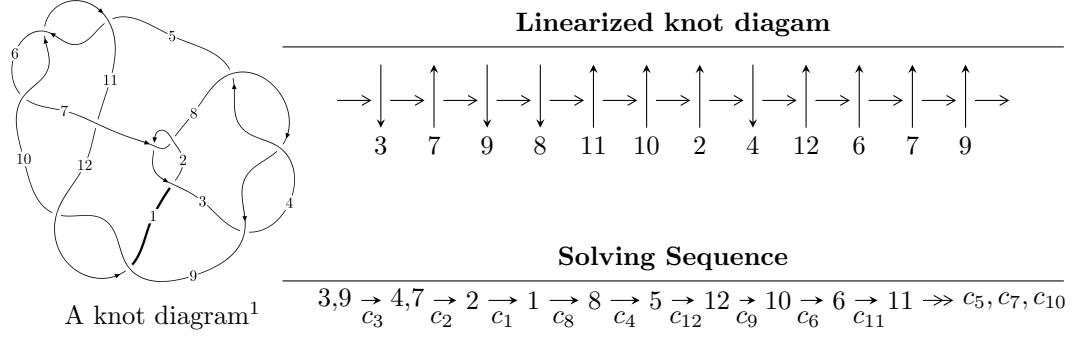


$12n_{0566}$  ( $K12n_{0566}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -4.65742 \times 10^{21} u^{31} - 2.20023 \times 10^{22} u^{30} + \dots + 9.36708 \times 10^{23} b + 5.12230 \times 10^{23}, \\
 &\quad 2.94856 \times 10^{25} u^{31} - 3.10386 \times 10^{25} u^{30} + \dots + 2.99747 \times 10^{25} a - 2.87196 \times 10^{25}, u^{32} - u^{31} + \dots - 2u + 1 \rangle \\
 I_2^u &= \langle b - u, a^5 - a^4 + 2a^3 - a^2 + a - 1, u^2 + 1 \rangle \\
 I_3^u &= \langle b - u, a, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle \\
 I_4^u &= \langle b - u, a, u^3 + u^2 + 2u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 51 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**I.**

$$I_1^u = \langle -4.66 \times 10^{21} u^{31} - 2.20 \times 10^{22} u^{30} + \dots + 9.37 \times 10^{23} b + 5.12 \times 10^{23}, 2.95 \times 10^{25} u^{31} - 3.10 \times 10^{25} u^{30} + \dots + 3.00 \times 10^{25} a - 2.87 \times 10^{25}, u^{32} - u^{31} + \dots - 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.983683u^{31} + 1.03549u^{30} + \dots + 42.1633u + 0.958130 \\ 0.00497211u^{31} + 0.0234890u^{30} + \dots + 1.12532u - 0.546841 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.495029u^{31} - 0.483684u^{30} + \dots + 26.1222u - 0.952046 \\ -0.0284611u^{31} + 0.0288036u^{30} + \dots + 0.536896u - 0.995028 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.466568u^{31} - 0.454881u^{30} + \dots + 26.6591u - 1.94707 \\ -0.0284611u^{31} + 0.0288036u^{30} + \dots + 0.536896u - 0.995028 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.466568u^{31} - 0.454881u^{30} + \dots + 26.6591u - 1.94707 \\ -0.0000739509u^{31} + 0.00179294u^{30} + \dots + 0.0937032u - 1.00672 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.935244u^{31} - 1.05640u^{30} + \dots - 35.9185u + 0.318643 \\ -0.00328364u^{31} - 0.0312396u^{30} + \dots + 1.93055u + 0.535840 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.357364u^{31} + 0.452611u^{30} + \dots - 8.86369u + 3.30364 \\ 0.136131u^{31} - 0.134930u^{30} + \dots - 6.56253u + 0.588091 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.465451u^{31} - 0.514663u^{30} + \dots - 8.17487u + 4.78562 \\ 0.151172u^{31} - 0.159734u^{30} + \dots - 2.72954u - 0.0680096 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $\frac{1674544166583428940712685}{3746832618160827210734692}u^{31} - \frac{3228763469657253763874131}{7493665236321654421469384}u^{30} + \dots + \frac{115090649984726751416336801}{7493665236321654421469384}u - \frac{4624345191860318935353055}{936708154540206802683673}$

