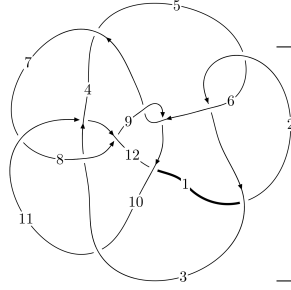
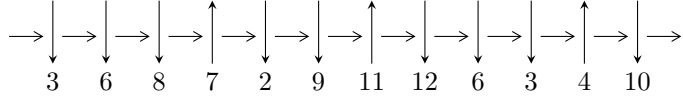


12n₀₅₃₈ (K12n₀₅₃₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$2,6 \xrightarrow{c_2} 3,9 \xrightarrow{c_6} 7 \xrightarrow{c_9} 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_4} 4 \xrightarrow{c_{12}} 12 \xrightarrow{c_8} 8 \twoheadrightarrow c_3, c_7, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle b - u, -1.88153 \times 10^{15}u^{21} - 8.14124 \times 10^{14}u^{20} + \dots + 7.04162 \times 10^{15}a - 1.77167 \times 10^{16}, u^{22} + u^{21} + \dots - u - 1 \rangle$$

$$I_2^u = \langle 3.24728 \times 10^{55}u^{29} + 4.53015 \times 10^{55}u^{28} + \dots + 1.62069 \times 10^{57}b + 2.03912 \times 10^{58}, -4.46743 \times 10^{57}u^{29} - 5.44501 \times 10^{57}u^{28} + \dots + 9.44863 \times 10^{59}a - 4.18593 \times 10^{60}, u^{30} + 2u^{29} + \dots + 4496u + 583 \rangle$$

$$I_3^u = \langle b + u, -2u^{10} - 10u^9 - 13u^8 + 10u^7 + 31u^6 + 4u^5 - 27u^4 - 5u^3 + 17u^2 + a + 5u - 4, u^{11} + 4u^{10} + 2u^9 - 9u^8 - 8u^7 + 9u^6 + 9u^5 - 7u^4 - 6u^3 + 3u^2 + 2u - 1 \rangle$$

$$I_4^u = \langle b + 1, u^2 + a - u, u^3 - u - 1 \rangle$$

$$I_5^u = \langle a^2 + b + 1, a^3 + a^2 + 2a + 1, u - 1 \rangle$$

$$I_6^u = \langle b + 1, a^3 + a^2 + 2a + 1, u - 1 \rangle$$

* 6 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 72 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, -1.88 \times 10^{15}u^{21} - 8.14 \times 10^{14}u^{20} + \dots + 7.04 \times 10^{15}a - 1.77 \times 10^{16}, u^{22} + u^{21} + \dots - u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.267202u^{21} + 0.115616u^{20} + \dots + 5.41231u + 2.51601 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.617336u^{21} + 0.765365u^{20} + \dots - 1.29850u + 1.66021 \\ 0.155989u^{21} + 0.149710u^{20} + \dots + 0.884384u + 0.151586 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.267202u^{21} + 0.115616u^{20} + \dots + 5.41231u + 2.51601 \\ -0.155989u^{21} - 0.149710u^{20} + \dots + 1.11562u - 0.151586 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.267202u^{21} + 0.115616u^{20} + \dots + 4.41231u + 2.51601 \\ -0.155989u^{21} - 0.149710u^{20} + \dots + 1.11562u - 0.151586 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.322075u^{21} - 0.212786u^{20} + \dots - 6.89909u - 3.09806 \\ -0.193421u^{21} - 0.0467415u^{20} + \dots - 0.323268u - 0.397732 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.305894u^{21} + 0.558047u^{20} + \dots - 0.813238u + 1.19414 \\ -0.124057u^{21} - 0.268999u^{20} + \dots + 0.865623u + 0.408142 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.536796u^{21} + 0.450130u^{20} + \dots + 6.96025u + 3.15781 \\ -0.105547u^{21} - 0.0829132u^{20} + \dots + 1.39238u + 0.00872824 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{2868088365347525}{4694410161939152}u^{21} - \frac{18112778300119}{586801270242394}u^{20} + \dots - \frac{981896352987059}{586801270242394}u - \frac{17835381551211165}{4694410161939152}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|---|
| c_1 | $u^{22} + 33u^{21} + \dots - 15u + 1$ |
| c_2, c_5, c_{10} | $u^{22} + u^{21} + \dots - u - 1$ |
