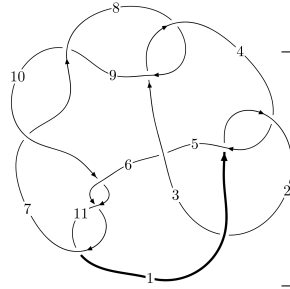
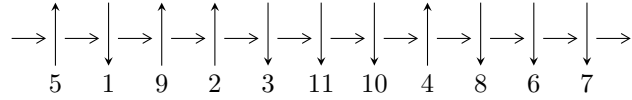


11a<sub>12</sub> (K11a<sub>12</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$6,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_6} 7 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 1,3 \xrightarrow{c_2} 2 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_3} 4 \longrightarrow c_1, c_4, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 5u^{52} - 9u^{51} + \dots + b - 4, 5u^{52} - 8u^{51} + \dots + 2a - 5, u^{53} - 3u^{52} + \dots + 6u^2 + 1 \rangle$$

$$I_2^u = \langle b, a^2 + a + 1, u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 55 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle 5u^{52} - 9u^{51} + \dots + b - 4, 5u^{52} - 8u^{51} + \dots + 2a - 5, u^{53} - 3u^{52} + \dots + 6u^2 + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{5}{2}u^{52} + 4u^{51} + \dots + \frac{1}{2}u + \frac{5}{2} \\ -5u^{52} + 9u^{51} + \dots + 3u + 4 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{9}{2}u^{52} + 8u^{51} + \dots + \frac{5}{2}u + \frac{9}{2} \\ -\frac{1}{2}u^{52} + u^{51} + \dots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{52} - u^{51} + \dots + \frac{11}{2}u + \frac{1}{2} \\ u^{16} - 6u^{14} + \dots - 6u^3 - 4u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ -u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{11}{2}u^{52} + 10u^{51} + \dots + \frac{5}{2}u + \frac{9}{2} \\ 2u^{52} - 3u^{51} + \dots - u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{11}{2}u^{52} + 10u^{51} + \dots + \frac{5}{2}u + \frac{9}{2} \\ 2u^{52} - 3u^{51} + \dots - u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $11u^{52} - 15u^{51} + \dots - 11u - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{53} + 2u^{52} + \dots - 3u - 1$
$c_2$	$u^{53} + 24u^{52} + \dots + u - 1$
$c_3, c_8$	$u^{53} + u^{52} + \dots + 12u + 4$
$c_5$	$u^{53} - 2u^{52} + \dots + 5u - 1$
$c_6, c_{10}, c_{11}$	$u^{53} - 3u^{52} + \dots + 6u^2 + 1$
$c_7, c_9$	$u^{53} + 15u^{52} + \dots - 120u - 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{53} + 24y^{52} + \dots + y - 1$
$c_2$	$y^{53} + 12y^{52} + \dots + 25y - 1$
$c_3, c_8$	$y^{53} + 15y^{52} + \dots - 120y - 16$
$c_5$	$y^{53} + 50y^{51} + \dots + 49y - 1$
$c_6, c_{10}, c_{11}$	$y^{53} - 43y^{52} + \dots - 12y - 1$
$c_7, c_9$	$y^{53} + 43y^{52} + \dots - 1248y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.968116 + 0.283551I$ $a = -0.381885 + 0.265140I$ $b = 0.072613 - 0.438240I$	$-2.32930 + 1.08642I$	$-8.77370 + 0.57725I$
