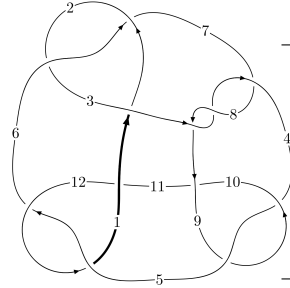
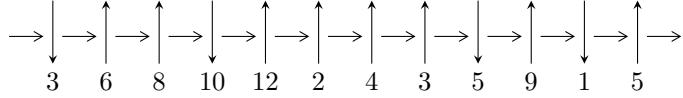


12n₀₅₅₄ (K12n₀₅₅₄)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,9 \xrightarrow{c_9} 10 \xrightarrow{c_4} 3,4 \xrightarrow{c_8} 1,8 \xrightarrow{c_{12}} 12 \xrightarrow{c_5} 6 \xrightarrow{c_2} 2 \xrightarrow{c_6} 7 \xrightarrow{c_{11}} 11 \longrightarrow c_1, c_3, c_7, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^5 - u^4 - 5u^3 - 5u^2 + 6d - 4u - 2, u^5 + u^4 - u^3 - u^2 + 12c - 8u - 4, \\ -u^5 - 4u^4 - 5u^3 - 8u^2 + 6b - 4u - 2, u^5 + u^4 + 5u^3 - u^2 + 12a - 2u - 4, \\ u^6 + 3u^5 + 7u^4 + 9u^3 + 8u^2 + 4u + 4 \rangle$$

$$I_2^u = \langle -u^3 + u^2 + 2d - 3u - 1, c + 1, b + u, u^3 - u^2 + 2a + 5u - 1, u^4 + 4u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle -u^3 + u^2 + 2d - 3u - 1, c + 1, -u^3 - u^2 + 2b - 5u - 5, -u^3 + u^2 + 2a - 5u + 3, u^4 + 4u^2 + 2u + 1 \rangle$$

$$I_4^u = \langle u^3 - u^2 + 2d + 5u + 1, 5u^3 - u^2 + 2c + 19u + 5, b + u, u^3 - u^2 + 2a + 5u - 1, u^4 + 4u^2 + 2u + 1 \rangle$$

$$I_5^u = \langle d + 1, 2c - u - 1, b, a - 1, u^2 - u + 2 \rangle$$

$$I_6^u = \langle d + 1, 2c - u - 1, b - u + 1, 2a - u + 1, u^2 - u + 2 \rangle$$

$$I_7^u = \langle d - u, c, b - u + 1, 2a - u + 1, u^2 - u + 2 \rangle$$

$$I_8^u = \langle d + 1, c, b, a - 1, u + 1 \rangle$$

$$I_9^u = \langle d, c - u, b - u, a - 1, u^2 + 1 \rangle$$

$$I_{10}^u = \langle d - u, c - 1, b + 1, a, u^2 + 1 \rangle$$

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$I_{11}^u = \langle d - u, c - 1, b - u, a - 1, u^2 + 1 \rangle$$

$$I_{12}^u = \langle d - u, cb - u + 1, a - 1, u^2 + 1 \rangle$$

$$I_1^v = \langle a, d - v, -av + c + 1, b - 1, v^2 + 1 \rangle$$

* 12 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 33 representations.