| c_3, c_8 | $u^{22} + u^{21} + \dots + 5u + 1$ |
| c_4 | $u^{22} + 2u^{21} + \dots - 126u + 103$ |
| c_6, c_9 | $u^{22} - 10u^{21} + \dots - 80u + 16$ |
| c_7 | $u^{22} + u^{21} + \dots + 36u + 8$ |
| c_{11} | $u^{22} - 13u^{21} + \dots + 2u + 4$ |
| c_{12} | $u^{22} + 4u^{21} + \dots - 281u - 83$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|---|
| c_1 | $y^{22} - 113y^{21} + \dots + 107y + 1$ |
| c_2, c_5, c_{10} | $y^{22} - 33y^{21} + \dots + 15y + 1$ |
| c_3, c_8 | $y^{22} - 9y^{21} + \dots - 25y + 1$ |
| c_4 | $y^{22} + 24y^{21} + \dots + 134916y + 10609$ |
| c_6, c_9 | $y^{22} + 6y^{21} + \dots - 672y + 256$ |
| c_7 | $y^{22} + 13y^{21} + \dots + 368y + 64$ |
| c_{11} | $y^{22} - y^{21} + \dots - 460y + 16$ |
| c_{12} | $y^{22} - 60y^{21} + \dots - 67175y + 6889$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.748970 + 0.444444I$ $a = -0.19228 + 1.51718I$ $b = -0.748970 + 0.444444I$ | $0.13615 - 1.92714I$ | $-10.34642 + 1.92836I$ |
| $u = -0.748970 - 0.444444I$ $a = -0.19228 - 1.51718I$ $b = -0.748970 - 0.444444I$ | $0.13615 + 1.92714I$ | $-10.34642 - 1.92836I$ |
| $u = -0.130611 + 0.725732I$ $a = -1.39284 - 0.49810I$ $b = -0.130611 + 0.725732I$ | $-0.18292 + 6.65611I$ | $-5.95007 - 7.18766I$ |
| $u = -0.130611 - 0.725732I$ $a = -1.39284 + 0.49810I$ $b = -0.130611 - 0.725732I$ | $-0.18292 - 6.65611I$ | $-5.95007 + 7.18766I$ |
| $u = 0.401084 + 0.542056I$ $a = 1.24737 + 1.06824I$ $b = 0.401084 + 0.542056I$ | $3.54902 + 1.72435I$ | $1.79964 - 0.73697I$ |
| $u = 0.401084 - 0.542056I$ $a = 1.24737 - 1.06824I$ $b = 0.401084 - 0.542056I$ | $3.54902 - 1.72435I$ | $1.79964 + 0.73697I$ |
| $u = -1.33424$ $a = -0.431084$ $b = -1.33424$ | -2.34301 | 2.73470 |
| $u = -0.056775 + 0.629497I$ $a = 0.785309 - 1.011460I$ $b = -0.056775 + 0.629497I$ | $-1.31504 + 2.14729I$ | $-8.96814 - 3.55690I$ |
| $u = -0.056775 - 0.629497I$ $a = 0.785309 + 1.011460I$ $b = -0.056775 - 0.629497I$ | $-1.31504 - 2.14729I$ | $-8.96814 + 3.55690I$ |
| $u = -0.287480 + 0.350556I$ $a = 1.135910 + 0.180293I$ $b = -0.287480 + 0.350556I$ | $-0.788001 + 1.021190I$ | $-5.92604 - 5.41331I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.287480 - 0.350556I$ | | |
| $a = 1.135910 - 0.180293I$ | $-0.788001 - 1.021190I$ | $-5.92604 + 5.41331I$ |
| $b = -0.287480 - 0.350556I$ | | |
| $u = 0.181344 + 0.303051I$ | | |
| $a = 1.69533 + 2.92707I$ | $0.04653 + 2.94961I$ | $-5.40179 + 1.97738I$ |
| $b = 0.181344 + 0.303051I$ | | |
| $u = 0.181344 - 0.303051I$ | | |
| $a = 1.69533 - 2.92707I$ | $0.04653 - 2.94961I$ | $-5.40179 - 1.97738I$ |
| $b = 0.181344 - 0.303051I$ | | |
| $u = 1.76598$ | | |
| $a = 0.362139$ | -9.32648 | -9.85720 |
| $b = 1.76598$ | | |
| $u = 1.88020 + 0.16813I$ | | |
| $a = 0.593976 + 0.598808I$ | $-13.59180 - 1.67864I$ | $-10.72705 - 0.48573I$ |
| $b = 1.88020 + 0.16813I$ | | |
| $u = 1.88020 - 0.16813I$ | | |
| $a = 0.593976 - 0.598808I$ | $-13.59180 + 1.67864I$ | $-10.72705 + 0.48573I$ |
| $b = 1.88020 - 0.16813I$ | | |
| $u = -1.95173 + 0.18984I$ | | |
| $a = -0.792024 + 0.526959I$ | $-15.4135 - 5.6943I$ | $-10.05870 + 3.46761I$ |
