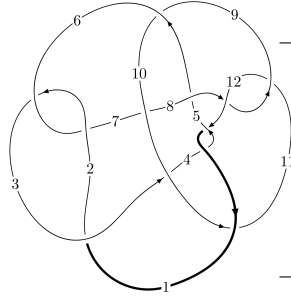
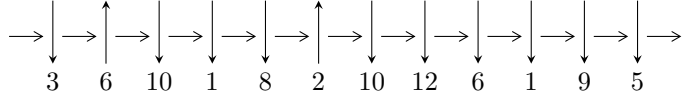


12n<sub>0527</sub> (K12n<sub>0527</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,6 \xrightarrow{c_2} 3,10 \xrightarrow{c_3} 4 \xrightarrow{c_6} 7 \xrightarrow{c_7} 8 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \rightsquigarrow c_4, c_8, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 378975u^{30} + 3018590u^{29} + \dots + 228821b - 6857553, \\ 12363803u^{30} + 93404174u^{29} + \dots + 2288210a - 220745786, u^{31} + 8u^{30} + \dots - 62u - 10 \rangle$$

$$I_2^u = \langle 3u^{18} - 6u^{17} + \dots + 2b + 2, -2u^{18}a + 10u^{18} + \dots - 3a + 21, u^{19} - 3u^{18} + \dots + 6u - 1 \rangle$$

$$I_3^u = \langle u^{14} - 4u^{13} + 12u^{12} - 24u^{11} + 40u^{10} - 52u^9 + 57u^8 - 49u^7 + 34u^6 - 18u^5 + 6u^4 - 2u^3 + b - u - 1, \\ u^{14} - 3u^{13} + 7u^{12} - 8u^{11} + 4u^{10} + 12u^9 - 34u^8 + 58u^7 - 68u^6 + 62u^5 - 44u^4 + 24u^3 - 11u^2 + 2a + 5u - 4, \\ u^{15} - 5u^{14} + \dots + 4u - 2 \rangle$$

$$I_4^u = \langle a^3u - a^3 + a^2u - a^2 + 3au + 3b + u - 1, a^4 - 3a^2u - a^2 + 2au + 2a - 2u - 2, u^2 + u + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 92 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 3.79 \times 10^5 u^{30} + 3.02 \times 10^6 u^{29} + \dots + 2.29 \times 10^5 b - 6.86 \times 10^6, 1.24 \times 10^7 u^{30} + 9.34 \times 10^7 u^{29} + \dots + 2.29 \times 10^6 a - 2.21 \times 10^8, u^{31} + 8u^{30} + \dots - 62u - 10 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -5.40326u^{30} - 40.8198u^{29} + \dots + 422.621u + 96.4709 \\ -1.65621u^{30} - 13.1919u^{29} + \dots + 143.370u + 29.9691 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -7.59786u^{30} - 57.1445u^{29} + \dots + 582.083u + 133.417 \\ -2.53663u^{30} - 19.5572u^{29} + \dots + 189.049u + 39.5947 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -5.06123u^{30} - 37.5873u^{29} + \dots + 394.034u + 92.8223 \\ -1.48595u^{30} - 10.9890u^{29} + \dots + 92.6272u + 21.5867 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2.01783u^{30} - 15.2733u^{29} + \dots + 183.285u + 43.3542 \\ -0.349286u^{30} - 3.00908u^{29} + \dots + 131.287u + 29.6924 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -4.17727u^{30} - 31.3609u^{29} + \dots + 302.304u + 68.6386 \\ -2.36578u^{30} - 18.6263u^{29} + \dots + 194.064u + 41.2391 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -5.40326u^{30} - 40.8198u^{29} + \dots + 422.621u + 96.4709 \\ -0.906058u^{30} - 7.88315u^{29} + \dots + 48.2085u + 5.90550 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2.85487u^{30} + 20.6866u^{29} + \dots - 172.102u - 39.1897 \\ -0.816394u^{30} - 6.48291u^{29} + \dots + 188.974u + 41.4018 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{1324375}{228821}u^{30} - \frac{9572041}{228821}u^{29} + \dots + \frac{117530906}{228821}u + \frac{30556088}{228821}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{31} + 20u^{30} + \dots + 684u - 100$
