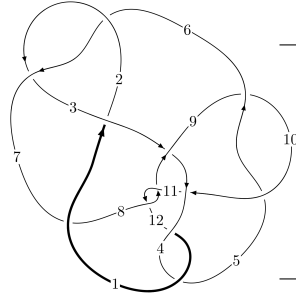
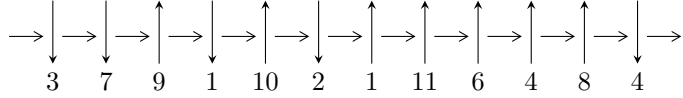


12n<sub>0587</sub> (K12n<sub>0587</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,7 \xrightarrow{c_2} 3,9 \xrightarrow{c_3} 4 \xrightarrow{c_1} 1 \xrightarrow{c_6} 6 \xrightarrow{c_9} 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 5 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \rightsquigarrow c_4, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -66u^{31} - 537u^{30} + \dots + 4b - 972, -243u^{31} - 1923u^{30} + \dots + 16a - 3048, \\ u^{32} + 9u^{31} + \dots + 128u + 16 \rangle$$

$$I_2^u = \langle -1.75141 \times 10^{21} a^7 u^5 + 4.76671 \times 10^{21} a^6 u^5 + \dots + 1.01718 \times 10^{23} a - 3.39686 \times 10^{22}, \\ -a^7 u^5 + 2a^6 u^5 + \dots - 7a - 3, u^6 - u^5 - u^4 + 2u^3 - u + 1 \rangle$$

$$I_3^u = \langle -5u^{21} - 4u^{20} + \dots + b + 7, -7u^{21} - 10u^{20} + \dots + 2a + 17, u^{22} - 6u^{20} + \dots - u + 2 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 102 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -66u^{31} - 537u^{30} + \dots + 4b - 972, -243u^{31} - 1923u^{30} + \dots + 16a - 3048, u^{32} + 9u^{31} + \dots + 128u + 16 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 15.1875u^{31} + 120.188u^{30} + \dots + 1410.75u + 190.500 \\ \frac{33}{2}u^{31} + \frac{537}{4}u^{30} + \dots + \frac{3507}{2}u + 243 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{79}{16}u^{31} - \frac{605}{16}u^{30} + \dots - \frac{619}{2}u - 38 \\ -\frac{53}{8}u^{31} - \frac{423}{8}u^{30} + \dots - 593u - 79 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 7.43750u^{31} + 64.9375u^{30} + \dots + 1101.75u + 154.500 \\ \frac{33}{4}u^{31} + 79u^{30} + \dots + \frac{2889}{2}u + 207 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -3.87500u^{31} - 41.7500u^{30} + \dots - 1002.75u - 142.500 \\ \frac{121}{8}u^{31} + \frac{865}{8}u^{30} + \dots + \frac{709}{2}u + 30 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{43}{16}u^{31} + \frac{369}{16}u^{30} + \dots + \frac{599}{2}u + 41 \\ \frac{35}{8}u^{31} + \frac{305}{8}u^{30} + \dots + 583u + 81 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - u^5 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 4.37500u^{31} + 25.7500u^{30} + \dots - 213.250u - 35.5000 \\ \frac{75}{8}u^{31} + \frac{527}{8}u^{30} + \dots + \frac{379}{2}u + 16 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-\frac{19}{2}u^{31} - \frac{149}{2}u^{30} + \dots - 710u - 78$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{32} + 15u^{31} + \dots + 1152u + 256$
$c_2, c_6$	$u^{32} - 9u^{31} + \dots - 128u + 16$
$c_3, c_5, c_9$	$u^{32} + 8u^{30} + \dots + 2u + 1$
$c_4, c_{12}$	$u^{32} + 21u^{30} + \dots + u + 1$
$c_7$	$u^{32} - 27u^{31} + \dots - 128512u + 13840$
$c_8, c_{11}$	$u^{32} + 15u^{31} + \dots + 544u + 64$