| $b = -1.95173 + 0.18984I$ | | |
| $u = -1.95173 - 0.18984I$ | | |
| $a = -0.792024 - 0.526959I$ | $-15.4135 + 5.6943I$ | $-10.05870 - 3.46761I$ |
| $b = -1.95173 - 0.18984I$ | | |
| $u = 1.97172 + 0.33031I$ | | |
| $a = 0.661105 + 0.393921I$ | $-14.3712 - 6.4475I$ | $-12.31821 + 5.34631I$ |
| $b = 1.97172 + 0.33031I$ | | |
| $u = 1.97172 - 0.33031I$ | | |
| $a = 0.661105 - 0.393921I$ | $-14.3712 + 6.4475I$ | $-12.31821 - 5.34631I$ |
| $b = 1.97172 - 0.33031I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.97465 + 0.36872I$ | | |
| $a = -0.707383 + 0.533233I$ | $-14.7419 + 15.2513I$ | $-9.04193 - 6.95312I$ |
| $b = -1.97465 + 0.36872I$ | | |
| $u = -1.97465 - 0.36872I$ | | |
| $a = -0.707383 - 0.533233I$ | $-14.7419 - 15.2513I$ | $-9.04193 + 6.95312I$ |
| $b = -1.97465 - 0.36872I$ | | |

$$\text{II. } I_2^u = \langle 3.25 \times 10^{55} u^{29} + 4.53 \times 10^{55} u^{28} + \dots + 1.62 \times 10^{57} b + 2.04 \times 10^{58}, -4.47 \times 10^{57} u^{29} - 5.45 \times 10^{57} u^{28} + \dots + 9.45 \times 10^{59} a - 4.19 \times 10^{60}, u^{30} + 2u^{29} + \dots + 4496u + 583 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00472813u^{29} + 0.00576275u^{28} + \dots + 27.0557u + 4.43020 \\ -0.0200364u^{29} - 0.0279520u^{28} + \dots - 67.4156u - 12.5818 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.00410451u^{29} + 0.0121031u^{28} + \dots + 6.61203u + 1.98039 \\ 0.00745135u^{29} + 0.0160502u^{28} + \dots + 0.792830u + 0.0832540 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00472813u^{29} + 0.00576275u^{28} + \dots + 27.0557u + 4.43020 \\ -0.0171807u^{29} - 0.0229105u^{28} + \dots - 53.5661u - 10.4285 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0247645u^{29} + 0.0337147u^{28} + \dots + 94.4714u + 17.0120 \\ -0.00141883u^{29} - 0.00143599u^{28} + \dots - 10.7523u - 3.36205 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.00504933u^{29} - 0.00945349u^{28} + \dots - 40.1713u - 6.41129 \\ 0.00262810u^{29} + 0.00887618u^{28} + \dots - 27.9565u - 3.77015 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00260386u^{29} + 0.00679584u^{28} + \dots - 7.78421u + 2.10200 \\ -0.0131077u^{29} - 0.00690705u^{28} + \dots - 102.987u - 16.3636 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.00606568u^{29} + 0.0116476u^{28} + \dots + 9.85622u - 0.550040 \\ 0.00608037u^{29} + 0.0164677u^{28} + \dots - 17.2937u - 1.45033 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $0.261146u^{29} + 0.287455u^{28} + \dots + 1402.90u + 219.809$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|--|
| c_1 | $u^{30} + 46u^{29} + \dots + 11608936u + 339889$ |
| c_2, c_5, c_{10} | $u^{30} + 2u^{29} + \dots + 4496u + 583$ |
| c_3, c_8 | $u^{30} + u^{29} + \dots + 58u - 11$ |
| c_4 | $u^{30} + 8u^{29} + \dots + 2447u + 271$ |
| c_6, c_9 | $(u^{15} + 7u^{14} + \dots + 4u + 1)^2$ |
| c_7 | $u^{30} + 3u^{29} + \dots + 356u + 88$ |
| c_{11} | $(u^{15} + 8u^{14} + \dots + 5u + 1)^2$ |
| c_{12} | $u^{30} + 2u^{29} + \dots + 197368u - 32296$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|--|
| c_1 | $y^{30} - 50y^{29} + \dots - 48946220611468y + 115524532321$ |