$c_2, c_6$	$u^{31} - 8u^{30} + \dots - 62u + 10$
$c_3, c_9$	$u^{31} + u^{30} + \dots + u + 1$
$c_4, c_5, c_{12}$	$u^{31} - u^{30} + \dots + 4u + 1$
$c_7, c_{10}$	$u^{31} - 3u^{30} + \dots + 5u + 1$
$c_8, c_{11}$	$u^{31} - 11u^{30} + \dots - 122u + 10$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{31} - 12y^{30} + \dots + 1252656y - 10000$
$c_2, c_6$	$y^{31} + 20y^{30} + \dots + 684y - 100$
$c_3, c_9$	$y^{31} - 29y^{30} + \dots + 23y - 1$
$c_4, c_5, c_{12}$	$y^{31} + 25y^{30} + \dots - 6y - 1$
$c_7, c_{10}$	$y^{31} - 29y^{30} + \dots - 105y - 1$
$c_8, c_{11}$	$y^{31} + 11y^{30} + \dots - 756y - 100$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.443501 + 0.881894I$		
$a = -1.036980 - 0.315517I$	$1.62568 - 2.07908I$	$-8.15071 + 3.76851I$
$b = -1.093880 - 0.219923I$		
$u = -0.443501 - 0.881894I$		
$a = -1.036980 + 0.315517I$	$1.62568 + 2.07908I$	$-8.15071 - 3.76851I$
$b = -1.093880 + 0.219923I$		
$u = -0.123465 + 0.920678I$		
$a = -0.63652 + 1.53942I$	$2.16097 - 0.39271I$	$-5.96156 - 1.22021I$
$b = 0.45891 + 1.91281I$		
$u = -0.123465 - 0.920678I$		
$a = -0.63652 - 1.53942I$	$2.16097 + 0.39271I$	$-5.96156 + 1.22021I$
$b = 0.45891 - 1.91281I$		
$u = 0.068946 + 1.101890I$		
$a = 0.291434 - 0.967985I$	$0.870446 + 0.149756I$	$-6.74421 + 0.11134I$
$b = -0.88132 - 1.46936I$		
$u = 0.068946 - 1.101890I$		
$a = 0.291434 + 0.967985I$	$0.870446 - 0.149756I$	$-6.74421 - 0.11134I$
$b = -0.88132 + 1.46936I$		
$u = -1.104440 + 0.109617I$		
$a = -1.138250 - 0.420860I$	$-4.10069 - 3.26217I$	$-7.80399 + 3.14222I$
$b = 0.173388 - 0.107344I$		
$u = -1.104440 - 0.109617I$		
$a = -1.138250 + 0.420860I$	$-4.10069 + 3.26217I$	$-7.80399 - 3.14222I$
$b = 0.173388 + 0.107344I$		
$u = -1.120450 + 0.048451I$		
$a = 1.313720 - 0.318482I$	$-1.92223 + 10.09630I$	$-6.60164 - 5.79982I$
$b = -0.155061 + 0.121217I$		
$u = -1.120450 - 0.048451I$		
$a = 1.313720 + 0.318482I$	$-1.92223 - 10.09630I$	$-6.60164 + 5.79982I$
$b = -0.155061 - 0.121217I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.805043 + 0.864131I$	$6.77889 + 0.72800I$	$1.42894 - 3.61029I$
$a = 0.256473 + 0.055333I$		
$b = -0.056375 - 0.617551I$		
$u = 0.805043 - 0.864131I$	$6.77889 - 0.72800I$	$1.42894 + 3.61029I$
$a = 0.256473 - 0.055333I$		
$b = -0.056375 + 0.617551I$		
$u = 0.106357 + 1.194790I$	$-4.49263 + 1.56261I$	$-18.4490 - 2.4112I$
$a = -0.585604 + 0.611175I$		
$b = 0.11850 + 1.64905I$		
$u = 0.106357 - 1.194790I$	$-4.49263 - 1.56261I$	$-18.4490 + 2.4112I$
$a = -0.585604 - 0.611175I$		
$b = 0.11850 - 1.64905I$		
$u = -0.255201 + 0.720413I$	$-0.379147 - 1.186170I$	$-4.44708 + 5.86244I$
$a = 0.353004 - 0.498369I$		
$b = 0.074523 - 0.477887I$		
$u = -0.255201 - 0.720413I$	$-0.379147 + 1.186170I$	$-4.44708 - 5.86244I$
$a = 0.353004 + 0.498369I$		
$b = 0.074523 + 0.477887I$		
$u = -0.287076 + 1.208000I$	$-0.11428 - 4.16519I$	$-8.00000 + 3.45619I$
$a = 0.591625 - 1.023160I$		
$b = 0.45808 - 2.00681I$		
$u = -0.287076 - 1.208000I$	$-0.11428 + 4.16519I$	$-8.00000 - 3.45619I$