$c_{10}$	$u^{32} + u^{31} + \dots - 24u + 10$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{32} + 5y^{31} + \dots + 843776y + 65536$
$c_2, c_6$	$y^{32} - 15y^{31} + \dots - 1152y + 256$
$c_3, c_5, c_9$	$y^{32} + 16y^{31} + \dots + 4y + 1$
$c_4, c_{12}$	$y^{32} + 42y^{31} + \dots - 21y + 1$
$c_7$	$y^{32} + 5y^{31} + \dots - 1955321984y + 191545600$
$c_8, c_{11}$	$y^{32} + 15y^{31} + \dots + 23552y + 4096$
$c_{10}$	$y^{32} - 29y^{31} + \dots - 2956y + 100$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.353223 + 0.914504I$ $a = 0.944290 - 0.963381I$ $b = -0.547471 - 1.203850I$	$1.14278 - 11.08640I$	$1.04376 + 6.11578I$
$u = -0.353223 - 0.914504I$ $a = 0.944290 + 0.963381I$ $b = -0.547471 + 1.203850I$	$1.14278 + 11.08640I$	$1.04376 - 6.11578I$
$u = -0.695104 + 0.783443I$ $a = -1.016910 - 0.357438I$ $b = -0.986887 + 0.548231I$	$5.02104 + 1.18323I$	$4.63011 - 3.73174I$
$u = -0.695104 - 0.783443I$ $a = -1.016910 + 0.357438I$ $b = -0.986887 - 0.548231I$	$5.02104 - 1.18323I$	$4.63011 + 3.73174I$
$u = -0.971427 + 0.423273I$ $a = 1.30738 - 0.94887I$ $b = 0.86839 - 1.47514I$	$-0.29798 + 3.82056I$	$0.73357 - 6.52529I$
$u = -0.971427 - 0.423273I$ $a = 1.30738 + 0.94887I$ $b = 0.86839 + 1.47514I$	$-0.29798 - 3.82056I$	$0.73357 + 6.52529I$
$u = -0.319145 + 0.868644I$ $a = -1.069240 + 0.753126I$ $b = 0.312955 + 1.169150I$	$2.75461 - 4.44216I$	$3.37878 + 2.54361I$
$u = -0.319145 - 0.868644I$ $a = -1.069240 - 0.753126I$ $b = 0.312955 - 1.169150I$	$2.75461 + 4.44216I$	$3.37878 - 2.54361I$
$u = -0.041796 + 0.911678I$ $a = 0.708186 - 0.291456I$ $b = -0.236115 - 0.657820I$	$-4.79614 - 1.53152I$	$1.62395 + 4.66418I$
$u = -0.041796 - 0.911678I$ $a = 0.708186 + 0.291456I$ $b = -0.236115 + 0.657820I$	$-4.79614 + 1.53152I$	$1.62395 - 4.66418I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.720598 + 0.879414I$ $a = 0.761879 + 0.617760I$ $b = 1.092280 - 0.224850I$	$3.47851 + 6.82150I$	$-0.20982 - 8.20349I$
$u = -0.720598 - 0.879414I$ $a = 0.761879 - 0.617760I$ $b = 1.092280 + 0.224850I$	$3.47851 - 6.82150I$	$-0.20982 + 8.20349I$
$u = 0.802808 + 0.175070I$ $a = -0.250305 - 0.176055I$ $b = 0.170125 + 0.185160I$	$-1.38436 - 0.59539I$	$-4.63872 + 0.87070I$
$u = 0.802808 - 0.175070I$ $a = -0.250305 + 0.176055I$ $b = 0.170125 - 0.185160I$	$-1.38436 + 0.59539I$	$-4.63872 - 0.87070I$
$u = -0.967071 + 0.715806I$ $a = 0.056661 - 0.893739I$ $b = -0.584948 - 0.904868I$	$4.22303 + 4.44069I$	$3.22085 + 0.12023I$
$u = -0.967071 - 0.715806I$ $a = 0.056661 + 0.893739I$ $b = -0.584948 + 0.904868I$	$4.22303 - 4.44069I$	$3.22085 - 0.12023I$
$u = 1.229680 + 0.226268I$ $a = -0.293850 - 0.315256I$ $b = 0.290008 + 0.454153I$	$-2.37206 + 1.13232I$	$-1.58887 - 1.12287I$
$u = 1.229680 - 0.226268I$ $a = -0.293850 + 0.315256I$ $b = 0.290008 - 0.454153I$	$-2.37206 - 1.13232I$	$-1.58887 + 1.12287I$
