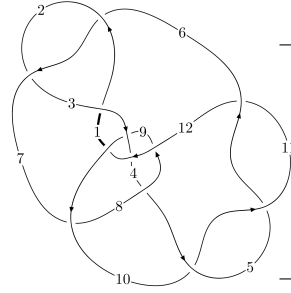
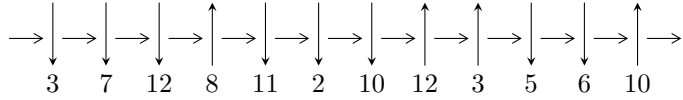


12n<sub>0559</sub> (K12n<sub>0559</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5, 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 6 \xrightarrow{c_{11}} 12 \xrightarrow{c_{12}} 1, 3 \xrightarrow{c_1} 2 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_4} 4 \xrightarrow{c_7} 7 \rightsquigarrow c_2, c_3, c_6$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.74895 \times 10^{16} u^{37} + 2.53324 \times 10^{16} u^{36} + \dots + 4.11981 \times 10^{16} b - 1.42189 \times 10^{17}, \\ -1.62383 \times 10^{17} u^{37} + 1.68076 \times 10^{17} u^{36} + \dots + 8.23961 \times 10^{16} a - 1.06430 \times 10^{18}, u^{38} - u^{37} + \dots + 7u - \\ I_2^u = \langle -u^5 + 2u^3 + b - u, -u^5 - 2u^3 a + 2u^4 + u^2 a + 2u^3 + a^2 + 2au - 3u^2 - a - u, u^6 - 3u^4 + 2u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 50 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2.75 \times 10^{16} u^{37} + 2.53 \times 10^{16} u^{36} + \dots + 4.12 \times 10^{16} b - 1.42 \times 10^{17}, -1.62 \times 10^{17} u^{37} + 1.68 \times 10^{17} u^{36} + \dots + 8.24 \times 10^{16} a - 1.06 \times 10^{18}, u^{38} - u^{37} + \dots + 7u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 + u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.97076u^{37} - 2.03985u^{36} + \dots - 21.0299u + 12.9168 \\ 0.667251u^{37} - 0.614893u^{36} + \dots - 9.05648u + 3.45135 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2.02554u^{37} - 1.32040u^{36} + \dots - 28.4281u + 5.80356 \\ -0.659268u^{37} + 0.328623u^{36} + \dots + 6.36982u - 3.31602 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3.06399u^{37} - 2.12216u^{36} + \dots - 40.8760u + 12.2142 \\ 0.0456579u^{37} + 0.419048u^{36} + \dots - 0.102231u - 1.50203 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 3.45135u^{37} - 2.78410u^{36} + \dots - 45.4240u + 15.1030 \\ 0.121448u^{37} + 0.408171u^{36} + \dots - 0.340899u - 1.30351 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1.50203u^{37} - 1.54769u^{36} + \dots - 13.7795u + 10.6164 \\ 0.477120u^{37} - 0.620718u^{36} + \dots - 7.41211u + 3.01833 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3.57280u^{37} - 2.37593u^{36} + \dots - 45.7649u + 13.7995 \\ 0.121448u^{37} + 0.408171u^{36} + \dots - 0.340899u - 1.30351 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{106268405583162365}{41198072891018797} u^{37} + \frac{98605685292409883}{41198072891018797} u^{36} + \dots + \frac{62037259094258982}{3169082530078369} u - \frac{858011531178729634}{41198072891018797}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{38} + 25u^{37} + \dots + 101u + 25$
$c_2, c_6$	$u^{38} - u^{37} + \dots + 11u - 5$
$c_3$	$u^{38} - 5u^{37} + \dots - 3u + 1$
$c_4, c_9$	$u^{38} - u^{37} + \dots + 23u - 1$
$c_5, c_{10}, c_{11}$	$u^{38} - u^{37} + \dots + 7u - 1$
$c_7$	$u^{38} - 5u^{37} + \dots - 40603u + 13213$
$c_8$	$u^{38} - 3u^{37} + \dots - u + 5$