$u = -0.968116 - 0.283551I$ $a = -0.381885 - 0.265140I$ $b = 0.072613 + 0.438240I$	$-2.32930 - 1.08642I$	$-8.77370 - 0.57725I$
$u = -0.108156 + 0.876063I$ $a = -1.32408 - 1.36471I$ $b = 1.61654 + 1.16042I$	$3.78899 + 9.71652I$	$-1.28115 - 7.65601I$
$u = -0.108156 - 0.876063I$ $a = -1.32408 + 1.36471I$ $b = 1.61654 - 1.16042I$	$3.78899 - 9.71652I$	$-1.28115 + 7.65601I$
$u = -0.082170 + 0.858832I$ $a = 1.44862 + 0.76672I$ $b = -1.73090 - 0.73690I$	$5.69104 + 4.47611I$	$1.74448 - 3.16326I$
$u = -0.082170 - 0.858832I$ $a = 1.44862 - 0.76672I$ $b = -1.73090 + 0.73690I$	$5.69104 - 4.47611I$	$1.74448 + 3.16326I$
$u = -0.007145 + 0.820800I$ $a = 1.52444 - 0.74981I$ $b = -1.84453 + 0.32226I$	$6.01459 + 1.53976I$	$2.52644 - 2.51375I$
$u = -0.007145 - 0.820800I$ $a = 1.52444 + 0.74981I$ $b = -1.84453 - 0.32226I$	$6.01459 - 1.53976I$	$2.52644 + 2.51375I$
$u = -1.18911$ $a = -0.404114$ $b = 1.21704$	$-2.34833$	$0$
$u = 0.031004 + 0.805221I$ $a = -1.40526 + 1.45329I$ $b = 1.78482 - 0.80414I$	$4.38710 - 3.67589I$	$0.16278 + 2.56525I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.031004 - 0.805221I$ $a = -1.40526 - 1.45329I$ $b = 1.78482 + 0.80414I$	$4.38710 + 3.67589I$	$0.16278 - 2.56525I$
$u = -0.108842 + 0.774169I$ $a = -0.215748 - 0.202638I$ $b = 0.884831 + 0.268769I$	$0.49494 + 2.64295I$	$-4.27164 - 3.21466I$
$u = -0.108842 - 0.774169I$ $a = -0.215748 + 0.202638I$ $b = 0.884831 - 0.268769I$	$0.49494 - 2.64295I$	$-4.27164 + 3.21466I$
$u = 1.226730 + 0.035206I$ $a = -0.322557 - 1.040730I$ $b = 0.081070 - 0.587091I$	$-2.80413 - 2.50478I$	0
$u = 1.226730 - 0.035206I$ $a = -0.322557 + 1.040730I$ $b = 0.081070 + 0.587091I$	$-2.80413 + 2.50478I$	0
$u = -0.616308 + 0.457732I$ $a = -0.500886 - 1.035960I$ $b = 0.030166 + 0.720650I$	$-3.24252 - 1.36437I$	$-10.10455 + 0.49514I$
$u = -0.616308 - 0.457732I$ $a = -0.500886 + 1.035960I$ $b = 0.030166 - 0.720650I$	$-3.24252 + 1.36437I$	$-10.10455 - 0.49514I$
$u = -1.163700 + 0.443994I$ $a = -0.632507 - 1.100300I$ $b = -1.092410 + 0.318801I$	$0.55249 - 5.00025I$	0
$u = -1.163700 - 0.443994I$ $a = -0.632507 + 1.100300I$ $b = -1.092410 - 0.318801I$	$0.55249 + 5.00025I$	0
$u = -1.218450 + 0.268078I$ $a = 0.170099 + 0.071272I$ $b = -0.35378 - 1.55230I$	$-2.73834 + 1.08871I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.218450 - 0.268078I$ $a = 0.170099 - 0.071272I$ $b = -0.35378 + 1.55230I$	$-2.73834 - 1.08871I$	0
$u = -1.191390 + 0.413451I$ $a = 0.165753 + 1.023680I$ $b = 1.384980 + 0.151319I$	$2.28411 + 0.08613I$	0