$u = -0.994634 + 0.800004I$ $a = 0.411302 + 0.751543I$ $b = 1.010330 + 0.418467I$	$2.67500 - 0.65003I$	$-3.51745 + 3.19613I$
$u = -0.994634 - 0.800004I$ $a = 0.411302 - 0.751543I$ $b = 1.010330 - 0.418467I$	$2.67500 + 0.65003I$	$-3.51745 - 3.19613I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.283860 + 0.162995I$		
$a = 0.258937 + 0.394634I$	$-4.52901 + 7.74803I$	$-4.31211 - 4.99223I$
$b = -0.268116 - 0.548861I$		
$u = 1.283860 - 0.162995I$		
$a = 0.258937 - 0.394634I$	$-4.52901 - 7.74803I$	$-4.31211 + 4.99223I$
$b = -0.268116 + 0.548861I$		
$u = -1.170100 + 0.596807I$		
$a = 1.63919 - 0.72952I$	$0.19538 + 9.84539I$	$0. - 6.14820I$
$b = 1.48263 - 1.83190I$		
$u = -1.170100 - 0.596807I$		
$a = 1.63919 + 0.72952I$	$0.19538 - 9.84539I$	$0. + 6.14820I$
$b = 1.48263 + 1.83190I$		
$u = -1.172780 + 0.623036I$		
$a = -1.77974 + 0.55524I$	$-1.3469 + 16.7119I$	$-1.47549 - 9.48564I$
$b = -1.74130 + 1.76001I$		
$u = -1.172780 - 0.623036I$		
$a = -1.77974 - 0.55524I$	$-1.3469 - 16.7119I$	$-1.47549 + 9.48564I$
$b = -1.74130 - 1.76001I$		
$u = -1.251720 + 0.492171I$		
$a = -1.122650 + 0.775593I$	$-8.47765 + 6.52307I$	$0. - 9.62472I$
$b = -1.02352 + 1.52336I$		
$u = -1.251720 - 0.492171I$		
$a = -1.122650 - 0.775593I$	$-8.47765 - 6.52307I$	$0. + 9.62472I$
$b = -1.02352 - 1.52336I$		
$u = 1.286480 + 0.428514I$		
$a = 0.229293 + 0.227589I$	$-8.94178 - 3.23445I$	$0$
$b = -0.197456 - 0.391044I$		
$u = 1.286480 - 0.428514I$		
$a = 0.229293 - 0.227589I$	$-8.94178 + 3.23445I$	$0$
$b = -0.197456 + 0.391044I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.445223 + 0.386227I$	$1.140960 - 0.214496I$	$8.54432 + 0.39190I$
$a = -1.53443 + 0.10941I$		
$b = -0.640907 + 0.641353I$		
$u = -0.445223 - 0.386227I$	$1.140960 + 0.214496I$	$8.54432 - 0.39190I$
$a = -1.53443 - 0.10941I$		
$b = -0.640907 - 0.641353I$		



$$\text{II. } I_2^u = \langle -1.75 \times 10^{21} a^7 u^5 + 4.77 \times 10^{21} a^6 u^5 + \dots + 1.02 \times 10^{23} a - 3.40 \times 10^{22}, -a^7 u^5 + 2a^6 u^5 + \dots - 7a - 3, u^6 - u^5 - u^4 + 2u^3 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0.0448967a^7 u^5 - 0.122193a^6 u^5 + \dots - 2.60750a + 0.870772 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0464052a^7 u^5 + 0.165108a^6 u^5 + \dots - 0.295632a + 2.29477 \\ -0.0396494a^7 u^5 + 0.0414630a^6 u^5 + \dots - 1.01369a + 2.96480 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00659432a^7 u^5 - 0.0344612a^6 u^5 + \dots - 1.43280a + 1.87590 \\ 0.0514910a^7 u^5 - 0.156654a^6 u^5 + \dots - 5.04030a + 2.74667 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0418578a^7 u^5 + 0.290122a^6 u^5 + \dots + 1.67460a + 2.21502 \\ -0.0967619a^7 u^5 + 0.233461a^6 u^5 + \dots + 2.80716a + 0.179361 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0205988a^7 u^5 - 0.0387646a^6 u^5 + \dots + 0.613393a + 