* 1 irreducible components of $\dim_{\mathbb{C}} = 1$

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -u^5 - u^4 + \dots + 6d - 2, u^5 + u^4 + \dots + 12c - 4, -u^5 - 4u^4 + \dots + 6b - 2, u^5 + u^4 + \dots + 12a - 4, u^6 + 3u^5 + \dots + 4u + 4 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{12}u^5 - \frac{1}{12}u^4 + \dots + \frac{2}{3}u + \frac{1}{3} \\ \frac{1}{6}u^5 + \frac{1}{6}u^4 + \dots + \frac{2}{3}u + \frac{1}{3} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{12}u^5 - \frac{1}{12}u^4 + \dots + \frac{1}{6}u + \frac{1}{3} \\ \frac{1}{6}u^5 + \frac{2}{3}u^4 + \dots + \frac{2}{3}u + \frac{1}{3} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{4}u^5 - \frac{3}{4}u^4 + \dots - \frac{5}{4}u^2 - \frac{1}{2}u \\ \frac{1}{3}u^5 + \frac{1}{3}u^4 + \dots + \frac{1}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{12}u^5 - \frac{1}{12}u^4 + \dots + \frac{1}{6}u + \frac{1}{3} \\ -\frac{1}{6}u^5 + \frac{1}{3}u^4 + \dots + \frac{1}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{12}u^5 + \frac{7}{12}u^4 + \dots + \frac{1}{3}u + \frac{2}{3} \\ -\frac{2}{3}u^5 - \frac{1}{6}u^4 + \dots - \frac{1}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u^3 + u^2 + \frac{1}{2}u + 1 \\ \frac{1}{3}u^5 + \frac{5}{6}u^4 + \dots + \frac{1}{3}u + \frac{2}{3} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{7}{12}u^5 + \frac{13}{12}u^4 + \dots + \frac{5}{6}u + \frac{2}{3} \\ \frac{1}{3}u^5 + \frac{7}{3}u^4 + \dots + \frac{4}{3}u + \frac{11}{3} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-u^5 - u^4 - u^3 + 5u^2 + 6u + 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_{11}	$u^6 + 2u^5 + 11u^4 + 8u^3 + 35u^2 + 6u + 1$
c_2, c_3, c_5 c_6, c_7, c_8 c_{12}	$u^6 + u^4 + 2u^3 + 5u^2 - 2u + 1$
c_4, c_9	$u^6 - 3u^5 + 7u^4 - 9u^3 + 8u^2 - 4u + 4$
c_{10}	$u^6 - 5u^5 + 11u^4 - 15u^3 + 48u^2 - 48u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{11}	$y^6 + 18y^5 + 159y^4 + 684y^3 + 1151y^2 + 34y + 1$
c_2, c_3, c_5 c_6, c_7, c_8 c_{12}	$y^6 + 2y^5 + 11y^4 + 8y^3 + 35y^2 + 6y + 1$
c_4, c_9	$y^6 + 5y^5 + 11y^4 + 15y^3 + 48y^2 + 48y + 16$
c_{10}	$y^6 - 3y^5 + 67y^4 + 383y^3 + 1216y^2 - 768y + 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.161386 + 0.788818I$ $a = 0.386240 + 0.341797I$ $b = -0.360068 + 0.335344I$ $c = 0.318404 + 0.521609I$ $d = -0.207282 + 0.359834I$	$0.555934 - 1.031130I$	$7.70744 + 6.55849I$
$u = 0.161386 - 0.788818I$ $a = 0.386240 - 0.341797I$ $b = -0.360068 - 0.335344I$ $c = 0.318404 - 0.521609I$ $d = -0.207282 - 0.359834I$	$0.555934 + 1.031130I$	$7.70744 - 6.55849I$
$u = -1.161390 + 0.788818I$ $a = -0.263365 - 0.996502I$ $b = 0.040620 - 1.297830I$ $c = -0.543326 + 0.748451I$ $d = 1.09193 + 0.94958I$	$3.25859 + 6.90945I$	$3.50627 - 5.32738I$
$u = -1.161390 - 0.788818I$ $a = -0.263365 + 0.996502I$ $b = 0.040620 + 1.297830I$ $c = -0.543326 - 0.748451I$ $d = 1.09193 - 0.94958I$	$3.25859 - 6.90945I$	$3.50627 + 5.32738I$
$u = -0.50000 + 1.69717I$ $a = -0.622875 + 0.704751I$ $b = -0.18055 + 2.20615I$ $c = 1.224920 - 0.254488I$ $d = -0.88465 - 1.40950I$	$10.9899 + 13.3339I$	$2.78630 - 6.00559I$
$u = -0.50000 - 1.69717I$ $a = -0.622875 - 0.704751I$ $b = -0.18055 - 2.20615I$ $c = 1.224920 + 0.254488I$ $d = -0.88465 + 1.40950I$	$10.9899 - 13.3339I$	$2.78630 + 6.00559I$

II.