$c_{12}$	$u^{38} + 3u^{37} + \dots - 17u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{38} - 17y^{37} + \dots - 41901y + 625$
$c_2, c_6$	$y^{38} - 25y^{37} + \dots - 101y + 25$
$c_3$	$y^{38} - 65y^{37} + \dots + 205y + 1$
$c_4, c_9$	$y^{38} + 53y^{37} + \dots - 195y + 1$
$c_5, c_{10}, c_{11}$	$y^{38} - 39y^{37} + \dots - 39y + 1$
$c_7$	$y^{38} - 49y^{37} + \dots - 3299858645y + 174583369$
$c_8$	$y^{38} + 59y^{37} + \dots - 201y + 25$
$c_{12}$	$y^{38} + 57y^{37} + \dots - 183y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.644745 + 0.752188I$ $a = 0.801740 - 0.434056I$ $b = 0.11351 - 1.82495I$	$-13.38780 - 2.90157I$	$-9.03118 + 0.30817I$
$u = -0.644745 - 0.752188I$ $a = 0.801740 + 0.434056I$ $b = 0.11351 + 1.82495I$	$-13.38780 + 2.90157I$	$-9.03118 - 0.30817I$
$u = -0.478467 + 0.830062I$ $a = 1.281060 - 0.364339I$ $b = -0.25094 - 1.78475I$	$-12.8639 + 8.1852I$	$-8.10422 - 5.25532I$
$u = -0.478467 - 0.830062I$ $a = 1.281060 + 0.364339I$ $b = -0.25094 + 1.78475I$	$-12.8639 - 8.1852I$	$-8.10422 + 5.25532I$
$u = 0.531918 + 0.751960I$ $a = -1.088960 - 0.565285I$ $b = 0.07319 - 1.72540I$	$-8.90525 - 2.50092I$	$-5.86634 + 2.56670I$
$u = 0.531918 - 0.751960I$ $a = -1.088960 + 0.565285I$ $b = 0.07319 + 1.72540I$	$-8.90525 + 2.50092I$	$-5.86634 - 2.56670I$
$u = 0.547239 + 0.502053I$ $a = 1.267080 + 0.591264I$ $b = -0.676584 + 0.904931I$	$-3.49790 - 4.12703I$	$-9.00602 + 6.42337I$
$u = 0.547239 - 0.502053I$ $a = 1.267080 - 0.591264I$ $b = -0.676584 - 0.904931I$	$-3.49790 + 4.12703I$	$-9.00602 - 6.42337I$
$u = 0.219443 + 0.699987I$ $a = -0.037483 - 0.669697I$ $b = 0.415341 + 1.142040I$	$-2.33417 + 0.42500I$	$-7.90152 + 0.53407I$
$u = 0.219443 - 0.699987I$ $a = -0.037483 + 0.669697I$ $b = 0.415341 - 1.142040I$	$-2.33417 - 0.42500I$	$-7.90152 - 0.53407I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.263470 + 0.115418I$ $a = 0.155909 + 0.360863I$ $b = -0.480768 + 0.017588I$	$-2.25857 + 0.57001I$	$-2.81061 + 0.I$
$u = -1.263470 - 0.115418I$ $a = 0.155909 - 0.360863I$ $b = -0.480768 - 0.017588I$	$-2.25857 - 0.57001I$	$-2.81061 + 0.I$
$u = 1.280750 + 0.149729I$ $a = 0.851613 + 1.095860I$ $b = -0.202776 + 1.036480I$	$-5.14131 - 2.83687I$	$-11.03494 + 3.31873I$
$u = 1.280750 - 0.149729I$ $a = 0.851613 - 1.095860I$ $b = -0.202776 - 1.036480I$	$-5.14131 + 2.83687I$	$-11.03494 - 3.31873I$
$u = 1.300970 + 0.201402I$ $a = -0.050909 + 0.890884I$ $b = 0.1131480 + 0.0174250I$	$-3.00626 - 4.83883I$	$-4.00000 + 6.35067I$
$u = 1.300970 - 0.201402I$ $a = -0.050909 - 0.890884I$ $b = 0.1131480 - 0.0174250I$	$-3.00626 + 4.83883I$	$-4.00000 - 6.35067I$
$u = -0.061251 + 0.594784I$ $a = -0.417558 + 1.055680I$ $b = 0.192238 - 0.029719I$	$1.20430 + 1.95319I$	$2.65095 - 4.43332I$
$u = -0.061251 - 0.594784I$ $a = -0.417558 - 1.055680I$ $b = 0.192238 + 0.029719I$	$1.20430 - 1.95319I$	$2.65095 + 4.43332I$
$u = -1.365440 + 0.327458I$ $a = -0.843246 + 0.605113I$ $b = -0.369076 + 1.327770I$	$-7.31262 + 3.36514I$	0