**(iv) u-Polynomials at the component**

| Crossings          | u-Polynomials at each crossing           |
|--------------------|--|
| $c_1$              | $u^{32} + 3u^{31} + \cdots - 20u + 1$    |
| $c_2, c_7$         | $u^{32} + u^{31} + \cdots - 10u^2 + 1$   |
| $c_3, c_4, c_8$    | $u^{32} + u^{31} + \cdots + 2u + 1$      |
| $c_5, c_6, c_{10}$ | $u^{32} + 2u^{31} + \cdots + 5u + 2$     |
| $c_9, c_{12}$      | $u^{32} + 8u^{31} + \cdots + 837u + 136$ |
| $c_{11}$           | $u^{32} - 2u^{31} + \cdots - 96u + 16$   |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing             |
|--------------------|--|
| $c_1$              | $y^{32} + 63y^{31} + \cdots - 48y + 1$         |
| $c_2, c_7$         | $y^{32} + 3y^{31} + \cdots - 20y + 1$          |
| $c_3, c_4, c_8$    | $y^{32} + 47y^{31} + \cdots - 84y + 1$         |
| $c_5, c_6, c_{10}$ | $y^{32} + 28y^{31} + \cdots + 19y + 4$         |
| $c_9, c_{12}$      | $y^{32} + 44y^{30} + \cdots - 169353y + 18496$ |
| $c_{11}$           | $y^{32} - 4y^{31} + \cdots - 256y + 256$       |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.149637 + 1.036980I$ |                                       |                      |
| $a = -0.417547 + 0.954803I$ | $1.43807 - 1.50420I$                  | $9.22727 + 3.53831I$ |
| $b = 0.302187 - 0.006644I$  |                                       |                      |
| $u = -0.149637 - 1.036980I$ |                                       |                      |
| $a = -0.417547 - 0.954803I$ | $1.43807 + 1.50420I$                  | $9.22727 - 3.53831I$ |
| $b = 0.302187 + 0.006644I$  |                                       |                      |
| $u = 0.570569 + 0.926273I$  |                                       |                      |
| $a = 0.652139 + 0.672144I$  | $0.356823 - 1.078380I$                | $5.98174 + 1.89501I$ |
| $b = -0.729100 + 0.429975I$ |                                       |                      |
| $u = 0.570569 - 0.926273I$  |                                       |                      |
| $a = 0.652139 - 0.672144I$  | $0.356823 + 1.078380I$                | $5.98174 - 1.89501I$ |
| $b = -0.729100 - 0.429975I$ |                                       |                      |
| $u = -0.759558 + 0.797956I$ |                                       |                      |
| $a = -0.669157 + 0.706117I$ | $2.84076 + 4.52561I$                  | $7.98035 - 6.47723I$ |
| $b = 0.806103 + 0.667276I$  |                                       |                      |
| $u = -0.759558 - 0.797956I$ |                                       |                      |
| $a = -0.669157 - 0.706117I$ | $2.84076 - 4.52561I$                  | $7.98035 + 6.47723I$ |
| $b = 0.806103 - 0.667276I$  |                                       |                      |
| $u = 0.080786 + 1.113860I$  |                                       |                      |
| $a = 0.450290 + 1.273100I$  | $-4.20210 + 4.53860I$                 | $4.95050 - 3.52289I$ |
| $b = -0.240058 - 0.218923I$ |                                       |                      |
| $u = 0.080786 - 1.113860I$  |                                       |                      |
| $a = 0.450290 - 1.273100I$  | $-4.20210 - 4.53860I$                 | $4.95050 + 3.52289I$ |
| $b = -0.240058 + 0.218923I$ |                                       |                      |
| $u = 0.856979 + 0.733531I$  |                                       |                      |
| $a = 0.658177 + 0.744370I$  | $-2.06044 - 8.15993I$                 | $2.47068 + 7.37481I$ |
| $b = -0.839448 + 0.780469I$ |                                       |                      |
| $u = 0.856979 - 0.733531I$  |                                       |                      |
| $a = 0.658177 - 0.744370I$  | $-2.06044 + 8.15993I$                 | $2.47068 - 7.37481I$ |
| $b = -0.839448 - 0.780469I$ |                                       |                      |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.388206 + 0.750499I$  |                                       |                       |
| $a = 0.618021 + 0.553690I$  | $0.37663 - 1.40948I$                  | $4.16499 + 4.71779I$  |
| $b = -0.445761 + 0.493038I$ |                                       |                       |
| $u = 0.388206 - 0.750499I$  |                                       |                       |
| $a = 0.618021 - 0.553690I$  | $0.37663 + 1.40948I$                  | $4.16499 - 4.71779I$  |
| $b = -0.445761 - 0.493038I$ |                                       |                       |
| $u = -0.564144 + 0.368266I$ |                                       |                       |
| $a = -1.072100 + 0.757048I$ | $-4.95649 + 1.03511I$                 | $-2.62837 - 3.37474I$ |
| $b = 0.426872 + 0.891946I$  |                                       |                       |