$u = -1.191390 - 0.413451I$ $a = 0.165753 - 1.023680I$ $b = 1.384980 - 0.151319I$	$2.28411 - 0.08613I$	0
$u = -0.430093 + 0.598904I$ $a = -1.44144 - 0.66547I$ $b = 0.441095 + 0.500611I$	$-2.63045 + 5.30697I$	$-7.17193 - 8.38740I$
$u = -0.430093 - 0.598904I$ $a = -1.44144 + 0.66547I$ $b = 0.441095 - 0.500611I$	$-2.63045 - 5.30697I$	$-7.17193 + 8.38740I$
$u = 1.244290 + 0.351593I$ $a = -0.585410 + 1.135750I$ $b = -1.101840 + 0.108048I$	$0.641453 - 0.489898I$	0
$u = 1.244290 - 0.351593I$ $a = -0.585410 - 1.135750I$ $b = -1.101840 - 0.108048I$	$0.641453 + 0.489898I$	0
$u = -1.294170 + 0.057870I$ $a = 0.733580 - 0.333474I$ $b = -2.30447 + 0.90915I$	$-4.79813 + 3.38896I$	0
$u = -1.294170 - 0.057870I$ $a = 0.733580 + 0.333474I$ $b = -2.30447 - 0.90915I$	$-4.79813 - 3.38896I$	0
$u = -1.262360 + 0.367119I$ $a = -0.757803 + 0.671105I$ $b = 1.92362 + 1.39721I$	$2.12308 + 2.73219I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.262360 - 0.367119I$ $a = -0.757803 - 0.671105I$ $b = 1.92362 - 1.39721I$	$2.12308 - 2.73219I$	0
$u = 1.273870 + 0.366638I$ $a = 0.073628 - 1.101770I$ $b = 1.35653 - 0.53361I$	$2.03469 - 5.80979I$	0
$u = 1.273870 - 0.366638I$ $a = 0.073628 + 1.101770I$ $b = 1.35653 + 0.53361I$	$2.03469 + 5.80979I$	0
$u = -1.291970 + 0.356069I$ $a = 1.120780 - 0.449943I$ $b = -2.13237 - 2.00334I$	$0.26166 + 7.85803I$	0
$u = -1.291970 - 0.356069I$ $a = 1.120780 + 0.449943I$ $b = -2.13237 + 2.00334I$	$0.26166 - 7.85803I$	0
$u = 1.355440 + 0.136049I$ $a = -0.753075 - 0.237855I$ $b = 0.928079 - 0.540827I$	$-5.74714 - 3.41063I$	0
$u = 1.355440 - 0.136049I$ $a = -0.753075 + 0.237855I$ $b = 0.928079 + 0.540827I$	$-5.74714 + 3.41063I$	0
$u = 1.333880 + 0.341289I$ $a = 0.269451 + 0.152167I$ $b = -0.70513 + 1.50804I$	$-4.03348 - 6.68828I$	0
$u = 1.333880 - 0.341289I$ $a = 0.269451 - 0.152167I$ $b = -0.70513 - 1.50804I$	$-4.03348 + 6.68828I$	0
$u = 1.329340 + 0.384853I$ $a = -0.862126 - 0.636182I$ $b = 1.64046 - 1.66007I$	$1.26818 - 8.94141I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.329340 - 0.384853I$ $a = -0.862126 + 0.636182I$ $b = 1.64046 + 1.66007I$	$1.26818 + 8.94141I$	0
$u = 1.398170 + 0.082873I$ $a = 0.626703 - 0.081349I$ $b = -0.96603 + 1.31820I$	$-9.55416 - 0.10492I$	0
$u = 1.398170 - 0.082873I$ $a = 0.626703 + 0.081349I$ $b = -0.96603 - 1.31820I$	$-9.55416 + 0.10492I$	0
$u = 1.347190 + 0.390740I$ $a = 1.171490 + 0.397318I$ $b = -1.70731 + 2.12421I$	$-0.7808 - 14.2618I$	0
$u = 1.347190 - 0.390740I$ $a = 1.171490 - 0.397318I$ $b = -1.70731 - 2.12421I$	$-0.7808 + 14.2618I$	0