$u = -1.365440 - 0.327458I$ $a = -0.843246 - 0.605113I$ $b = -0.369076 - 1.327770I$	$-7.31262 - 3.36514I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.408360 + 0.089637I$ $a = 0.48516 + 1.53710I$ $b = -0.507713 + 1.049310I$	$-5.54125 - 2.92041I$	0
$u = 1.408360 - 0.089637I$ $a = 0.48516 - 1.53710I$ $b = -0.507713 - 1.049310I$	$-5.54125 + 2.92041I$	0
$u = -1.45723 + 0.02361I$ $a = -0.27899 - 2.06538I$ $b = 0.43890 - 1.34446I$	$-7.45168 + 2.35722I$	0
$u = -1.45723 - 0.02361I$ $a = -0.27899 + 2.06538I$ $b = 0.43890 + 1.34446I$	$-7.45168 - 2.35722I$	0
$u = -0.528921$ $a = 0.210332$ $b = -0.547836$	$-1.28259$	$-8.18110$
$u = 1.48529$ $a = 0.507416$ $b = 1.07105$	$-7.77665$	0
$u = -0.269231 + 0.414079I$ $a = -1.058820 + 0.163044I$ $b = 0.294017 + 0.615100I$	$-0.254814 + 1.145580I$	$-3.55444 - 5.99940I$
$u = -0.269231 - 0.414079I$ $a = -1.058820 - 0.163044I$ $b = 0.294017 - 0.615100I$	$-0.254814 - 1.145580I$	$-3.55444 + 5.99940I$
$u = -1.51707 + 0.17151I$ $a = -0.106102 + 1.396060I$ $b = 0.998525 + 0.969650I$	$-10.27140 + 6.63615I$	0
$u = -1.51707 - 0.17151I$ $a = -0.106102 - 1.396060I$ $b = 0.998525 - 0.969650I$	$-10.27140 - 6.63615I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.52395 + 0.30793I$ $a = -1.14837 - 1.87775I$ $b = 0.37644 - 1.80124I$	$-19.3511 - 12.3559I$	0
$u = 1.52395 - 0.30793I$ $a = -1.14837 + 1.87775I$ $b = 0.37644 + 1.80124I$	$-19.3511 + 12.3559I$	0
$u = -1.53293 + 0.26223I$ $a = 1.00320 - 2.03551I$ $b = -0.19546 - 1.80459I$	$-15.6450 + 6.2232I$	0
$u = -1.53293 - 0.26223I$ $a = 1.00320 + 2.03551I$ $b = -0.19546 + 1.80459I$	$-15.6450 - 6.2232I$	0
$u = 1.58427 + 0.22493I$ $a = -0.76018 - 1.95860I$ $b = 0.01038 - 1.96358I$	$18.6754 - 0.6900I$	0
$u = 1.58427 - 0.22493I$ $a = -0.76018 + 1.95860I$ $b = 0.01038 + 1.96358I$	$18.6754 + 0.6900I$	0
$u = 0.214741 + 0.039322I$ $a = 4.08599 - 2.69357I$ $b = -0.103979 - 1.039010I$	$-1.75783 - 2.05331I$	$-11.26159 + 3.08731I$
$u = 0.214741 - 0.039322I$ $a = 4.08599 + 2.69357I$ $b = -0.103979 + 1.039010I$	$-1.75783 + 2.05331I$	$-11.26159 - 3.08731I$



$$\text{II. } I_2^u = \langle -u^5 + 2u^3 + b - u, -u^5 + 2u^4 + \dots + a^2 - a, u^6 - 3u^4 + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 + u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ u^5 - 2u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 - au + u^2 + a + u \\ -u^3a + au + u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5a - 2u^3a + au + 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - 2u^2 + 1 \\ -u^4 + au + u^2 - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^5 + 3u^3 - 2u \\ -u^4a + 2u^5 + u^2a - 4u^3 + a + 2u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} au - u^2 \\ -u^4 + au + u^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u^4a + 4u^4 - 8u^2a - 8u^2 + 4u - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^6$
$c_2, c_6, c_8$	$(u^4 - u^2 + 1)^3$
$c_3$	$u^{12} + 6u^{11} + \dots - 2u + 1$
$c_4, c_9$	$(u^2 + 1)^6$
$c_5, c_{10}, c_{11}$	$(u^6 - 3u^4 + 2u^2 + 1)^2$
$c_7$	$u^{12} - 12u^{11} + \dots - 2u + 1$