| $u = -0.564144 - 0.368266I$ |                                       |                       |
| $a = -1.072100 - 0.757048I$ | $-4.95649 - 1.03511I$                 | $-2.62837 + 3.37474I$ |
| $b = 0.426872 - 0.891946I$  |                                       |                       |
| $u = -0.14043 + 1.61047I$   |                                       |                       |
| $a = 1.344160 + 0.225189I$  | $1.96786 + 3.39058I$                  | 0                     |
| $b = -0.909776 - 0.978319I$ |                                       |                       |
| $u = -0.14043 - 1.61047I$   |                                       |                       |
| $a = 1.344160 - 0.225189I$  | $1.96786 - 3.39058I$                  | 0                     |
| $b = -0.909776 + 0.978319I$ |                                       |                       |
| $u = 0.31474 + 1.69085I$    |                                       |                       |
| $a = -1.283680 - 0.037904I$ | $6.02211 - 12.78960I$                 | 0                     |
| $b = 0.93918 - 1.20942I$    |                                       |                       |
| $u = 0.31474 - 1.69085I$    |                                       |                       |
| $a = -1.283680 + 0.037904I$ | $6.02211 + 12.78960I$                 | 0                     |
| $b = 0.93918 + 1.20942I$    |                                       |                       |
| $u = 0.20411 + 1.72625I$    |                                       |                       |
| $a = -1.226140 + 0.091965I$ | $9.50782 - 4.34458I$                  | 0                     |
| $b = 1.02007 - 1.09862I$    |                                       |                       |
| $u = 0.20411 - 1.72625I$    |                                       |                       |
| $a = -1.226140 - 0.091965I$ | $9.50782 + 4.34458I$                  | 0                     |
| $b = 1.02007 + 1.09862I$    |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.27493 + 1.71725I$   |                                       |                       |
| $a = 1.249820 + 0.010579I$  | $11.3763 + 8.7540I$                   | 0                     |
| $b = -0.98277 - 1.17471I$   |                                       |                       |
| $u = -0.27493 - 1.71725I$   |                                       |                       |
| $a = 1.249820 - 0.010579I$  | $11.3763 - 8.7540I$                   | 0                     |
| $b = -0.98277 + 1.17471I$   |                                       |                       |
| $u = 0.08047 + 1.76969I$    |                                       |                       |
| $a = -1.133210 + 0.199889I$ | $9.94630 - 3.44071I$                  | 0                     |
| $b = 1.12271 - 0.97669I$    |                                       |                       |
| $u = 0.08047 - 1.76969I$    |                                       |                       |
| $a = -1.133210 - 0.199889I$ | $9.94630 + 3.44071I$                  | 0                     |
| $b = 1.12271 + 0.97669I$    |                                       |                       |
| $u = -0.07166 + 1.77723I$   |                                       |                       |
| $a = -1.040780 + 0.308237I$ | $7.36926 + 5.04799I$                  | 0                     |
| $b = 1.20703 - 0.80705I$    |                                       |                       |
| $u = -0.07166 - 1.77723I$   |                                       |                       |
| $a = -1.040780 - 0.308237I$ | $7.36926 - 5.04799I$                  | 0                     |
| $b = 1.20703 + 0.80705I$    |                                       |                       |
| $u = 0.00485 + 1.78607I$    |                                       |                       |
| $a = 1.074930 + 0.259134I$  | $12.35040 - 0.91754I$                 | 0                     |
| $b = -1.18249 - 0.88752I$   |                                       |                       |
| $u = 0.00485 - 1.78607I$    |                                       |                       |
| $a = 1.074930 - 0.259134I$  | $12.35040 + 0.91754I$                 | 0                     |
| $b = -1.18249 + 0.88752I$   |                                       |                       |
| $u = -0.156144 + 0.076843I$ |                                       |                       |
| $a = -4.97166 - 4.58572I$   | $-7.55319 - 4.33239I$                 | $-6.63531 + 3.69864I$ |
| $b = 0.069135 - 1.045370I$  |                                       |                       |
| $u = -0.156144 - 0.076843I$ |                                       |                       |
| $a = -4.97166 + 4.58572I$   | $-7.55319 + 4.33239I$                 | $-6.63531 - 3.69864I$ |
| $b = 0.069135 + 1.045370I$  |                                       |                       |

| Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = 0.1157890 + 0.0692134I$ |                                       |                       |
| $a = 6.26675 - 1.88119I$     | $-2.01181 - 1.57269I$                 | $-2.90508 + 4.76814I$ |
| $b = -0.063886 + 0.968637I$  |                                       |                       |
| $u = 0.1157890 - 0.0692134I$ |                                       |                       |
| $a = 6.26675 + 1.88119I$     | $-2.01181 + 1.57269I$                 | $-2.90508 - 4.76814I$ |
| $b = -0.063886 - 0.968637I$  |                                       |                       |

$$\text{II. } I_2^u = \langle b - u, a^5 - a^4 + 2a^3 - a^2 + a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} au + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} au \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} au \\ -au - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^2u \\ a^2u + a + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^4 - a^3 + a^2 + 1 \\ a^4u - a^4 + a^2u - a^2 + u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3u + au \\ -a^2 - au - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a^3 - 4a^2 + 4a$

**(iv) u-Polynomials at the component**

| Crossings                     | u-Polynomials at each crossing          |
|-------------------------------|---|
| $c_1$                         | $(u - 1)^{10}$                          |
| $c_2, c_3, c_4$<br>$c_7, c_8$ | $(u^2 + 1)^5$                           |
| $c_5, c_6, c_{10}$            | $u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1$ |
| $c_9$                         | $(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$    |
| $c_{11}$                      | $u^{10} + u^8 + 8u^6 + 3u^4 + 3u^2 + 1$ |
| $c_{12}$                      | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$    |

**(v) Riley Polynomials at the component**

| Crossings                     | Riley Polynomials at each crossing     |
|-------------------------------|--|
| $c_1$                         | $(y - 1)^{10}$                         |
| $c_2, c_3, c_4$<br>$c_7, c_8$ | $(y + 1)^{10}$                         |
| $c_5, c_6, c_{10}$            | $(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$ |
| $c_9, c_{12}$                 | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$  |
| $c_{11}$                      | $(y^5 + y^4 + 8y^3 + 3y^2 + 3y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 1.000000I$             | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                       |
| $a = -0.339110 + 0.822375I$ | $-0.32910 - 1.53058I$                 | $3.48489 + 4.43065I$  |
| $b = 1.000000I$             |                                       |                       |
| $u = 1.000000I$             |                                       |                       |
| $a = -0.339110 - 0.822375I$ | $-0.32910 + 1.53058I$                 | $3.48489 - 4.43065I$  |
| $b = 1.000000I$             |                                       |                       |
| $u = 1.000000I$             |                                       |                       |
| $a = 0.766826$              | $-2.40108$                            | $2.51890$             |
| $b = 1.000000I$             |                                       |                       |
| $u = 1.000000I$             |                                       |                       |
| $a = 0.455697 + 1.200150I$  | $-5.87256 + 4.40083I$                 | $-0.74431 - 3.49859I$ |
| $b = 1.000000I$             |                                       |                       |
| $u = 1.000000I$             |                                       |                       |
| $a = 0.455697 - 1.200150I$  | $-5.87256 - 4.40083I$                 | $-0.74431 + 3.49859I$ |
| $b = 1.000000I$             |                                       |                       |
| $u = -1.000000I$            |                                       |                       |
| $a = -0.339110 + 0.822375I$ | $-0.32910 - 1.53058I$                 | $3.48489 + 4.43065I$  |
| $b = -1.000000I$            |                                       |                       |
| $u = -1.000000I$            |                                       |                       |
| $a = -0.339110 - 0.822375I$ | $-0.32910 + 1.53058I$                 | $3.48489 - 4.43065I$  |
| $b = -1.000000I$            |                                       |                       |
| $u = -1.000000I$            |                                       |                       |
| $a = 0.766826$              | $-2.40108$                            | $2.51890$             |
| $b = -1.000000I$            |                                       |                       |
| $u = -1.000000I$            |                                       |                       |
| $a = 0.455697 + 1.200150I$  | $-5.87256 + 4.40083I$                 | $-0.74431 - 3.49859I$ |
| $b = -1.000000I$            |                                       |                       |
| $u = -1.000000I$            |                                       |                       |
| $a = 0.455697 - 1.200150I$  | $-5.87256 - 4.40083I$                 | $-0.74431 + 3.49859I$ |
| $b = -1.000000I$            |                                       |                       |