$a = 0.591625 + 1.023160I$		
$b = 0.45808 + 2.00681I$		
$u = 0.839144 + 0.959645I$	$6.52389 + 5.44822I$	$-3.50283 + 0.I$
$a = -0.126368 + 0.182032I$		
$b = 0.546509 + 0.211498I$		
$u = 0.839144 - 0.959645I$	$6.52389 - 5.44822I$	$-3.50283 + 0.I$
$a = -0.126368 - 0.182032I$		
$b = 0.546509 - 0.211498I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.55841 + 1.36375I$ $a = -0.031464 - 1.250450I$ $b = 0.13295 - 2.63897I$	$-6.0602 - 16.0464I$	0
$u = -0.55841 - 1.36375I$ $a = -0.031464 + 1.250450I$ $b = 0.13295 + 2.63897I$	$-6.0602 + 16.0464I$	0
$u = -0.523642 + 0.015251I$ $a = 1.36675 + 1.50756I$ $b = 0.340155 + 0.377383I$	$3.48762 - 1.00607I$	$-1.97801 + 2.70347I$
$u = -0.523642 - 0.015251I$ $a = 1.36675 - 1.50756I$ $b = 0.340155 - 0.377383I$	$3.48762 + 1.00607I$	$-1.97801 - 2.70347I$
$u = -0.47698 + 1.40113I$ $a = -0.090020 + 1.114860I$ $b = -0.12726 + 2.47258I$	$-8.91065 - 8.81717I$	0
$u = -0.47698 - 1.40113I$ $a = -0.090020 - 1.114860I$ $b = -0.12726 - 2.47258I$	$-8.91065 + 8.81717I$	0
$u = -0.59892 + 1.37175I$ $a = 0.349486 + 0.852345I$ $b = 0.51025 + 1.90344I$	$-8.00712 - 2.87739I$	0
$u = -0.59892 - 1.37175I$ $a = 0.349486 - 0.852345I$ $b = 0.51025 - 1.90344I$	$-8.00712 + 2.87739I$	0
$u = -0.48869 + 1.42613I$ $a = -0.291444 - 0.902646I$ $b = -0.69470 - 2.05198I$	$-6.65609 + 4.30866I$	0
$u = -0.48869 - 1.42613I$ $a = -0.291444 + 0.902646I$ $b = -0.69470 + 2.05198I$	$-6.65609 - 4.30866I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.322569$		
$a = 1.42830$	-1.08738	-6.65470
$b = -0.609341$		



$$\text{II. } I_2^u = \langle 3u^{18} - 6u^{17} + \dots + 2b + 2, -2u^{18}a + 10u^{18} + \dots - 3a + 21, u^{19} - 3u^{18} + \dots + 6u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -\frac{3}{2}u^{18} + 3u^{17} + \dots + \frac{9}{2}u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{3}{2}u^{18} + 4u^{17} + \dots + \frac{39}{2}u - 4 \\ -\frac{3}{2}u^{18}a - \frac{1}{2}u^{18} + \dots - \frac{3}{2}a + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{3}{2}u^{18}a + u^{18} + \dots - \frac{5}{2}a + 4 \\ -\frac{1}{2}u^{18}a - 2u^{18} + \dots - \frac{3}{2}a + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{18} - \frac{5}{2}u^{17} + \dots + a + \frac{5}{2} \\ -\frac{5}{2}u^{18} + \frac{13}{2}u^{17} + \dots + 8u - \frac{3}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{18}a - \frac{3}{2}u^{18} + \dots + a - 5 \\ -u^{18}a - \frac{1}{2}u^{18} + \dots - \frac{5}{2}a + 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -\frac{3}{2}u^{18} + 3u^{17} + \dots + \frac{9}{2}u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^{18}a + u^{18} + \dots + \frac{3}{2}a + \frac{5}{2} \\ u^{18}a - \frac{3}{2}u^{18} + \dots + \frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -8u^{18} + 25u^{17} - 84u^{16} + 166u^{15} - 312u^{14} + 471u^{13} - 637u^{12} + 808u^{11} - 877u^{10} + 947u^9 - 869u^8 + 754u^7 - 616u^6 + 432u^5 - 334u^4 + 206u^3 - 115u^2 + 43u - 11$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{19} + 13u^{18} + \dots + 2u - 1)^2$
