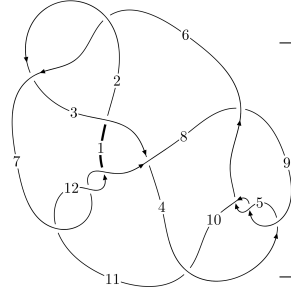
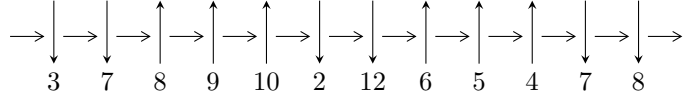


12n<sub>0578</sub> (K12n<sub>0578</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$7,12 \xrightarrow{c_7} 3,8 \xrightarrow{c_3} 4 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_6} 6 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 11 \xrightarrow{c_{10}} 10 \xrightarrow{c_5} 5 \twoheadrightarrow c_4, c_9, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle b - u, u^{23} - u^{22} + \dots + 16a + 1, u^{25} - u^{24} + \dots + 3u^2 - 1 \rangle$$

$$I_2^u = \langle -36334607050217u^{29} + 39477995355924u^{28} + \dots + 2200950009156001b - 1119770521665287, \\ -u^{29} + u^{28} + \dots + 7a - 6, u^{30} - u^{29} + \dots + 6u + 7 \rangle$$

$$I_3^u = \langle b + 1, a^4 + 4a^3 + 9a^2 + 10a + 7, u - 1 \rangle$$

$$I_4^u = \langle b - 1, a^4 - 4a^3 + 7a^2 - 6a + 1, u + 1 \rangle$$

$$I_5^u = \langle b + 1, a + 1, u - 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 64 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, u^{23} - u^{22} + \dots + 16a + 1, u^{25} - u^{24} + \dots + 3u^2 - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{16}u^{23} + \frac{1}{16}u^{22} + \dots - 2u - \frac{1}{16} \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ \frac{1}{16}u^{23} - \frac{1}{16}u^{22} + \dots + u + \frac{1}{16} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{16}u^{23} + \frac{1}{16}u^{22} + \dots - u - \frac{1}{16} \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{16}u^{24} - \frac{1}{16}u^{23} + \dots + \frac{1}{16}u + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{9}{16}u^{24} - \frac{5}{8}u^{23} + \dots + \frac{11}{16}u + \frac{15}{16} \\ -\frac{1}{16}u^{24} + \frac{1}{16}u^{23} + \dots + u^2 - \frac{1}{16}u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{16}u^{23} + \frac{1}{16}u^{22} + \dots + u - \frac{1}{16} \\ -0.0625000u^{24} + 0.5000000u^{23} + \dots + 0.9375000u + 0.5625000 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1.18750u^{24} - 1.81250u^{23} + \dots + 0.812500u + 0.625000 \\ -0.625000u^{24} + 1.43750u^{23} + \dots + 0.625000u + 1.18750 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $\frac{9}{4}u^{24} - \frac{15}{8}u^{23} + \dots + u - \frac{19}{8}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{25} + 7u^{24} + \dots + 6u + 1$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$u^{25} - u^{24} + \dots + 3u^2 - 1$
$c_3$	$u^{25} + 3u^{24} + \dots - 688u - 178$
$c_4, c_5, c_9$	$u^{25} - 3u^{24} + \dots - 5u^2 - 2$
$c_8, c_{10}$	$u^{25} + 9u^{24} + \dots + 92u + 14$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{25} + 33y^{24} + \dots + 2y - 1$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$y^{25} - 7y^{24} + \dots + 6y - 1$