0.382177 \\ 0.00837862a^7 u^5 - 0.0176083a^6 u^5 + \dots + 0.996366a + 1.27350 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^5 - u^4 - 2u^3 + u^2 + u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0555186a^7 u^5 - 0.206112a^6 u^5 + \dots - 0.522508a - 1.82114 \\ 0.0445458a^7 u^5 - 0.178610a^6 u^5 + \dots - 1.10562a - 0.819014 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{4218289331032938010964}{39009694828428132113233} a^7 u^5 - \frac{881458935488935727072}{39009694828428132113233} a^6 u^5 + \dots - \frac{457197832689430921693344}{39009694828428132113233} a + \frac{213457719652228846802666}{39009694828428132113233}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^8$
$c_2, c_6$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^8$
$c_3, c_5, c_9$	$u^{48} - u^{47} + \dots + 1188u + 891$
$c_4, c_{12}$	$u^{48} - 3u^{47} + \dots + 2288u + 457$
$c_8, c_{11}$	$(u^4 - u^3 + u^2 + 1)^{12}$
$c_{10}$	$u^{48} - u^{47} + \dots - 56112u + 5549$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^8$
$c_2, c_6$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^8$
$c_3, c_5, c_9$	$y^{48} + 27y^{47} + \dots + 36823248y + 793881$
$c_4, c_{12}$	$y^{48} + 15y^{47} + \dots - 4710308y + 208849$
$c_8, c_{11}$	$(y^4 + y^3 + 3y^2 + 2y + 1)^{12}$
$c_{10}$	$y^{48} + 3y^{47} + \dots - 1819227006y + 30791401$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.002190 + 0.295542I$		
$a = 0.507592 + 0.582683I$	$-7.03641 + 2.33941I$	$-7.54346 - 5.70297I$
$b = 0.937656 - 1.013070I$		
$u = -1.002190 + 0.295542I$		
$a = 1.135000 - 0.676144I$	$-7.03641 + 2.33941I$	$-7.54346 - 5.70297I$
$b = 0.680912 + 0.433947I$		
$u = -1.002190 + 0.295542I$		
$a = -0.59164 + 1.37928I$	$-7.03641 - 0.49080I$	$-7.54346 + 4.11452I$
$b = 0.352015 + 0.153786I$		
$u = -1.002190 + 0.295542I$		
$a = 0.281512 + 0.236466I$	$-7.03641 - 0.49080I$	$-7.54346 + 4.11452I$
$b = -0.18530 + 1.55716I$		
$u = -1.002190 + 0.295542I$		
$a = -1.02156 + 1.37764I$	$-0.03467 - 2.23966I$	$-3.88998 + 1.77057I$
$b = -1.36997 + 1.97493I$		
$u = -1.002190 + 0.295542I$		
$a = 1.38666 - 1.35941I$	$-0.03467 + 4.08827I$	$-3.88998 - 3.35903I$
$b = 1.47255 - 1.58489I$		
$u = -1.002190 + 0.295542I$		
$a = 1.78082 - 1.05627I$	$-0.03467 + 4.08827I$	$-3.88998 - 3.35903I$
$b = 0.98793 - 1.77221I$		
$u = -1.002190 + 0.295542I$		
$a = -1.79224 + 1.44209I$	$-0.03467 - 2.23966I$	$-3.88998 + 1.77057I$
$b = -0.61665 + 1.68258I$		
$u = -1.002190 - 0.295542I$		
$a = 0.507592 - 0.582683I$	$-7.03641 - 2.33941I$	$-7.54346 + 5.70297I$
$b = 0.937656 + 1.013070I$		
$u = -1.002190 - 0.295542I$		
$a = 1.135000 + 0.676144I$	$-7.03641 - 2.33941I$	$-7.54346 + 5.70297I$
$b = 0.680912 - 0.433947I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.002190 - 0.295542I$ $a = -0.59164 - 1.37928I$ $b = 0.352015 - 0.153786I$	$-7.03641 + 0.49080I$	$-7.54346 - 4.11452I$