$c_2, c_6$	$(u^{19} + 3u^{18} + \dots + 6u + 1)^2$
$c_3, c_9$	$u^{38} + u^{37} + \dots + 5696u + 908$
$c_4, c_5, c_{12}$	$u^{38} - 3u^{37} + \dots + 10u^2 + 4$
$c_7, c_{10}$	$u^{38} - 5u^{37} + \dots - 28450u + 4625$
$c_8, c_{11}$	$(u^{19} + 5u^{18} + \dots + 20u + 7)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{19} - 11y^{18} + \dots + 38y - 1)^2$
$c_2, c_6$	$(y^{19} + 13y^{18} + \dots + 2y - 1)^2$
$c_3, c_9$	$y^{38} - 35y^{37} + \dots - 10830384y + 824464$
$c_4, c_5, c_{12}$	$y^{38} + 5y^{37} + \dots + 80y + 16$
$c_7, c_{10}$	$y^{38} - 37y^{37} + \dots + 236310000y + 21390625$
$c_8, c_{11}$	$(y^{19} + 11y^{18} + \dots - 300y - 49)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.041110 + 0.058191I$ $a = -1.346300 - 0.087992I$ $b = -0.070727 + 0.324415I$	$-4.78729 - 1.81592I$	$-6.58607 + 3.74202I$
$u = 1.041110 + 0.058191I$ $a = 1.44689 - 0.14447I$ $b = -0.184376 + 0.150737I$	$-4.78729 - 1.81592I$	$-6.58607 + 3.74202I$
$u = 1.041110 - 0.058191I$ $a = -1.346300 + 0.087992I$ $b = -0.070727 - 0.324415I$	$-4.78729 + 1.81592I$	$-6.58607 - 3.74202I$
$u = 1.041110 - 0.058191I$ $a = 1.44689 + 0.14447I$ $b = -0.184376 - 0.150737I$	$-4.78729 + 1.81592I$	$-6.58607 - 3.74202I$
$u = 0.228070 + 1.071510I$ $a = -0.328351 - 0.989425I$ $b = -0.07397 - 3.02445I$	$0.90159 + 7.11721I$	$-6.24817 - 10.02307I$
$u = 0.228070 + 1.071510I$ $a = 1.72904 + 1.08620I$ $b = 1.44083 + 0.92301I$	$0.90159 + 7.11721I$	$-6.24817 - 10.02307I$
$u = 0.228070 - 1.071510I$ $a = -0.328351 + 0.989425I$ $b = -0.07397 + 3.02445I$	$0.90159 - 7.11721I$	$-6.24817 + 10.02307I$
$u = 0.228070 - 1.071510I$ $a = 1.72904 - 1.08620I$ $b = 1.44083 - 0.92301I$	$0.90159 - 7.11721I$	$-6.24817 + 10.02307I$
$u = -0.624126 + 0.935674I$ $a = -0.798110 - 0.979366I$ $b = 0.076909 - 1.392880I$	$2.36034 - 1.09097I$	$-8.98199 - 1.95962I$
$u = -0.624126 + 0.935674I$ $a = -0.346295 - 0.494801I$ $b = -1.004870 - 0.509384I$	$2.36034 - 1.09097I$	$-8.98199 - 1.95962I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.624126 - 0.935674I$ $a = -0.798110 + 0.979366I$ $b = 0.076909 + 1.392880I$	$2.36034 + 1.09097I$	$-8.98199 + 1.95962I$
$u = -0.624126 - 0.935674I$ $a = -0.346295 + 0.494801I$ $b = -1.004870 + 0.509384I$	$2.36034 + 1.09097I$	$-8.98199 + 1.95962I$
$u = -0.616732 + 0.611232I$ $a = 0.432266 + 0.956807I$ $b = 0.430328 - 0.206177I$	$3.24466 - 3.79929I$	$-3.99786 + 7.09998I$
$u = -0.616732 + 0.611232I$ $a = 1.37057 + 0.50609I$ $b = 0.46061 + 1.35578I$	$3.24466 - 3.79929I$	$-3.99786 + 7.09998I$
$u = -0.616732 - 0.611232I$ $a = 0.432266 - 0.956807I$ $b = 0.430328 + 0.206177I$	$3.24466 + 3.79929I$	$-3.99786 - 7.09998I$
$u = -0.616732 - 0.611232I$ $a = 1.37057 - 0.50609I$ $b = 0.46061 - 1.35578I$	$3.24466 + 3.79929I$	$-3.99786 - 7.09998I$
$u = 0.081532 + 1.192440I$ $a = -0.965035 + 0.213609I$ $b = -0.296783 + 0.704590I$	$-4.55800 + 1.47269I$	$-15.5511 - 4.2071I$
$u = 0.081532 + 1.192440I$ $a = -0.237799 + 0.845382I$ $b = 0.16123 + 2.37600I$	$-4.55800 + 1.47269I$	$-15.5511 - 4.2071I$