$c_3$	$y^{25} - 9y^{24} + \dots - 428404y - 31684$
$c_4, c_5, c_9$	$y^{25} - 21y^{24} + \dots - 20y - 4$
$c_8, c_{10}$	$y^{25} + 15y^{24} + \dots - 244y - 196$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.785518 + 0.372640I$		
$a = 0.62353 - 2.12777I$	$-2.17521 + 5.68827I$	$-0.75349 - 8.49425I$
$b = -0.785518 + 0.372640I$		
$u = -0.785518 - 0.372640I$		
$a = 0.62353 + 2.12777I$	$-2.17521 - 5.68827I$	$-0.75349 + 8.49425I$
$b = -0.785518 - 0.372640I$		
$u = 0.755648 + 0.329653I$		
$a = -0.90101 - 2.06111I$	$-6.02340 - 1.36429I$	$-4.30078 + 5.12755I$
$b = 0.755648 + 0.329653I$		
$u = 0.755648 - 0.329653I$		
$a = -0.90101 + 2.06111I$	$-6.02340 + 1.36429I$	$-4.30078 - 5.12755I$
$b = 0.755648 - 0.329653I$		
$u = -0.845914 + 0.820525I$		
$a = -0.231288 - 1.378290I$	$1.53021 + 1.97230I$	$-1.25071 - 1.01903I$
$b = -0.845914 + 0.820525I$		
$u = -0.845914 - 0.820525I$		
$a = -0.231288 + 1.378290I$	$1.53021 - 1.97230I$	$-1.25071 + 1.01903I$
$b = -0.845914 - 0.820525I$		
$u = 0.265507 + 0.770529I$		
$a = -0.071679 - 1.030960I$	$4.72198 - 3.16963I$	$6.44572 + 4.63465I$
$b = 0.265507 + 0.770529I$		
$u = 0.265507 - 0.770529I$		
$a = -0.071679 + 1.030960I$	$4.72198 + 3.16963I$	$6.44572 - 4.63465I$
$b = 0.265507 - 0.770529I$		
$u = -0.730832 + 0.286998I$		
$a = 1.17630 - 1.94700I$	$-2.02761 - 2.93831I$	$0.12922 - 1.80135I$
$b = -0.730832 + 0.286998I$		
$u = -0.730832 - 0.286998I$		
$a = 1.17630 + 1.94700I$	$-2.02761 + 2.93831I$	$0.12922 + 1.80135I$
$b = -0.730832 - 0.286998I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.964582 + 0.777415I$ $a = 0.38162 - 1.45780I$ $b = 0.964582 + 0.777415I$	$3.01562 - 5.74190I$	$0.65811 + 6.60844I$
$u = 0.964582 - 0.777415I$ $a = 0.38162 + 1.45780I$ $b = 0.964582 - 0.777415I$	$3.01562 + 5.74190I$	$0.65811 - 6.60844I$
$u = 0.834411 + 0.917128I$ $a = 0.245471 - 1.273980I$ $b = 0.834411 + 0.917128I$	$6.70653 + 1.49728I$	$3.61002 - 0.12989I$
$u = 0.834411 - 0.917128I$ $a = 0.245471 + 1.273980I$ $b = 0.834411 - 0.917128I$	$6.70653 - 1.49728I$	$3.61002 + 0.12989I$
$u = 1.075630 + 0.727569I$ $a = 0.57040 - 1.51015I$ $b = 1.075630 + 0.727569I$	$2.19442 - 6.05278I$	$-0.77143 + 3.74618I$
$u = 1.075630 - 0.727569I$ $a = 0.57040 + 1.51015I$ $b = 1.075630 - 0.727569I$	$2.19442 + 6.05278I$	$-0.77143 - 3.74618I$
$u = -1.129150 + 0.745345I$ $a = -0.64410 - 1.44902I$ $b = -1.129150 + 0.745345I$	$-0.44383 + 10.34840I$	$-3.77176 - 7.45516I$
$u = -1.129150 - 0.745345I$ $a = -0.64410 + 1.44902I$ $b = -1.129150 - 0.745345I$	$-0.44383 - 10.34840I$	$-3.77176 + 7.45516I$
$u = -1.040970 + 0.866286I$ $a = -0.469635 - 1.328000I$ $b = -1.040970 + 0.866286I$	$9.76977 + 6.71873I$	$4.67666 - 4.93521I$