$u = -1.002190 - 0.295542I$ $a = 0.281512 - 0.236466I$ $b = -0.18530 - 1.55716I$	$-7.03641 + 0.49080I$	$-7.54346 - 4.11452I$
$u = -1.002190 - 0.295542I$ $a = -1.02156 - 1.37764I$ $b = -1.36997 - 1.97493I$	$-0.03467 + 2.23966I$	$-3.88998 - 1.77057I$
$u = -1.002190 - 0.295542I$ $a = 1.38666 + 1.35941I$ $b = 1.47255 + 1.58489I$	$-0.03467 - 4.08827I$	$-3.88998 + 3.35903I$
$u = -1.002190 - 0.295542I$ $a = 1.78082 + 1.05627I$ $b = 0.98793 + 1.77221I$	$-0.03467 - 4.08827I$	$-3.88998 + 3.35903I$
$u = -1.002190 - 0.295542I$ $a = -1.79224 - 1.44209I$ $b = -0.61665 - 1.68258I$	$-0.03467 + 2.23966I$	$-3.88998 - 1.77057I$
$u = 0.428243 + 0.664531I$ $a = -0.818193 + 0.122997I$ $b = -0.51591 - 1.51973I$	$3.74655 + 4.08827I$	$3.54346 - 3.35903I$
$u = 0.428243 + 0.664531I$ $a = 0.597673 - 0.407666I$ $b = 0.74823 + 1.23067I$	$3.74655 - 2.23966I$	$3.54346 + 1.77057I$
$u = 0.428243 + 0.664531I$ $a = -0.682635 - 1.191630I$ $b = 0.70891 - 1.33525I$	$-3.25520 + 2.33941I$	$-0.11002 - 5.70297I$
$u = 0.428243 + 0.664531I$ $a = 0.12918 + 1.52416I$ $b = -0.648527 + 1.032200I$	$-3.25520 - 0.49080I$	$-0.11002 + 4.11452I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.428243 + 0.664531I$ $a = -0.65313 - 1.39681I$ $b = 0.957528 - 0.738558I$	$-3.25520 - 0.49080I$	$-0.11002 + 4.11452I$
$u = 0.428243 + 0.664531I$ $a = -1.82121 - 0.04768I$ $b = -0.526856 - 0.222592I$	$3.74655 - 2.23966I$	$3.54346 + 1.77057I$
$u = 0.428243 + 0.664531I$ $a = 0.93397 + 1.66866I$ $b = -0.499539 + 0.963939I$	$-3.25520 + 2.33941I$	$-0.11002 - 5.70297I$
$u = 0.428243 + 0.664531I$ $a = 1.96937 + 0.49277I$ $b = 0.432121 + 0.491042I$	$3.74655 + 4.08827I$	$3.54346 - 3.35903I$
$u = 0.428243 - 0.664531I$ $a = -0.818193 - 0.122997I$ $b = -0.51591 + 1.51973I$	$3.74655 - 4.08827I$	$3.54346 + 3.35903I$
$u = 0.428243 - 0.664531I$ $a = 0.597673 + 0.407666I$ $b = 0.74823 - 1.23067I$	$3.74655 + 2.23966I$	$3.54346 - 1.77057I$
$u = 0.428243 - 0.664531I$ $a = -0.682635 + 1.191630I$ $b = 0.70891 + 1.33525I$	$-3.25520 - 2.33941I$	$-0.11002 + 5.70297I$
$u = 0.428243 - 0.664531I$ $a = 0.12918 - 1.52416I$ $b = -0.648527 - 1.032200I$	$-3.25520 + 0.49080I$	$-0.11002 - 4.11452I$
$u = 0.428243 - 0.664531I$ $a = -0.65313 + 1.39681I$ $b = 0.957528 + 0.738558I$	$-3.25520 + 0.49080I$	$-0.11002 - 4.11452I$
$u = 0.428243 - 0.664531I$ $a = -1.82121 + 0.04768I$ $b = -0.526856 + 0.222592I$	$3.74655 + 2.23966I$	$3.54346 - 1.77057I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.428243 - 0.664531I$ $a = 0.93397 - 1.66866I$ $b = -0.499539 - 0.963939I$	$-3.25520 - 2.33941I$	$-0.11002 + 5.70297I$
$u = 0.428243 - 0.664531I$ $a = 1.96937 - 0.49277I$ $b = 0.432121 - 0.491042I$	$3.74655 - 4.08827I$	$3.54346 + 3.35903I$
$u = 1.073950 + 0.558752I$ $a = 0.263523 + 0.901679I$ $b = 0.32755 + 1.80005I$	$1.85594 - 2.52906I$	$-0.17326 + 2.94577I$