| c_2, c_5, c_{10} | $y^{30} - 46y^{29} + \dots - 11608936y + 339889$ |
| c_3, c_8 | $y^{30} - 3y^{29} + \dots - 3056y + 121$ |
| c_4 | $y^{30} + 64y^{29} + \dots - 1263195y + 73441$ |
| c_6, c_9 | $(y^{15} - 3y^{14} + \dots + 36y - 1)^2$ |
| c_7 | $y^{30} + 17y^{29} + \dots + 280176y + 7744$ |
| c_{11} | $(y^{15} + 28y^{13} + \dots - 9y - 1)^2$ |
| c_{12} | $y^{30} - 22y^{29} + \dots - 9540868384y + 1043031616$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = 0.733366 + 0.760399I$ $a = -0.932743 + 0.643875I$ $b = -1.086660 + 0.495175I$ | $-3.92076 - 0.11084I$ | $-19.2470 + 2.6115I$ |
| $u = 0.733366 - 0.760399I$ $a = -0.932743 - 0.643875I$ $b = -1.086660 - 0.495175I$ | $-3.92076 + 0.11084I$ | $-19.2470 - 2.6115I$ |
| $u = 1.102460 + 0.135538I$ $a = 0.850106 - 0.383862I$ $b = 1.20887 - 1.10475I$ | $-4.14672 + 8.45942I$ | $-10.28669 - 6.66978I$ |
| $u = 1.102460 - 0.135538I$ $a = 0.850106 + 0.383862I$ $b = 1.20887 + 1.10475I$ | $-4.14672 - 8.45942I$ | $-10.28669 + 6.66978I$ |
| $u = -0.873450 + 0.022311I$ $a = -0.450314 - 0.183725I$ $b = -1.86355 + 1.25575I$ | $-2.83938 + 0.15495I$ | $-69.8860 - 16.0941I$ |
| $u = -0.873450 - 0.022311I$ $a = -0.450314 + 0.183725I$ $b = -1.86355 - 1.25575I$ | $-2.83938 - 0.15495I$ | $-69.8860 + 16.0941I$ |
| $u = -0.965004 + 0.592094I$ $a = 0.798906 + 0.014589I$ $b = 1.027040 + 0.648501I$ | $-2.16274 + 2.22327I$ | $-10.93751 - 4.89170I$ |
| $u = -0.965004 - 0.592094I$ $a = 0.798906 - 0.014589I$ $b = 1.027040 - 0.648501I$ | $-2.16274 - 2.22327I$ | $-10.93751 + 4.89170I$ |
| $u = 1.133110 + 0.242313I$ $a = -0.356690 - 1.137480I$ $b = -0.340336 - 0.281341I$ | $1.41649 - 4.96313I$ | $-5.21468 + 7.56800I$ |
| $u = 1.133110 - 0.242313I$ $a = -0.356690 + 1.137480I$ $b = -0.340336 + 0.281341I$ | $1.41649 + 4.96313I$ | $-5.21468 - 7.56800I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -1.086660 + 0.495175I$ $a = 0.812020 + 0.588181I$ $b = 0.733366 + 0.760399I$ | $-3.92076 - 0.11084I$ | $-19.2470 + 2.6115I$ |
| $u = -1.086660 - 0.495175I$ $a = 0.812020 - 0.588181I$ $b = 0.733366 - 0.760399I$ | $-3.92076 + 0.11084I$ | $-19.2470 - 2.6115I$ |
| $u = 1.027040 + 0.648501I$ $a = -0.340958 + 0.662159I$ $b = -0.965004 + 0.592094I$ | $-2.16274 + 2.22327I$ | $-10.93751 - 4.89170I$ |
| $u = 1.027040 - 0.648501I$ $a = -0.340958 - 0.662159I$ $b = -0.965004 - 0.592094I$ | $-2.16274 - 2.22327I$ | $-10.93751 + 4.89170I$ |
| $u = -1.24424$ $a = 0.162086$ $b = -0.214799$ | -2.25644 | 3.80230 |
| $u = -0.340336 + 0.281341I$ $a = 2.20884 - 2.21512I$ $b = 1.133110 - 0.242313I$ | $1.41649 + 4.96313I$ | $-5.21468 - 7.56800I$ |
| $u = -0.340336 - 0.281341I$ $a = 2.20884 + 2.21512I$ $b = 1.133110 + 0.242313I$ | $1.41649 - 4.96313I$ | $-5.21468 + 7.56800I$ |
| $u = 1.20887 + 1.10475I$ $a = 0.572773 - 0.268684I$ $b = 1.102460 - 0.135538I$ | $-4.14672 - 8.45942I$ | $-6.00000 + 6.66978I$ |
| $u = 1.20887 - 1.10475I$ $a = 0.572773 + 0.268684I$ $b = 1.102460 + 0.135538I$ | $-4.14672 + 8.45942I$ | $-6.00000 - 6.66978I$ |
| $u = -0.214799$ $a = 0.938895$ $b = -1.24424$ | -2.25644 | 3.80230 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 1.81586 + 0.25309I$ $a = -0.879383 - 0.431389I$ $b = -2.13925 - 0.18775I$ | $-14.0337 - 3.5387I$ | 0 |