$u = -1.040970 - 0.866286I$ $a = -0.469635 + 1.328000I$ $b = -1.040970 - 0.866286I$	$9.76977 - 6.71873I$	$4.67666 + 4.93521I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.156880 + 0.765655I$ $a = 0.66857 - 1.39962I$ $b = 1.156880 + 0.765655I$	$4.4401 - 14.5092I$	$0.55817 + 8.79115I$
$u = 1.156880 - 0.765655I$ $a = 0.66857 + 1.39962I$ $b = 1.156880 - 0.765655I$	$4.4401 + 14.5092I$	$0.55817 - 8.79115I$
$u = -0.260838 + 0.456783I$ $a = 0.277904 - 0.859001I$ $b = -0.260838 + 0.456783I$	$0.037229 + 0.975136I$	$0.76804 - 7.07893I$
$u = -0.260838 - 0.456783I$ $a = 0.277904 + 0.859001I$ $b = -0.260838 - 0.456783I$	$0.037229 - 0.975136I$	$0.76804 + 7.07893I$
$u = 0.481143$ $a = -1.25216$ $b = 0.481143$	$2.56662$	$2.00450$

$$\text{II. } I_2^u = \langle -3.63 \times 10^{13} u^{29} + 3.95 \times 10^{13} u^{28} + \dots + 2.20 \times 10^{15} b - 1.12 \times 10^{15}, -u^{29} + u^{28} + \dots + 7a - 6, u^{30} - u^{29} + \dots + 6u + 7 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{7}u^{29} - \frac{1}{7}u^{28} + \dots - \frac{76}{7}u + \frac{6}{7} \\ 0.0165086u^{29} - 0.0179368u^{28} + \dots - 3.56720u + 0.508767 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.159366u^{29} - 0.160794u^{28} + \dots - 13.4243u + 1.36591 \\ 0.139320u^{29} - 0.0522821u^{28} + \dots - 3.67419u + 0.518764 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.159366u^{29} - 0.160794u^{28} + \dots - 14.4243u + 1.36591 \\ 0.0165086u^{29} - 0.0179368u^{28} + \dots - 3.56720u + 0.508767 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0741092u^{29} + 0.213429u^{28} + \dots + 2.77558u - 4.11884 \\ -0.00142820u^{29} + 0.124240u^{28} + \dots + 0.409715u - 1.11556 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.156177u^{29} + 0.104902u^{28} + \dots + 1.37289u - 3.42762 \\ -0.173390u^{29} + 0.0449879u^{28} + \dots + 0.143610u - 0.680215 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0971736u^{29} - 0.270564u^{28} + \dots - 12.6008u + 0.726652 \\ -0.0512747u^{29} - 0.0842981u^{28} + \dots - 2.49055u + 1.09324 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.167585u^{29} - 0.278986u^{28} + \dots - 14.6020u - 3.43422 \\ -0.446571u^{29} - 0.0855200u^{28} + \dots - 2.42870u + 1.17310 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{2576715548071340}{2200950009156001}u^{29} - \frac{754152713873936}{2200950009156001}u^{28} + \dots + \frac{5415273681221840}{2200950009156001}u + \frac{25651780906655686}{2200950009156001}$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{30} + 13u^{29} + \dots + 1100u + 49$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$u^{30} - u^{29} + \dots + 6u + 7$
$c_3$	$(u^{15} - u^{14} + \dots - 2u - 1)^2$
$c_4, c_5, c_9$	$(u^{15} + u^{14} + \dots - 2u - 1)^2$