$u = 1.073950 + 0.558752I$ $a = -0.660126 - 1.071870I$ $b = -0.74546 - 2.12446I$	$1.85594 - 8.85698I$	$-0.17326 + 8.07537I$
$u = 1.073950 + 0.558752I$ $a = -0.92630 - 1.19417I$ $b = 0.220804 - 1.115600I$	$1.85594 - 2.52906I$	$-0.17326 + 2.94577I$
$u = 1.073950 + 0.558752I$ $a = 1.69735 - 0.19586I$ $b = 1.96152 + 1.09909I$	$-5.14581 - 4.27792I$	$-3.82674 + 0.60183I$
$u = 1.073950 + 0.558752I$ $a = -1.78478 - 0.33884I$ $b = -2.08469 - 1.42090I$	$-5.14581 - 7.10813I$	$-3.82674 + 10.41931I$
$u = 1.073950 + 0.558752I$ $a = -1.85640 - 0.05757I$ $b = -1.93230 - 0.73805I$	$-5.14581 - 4.27792I$	$-3.82674 + 0.60183I$
$u = 1.073950 + 0.558752I$ $a = 1.35622 + 1.27256I$ $b = 0.11003 + 1.51998I$	$1.85594 - 8.85698I$	$-0.17326 + 8.07537I$
$u = 1.073950 + 0.558752I$ $a = 2.06935 + 0.24643I$ $b = 1.72743 + 1.36115I$	$-5.14581 - 7.10813I$	$-3.82674 + 10.41931I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.073950 - 0.558752I$ $a = 0.263523 - 0.901679I$ $b = 0.32755 - 1.80005I$	$1.85594 + 2.52906I$	$-0.17326 - 2.94577I$
$u = 1.073950 - 0.558752I$ $a = -0.660126 + 1.071870I$ $b = -0.74546 + 2.12446I$	$1.85594 + 8.85698I$	$-0.17326 - 8.07537I$
$u = 1.073950 - 0.558752I$ $a = -0.92630 + 1.19417I$ $b = 0.220804 + 1.115600I$	$1.85594 + 2.52906I$	$-0.17326 - 2.94577I$
$u = 1.073950 - 0.558752I$ $a = 1.69735 + 0.19586I$ $b = 1.96152 - 1.09909I$	$-5.14581 + 4.27792I$	$-3.82674 - 0.60183I$
$u = 1.073950 - 0.558752I$ $a = -1.78478 + 0.33884I$ $b = -2.08469 + 1.42090I$	$-5.14581 + 7.10813I$	$-3.82674 - 10.41931I$
$u = 1.073950 - 0.558752I$ $a = -1.85640 + 0.05757I$ $b = -1.93230 + 0.73805I$	$-5.14581 + 4.27792I$	$-3.82674 - 0.60183I$
$u = 1.073950 - 0.558752I$ $a = 1.35622 - 1.27256I$ $b = 0.11003 - 1.51998I$	$1.85594 + 8.85698I$	$-0.17326 - 8.07537I$
$u = 1.073950 - 0.558752I$ $a = 2.06935 - 0.24643I$ $b = 1.72743 - 1.36115I$	$-5.14581 + 7.10813I$	$-3.82674 - 10.41931I$



$$\text{III. } I_3^u = \langle -5u^{21} - 4u^{20} + \dots + b + 7, -7u^{21} - 10u^{20} + \dots + 2a + 17, u^{22} - 6u^{20} + \dots - u + 2 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{7}{2}u^{21} + 5u^{20} + \dots + 2u - \frac{17}{2} \\ 5u^{21} + 4u^{20} + \dots - 5u - 7 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{3}{2}u^{21} - u^{20} + \dots + 5u + \frac{7}{2} \\ -u^{21} + 6u^{19} + \dots + u + 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{7}{2}u^{21} + 4u^{20} + \dots - 2u - \frac{13}{2} \\ 5u^{21} + 3u^{20} + \dots - 9u - 5 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{5}{2}u^{21} + 2u^{20} + \dots - 2u + \frac{3}{2} \\ 3u^{21} + 3u^{20} + \dots + u - 5 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{3}{2}u^{21} + 9u^{19} + \dots + 6u + \frac{1}{2} \\ -u^{21} + u^{20} + \dots + 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - u^5 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{5}{2}u^{21} + 