$u = 0.081532 - 1.192440I$ $a = -0.965035 - 0.213609I$ $b = -0.296783 - 0.704590I$	$-4.55800 - 1.47269I$	$-15.5511 + 4.2071I$
$u = 0.081532 - 1.192440I$ $a = -0.237799 - 0.845382I$ $b = 0.16123 - 2.37600I$	$-4.55800 - 1.47269I$	$-15.5511 + 4.2071I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.116911 + 1.229070I$ $a = 0.18036 - 1.53816I$ $b = 0.50210 - 2.49405I$	$-2.01094 - 5.15095I$	$-12.30071 + 5.73853I$
$u = -0.116911 + 1.229070I$ $a = 0.180096 - 0.187932I$ $b = -1.54583 - 0.63107I$	$-2.01094 - 5.15095I$	$-12.30071 + 5.73853I$
$u = -0.116911 - 1.229070I$ $a = 0.18036 + 1.53816I$ $b = 0.50210 + 2.49405I$	$-2.01094 + 5.15095I$	$-12.30071 - 5.73853I$
$u = -0.116911 - 1.229070I$ $a = 0.180096 + 0.187932I$ $b = -1.54583 + 0.63107I$	$-2.01094 + 5.15095I$	$-12.30071 - 5.73853I$
$u = 0.54636 + 1.32865I$ $a = -0.262991 + 1.071060I$ $b = -0.65067 + 2.41212I$	$-8.72835 + 7.47965I$	$-8.40298 - 6.61968I$
$u = 0.54636 + 1.32865I$ $a = 0.186121 - 1.293220I$ $b = -0.03780 - 2.40287I$	$-8.72835 + 7.47965I$	$-8.40298 - 6.61968I$
$u = 0.54636 - 1.32865I$ $a = -0.262991 - 1.071060I$ $b = -0.65067 - 2.41212I$	$-8.72835 - 7.47965I$	$-8.40298 + 6.61968I$
$u = 0.54636 - 1.32865I$ $a = 0.186121 + 1.293220I$ $b = -0.03780 + 2.40287I$	$-8.72835 - 7.47965I$	$-8.40298 + 6.61968I$
$u = 0.47814 + 1.36384I$ $a = 0.059304 - 0.997948I$ $b = 0.53165 - 2.02906I$	$-9.27627 + 3.56613I$	$-9.74898 + 0.43427I$
$u = 0.47814 + 1.36384I$ $a = -0.186195 + 1.207920I$ $b = -0.11776 + 2.60978I$	$-9.27627 + 3.56613I$	$-9.74898 + 0.43427I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.47814 - 1.36384I$		
$a = 0.059304 + 0.997948I$	$-9.27627 - 3.56613I$	$-9.74898 - 0.43427I$
$b = 0.53165 + 2.02906I$		
$u = 0.47814 - 1.36384I$		
$a = -0.186195 - 1.207920I$	$-9.27627 - 3.56613I$	$-9.74898 - 0.43427I$
$b = -0.11776 - 2.60978I$		
$u = 0.308272 + 0.388000I$		
$a = -2.35893 + 0.54355I$	$2.82450 - 4.64371I$	$-0.81427 + 2.09655I$
$b = 0.114594 - 0.630026I$		
$u = 0.308272 + 0.388000I$		
$a = 1.78966 + 1.71963I$	$2.82450 - 4.64371I$	$-0.81427 + 2.09655I$
$b = 1.44880 + 0.41504I$		
$u = 0.308272 - 0.388000I$		
$a = -2.35893 - 0.54355I$	$2.82450 + 4.64371I$	$-0.81427 - 2.09655I$
$b = 0.114594 + 0.630026I$		
$u = 0.308272 - 0.388000I$		
$a = 1.78966 - 1.71963I$	$2.82450 + 4.64371I$	$-0.81427 - 2.09655I$
$b = 1.44880 - 0.41504I$		
$u = 0.348561$		
$a = 1.45571 + 0.80946I$	$-1.06383$	$-4.73570$
$b = -0.684266 + 0.183801I$		
$u = 0.348561$		
$a = 1.45571 - 0.80946I$	$-1.06383$	$-4.73570$
$b = -0.684266 - 0.183801I$		