$c_8, c_{10}$	$(u^{15} - 3u^{14} + \dots + 4u^2 - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{30} + 7y^{29} + \dots - 441680y + 2401$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$y^{30} - 13y^{29} + \dots - 1100y + 49$
$c_3$	$(y^{15} - 17y^{14} + \dots + 8y - 1)^2$
$c_4, c_5, c_9$	$(y^{15} - 13y^{14} + \dots + 8y - 1)^2$
$c_8, c_{10}$	$(y^{15} + 7y^{14} + \dots + 8y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.933632 + 0.405000I$ $a = -0.901456 + 0.391043I$ $b = -1.243160 + 0.162791I$	$-1.99092 + 1.64925I$	$-2.39367 - 0.16522I$
$u = 0.933632 - 0.405000I$ $a = -0.901456 - 0.391043I$ $b = -1.243160 - 0.162791I$	$-1.99092 - 1.64925I$	$-2.39367 + 0.16522I$
$u = 0.666225 + 0.833796I$ $a = -0.584884 + 0.731996I$ $b = 0.815806 - 0.779519I$	$3.47397 + 0.15908I$	$1.79403 + 0.85194I$
$u = 0.666225 - 0.833796I$ $a = -0.584884 - 0.731996I$ $b = 0.815806 + 0.779519I$	$3.47397 - 0.15908I$	$1.79403 - 0.85194I$
$u = -0.786352 + 0.445678I$ $a = 0.962512 + 0.545520I$ $b = 1.273190 + 0.075844I$	$-5.46412 + 1.81248I$	$-5.85619 - 4.33913I$
$u = -0.786352 - 0.445678I$ $a = 0.962512 - 0.545520I$ $b = 1.273190 - 0.075844I$	$-5.46412 - 1.81248I$	$-5.85619 + 4.33913I$
$u = 1.10731$ $a = -0.903090$ $b = -0.270107$	2.23561	5.03940
$u = -0.582390 + 0.944453I$ $a = 0.473038 + 0.767119I$ $b = -0.944169 - 0.806161I$	$1.23287 - 4.11725I$	$-1.40312 + 3.71929I$
$u = -0.582390 - 0.944453I$ $a = 0.473038 - 0.767119I$ $b = -0.944169 + 0.806161I$	$1.23287 + 4.11725I$	$-1.40312 - 3.71929I$
$u = 0.815806 + 0.779519I$ $a = -0.640758 + 0.612257I$ $b = 0.666225 - 0.833796I$	$3.47397 - 0.15908I$	$1.79403 - 0.85194I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.815806 - 0.779519I$ $a = -0.640758 - 0.612257I$ $b = 0.666225 + 0.833796I$	$3.47397 + 0.15908I$	$1.79403 + 0.85194I$
$u = 0.689418 + 0.518899I$ $a = -0.925949 + 0.696926I$ $b = -1.305660 + 0.019757I$	$-1.10658 - 5.45324I$	$-0.00468 + 6.35130I$
$u = 0.689418 - 0.518899I$ $a = -0.925949 - 0.696926I$ $b = -1.305660 - 0.019757I$	$-1.10658 + 5.45324I$	$-0.00468 - 6.35130I$
$u = -1.13884$ $a = 0.878083$ $b = 0.734573$	$-2.69194$	$4.62820$
$u = 0.583255 + 1.014300I$ $a = -0.426049 + 0.740911I$ $b = 0.987724 - 0.853962I$	$6.22908 + 8.01682I$	$3.04132 - 4.89679I$
$u = 0.583255 - 1.014300I$ $a = -0.426049 - 0.740911I$ $b = 0.987724 + 0.853962I$	$6.22908 - 8.01682I$	$3.04132 + 4.89679I$
$u = -0.944169 + 0.806161I$ $a = 0.612560 + 0.523023I$ $b = -0.582390 - 0.944453I$	$1.23287 + 4.11725I$	$-1.40312 - 3.71929I$
$u = -0.944169 - 0.806161I$ $a = 0.612560 - 0.523023I$ $b = -0.582390 + 0.944453I$	$1.23287 - 4.11725I$	$-1.40312 + 3.71929I$
$u = -1.243160 + 0.162791I$ $a = 0.790842 + 0.103561I$ $b = 0.933632 + 0.405000I$	$-1.99092 + 1.64925I$	$-2.39367 - 0.16522I$