| $u = 1.81586 - 0.25309I$ $a = -0.879383 + 0.431389I$ $b = -2.13925 + 0.18775I$ | $-14.0337 + 3.5387I$ | 0 |
| $u = 1.88905 + 0.21159I$ $a = -0.720062 - 0.679808I$ $b = -1.91198 - 0.46830I$ | $-12.66340 - 6.19285I$ | 0 |
| $u = 1.88905 - 0.21159I$ $a = -0.720062 + 0.679808I$ $b = -1.91198 + 0.46830I$ | $-12.66340 + 6.19285I$ | 0 |
| $u = -1.91198 + 0.46830I$ $a = 0.773799 - 0.561815I$ $b = 1.88905 - 0.21159I$ | $-12.66340 + 6.19285I$ | 0 |
| $u = -1.91198 - 0.46830I$ $a = 0.773799 + 0.561815I$ $b = 1.88905 + 0.21159I$ | $-12.66340 - 6.19285I$ | 0 |
| $u = -2.13925 + 0.18775I$ $a = 0.731046 - 0.406052I$ $b = 1.81586 - 0.25309I$ | $-14.0337 + 3.5387I$ | 0 |
| $u = -2.13925 - 0.18775I$ $a = 0.731046 + 0.406052I$ $b = 1.81586 + 0.25309I$ | $-14.0337 - 3.5387I$ | 0 |
| $u = -1.86355 + 1.25575I$ $a = -0.109258 - 0.154344I$ $b = -0.873450 + 0.022311I$ | $-2.83938 + 0.15495I$ | 0 |
| $u = -1.86355 - 1.25575I$ $a = -0.109258 + 0.154344I$ $b = -0.873450 - 0.022311I$ | $-2.83938 - 0.15495I$ | 0 |

$$\text{III. } I_3^u = \langle b + u, -2u^{10} - 10u^9 + \dots + a - 4, u^{11} + 4u^{10} + \dots + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2u^{10} + 10u^9 + \dots - 5u + 4 \\ -u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 4u^{10} + 17u^9 + \dots + u + 6 \\ u^{10} + 4u^9 + 3u^8 - 6u^7 - 9u^6 + u^5 + 9u^4 + u^3 - 6u^2 - u + 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2u^{10} + 10u^9 + \dots - 5u + 4 \\ u^{10} + 4u^9 + 3u^8 - 6u^7 - 9u^6 + u^5 + 9u^4 + u^3 - 6u^2 - 3u + 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 2u^{10} + 10u^9 + \dots - 4u + 4 \\ u^{10} + 4u^9 + 3u^8 - 6u^7 - 9u^6 + u^5 + 9u^4 + 2u^3 - 6u^2 - 3u + 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -4u^{10} - 18u^9 + \dots + 3u - 5 \\ -2u^9 - 7u^8 - u^7 + 16u^6 + 6u^5 - 15u^4 - 4u^3 + 10u^2 + 2u - 2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 3u^{10} + 13u^9 + \dots - 2u + 6 \\ u^{10} + 5u^9 + 5u^8 - 10u^7 - 16u^6 + 8u^5 + 16u^4 - 5u^3 - 10u^2 + u + 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 6u^{10} + 25u^9 + \dots - 4u + 8 \\ 2u^{10} + 8u^9 + 5u^8 - 14u^7 - 14u^6 + 10u^5 + 12u^4 - 7u^3 - 7u^2 + u + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -11u^{10} - 54u^9 - 64u^8 + 66u^7 + 156u^6 - 8u^5 - 139u^4 - 6u^3 + 92u^2 + 14u - 33$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $u^{11} - 12u^{10} + \dots + 10u - 1$ |
| c_2, c_{10} | $u^{11} + 4u^{10} + 2u^9 - 9u^8 - 8u^7 + 9u^6 + 9u^5 - 7u^4 - 6u^3 + 3u^2 + 2u - 1$ |
| c_3, c_8 | $u^{11} - u^9 + u^8 + 3u^7 - u^6 - u^5 - 2u^4 - 2u^3 + 3u^2 + u - 1$ |
| c_4 | $u^{11} + u^{10} + 4u^9 + u^8 + 7u^7 - 4u^6 - 3u^5 - 7u^4 + 5u^3 + u^2 - 1$ |
| c_5 | $u^{11} - 4u^{10} + 2u^9 + 9u^8 - 8u^7 - 9u^6 + 9u^5 + 7u^4 - 6u^3 - 3u^2 + 2u + 1$ |
| c_6 | $u^{11} - 4u^{10} + \dots + 4u - 1$ |
| c_7 | $u^{11} + u^{10} + \dots + 9u + 1$ |
| c_9 | $u^{11} + 4u^{10} + \dots + 4u + 1$ |
| c_{11} | $u^{11} - 5u^{10} + 13u^9 - 20u^8 + 20u^7 - 13u^6 + 7u^5 - 5u^4 + 3u^3 - u^2 - 1$ |