**III.**

$$I_3^u = \langle u^{14} - 4u^{13} + \dots + b - 1, u^{14} - 3u^{13} + \dots + 2a - 4, u^{15} - 5u^{14} + \dots + 4u - 2 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u^{14} + \frac{3}{2}u^{13} + \dots - \frac{5}{2}u + 2 \\ -u^{14} + 4u^{13} + \dots + u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{3}{2}u^{14} + \frac{15}{2}u^{13} + \dots + \frac{11}{2}u + 1 \\ -u^{14} + 6u^{13} + \dots + 9u - 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u^{14} - \frac{3}{2}u^{13} + \dots + \frac{9}{2}u - 3 \\ u^{14} - 4u^{13} + \dots - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}u^{14} + \frac{3}{2}u^{13} + \dots - \frac{3}{2}u + 1 \\ -u^{14} + 3u^{13} + \dots + u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{3}{2}u^{14} + \frac{13}{2}u^{13} + \dots + \frac{5}{2}u + 2 \\ -u^{14} + 5u^{13} + \dots + 7u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}u^{14} + \frac{3}{2}u^{13} + \dots - \frac{5}{2}u + 2 \\ -u^{14} + 3u^{13} + \dots - 2u + 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^{14} - \frac{7}{2}u^{13} + \dots - \frac{17}{2}u + 2 \\ -u^{14} + 3u^{13} + \dots - 6u + 3 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $-5u^{14} + 25u^{13} - 82u^{12} + 189u^{11} - 343u^{10} + 505u^9 - 614u^8 + 627u^7 - 530u^6 + 382u^5 - 230u^4 + 128u^3 - 69u^2 + 30u - 22$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} - 9u^{14} + \dots - 36u + 4$
$c_2$	$u^{15} - 5u^{14} + \dots + 4u - 2$
$c_3, c_9$	$u^{15} - u^{14} + \dots + 2u + 1$
$c_4$	$u^{15} + u^{14} + \dots + u + 1$
$c_5, c_{12}$	$u^{15} - u^{14} + \dots + u - 1$
$c_6$	$u^{15} + 5u^{14} + \dots + 4u + 2$
$c_7, c_{10}$	$u^{15} - 3u^{14} + \dots - 2u - 1$
$c_8$	$u^{15} - 8u^{14} + \dots - 13u^2 + 2$
$c_{11}$	$u^{15} + 8u^{14} + \dots + 13u^2 - 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} + y^{14} + \dots + 8y - 16$
$c_2, c_6$	$y^{15} + 9y^{14} + \dots - 36y - 4$
$c_3, c_9$	$y^{15} - 7y^{14} + \dots + 10y - 1$
$c_4, c_5, c_{12}$	$y^{15} + 7y^{14} + \dots - 3y - 1$
$c_7, c_{10}$	$y^{15} - 15y^{14} + \dots + 2y - 1$
$c_8, c_{11}$	$y^{15} + 4y^{14} + \dots + 52y - 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.04105$ $a = -1.34448$ $b = 0.0574551$	$-5.05234$	$-7.86790$
$u = 0.142498 + 1.177400I$ $a = 0.797818 + 0.992560I$ $b = 0.36789 + 2.16887I$	$-0.25982 + 6.07751I$	$-9.42891 - 6.08368I$
$u = 0.142498 - 1.177400I$ $a = 0.797818 - 0.992560I$ $b = 0.36789 - 2.16887I$	$-0.25982 - 6.07751I$	$-9.42891 + 6.08368I$
$u = -0.148124 + 1.190680I$ $a = -0.655334 - 0.497245I$ $b = -0.05017 - 1.63184I$	$-4.01281 - 1.46048I$	$-1.86959 - 1.16010I$
$u = -0.148124 - 1.190680I$ $a = -0.655334 + 0.497245I$ $b = -0.05017 + 1.63184I$	$-4.01281 + 1.46048I$	$-1.86959 + 1.16010I$
$u = 0.887881 + 0.860290I$ $a = 0.167268 - 0.597728I$ $b = -0.258465 - 0.613512I$	$6.43693 + 6.13733I$	$-4.68757 - 9.65401I$
$u = 0.887881 - 0.860290I$ $a = 0.167268 + 0.597728I$ $b = -0.258465 + 0.613512I$	$6.43693 - 6.13733I$	$-4.68757 + 9.65401I$
$u = 0.875773 + 0.967963I$ $a = -0.497404 + 0.294113I$ $b = -0.306201 + 0.669414I$	$6.12254 + 0.37048I$	$-8.78610 + 1.49023I$
$u = 0.875773 - 0.967963I$ $a = -0.497404 - 0.294113I$ $b = -0.306201 - 0.669414I$	$6.12254 - 0.37048I$	$-8.78610 - 1.49023I$
$u = 0.033850 + 0.679992I$ $a = 1.52172 - 0.70551I$ $b = 1.200660 + 0.615415I$	$1.81263 - 5.19090I$	$-8.70220 + 5.73716I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.033850 - 0.679992I$	$1.81263 + 5.19090I$	$-8.70220 - 5.73716I$
