 6.61882I$
$b = -0.828025 + 0.974687I$		
$u = -0.170012 - 0.579072I$		
$a = -1.35194 + 3.13856I$	$2.04978 - 2.32699I$	$7.18975 + 6.61882I$
$b = -0.506239 - 0.595906I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$(u^{12} - 7u^{11} + \dots - 7u + 1)(u^{12} - 7u^{11} + \dots - 9u + 1)$ $\cdot (u^{22} + 13u^{21} + \dots + 6u + 1)(u^{60} + 30u^{59} + \dots + 31603u + 2209)$
$c_2, c_6$	$(u^{12} + u^{11} + \dots + u + 1)(u^{12} + u^{11} + \dots + u + 1)(u^{22} + u^{21} + \dots - 2u + 1)$ $\cdot (u^{60} - 2u^{59} + \dots + 81u + 47)$
$c_3$	$((u^6 - u^5 + 3u^4 - 2u^3 + 3u^2 + 1)^2)(u^{12} + 2u^{11} + \dots + 6u^2 + 1)$ $\cdot (u^{22} + 11u^{21} + \dots + 232u + 32)(u^{30} - 5u^{29} + \dots - 2u + 1)^2$
$c_4$	$((u^6 + 2u^4 + 2u^3 + u + 1)^2)(u^{12} - 2u^{11} + \dots - 2u + 1)$ $\cdot (u^{22} - 15u^{21} + \dots - 480u + 64)(u^{30} + 6u^{29} + \dots + 9u + 1)^2$
$c_5, c_{11}$	$(u^{12} - u^{11} + \dots - u + 1)(u^{12} - u^{11} + \dots - u + 1)(u^{22} + u^{21} + \dots - 2u + 1)$ $\cdot (u^{60} - 2u^{59} + \dots + 81u + 47)$
$c_7, c_{12}$	$(u^{12} + 2u^{10} - u^9 + u^8 - 2u^7 + u^6 + 4u^4 + 3u^3 - 2u^2 + 1)$ $\cdot (u^{12} + 4u^{10} + 5u^9 + 6u^8 + 11u^7 + 9u^6 + 6u^5 + 2u^4 - 2u^3 - 2u^2 + 1)$ $\cdot (u^{22} + 13u^{20} + \dots - u + 1)(u^{60} + 5u^{59} + \dots - 18u + 1)$
$c_8, c_9$	$((u^6 + u^5 + 3u^4 + 2u^3 + 3u^2 + 1)^2)(u^{12} - 2u^{11} + \dots + 6u^2 + 1)$ $\cdot (u^{22} + 11u^{21} + \dots + 232u + 32)(u^{30} - 5u^{29} + \dots - 2u + 1)^2$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$(y^{12} + 3y^{11} + \dots + 3y + 1)(y^{12} + 3y^{11} + \dots - 11y + 1)$ $\cdot (y^{22} + y^{21} + \dots + 34y + 1)(y^{60} + 6y^{59} + \dots - 9.00819 \times 10^7 y + 4879681)$
$c_2, c_5, c_6$ $c_{11}$	$(y^{12} + 7y^{11} + \dots + 9y + 1)(y^{12} + 7y^{11} + \dots + 7y + 1)$ $\cdot (y^{22} + 13y^{21} + \dots + 6y + 1)(y^{60} + 30y^{59} + \dots + 31603y + 2209)$
$c_3, c_8, c_9$	$(y^6 + 5y^5 + 11y^4 + 16y^3 + 15y^2 + 6y + 1)^2$ $\cdot (y^{12} + 10y^{11} + \dots + 12y + 1)(y^{22} + 11y^{21} + \dots + 3264y + 1024)$ $\cdot (y^{30} + 9y^{29} + \dots + 14y + 1)^2$
$c_4$	$((y^6 + 4y^5 + 4y^4 - 2y^3 - y + 1)^2)(y^{12} + 6y^{11} + \dots - 2y + 1)$ $\cdot (y^{22} + 7y^{21} + \dots + 39936y + 4096)(y^{30} + 10y^{29} + \dots - 9y + 1)^2$
$c_7, c_{12}$	$(y^{12} + 4y^{11} + \dots - 4y + 1)(y^{12} + 8y^{11} + \dots - 4y + 1)$ $\cdot (y^{22} + 26y^{21} + \dots + 17y + 1)(y^{60} + 39y^{59} + \dots - 40y + 1)$