$$I_2^u = \langle -u^3 + u^2 + 2d - 3u - 1, c + 1, b + u, u^3 - u^2 + 2a + 5u - 1, u^4 + 4u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ \frac{1}{2}u^3 - \frac{1}{2}u^2 + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{5}{2}u + \frac{1}{2} \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{3}{2}u + \frac{1}{2} \\ \frac{1}{2}u^3 - \frac{1}{2}u^2 + \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{5}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^3 - \frac{1}{2}u^2 - \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{3}{2}u + \frac{3}{2} \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 - 3u - 1 \\ u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 + 2u \\ -\frac{3}{2}u^3 - \frac{3}{2}u^2 - \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^3 - 14u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^4 - u^3 + 16u + 16$
c_2, c_6	$u^4 - 3u^3 + 4u^2 - 4u + 4$
c_3, c_5, c_7 c_8, c_{12}	$u^4 + 3u^3 + 5u^2 + 3u + 2$
c_4, c_9	$u^4 + 4u^2 - 2u + 1$
c_{10}	$u^4 - 8u^3 + 18u^2 - 4u + 1$
c_{11}	$u^4 + u^3 + 11u^2 + 11u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^4 - y^3 + 64y^2 - 256y + 256$
c_2, c_6	$y^4 - y^3 + 16y + 16$
c_3, c_5, c_7 c_8, c_{12}	$y^4 + y^3 + 11y^2 + 11y + 4$
c_4, c_9	$y^4 + 8y^3 + 18y^2 + 4y + 1$
c_{10}	$y^4 - 28y^3 + 262y^2 + 20y + 1$
c_{11}	$y^4 + 21y^3 + 107y^2 - 33y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.264316 + 0.422125I$ $a = 1.04521 - 1.17351I$ $b = 0.264316 - 0.422125I$ $c = -1.00000$ $d = 0.219104 + 0.751390I$	$-3.71660 + 1.17563I$	$-0.79089 - 5.96277I$
$u = -0.264316 - 0.422125I$ $a = 1.04521 + 1.17351I$ $b = 0.264316 + 0.422125I$ $c = -1.00000$ $d = 0.219104 - 0.751390I$	$-3.71660 - 1.17563I$	$-0.79089 + 5.96277I$
$u = 0.26432 + 1.99036I$ $a = -0.545213 - 0.715953I$ $b = -0.26432 - 1.99036I$ $c = -1.00000$ $d = 1.28090 - 1.27441I$	$13.5862 - 4.7517I$	$4.79089 + 2.00586I$
$u = 0.26432 - 1.99036I$ $a = -0.545213 + 0.715953I$ $b = -0.26432 + 1.99036I$ $c = -1.00000$ $d = 1.28090 + 1.27441I$	$13.5862 + 4.7517I$	$4.79089 - 2.00586I$

$$\text{III. } I_3^u = \langle -u^3 + u^2 + 2d - 3u - 1, c + 1, -u^3 - u^2 + 2b - 5u - 5, -u^3 + u^2 + 2a - 5u + 3, u^4 + 4u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ \frac{1}{2}u^3 - \frac{1}{2}u^2 + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u^3 - \frac{1}{2}u^2 + \frac{5}{2}u - \frac{3}{2} \\ \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{5}{2}u + \frac{5}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{3}{2}u + \frac{1}{2} \\ \frac{1}{2}u^3 - \frac{1}{2}u^2 + \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^3 - \frac{1}{2}u^2 + \frac{5}{2}u - \frac{3}{2} \\ u^3 + 3u + 3 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{3}{2}u^3 - \frac{1}{2}u^2 + \frac{11}{2}u + \frac{5}{2} \\ -\frac{3}{2}u^3 + \frac{3}{2}u^2 - \frac{9}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 - u^2 + 3u - 2 \\ 3u + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 + 2u \\ -\frac{3}{2}u^3 - \frac{3}{2}u^2 - \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^3 - 14u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^4 + u^3 + 11u^2 + 11u + 4$
c_2, c_3, c_6 c_7, c_8	$u^4 + 3u^3 + 5u^2 + 3u + 2$
c_4, c_9	$u^4 + 4u^2 - 2u + 1$
c_5, c_{12}	$u^4 - 3u^3 + 4u^2 - 4u + 4$
c_{10}	$u^4 - 8u^3 + 18u^2 - 4u + 1$
c_{11}	$u^4 - u^3 + 16u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^4 + 21y^3 + 107y^2 - 33y + 16$
c_2, c_3, c_6 c_7, c_8	$y^4 + y^3 + 11y^2 + 11y + 4$
c_4, c_9	$y^4 + 8y^3 + 18y^2 + 4y + 1$
c_5, c_{12}	$y^4 - y^3 + 16y + 16$
c_{10}	$y^4 - 28y^3 + 262y^2 + 20y + 1$
c_{11}	$y^4 - y^3 + 64y^2 - 256y + 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.264316 + 0.422125I$ $a = -2.04521 + 1.17351I$ $b = 1.84646 + 0.95037I$ $c = -1.00000$ $d = 0.219104 + 0.751390I$	$-3.71660 + 1.17563I$	$-0.79089 - 5.96277I$
$u = -0.264316 - 0.422125I$ $a = -2.04521 - 1.17351I$ $b = 1.84646 - 0.95037I$ $c = -1.00000$ $d = 0.219104 - 0.751390I$	$-3.71660 - 1.17563I$	$-0.79089 + 5.96277I$
$u = 0.26432 + 1.99036I$ $a = -0.454787 + 0.715953I$ $b = -0.34646 + 1.76812I$ $c = -1.00000$ $d = 1.28090 - 1.27441I$	$13.5862 - 4.7517I$	$4.79089 + 2.00586I$
$u = 0.26432 - 1.99036I$ $a = -0.454787 - 0.715953I$ $b = -0.34646 - 1.76812I$ $c = -1.00000$ $d = 1.28090 + 1.27441I$	$13.5862 + 4.7517I$	$4.79089 - 2.00586I$