$$\text{III. } I_3^u = \langle b - u, a, u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 + 2u^3 + u \\ 2u^5 + 2u^3 + 2u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2u^5 + u^4 - 4u^3 + 3u^2 - 3u + 3 \\ -3u^5 + 2u^4 - 4u^3 + 3u^2 - u + 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ 2u^4 + 3u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^3 - 4u + 6$

**(iv) u-Polynomials at the component**

| Crossings                     | u-Polynomials at each crossing            |
|-------------------------------|---|
| $c_1$                         | $u^6 + 3u^5 + 4u^4 + 2u^3 + 1$            |
| $c_2, c_3, c_4$<br>$c_7, c_8$ | $u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$ |
| $c_5, c_6, c_{10}$            | $(u^3 - u^2 + 2u - 1)^2$                  |
| $c_9, c_{11}, c_{12}$         | $(u^3 + u^2 - 1)^2$                       |

**(v) Riley Polynomials at the component**

| Crossings                     | Riley Polynomials at each crossing   |
|-------------------------------|--------------------------------------|
| $c_1$                         | $y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$ |
| $c_2, c_3, c_4$<br>$c_7, c_8$ | $y^6 + 3y^5 + 4y^4 + 2y^3 + 1$       |
| $c_5, c_6, c_{10}$            | $(y^3 + 3y^2 + 2y - 1)^2$            |
| $c_9, c_{11}, c_{12}$         | $(y^3 - y^2 + 2y - 1)^2$             |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.498832 + 1.001300I$ |                                       |                      |
| $a = 0$                     | $-3.02413 + 2.82812I$                 | $2.49024 - 2.97945I$ |
| $b = -0.498832 + 1.001300I$ |                                       |                      |
| $u = -0.498832 - 1.001300I$ |                                       |                      |
| $a = 0$                     | $-3.02413 - 2.82812I$                 | $2.49024 + 2.97945I$ |
| $b = -0.498832 - 1.001300I$ |                                       |                      |
| $u = 0.284920 + 1.115140I$  |                                       |                      |
| $a = 0$                     | 1.11345                               | $9.01951 + 0.I$      |
| $b = 0.284920 + 1.115140I$  |                                       |                      |
| $u = 0.284920 - 1.115140I$  |                                       |                      |
| $a = 0$                     | 1.11345                               | $9.01951 + 0.I$      |
| $b = 0.284920 - 1.115140I$  |                                       |                      |
| $u = 0.713912 + 0.305839I$  |                                       |                      |
| $a = 0$                     | $-3.02413 + 2.82812I$                 | $2.49024 - 2.97945I$ |
| $b = 0.713912 + 0.305839I$  |                                       |                      |
| $u = 0.713912 - 0.305839I$  |                                       |                      |
| $a = 0$                     | $-3.02413 - 2.82812I$                 | $2.49024 + 2.97945I$ |
| $b = 0.713912 - 0.305839I$  |                                       |                      |

$$\text{IV. } I_4^u = \langle b - u, a, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u \\ -u^2 - u - 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ u^2 + u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^2 + 1 \\ u^2 + u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1 \\ 2u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ 2u^2 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^2 + 1 \\ u^2 + 2u + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^2 + 4u + 10$