$u = -1.243160 - 0.162791I$ $a = 0.790842 - 0.103561I$ $b = 0.933632 - 0.405000I$	$-1.99092 - 1.64925I$	$-2.39367 + 0.16522I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.803987 + 0.969115I$ $a = 0.507062 + 0.611206I$ $b = -0.803987 - 0.969115I$	10.5121	$5.97706 + 0.I$
$u = -0.803987 - 0.969115I$ $a = 0.507062 - 0.611206I$ $b = -0.803987 + 0.969115I$	10.5121	$5.97706 + 0.I$
$u = 0.734573$ $a = -1.36134$ $b = -1.13884$	-2.69194	4.62820
$u = 1.273190 + 0.075844I$ $a = -0.782653 + 0.046623I$ $b = -0.786352 + 0.445678I$	$-5.46412 + 1.81248I$	$-5.85619 - 4.33913I$
$u = 1.273190 - 0.075844I$ $a = -0.782653 - 0.046623I$ $b = -0.786352 - 0.445678I$	$-5.46412 - 1.81248I$	$-5.85619 + 4.33913I$
$u = 0.987724 + 0.853962I$ $a = -0.579361 + 0.500902I$ $b = 0.583255 - 1.014300I$	$6.22908 - 8.01682I$	$3.04132 + 4.89679I$
$u = 0.987724 - 0.853962I$ $a = -0.579361 - 0.500902I$ $b = 0.583255 + 1.014300I$	$6.22908 + 8.01682I$	$3.04132 - 4.89679I$
$u = -1.305660 + 0.019757I$ $a = 0.765721 + 0.011587I$ $b = 0.689418 + 0.518899I$	$-1.10658 - 5.45324I$	$-0.00468 + 6.35130I$
$u = -1.305660 - 0.019757I$ $a = 0.765721 - 0.011587I$ $b = 0.689418 - 0.518899I$	$-1.10658 + 5.45324I$	$-0.00468 - 6.35130I$
$u = -0.270107$ $a = 3.70223$ $b = 1.10731$	2.23561	5.03940

$$\text{III. } I_3^u = \langle b + 1, a^4 + 4a^3 + 9a^2 + 10a + 7, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -a - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a - 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a^2 + a + 1 \\ -a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a + 2 \\ a^2 + 3a + 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a^3 + a^2 + a - 3 \\ -a^3 - 5a^2 - 9a - 9 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a^2 - 8a - 16$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$	$(u - 1)^4$
$c_3, c_8, c_{10}$	$u^4 + 3u^2 + 3$
$c_4, c_5, c_9$	$u^4 - 3u^2 + 3$
$c_6, c_{11}, c_{12}$	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{11}, c_{12}$	$(y - 1)^4$
$c_3, c_8, c_{10}$	$(y^2 + 3y + 3)^2$
$c_4, c_5, c_9$	$(y^2 - 3y + 3)^2$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -0.65937 + 1.27123I$ $b = -1.00000$	$-3.28987 + 4.05977I$	$-6.00000 - 3.46410I$
$u = 1.00000$ $a = -0.65937 - 1.27123I$ $b = -1.00000$	$-3.28987 - 4.05977I$	$-6.00000 + 3.46410I$
$u = 1.00000$ $a = -1.34063 + 1.27123I$ $b = -1.00000$	$-3.28987 - 4.05977I$	$-6.00000 + 3.46410I$
$u = 1.00000$ $a = -1.34063 - 1.27123I$ $b = -1.00000$	$-3.28987 + 4.05977I$	$-6.00000 - 3.46410I$