$$\text{IV. } I_4^u = \langle u^3 - u^2 + 2d + 5u + 1, 5u^3 - u^2 + 2c + 19u + 5, b + u, u^3 - u^2 + 2a + 5u - 1, u^4 + 4u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{5}{2}u^3 + \frac{1}{2}u^2 - \frac{19}{2}u - \frac{5}{2} \\ -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{5}{2}u + \frac{1}{2} \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 - 4 \\ -\frac{1}{2}u^3 - \frac{1}{2}u^2 - \frac{1}{2}u - \frac{3}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{1}{2}u^2 - \frac{5}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^3 - \frac{1}{2}u^2 - \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u^3 + \frac{1}{2}u^2 + \frac{3}{2}u + \frac{3}{2} \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^3 + u^2 - 7u - 2 \\ -u^2 - 3u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u^3 + \frac{3}{2}u^2 - \frac{1}{2}u + \frac{7}{2} \\ \frac{3}{2}u^3 - \frac{1}{2}u^2 - \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^3 - 14u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_{11}	$u^4 + u^3 + 11u^2 + 11u + 4$
c_2, c_5, c_6 c_{12}	$u^4 + 3u^3 + 5u^2 + 3u + 2$
c_3, c_7, c_8	$u^4 - 3u^3 + 4u^2 - 4u + 4$
c_4, c_9	$u^4 + 4u^2 - 2u + 1$
c_{10}	$u^4 - 8u^3 + 18u^2 - 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{11}	$y^4 + 21y^3 + 107y^2 - 33y + 16$
c_2, c_5, c_6 c_{12}	$y^4 + y^3 + 11y^2 + 11y + 4$
c_3, c_7, c_8	$y^4 - y^3 + 16y + 16$
c_4, c_9	$y^4 + 8y^3 + 18y^2 + 4y + 1$
c_{10}	$y^4 - 28y^3 + 262y^2 + 20y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.264316 + 0.422125I$ $a = 1.04521 - 1.17351I$ $b = 0.264316 - 0.422125I$ $c = -0.35023 - 4.15490I$ $d = 0.045213 - 1.173520I$	$-3.71660 + 1.17563I$	$-0.79089 - 5.96277I$
$u = -0.264316 - 0.422125I$ $a = 1.04521 + 1.17351I$ $b = 0.264316 + 0.422125I$ $c = -0.35023 + 4.15490I$ $d = 0.045213 + 1.173520I$	$-3.71660 - 1.17563I$	$-0.79089 + 5.96277I$
$u = 0.26432 + 1.99036I$ $a = -0.545213 - 0.715953I$ $b = -0.26432 - 1.99036I$ $c = 0.850232 + 0.286979I$ $d = -1.54521 - 0.71595I$	$13.5862 - 4.7517I$	$4.79089 + 2.00586I$
$u = 0.26432 - 1.99036I$ $a = -0.545213 + 0.715953I$ $b = -0.26432 + 1.99036I$ $c = 0.850232 - 0.286979I$ $d = -1.54521 + 0.71595I$	$13.5862 + 4.7517I$	$4.79089 - 2.00586I$