$c_{12}$	$(u^3 + u^2 - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)^6$
$c_2, c_6, c_8$	$(y^2 - y + 1)^6$
$c_3$	$y^{12} + 10y^{11} + \dots - 40y + 1$
$c_4, c_9$	$(y + 1)^{12}$
$c_5, c_{10}, c_{11}$	$(y^3 - 3y^2 + 2y + 1)^4$
$c_7$	$y^{12} - 14y^{11} + \dots + 14y + 1$
$c_{12}$	$(y^3 - y^2 + 2y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.307140 + 0.215080I$ $a = 0.900631 + 0.022679I$ $b = 1.000000I$	$-4.66906 - 4.85801I$	$-9.50976 + 6.44355I$
$u = 1.307140 + 0.215080I$ $a = -0.073266 + 1.169920I$ $b = 1.000000I$	$-4.66906 - 0.79824I$	$-9.50976 - 0.48465I$
$u = 1.307140 - 0.215080I$ $a = 0.900631 - 0.022679I$ $b = -1.000000I$	$-4.66906 + 4.85801I$	$-9.50976 - 6.44355I$
$u = 1.307140 - 0.215080I$ $a = -0.073266 - 1.169920I$ $b = -1.000000I$	$-4.66906 + 0.79824I$	$-9.50976 + 0.48465I$
$u = -1.307140 + 0.215080I$ $a = -1.56299 + 0.58496I$ $b = 1.000000I$	$-4.66906 + 0.79824I$	$-9.50976 + 0.48465I$
$u = -1.307140 + 0.215080I$ $a = -0.58909 + 1.73220I$ $b = 1.000000I$	$-4.66906 + 4.85801I$	$-9.50976 - 6.44355I$
$u = -1.307140 - 0.215080I$ $a = -1.56299 - 0.58496I$ $b = -1.000000I$	$-4.66906 - 0.79824I$	$-9.50976 - 0.48465I$
$u = -1.307140 - 0.215080I$ $a = -0.58909 - 1.73220I$ $b = -1.000000I$	$-4.66906 - 4.85801I$	$-9.50976 + 6.44355I$
$u = 0.569840I$ $a = 0.662359 + 0.392362I$ $b = 1.000000I$	$-0.53148 - 2.02988I$	$-2.98049 + 3.46410I$
$u = 0.569840I$ $a = 0.66236 - 1.90212I$ $b = 1.000000I$	$-0.53148 + 2.02988I$	$-2.98049 - 3.46410I$

Solutions to $I_2^u$		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$-0.569840I$		
$a =$	$0.662359 - 0.392362I$	$-0.53148 + 2.02988I$	$-2.98049 - 3.46410I$
$b =$	$-1.000000I$		
$u =$	$-0.569840I$		
$a =$	$0.66236 + 1.90212I$	$-0.53148 - 2.02988I$	$-2.98049 + 3.46410I$
$b =$	$-1.000000I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^6)(u^{38} + 25u^{37} + \dots + 101u + 25)$
$c_2, c_6$	$((u^4 - u^2 + 1)^3)(u^{38} - u^{37} + \dots + 11u - 5)$
$c_3$	$(u^{12} + 6u^{11} + \dots - 2u + 1)(u^{38} - 5u^{37} + \dots - 3u + 1)$
$c_4, c_9$	$((u^2 + 1)^6)(u^{38} - u^{37} + \dots + 23u - 1)$
$c_5, c_{10}, c_{11}$	$((u^6 - 3u^4 + 2u^2 + 1)^2)(u^{38} - u^{37} + \dots + 7u - 1)$
$c_7$	$(u^{12} - 12u^{11} + \dots - 2u + 1)(u^{38} - 5u^{37} + \dots - 40603u + 13213)$
$c_8$	$((u^4 - u^2 + 1)^3)(u^{38} - 3u^{37} + \dots - u + 5)$
$c_{12}$	$((u^3 + u^2 - 1)^4)(u^{38} + 3u^{37} + \dots - 17u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^6)(y^{38} - 17y^{37} + \dots - 41901y + 625)$
$c_2, c_6$	$((y^2 - y + 1)^6)(y^{38} - 25y^{37} + \dots - 101y + 25)$
$c_3$	$(y^{12} + 10y^{11} + \dots - 40y + 1)(y^{38} - 65y^{37} + \dots + 205y + 1)$
$c_4, c_9$	$((y + 1)^{12})(y^{38} + 53y^{37} + \dots - 195y + 1)$
$c_5, c_{10}, c_{11}$	$((y^3 - 3y^2 + 2y + 1)^4)(y^{38} - 39y^{37} + \dots - 39y + 1)$
$c_7$	$(y^{12} - 14y^{11} + \dots + 14y + 1)$ $\cdot (y^{38} - 49y^{37} + \dots - 3299858645y + 174583369)$
$c_8$	$((y^2 - y + 1)^6)(y^{38} + 59y^{37} + \dots - 201y + 25)$
$c_{12}$	$((y^3 - y^2 + 2y - 1)^4)(y^{38} + 57y^{37} + \dots - 183y + 1)$