| c_{12} | $u^{11} + 7u^{10} + \dots + 7u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|---------------------------------------|
| c_1 | $y^{11} - 24y^{10} + \dots + 6y - 1$ |
| c_2, c_5, c_{10} | $y^{11} - 12y^{10} + \dots + 10y - 1$ |
| c_3, c_8 | $y^{11} - 2y^{10} + \dots + 7y - 1$ |
| c_4 | $y^{11} + 7y^{10} + \dots + 2y - 1$ |
| c_6, c_9 | $y^{11} + 6y^{10} + \dots - 6y - 1$ |
| c_7 | $y^{11} + 7y^{10} + \dots + 59y - 1$ |
| c_{11} | $y^{11} + y^{10} + \dots - 2y - 1$ |
| c_{12} | $y^{11} - 17y^{10} + \dots - 7y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.783748 + 0.507589I$ $a = -0.655301 + 0.652413I$ $b = 0.783748 - 0.507589I$ | $-1.51867 + 8.25174I$ | $-7.26021 - 7.31178I$ |
| $u = -0.783748 - 0.507589I$ $a = -0.655301 - 0.652413I$ $b = 0.783748 + 0.507589I$ | $-1.51867 - 8.25174I$ | $-7.26021 + 7.31178I$ |
| $u = 1.09593$ $a = -0.532565$ $b = -1.09593$ | -2.75997 | -16.4390 |
| $u = -1.038820 + 0.472232I$ $a = 0.374208 - 1.064480I$ $b = 1.038820 - 0.472232I$ | $0.22754 + 6.88359I$ | $-6.74283 - 7.96199I$ |
| $u = -1.038820 - 0.472232I$ $a = 0.374208 + 1.064480I$ $b = 1.038820 + 0.472232I$ | $0.22754 - 6.88359I$ | $-6.74283 + 7.96199I$ |
| $u = 0.688260 + 0.474217I$ $a = 0.128118 + 0.656640I$ $b = -0.688260 - 0.474217I$ | $-2.33645 - 0.11538I$ | $-12.41153 + 0.34745I$ |
| $u = 0.688260 - 0.474217I$ $a = 0.128118 - 0.656640I$ $b = -0.688260 + 0.474217I$ | $-2.33645 + 0.11538I$ | $-12.41153 - 0.34745I$ |
| $u = 0.526465 + 0.148349I$ $a = -1.33892 - 1.68823I$ $b = -0.526465 - 0.148349I$ | $-0.17031 - 3.59582I$ | $-8.70170 + 8.76278I$ |
| $u = 0.526465 - 0.148349I$ $a = -1.33892 + 1.68823I$ $b = -0.526465 + 0.148349I$ | $-0.17031 + 3.59582I$ | $-8.70170 - 8.76278I$ |
| $u = -1.94012 + 0.28522I$ $a = 0.758182 - 0.505152I$ $b = 1.94012 - 0.28522I$ | $-12.91640 + 4.72001I$ | $-9.66405 - 2.38742I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|-----------------------|
| $u = -1.94012 - 0.28522I$ | | |
| $a = 0.758182 + 0.505152I$ | $-12.91640 - 4.72001I$ | $-9.66405 + 2.38742I$ |
| $b = 1.94012 + 0.28522I$ | | |

$$\text{IV. } I_4^u = \langle b + 1, u^2 + a - u, u^3 - u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + u \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 - 2 \\ u^2 - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + u \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + u + 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 - u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^2 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-7u^2 - u - 5$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|--------------------------------|
| c_1 | $u^3 - 2u^2 + u - 1$ |
| c_2, c_4, c_{11} | $u^3 - u - 1$ |
| c_3 | $u^3 + u^2 - 1$ |
| c_5 | $u^3 - u + 1$ |
| c_6, c_8 | $u^3 - u^2 + 2u - 1$ |
| c_7 | $u^3 + 2u^2 + 3u + 1$ |
| c_9 | $u^3 + u^2 + 2u + 1$ |
| c_{10} | $(u - 1)^3$ |
| c_{12} | u^3 |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| c_1 | $y^3 - 2y^2 - 3y - 1$ |
| c_2, c_4, c_5 c_{11} | $y^3 - 2y^2 + y - 1$ |
| c_3 | $y^3 - y^2 + 2y - 1$ |
| c_6, c_8, c_9 | $y^3 + 3y^2 + 2y - 1$ |
| c_7 | $y^3 + 2y^2 + 5y - 1$ |