$$V. I_5^u = \langle d + 1, 2c - u - 1, b, a - 1, u^2 - u + 2 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}u + \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{3}{2}u - \frac{1}{2} \\ -3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u - 1 \\ u - 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_6, c_7, c_8	$(u - 1)^2$
c_4, c_5, c_9 c_{12}	$u^2 + u + 2$
c_{10}	$u^2 - 3u + 4$
c_{11}	$u^2 + 3u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_6, c_7, c_8	$(y - 1)^2$
c_4, c_5, c_9 c_{12}	$y^2 + 3y + 4$
c_{10}, c_{11}	$y^2 - y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.50000 + 1.32288I$ $a = 1.00000$ $b = 0$ $c = 0.750000 + 0.661438I$ $d = -1.00000$	1.64493	6.00000
$u = 0.50000 - 1.32288I$ $a = 1.00000$ $b = 0$ $c = 0.750000 - 0.661438I$ $d = -1.00000$	1.64493	6.00000

$$\text{VI. } I_6^u = \langle d + 1, 2c - u - 1, b - u + 1, 2a - u + 1, u^2 - u + 2 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{2}u + \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u + \frac{3}{2} \\ 2u - 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{3}{2}u - \frac{1}{2} \\ -3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u - 1 \\ u - 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^2 + 3u + 4$
c_2, c_4, c_6 c_9	$u^2 + u + 2$
c_3, c_5, c_7 c_8, c_{11}, c_{12}	$(u - 1)^2$
c_{10}	$u^2 - 3u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{10}	$y^2 - y + 16$
c_2, c_4, c_6 c_9	$y^2 + 3y + 4$
c_3, c_5, c_7 c_8, c_{11}, c_{12}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.50000 + 1.32288I$ $a = -0.250000 + 0.661438I$ $b = -0.50000 + 1.32288I$ $c = 0.750000 + 0.661438I$ $d = -1.00000$	1.64493	6.00000
$u = 0.50000 - 1.32288I$ $a = -0.250000 - 0.661438I$ $b = -0.50000 - 1.32288I$ $c = 0.750000 - 0.661438I$ $d = -1.00000$	1.64493	6.00000

$$\text{VII. } I_7^u = \langle d - u, c, b - u + 1, 2a - u + 1, u^2 - u + 2 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u + 1 \\ u + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u - 1 \\ u - 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_5 c_6, c_{11}, c_{12}	$(u - 1)^2$
c_3, c_4, c_7 c_8, c_9	$u^2 + u + 2$
c_{10}	$u^2 - 3u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5 c_6, c_{11}, c_{12}	$(y - 1)^2$
c_3, c_4, c_7 c_8, c_9	$y^2 + 3y + 4$
c_{10}	$y^2 - y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.50000 + 1.32288I$ $a = -0.250000 + 0.661438I$ $b = -0.50000 + 1.32288I$ $c = 0$ $d = 0.50000 + 1.32288I$	1.64493	6.00000
$u = 0.50000 - 1.32288I$ $a = -0.250000 - 0.661438I$ $b = -0.50000 - 1.32288I$ $c = 0$ $d = 0.50000 - 1.32288I$	1.64493	6.00000

VIII. $I_8^u = \langle d + 1, c, b, a - 1, u + 1 \rangle$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 6

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_2, c_3 c_4, c_5, c_6 c_7, c_8, c_9 c_{11}, c_{12}	$u - 1$
c_{10}	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	
c_4, c_5, c_6	$y - 1$
c_7, c_8, c_9	
c_{10}, c_{11}, c_{12}	

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_{\mathfrak{g}}^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.00000$		
$b = 0$	1.64493	6.00000
$c = 0$		
$d = -1.00000$		

$$\text{IX. } I_9^u = \langle d, c - u, b - u, a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u + 1 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_{10}, c_{11}	$(u - 1)^2$
c_2, c_4, c_5 c_6, c_9, c_{12}	$u^2 + 1$
c_3, c_7, c_8	u^2

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{10}, c_{11}	$(y - 1)^2$
c_2, c_4, c_5 c_6, c_9, c_{12}	$(y + 1)^2$
c_3, c_7, c_8	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_9^u		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.000000I$	-1.64493	4.00000
$a =$	1.00000		
$b =$	$1.000000I$		
$c =$	$1.000000I$		
$d =$	0		
$u =$	$-1.000000I$	-1.64493	4.00000
$a =$	1.00000		
$b =$	$-1.000000I$		
$c =$	$-1.000000I$		
$d =$	0		

$$\mathbf{X. } I_{10}^u = \langle d - u, c - 1, b + 1, a, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u + 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_{10}	$(u - 1)^2$
c_2, c_3, c_4 c_6, c_7, c_8 c_9	$u^2 + 1$
c_5, c_{11}, c_{12}	u^2