$a = 1.52172 + 0.70551I$		
$b = 1.200660 - 0.615415I$		
$u = -0.336015 + 0.511815I$	$-1.61892 - 0.67704I$	$-12.66646 + 4.31369I$
$a = 0.171836 + 0.846334I$		
$b = -0.756395 - 0.011183I$		
$u = -0.336015 - 0.511815I$	$-1.61892 + 0.67704I$	$-12.66646 - 4.31369I$
$a = 0.171836 - 0.846334I$		
$b = -0.756395 + 0.011183I$		
$u = 0.52361 + 1.34992I$	$-9.24424 + 5.57231I$	$-9.92521 - 3.30109I$
$a = 0.166332 - 1.108050I$		
$b = 0.27395 - 2.30620I$		
$u = 0.52361 - 1.34992I$	$-9.24424 - 5.57231I$	$-9.92521 + 3.30109I$
$a = 0.166332 + 1.108050I$		
$b = 0.27395 + 2.30620I$		

$$\text{IV. } I_4^u = \langle a^3u - a^3 + a^2u - a^2 + 3au + 3b + u - 1, a^4 - 3a^2u - a^2 + 2au + 2a - 2u - 2, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -\frac{1}{3}a^3u - \frac{1}{3}a^2u + \cdots + \frac{1}{3}a^2 + \frac{1}{3} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{3}a^3u - \frac{1}{3}a^2u + \cdots - a + \frac{7}{3} \\ -a^3u + a^2 - au - 2a + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{2}{3}a^3u - \frac{1}{3}a^2u + \cdots + a - \frac{2}{3} \\ \frac{2}{3}a^3u - \frac{1}{3}a^2u + \cdots + a + \frac{1}{3} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{3}a^3u + \frac{1}{3}a^2u + \cdots + a + \frac{2}{3} \\ a^3 + a^2 - 2au + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{2}{3}a^3u + \frac{1}{3}a^2u + \cdots - 2a + \frac{11}{3} \\ -\frac{4}{3}a^3u + \frac{2}{3}a^2u + \cdots - 3a + \frac{13}{3} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -\frac{1}{3}a^3u - \frac{1}{3}a^2u + \cdots + a + \frac{1}{3} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a^3u + a^3 - au + 2a + u \\ a^3u + a^3 - a^2u - au + 2a + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$(u^2 - u + 1)^4$
$c_2$	$(u^2 + u + 1)^4$
$c_3, c_9$	$u^8 - 5u^6 + 2u^5 + 11u^4 - 2u^3 - 6u^2 + 4u + 4$
$c_4$	$u^8 + 2u^7 + 7u^6 + 8u^5 + 15u^4 + 10u^3 + 10u^2 + 4u + 4$
$c_5, c_{12}$	$u^8 - 2u^7 + 7u^6 - 8u^5 + 15u^4 - 10u^3 + 10u^2 - 4u + 4$
$c_7, c_8, c_{10}$ $c_{11}$	$(u^2 + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$	$(y^2 + y + 1)^4$
$c_3, c_9$	$y^8 - 10y^7 + 47y^6 - 126y^5 + 197y^4 - 192y^3 + 140y^2 - 64y + 16$
$c_4, c_5, c_{12}$	$y^8 + 10y^7 + 47y^6 + 126y^5 + 197y^4 + 192y^3 + 140y^2 + 64y + 16$
$c_7, c_8, c_{10}$ $c_{11}$	$(y + 1)^8$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0.178142 - 0.892797I$	$3.28987 - 2.02988I$	$-2.00000 + 3.46410I$
$b = -0.687884 - 0.392797I$		
$u = -0.500000 + 0.866025I$		
$a = 0.603323 + 0.513523I$	$3.28987 - 2.02988I$	$-2.00000 + 3.46410I$
$b = 1.46935 + 0.01352I$		
$u = -0.500000 + 0.866025I$		
$a = 0.68788 + 1.39280I$	$3.28987 - 2.02988I$	$-2.00000 + 3.46410I$
$b = -0.17814 + 1.89280I$		
$u = -0.500000 + 0.866025I$		
$a = -1.46935 - 1.01352I$	$3.28987 - 2.02988I$	$-2.00000 + 3.46410I$
$b = -0.60332 - 1.51352I$		
$u = -0.500000 - 0.866025I$		
$a = 0.178142 + 0.892797I$	$3.28987 + 2.02988I$	$-2.00000 - 3.46410I$
$b = -0.687884 + 0.392797I$		