**(iv) u-Polynomials at the component**

| Crossings   | u-Polynomials at each crossing |
|---|--------------------------------|
| $c_1$   | $u^3 + 3u^2 + 2u - 1$          |
| $c_2, c_3, c_4$<br>$c_5, c_6, c_7$<br>$c_8, c_{10}$ | $u^3 - u^2 + 2u - 1$           |
| $c_9, c_{11}, c_{12}$                               | $u^3 + u^2 - 1$                |

**(v) Riley Polynomials at the component**

| Crossings   | Riley Polynomials at each crossing |
|---|------------------------------------|
| $c_1$   | $y^3 - 5y^2 + 10y - 1$             |
| $c_2, c_3, c_4$<br>$c_5, c_6, c_7$<br>$c_8, c_{10}$ | $y^3 + 3y^2 + 2y - 1$              |
| $c_9, c_{11}, c_{12}$                               | $y^3 - y^2 + 2y - 1$               |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_4^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.215080 + 1.307140I$ |                                       |                      |
| $a = 0$                     | $-3.02413 - 2.82812I$                 | $2.49024 + 2.97945I$ |
| $b = -0.215080 + 1.307140I$ |                                       |                      |
| $u = -0.215080 - 1.307140I$ |                                       |                      |
| $a = 0$                     | $-3.02413 + 2.82812I$                 | $2.49024 - 2.97945I$ |
| $b = -0.215080 - 1.307140I$ |                                       |                      |
| $u = -0.569840$             |                                       |                      |
| $a = 0$                     | 1.11345                               | 9.01950              |
| $b = -0.569840$             |                                       |                      |

## V. u-Polynomials

| Crossings          | u-Polynomials at each crossing  |
|--------------------|---|
| $c_1$              | $(u - 1)^{10}(u^3 + 3u^2 + 2u - 1)(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)$<br>$\cdot (u^{32} + 3u^{31} + \dots - 20u + 1)$           |
| $c_2, c_7$         | $(u^2 + 1)^5(u^3 - u^2 + 2u - 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$<br>$\cdot (u^{32} + u^{31} + \dots - 10u^2 + 1)$ |
| $c_3, c_4, c_8$    | $(u^2 + 1)^5(u^3 - u^2 + 2u - 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$<br>$\cdot (u^{32} + u^{31} + \dots + 2u + 1)$    |
| $c_5, c_6, c_{10}$ | $(u^3 - u^2 + 2u - 1)^3(u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1)$<br>$\cdot (u^{32} + 2u^{31} + \dots + 5u + 2)$              |
| $c_9$              | $(u^3 + u^2 - 1)^3(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$<br>$\cdot (u^{32} + 8u^{31} + \dots + 837u + 136)$                    |
| $c_{11}$           | $(u^3 + u^2 - 1)^3(u^{10} + u^8 + 8u^6 + 3u^4 + 3u^2 + 1)$<br>$\cdot (u^{32} - 2u^{31} + \dots - 96u + 16)$                 |
| $c_{12}$           | $(u^3 + u^2 - 1)^3(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$<br>$\cdot (u^{32} + 8u^{31} + \dots + 837u + 136)$                    |

## VI. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing  |
|--------------------|---|
| $c_1$              | $(y - 1)^{10}(y^3 - 5y^2 + 10y - 1)(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)$<br>$\cdot (y^{32} + 63y^{31} + \dots - 48y + 1)$ |
| $c_2, c_7$         | $(y + 1)^{10}(y^3 + 3y^2 + 2y - 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$<br>$\cdot (y^{32} + 3y^{31} + \dots - 20y + 1)$         |
| $c_3, c_4, c_8$    | $(y + 1)^{10}(y^3 + 3y^2 + 2y - 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$<br>$\cdot (y^{32} + 47y^{31} + \dots - 84y + 1)$        |
| $c_5, c_6, c_{10}$ | $(y^3 + 3y^2 + 2y - 1)^3(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$<br>$\cdot (y^{32} + 28y^{31} + \dots + 19y + 4)$            |
| $c_9, c_{12}$      | $(y^3 - y^2 + 2y - 1)^3(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$<br>$\cdot (y^{32} + 44y^{30} + \dots - 169353y + 18496)$      |
| $c_{11}$           | $(y^3 - y^2 + 2y - 1)^3(y^5 + y^4 + 8y^3 + 3y^2 + 3y + 1)^2$<br>$\cdot (y^{32} - 4y^{31} + \dots - 256y + 256)$           |