| c_{10} | $(y - 1)^3$ |
| c_{12} | y^3 |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.662359 + 0.562280I$ $a = -0.78492 + 1.30714I$ $b = -1.00000$ | $1.37919 - 2.82812I$ | $-5.19557 + 4.65175I$ |
| $u = -0.662359 - 0.562280I$ $a = -0.78492 - 1.30714I$ $b = -1.00000$ | $1.37919 + 2.82812I$ | $-5.19557 - 4.65175I$ |
| $u = 1.32472$ $a = -0.430160$ $b = -1.00000$ | -2.75839 | -18.6090 |

$$\mathbf{V. } I_5^u = \langle a^2 + b + 1, a^3 + a^2 + 2a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -a^2 - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -a^2 \\ -a^2 - a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -a^2 + a - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^2 + a + 1 \\ a \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a^2 - 2a \\ -2a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a^2 \\ -2a^2 - a - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a^2 \\ -a^2 - a \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-8a^2 - 7a - 20$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------------|--------------------------------|
| c_1, c_2 | $(u - 1)^3$ |
| c_3, c_4, c_6 | $u^3 - u^2 + 2u - 1$ |
| c_5 | $(u + 1)^3$ |
| c_7 | u^3 |
| c_8 | $u^3 + u^2 - 1$ |
| c_9, c_{12} | $u^3 + u^2 + 2u + 1$ |
| c_{10}, c_{11} | $u^3 - u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|----------------------------------|------------------------------------|
| c_1, c_2, c_5 | $(y - 1)^3$ |
| c_3, c_4, c_6 c_9, c_{12} | $y^3 + 3y^2 + 2y - 1$ |
| c_7 | y^3 |
| c_8 | $y^3 - y^2 + 2y - 1$ |
| c_{10}, c_{11} | $y^3 - 2y^2 + y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.00000$ $a = -0.215080 + 1.307140I$ $b = 0.662359 + 0.562280I$ | $1.37919 + 2.82812I$ | $-5.19557 - 4.65175I$ |
| $u = 1.00000$ $a = -0.215080 - 1.307140I$ $b = 0.662359 - 0.562280I$ | $1.37919 - 2.82812I$ | $-5.19557 + 4.65175I$ |
| $u = 1.00000$ $a = -0.569840$ $b = -1.32472$ | -2.75839 | -18.6090 |

$$\text{VI. } I_6^u = \langle b + 1, a^3 + a^2 + 2a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -a^2 \\ a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ a - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a + 1 \\ a \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^2 + a + 1 \\ a^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a^2 \\ -a^2 + a - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a^2 \\ a + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-5a^2 - 4a - 16$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--------------------------------|
| c_1, c_2, c_{10} c_{11} | $(u - 1)^3$ |
| c_3, c_4, c_8 | $u^3 + u^2 - 1$ |
| c_5 | $(u + 1)^3$ |
| c_6 | $u^3 - u^2 + 2u - 1$ |
| c_7 | u^3 |
| c_9, c_{12} | $u^3 + u^2 + 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------------|------------------------------------|
| c_1, c_2, c_5 c_{10}, c_{11} | $(y - 1)^3$ |
| c_3, c_4, c_8 | $y^3 - y^2 + 2y - 1$ |
| c_6, c_9, c_{12} | $y^3 + 3y^2 + 2y - 1$ |
| c_7 | y^3 |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_6^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.00000$ $a = -0.215080 + 1.307140I$ $b = -1.00000$ | $1.37919 + 2.82812I$ | $-6.82789 - 2.41717I$ |