$u = 1.397480 + 0.165043I$ $a = 0.932544 + 0.257510I$ $b = -1.53992 + 0.33246I$	$-8.47430 - 7.85966I$	0
$u = 1.397480 - 0.165043I$ $a = 0.932544 - 0.257510I$ $b = -1.53992 - 0.33246I$	$-8.47430 + 7.85966I$	0
$u = -0.340173 + 0.453801I$ $a = 1.060390 + 0.375276I$ $b = -0.159985 - 0.452155I$	$-0.42373 + 1.39478I$	$-2.79014 - 5.25225I$
$u = -0.340173 - 0.453801I$ $a = 1.060390 - 0.375276I$ $b = -0.159985 + 0.452155I$	$-0.42373 - 1.39478I$	$-2.79014 + 5.25225I$
$u = 0.020226 + 0.357518I$ $a = 2.02061 + 0.44390I$ $b = -0.218240 - 0.573207I$	$0.51548 + 1.38171I$	$2.20295 - 4.47540I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.020226 - 0.357518I$	$0.51548 - 1.38171I$	$2.20295 + 4.47540I$
$a = 2.02061 - 0.44390I$		
$b = -0.218240 + 0.573207I$		
$u = 0.219966 + 0.200182I$	$-0.24387 - 2.48522I$	$1.64376 + 3.61634I$
$a = -3.43324 - 0.35025I$		
$b = 0.603600 + 0.354674I$		
$u = 0.219966 - 0.200182I$	$-0.24387 + 2.48522I$	$1.64376 - 3.61634I$
$a = -3.43324 + 0.35025I$		
$b = 0.603600 - 0.354674I$		

$$\text{II. } I_2^u = \langle b, a^2 + a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a - 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$u^2 + u + 1$
$c_3, c_7, c_8$ $c_9$	$u^2$
$c_4$	$u^2 - u + 1$
$c_6$	$(u - 1)^2$
$c_{10}, c_{11}$	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$y^2 + y + 1$
$c_3, c_7, c_8$ $c_9$	$y^2$
$c_6, c_{10}, c_{11}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -0.500000 + 0.866025I$	$-1.64493 + 2.02988I$	$-3.00000 - 3.46410I$
$b = 0$		
$u = -1.00000$		
$a = -0.500000 - 0.866025I$	$-1.64493 - 2.02988I$	$-3.00000 + 3.46410I$
$b = 0$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + u + 1)(u^{53} + 2u^{52} + \dots - 3u - 1)$
$c_2$	$(u^2 + u + 1)(u^{53} + 24u^{52} + \dots + u - 1)$
$c_3, c_8$	$u^2(u^{53} + u^{52} + \dots + 12u + 4)$
$c_4$	$(u^2 - u + 1)(u^{53} + 2u^{52} + \dots - 3u - 1)$
$c_5$	$(u^2 + u + 1)(u^{53} - 2u^{52} + \dots + 5u - 1)$
$c_6$	$((u - 1)^2)(u^{53} - 3u^{52} + \dots + 6u^2 + 1)$
$c_7, c_9$	$u^2(u^{53} + 15u^{52} + \dots - 120u - 16)$
$c_{10}, c_{11}$	$((u + 1)^2)(u^{53} - 3u^{52} + \dots + 6u^2 + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y^2 + y + 1)(y^{53} + 24y^{52} + \dots + y - 1)$
$c_2$	$(y^2 + y + 1)(y^{53} + 12y^{52} + \dots + 25y - 1)$
$c_3, c_8$	$y^2(y^{53} + 15y^{52} + \dots - 120y - 16)$
$c_5$	$(y^2 + y + 1)(y^{53} + 50y^{51} + \dots + 49y - 1)$
$c_6, c_{10}, c_{11}$	$((y - 1)^2)(y^{53} - 43y^{52} + \dots - 12y - 1)$
$c_7, c_9$	$y^2(y^{53} + 43y^{52} + \dots - 1248y - 256)$