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{10}	$(y - 1)^2$
c_2, c_3, c_4 c_6, c_7, c_8 c_9	$(y + 1)^2$
c_5, c_{11}, c_{12}	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_{10}^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = 0$ $b = -1.00000$ $c = 1.00000$ $d = 1.000000I$	-1.64493	4.00000
$u = -1.000000I$ $a = 0$ $b = -1.00000$ $c = 1.00000$ $d = -1.000000I$	-1.64493	4.00000

$$\text{XI. } I_{11}^u = \langle d - u, c - 1, b - u, a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u + 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 4

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_6	u^2
c_3, c_4, c_5 c_7, c_8, c_9 c_{12}	$u^2 + 1$
c_{10}, c_{11}	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6	y^2
c_3, c_4, c_5 c_7, c_8, c_9 c_{12}	$(y + 1)^2$
c_{10}, c_{11}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_{11}^u		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.000000I$	-1.64493	4.00000
$a =$	1.00000		
$b =$	$1.000000I$		
$c =$	1.00000		
$d =$	$1.000000I$		
$u =$	$-1.000000I$	-1.64493	4.00000
$a =$	1.00000		
$b =$	$-1.000000I$		
$c =$	1.00000		
$d =$	$-1.000000I$		

$$\text{XII. } I_{12}^u = \langle d - u, cb - u + 1, a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} c \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} cu + 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ bu \end{pmatrix}$$

$$a_2 = \begin{pmatrix} c + 1 \\ b + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -cu \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -2

(iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.

(v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to I_{12}^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$		
$b = \dots$	-3.28987	-2.00000
$c = \dots$		
$d = \dots$		

$$\text{XIII. } I_1^v = \langle a, d - v, -av + c + 1, b - 1, v^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ v \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -v + 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ v + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -v \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -8

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_{11}	$(u - 1)^2$
c_2, c_3, c_5 c_6, c_7, c_8 c_{12}	$u^2 + 1$
c_4, c_9, c_{10}	u^2

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{11}	$(y - 1)^2$
c_2, c_3, c_5 c_6, c_7, c_8 c_{12}	$(y + 1)^2$
c_4, c_9, c_{10}	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.000000I$ $a = 0$ $b = 1.00000$ $c = -1.00000$ $d = 1.000000I$	-4.93480	-8.00000
$v = -1.000000I$ $a = 0$ $b = 1.00000$ $c = -1.00000$ $d = -1.000000I$	-4.93480	-8.00000

XIV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_{11}	$u^2(u-1)^{11}(u^2+3u+4)(u^4-u^3+16u+16)$ $\cdot ((u^4+u^3+11u^2+11u+4)^2)(u^6+2u^5+\dots+6u+1)$
c_2, c_3, c_5 c_6, c_7, c_8 c_{12}	$u^2(u-1)^5(u^2+1)^3(u^2+u+2)(u^4-3u^3+4u^2-4u+4)$ $\cdot (u^4+3u^3+5u^2+3u+2)^2(u^6+u^4+2u^3+5u^2-2u+1)$
c_4, c_9	$u^2(u-1)(u^2+1)^3(u^2+u+2)^3(u^4+4u^2-2u+1)^3$ $\cdot (u^6-3u^5+7u^4-9u^3+8u^2-4u+4)$
c_{10}	$u^2(u-1)^6(u+1)(u^2-3u+4)^3(u^4-8u^3+18u^2-4u+1)^3$ $\cdot (u^6-5u^5+11u^4-15u^3+48u^2-48u+16)$

XV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_{11}	$y^2(y-1)^{11}(y^2-y+16)(y^4-y^3+64y^2-256y+256)$ $\cdot (y^4+21y^3+107y^2-33y+16)^2$ $\cdot (y^6+18y^5+159y^4+684y^3+1151y^2+34y+1)$
c_2, c_3, c_5 c_6, c_7, c_8 c_{12}	$y^2(y-1)^5(y+1)^6(y^2+3y+4)(y^4-y^3+16y+16)$ $\cdot ((y^4+y^3+11y^2+11y+4)^2)(y^6+2y^5+\dots+6y+1)$
c_4, c_9	$y^2(y-1)(y+1)^6(y^2+3y+4)^3(y^4+8y^3+18y^2+4y+1)^3$ $\cdot (y^6+5y^5+11y^4+15y^3+48y^2+48y+16)$
c_{10}	$y^2(y-1)^7(y^2-y+16)^3(y^4-28y^3+262y^2+20y+1)^3$ $\cdot (y^6-3y^5+67y^4+383y^3+1216y^2-768y+256)$