| $u = 1.00000$ $a = -0.215080 - 1.307140I$ $b = -1.00000$ | $1.37919 - 2.82812I$ | $-6.82789 + 2.41717I$ |
| $u = 1.00000$ $a = -0.569840$ $b = -1.00000$ | -2.75839 | -15.3440 |

VII. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $((u-1)^6)(u^3-2u^2+u-1)(u^{11}-12u^{10}+\dots+10u-1)$ $\cdot (u^{22}+33u^{21}+\dots-15u+1)$ $\cdot (u^{30}+46u^{29}+\dots+11608936u+339889)$ |
| c_2, c_{10} | $(u-1)^6(u^3-u-1)$ $\cdot (u^{11}+4u^{10}+2u^9-9u^8-8u^7+9u^6+9u^5-7u^4-6u^3+3u^2+2u-1)$ $\cdot (u^{22}+u^{21}+\dots-u-1)(u^{30}+2u^{29}+\dots+4496u+583)$ |
| c_3, c_8 | $(u^3-u^2+2u-1)(u^3+u^2-1)^2$ $\cdot (u^{11}-u^9+u^8+3u^7-u^6-u^5-2u^4-2u^3+3u^2+u-1)$ $\cdot (u^{22}+u^{21}+\dots+5u+1)(u^{30}+u^{29}+\dots+58u-11)$ |
| c_4 | $(u^3-u-1)(u^3-u^2+2u-1)(u^3+u^2-1)$ $\cdot (u^{11}+u^{10}+4u^9+u^8+7u^7-4u^6-3u^5-7u^4+5u^3+u^2-1)$ $\cdot (u^{22}+2u^{21}+\dots-126u+103)(u^{30}+8u^{29}+\dots+2447u+271)$ |
| c_5 | $(u+1)^6(u^3-u+1)$ $\cdot (u^{11}-4u^{10}+2u^9+9u^8-8u^7-9u^6+9u^5+7u^4-6u^3-3u^2+2u+1)$ $\cdot (u^{22}+u^{21}+\dots-u-1)(u^{30}+2u^{29}+\dots+4496u+583)$ |
| c_6 | $((u^3-u^2+2u-1)^3)(u^{11}-4u^{10}+\dots+4u-1)$ $\cdot ((u^{15}+7u^{14}+\dots+4u+1)^2)(u^{22}-10u^{21}+\dots-80u+16)$ |
| c_7 | $u^6(u^3+2u^2+3u+1)(u^{11}+u^{10}+\dots+9u+1)(u^{22}+u^{21}+\dots+36u+8)$ $\cdot (u^{30}+3u^{29}+\dots+356u+88)$ |
| c_9 | $((u^3+u^2+2u+1)^3)(u^{11}+4u^{10}+\dots+4u+1)$ $\cdot ((u^{15}+7u^{14}+\dots+4u+1)^2)(u^{22}-10u^{21}+\dots-80u+16)$ |
| c_{11} | $(u-1)^3(u^3-u-1)^2$ $\cdot (u^{11}-5u^{10}+13u^9-20u^8+20u^7-13u^6+7u^5-5u^4+3u^3-u^2-1)$ $\cdot ((u^{15}+8u^{14}+\dots+5u+1)^2)(u^{22}-13u^{21}+\dots+2u+4)$ |
| c_{12} | $u^3(u^3+u^2+2u+1)^2(u^{11}+7u^{10}+\dots+7u+1)$ $\cdot (u^{22}+4u^{21}+\dots-281u-83)(u^{30}+2u^{29}+\dots+197368u-32296)$ |

VIII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------|---|
| c_1 | $((y-1)^6)(y^3-2y^2-3y-1)(y^{11}-24y^{10}+\dots+6y-1)$ $\cdot (y^{22}-113y^{21}+\dots+107y+1)$ $\cdot (y^{30}-50y^{29}+\dots-48946220611468y+115524532321)$ |
| c_2, c_5, c_{10} | $((y-1)^6)(y^3-2y^2+y-1)(y^{11}-12y^{10}+\dots+10y-1)$ $\cdot (y^{22}-33y^{21}+\dots+15y+1)$ $\cdot (y^{30}-46y^{29}+\dots-11608936y+339889)$ |
| c_3, c_8 | $((y^3-y^2+2y-1)^2)(y^3+3y^2+2y-1)(y^{11}-2y^{10}+\dots+7y-1)$ $\cdot (y^{22}-9y^{21}+\dots-25y+1)(y^{30}-3y^{29}+\dots-3056y+121)$ |
| c_4 | $(y^3-2y^2+y-1)(y^3-y^2+2y-1)(y^3+3y^2+2y-1)$ $\cdot (y^{11}+7y^{10}+\dots+2y-1)(y^{22}+24y^{21}+\dots+134916y+10609)$ $\cdot (y^{30}+64y^{29}+\dots-1263195y+73441)$ |
| c_6, c_9 | $((y^3+3y^2+2y-1)^3)(y^{11}+6y^{10}+\dots-6y-1)$ $\cdot ((y^{15}-3y^{14}+\dots+36y-1)^2)(y^{22}+6y^{21}+\dots-672y+256)$ |
| c_7 | $y^6(y^3+2y^2+5y-1)(y^{11}+7y^{10}+\dots+59y-1)$ $\cdot (y^{22}+13y^{21}+\dots+368y+64)(y^{30}+17y^{29}+\dots+280176y+7744)$ |
| c_{11} | $((y-1)^3)(y^3-2y^2+y-1)^2(y^{11}+y^{10}+\dots-2y-1)$ $\cdot ((y^{15}+28y^{13}+\dots-9y-1)^2)(y^{22}-y^{21}+\dots-460y+16)$ |
| c_{12} | $y^3(y^3+3y^2+2y-1)^2(y^{11}-17y^{10}+\dots-7y-1)$ $\cdot (y^{22}-60y^{21}+\dots-67175y+6889)$ $\cdot (y^{30}-22y^{29}+\dots-9540868384y+1043031616)$ |