$$\text{IV. } I_4^u = \langle b - 1, a^4 - 4a^3 + 7a^2 - 6a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -a + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a^2 - a + 1 \\ a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a - 2 \\ -a^2 + 3a - 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a^3 + 3a^2 - 5a + 3 \\ -a^3 + 3a^2 - 5a + 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a^2 - 8a$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_{11}$ $c_{12}$	$(u - 1)^4$
$c_2, c_7$	$(u + 1)^4$
$c_3, c_8, c_{10}$	$u^4 + u^2 - 1$
$c_4, c_5, c_9$	$u^4 - u^2 - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{11}, c_{12}$	$(y - 1)^4$
$c_3, c_8, c_{10}$	$(y^2 + y - 1)^2$
$c_4, c_5, c_9$	$(y^2 - y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 1.00000 + 1.27202I$ $b = 1.00000$	-7.23771	$-10.47214 + 0.I$
$u = -1.00000$ $a = 1.00000 - 1.27202I$ $b = 1.00000$	-7.23771	$-10.47214 + 0.I$
$u = -1.00000$ $a = 1.78615$ $b = 1.00000$	0.657974	-1.52790
$u = -1.00000$ $a = 0.213849$ $b = 1.00000$	0.657974	-1.52790

$$\mathbf{V. } I_5^u = \langle b + 1, a + 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -12**

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$	$u - 1$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$u$
$c_6, c_{11}, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{11}, c_{12}$	$y - 1$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$y$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -1.00000$	-3.28987	-12.0000
$b = -1.00000$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^9)(u^{25} + 7u^{24} + \dots + 6u + 1)(u^{30} + 13u^{29} + \dots + 1100u + 49)$
$c_2, c_7$	$((u-1)^5)(u+1)^4(u^{25} - u^{24} + \dots + 3u^2 - 1)(u^{30} - u^{29} + \dots + 6u + 7)$
$c_3$	$u(u^4 + u^2 - 1)(u^4 + 3u^2 + 3)(u^{15} - u^{14} + \dots - 2u - 1)^2$ $\cdot (u^{25} + 3u^{24} + \dots - 688u - 178)$
$c_4, c_5, c_9$	$u(u^4 - 3u^2 + 3)(u^4 - u^2 - 1)(u^{15} + u^{14} + \dots - 2u - 1)^2$ $\cdot (u^{25} - 3u^{24} + \dots - 5u^2 - 2)$
$c_6, c_{11}, c_{12}$	$((u-1)^4)(u+1)^5(u^{25} - u^{24} + \dots + 3u^2 - 1)(u^{30} - u^{29} + \dots + 6u + 7)$
$c_8, c_{10}$	$u(u^4 + u^2 - 1)(u^4 + 3u^2 + 3)(u^{15} - 3u^{14} + \dots + 4u^2 - 1)^2$ $\cdot (u^{25} + 9u^{24} + \dots + 92u + 14)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^9)(y^{25} + 33y^{24} + \dots + 2y - 1)$ $\cdot (y^{30} + 7y^{29} + \dots - 441680y + 2401)$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$((y-1)^9)(y^{25} - 7y^{24} + \dots + 6y - 1)(y^{30} - 13y^{29} + \dots - 1100y + 49)$
$c_3$	$y(y^2 + y - 1)^2(y^2 + 3y + 3)^2(y^{15} - 17y^{14} + \dots + 8y - 1)^2$ $\cdot (y^{25} - 9y^{24} + \dots - 428404y - 31684)$
$c_4, c_5, c_9$	$y(y^2 - 3y + 3)^2(y^2 - y - 1)^2(y^{15} - 13y^{14} + \dots + 8y - 1)^2$ $\cdot (y^{25} - 21y^{24} + \dots - 20y - 4)$
$c_8, c_{10}$	$y(y^2 + y - 1)^2(y^2 + 3y + 3)^2(y^{15} + 7y^{14} + \dots + 8y - 1)^2$ $\cdot (y^{25} + 15y^{24} + \dots - 244y - 196)$