$u = -0.500000 - 0.866025I$		
$a = 0.603323 - 0.513523I$	$3.28987 + 2.02988I$	$-2.00000 - 3.46410I$
$b = 1.46935 - 0.01352I$		
$u = -0.500000 - 0.866025I$		
$a = 0.68788 - 1.39280I$	$3.28987 + 2.02988I$	$-2.00000 - 3.46410I$
$b = -0.17814 - 1.89280I$		
$u = -0.500000 - 0.866025I$		
$a = -1.46935 + 1.01352I$	$3.28987 + 2.02988I$	$-2.00000 - 3.46410I$
$b = -0.60332 + 1.51352I$		



## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^4)(u^{15} - 9u^{14} + \dots - 36u + 4)$ $\cdot ((u^{19} + 13u^{18} + \dots + 2u - 1)^2)(u^{31} + 20u^{30} + \dots + 684u - 100)$
$c_2$	$((u^2 + u + 1)^4)(u^{15} - 5u^{14} + \dots + 4u - 2)(u^{19} + 3u^{18} + \dots + 6u + 1)^2$ $\cdot (u^{31} - 8u^{30} + \dots - 62u + 10)$
$c_3, c_9$	$(u^8 - 5u^6 + \dots + 4u + 4)(u^{15} - u^{14} + \dots + 2u + 1)$ $\cdot (u^{31} + u^{30} + \dots + u + 1)(u^{38} + u^{37} + \dots + 5696u + 908)$
$c_4$	$(u^8 + 2u^7 + 7u^6 + 8u^5 + 15u^4 + 10u^3 + 10u^2 + 4u + 4)$ $\cdot (u^{15} + u^{14} + \dots + u + 1)(u^{31} - u^{30} + \dots + 4u + 1)$ $\cdot (u^{38} - 3u^{37} + \dots + 10u^2 + 4)$
$c_5, c_{12}$	$(u^8 - 2u^7 + 7u^6 - 8u^5 + 15u^4 - 10u^3 + 10u^2 - 4u + 4)$ $\cdot (u^{15} - u^{14} + \dots + u - 1)(u^{31} - u^{30} + \dots + 4u + 1)$ $\cdot (u^{38} - 3u^{37} + \dots + 10u^2 + 4)$
$c_6$	$((u^2 - u + 1)^4)(u^{15} + 5u^{14} + \dots + 4u + 2)(u^{19} + 3u^{18} + \dots + 6u + 1)^2$ $\cdot (u^{31} - 8u^{30} + \dots - 62u + 10)$
$c_7, c_{10}$	$((u^2 + 1)^4)(u^{15} - 3u^{14} + \dots - 2u - 1)(u^{31} - 3u^{30} + \dots + 5u + 1)$ $\cdot (u^{38} - 5u^{37} + \dots - 28450u + 4625)$
$c_8$	$((u^2 + 1)^4)(u^{15} - 8u^{14} + \dots - 13u^2 + 2)(u^{19} + 5u^{18} + \dots + 20u + 7)^2$ $\cdot (u^{31} - 11u^{30} + \dots - 122u + 10)$
$c_{11}$	$((u^2 + 1)^4)(u^{15} + 8u^{14} + \dots + 13u^2 - 2)(u^{19} + 5u^{18} + \dots + 20u + 7)^2$ $\cdot (u^{31} - 11u^{30} + \dots - 122u + 10)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^4)(y^{15} + y^{14} + \dots + 8y - 16)$ $\cdot (y^{19} - 11y^{18} + \dots + 38y - 1)^2$ $\cdot (y^{31} - 12y^{30} + \dots + 1252656y - 10000)$
$c_2, c_6$	$((y^2 + y + 1)^4)(y^{15} + 9y^{14} + \dots - 36y - 4)$ $\cdot ((y^{19} + 13y^{18} + \dots + 2y - 1)^2)(y^{31} + 20y^{30} + \dots + 684y - 100)$
$c_3, c_9$	$(y^8 - 10y^7 + 47y^6 - 126y^5 + 197y^4 - 192y^3 + 140y^2 - 64y + 16)$ $\cdot (y^{15} - 7y^{14} + \dots + 10y - 1)(y^{31} - 29y^{30} + \dots + 23y - 1)$ $\cdot (y^{38} - 35y^{37} + \dots - 10830384y + 824464)$
$c_4, c_5, c_{12}$	$(y^8 + 10y^7 + 47y^6 + 126y^5 + 197y^4 + 192y^3 + 140y^2 + 64y + 16)$ $\cdot (y^{15} + 7y^{14} + \dots - 3y - 1)(y^{31} + 25y^{30} + \dots - 6y - 1)$ $\cdot (y^{38} + 5y^{37} + \dots + 80y + 16)$
$c_7, c_{10}$	$((y + 1)^8)(y^{15} - 15y^{14} + \dots + 2y - 1)(y^{31} - 29y^{30} + \dots - 105y - 1)$ $\cdot (y^{38} - 37y^{37} + \dots + 236310000y + 21390625)$
$c_8, c_{11}$	$((y + 1)^8)(y^{15} + 4y^{14} + \dots + 52y - 4)$ $\cdot ((y^{19} + 11y^{18} + \dots - 300y - 49)^2)(y^{31} + 11y^{30} + \dots - 756y - 100)$