2u^{20} + \dots - 2u - \frac{1}{2} \\ 2u^{21} + 2u^{20} + \dots + 4u - 5 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -12u^{21} - 5u^{20} + 65u^{19} + 29u^{18} - 189u^{17} - 87u^{16} + 341u^{15} + 140u^{14} - 435u^{13} - 105u^{12} + 395u^{11} - 41u^{10} - 271u^9 + 192u^8 + 121u^7 - 220u^6 - 4u^5 + 158u^4 - 42u^3 - 66u^2 + 23u + 18$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{22} - 12u^{21} + \dots - 33u + 4$
$c_2$	$u^{22} - 6u^{20} + \dots - u + 2$
$c_3, c_9$	$u^{22} + 9u^{20} + \dots - u + 1$
$c_4$	$u^{22} + 2u^{20} + \dots - 2u + 1$
$c_5$	$u^{22} + 9u^{20} + \dots + u + 1$
$c_6$	$u^{22} - 6u^{20} + \dots + u + 2$
$c_7$	$u^{22} + 2u^{20} + \dots + u + 2$
$c_8$	$u^{22} + 4u^{21} + \dots + 9u^2 + 1$
$c_{10}$	$u^{22} + u^{21} + \dots + 161u + 208$
$c_{11}$	$u^{22} - 4u^{21} + \dots + 9u^2 + 1$
$c_{12}$	$u^{22} + 2u^{20} + \dots + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{22} + 4y^{21} + \dots - 17y + 16$
$c_2, c_6$	$y^{22} - 12y^{21} + \dots - 33y + 4$
$c_3, c_5, c_9$	$y^{22} + 18y^{21} + \dots - 5y + 1$
$c_4, c_{12}$	$y^{22} + 4y^{21} + \dots - 10y + 1$
$c_7$	$y^{22} + 4y^{21} + \dots - 33y + 4$
$c_8, c_{11}$	$y^{22} + 14y^{21} + \dots + 18y + 1$
$c_{10}$	$y^{22} + y^{21} + \dots - 79169y + 43264$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.961848 + 0.296339I$ $a = -2.00016 - 1.79386I$ $b = -1.39226 - 2.31814I$	$0.56453 - 4.62883I$	$5.59956 + 11.73591I$
$u = 0.961848 - 0.296339I$ $a = -2.00016 + 1.79386I$ $b = -1.39226 + 2.31814I$	$0.56453 + 4.62883I$	$5.59956 - 11.73591I$
$u = -1.002840 + 0.352792I$ $a = 0.468251 - 0.558052I$ $b = -0.272706 + 0.724834I$	$-6.83956 + 0.45717I$	$-4.57919 - 4.81225I$
$u = -1.002840 - 0.352792I$ $a = 0.468251 + 0.558052I$ $b = -0.272706 - 0.724834I$	$-6.83956 - 0.45717I$	$-4.57919 + 4.81225I$
$u = -0.843470 + 0.703506I$ $a = -0.034848 - 0.250819I$ $b = 0.205846 + 0.187042I$	$3.60508 + 5.33056I$	$-0.09464 - 5.51436I$
$u = -0.843470 - 0.703506I$ $a = -0.034848 + 0.250819I$ $b = 0.205846 - 0.187042I$	$3.60508 - 5.33056I$	$-0.09464 + 5.51436I$
$u = 0.173815 + 0.853261I$ $a = -0.694604 - 0.751121I$ $b = 0.520170 - 0.723235I$	$-5.80927 + 0.76774I$	$-5.23209 + 0.08222I$
$u = 0.173815 - 0.853261I$ $a = -0.694604 + 0.751121I$ $b = 0.520170 + 0.723235I$	$-5.80927 - 0.76774I$	$-5.23209 - 0.08222I$
$u = 0.817172 + 0.275112I$ $a = 1.64987 + 2.09307I$ $b = 0.77240 + 2.16430I$	$1.11933 + 2.14001I$	$6.11579 - 0.86458I$
$u = 0.817172 - 0.275112I$ $a = 1.64987 - 2.09307I$ $b = 0.77240 - 2.16430I$	$1.11933 - 2.14001I$	$6.11579 + 0.86458I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.918631 + 0.703076I$ $a = 0.215399 + 0.106652I$ $b = -0.272856 + 0.053468I$	$3.37208 + 0.07368I$	$2.57677 - 1.78560I$
$u = -0.918631 - 0.703076I$ $a = 0.215399 - 0.106652I$ $b = -0.272856 - 0.053468I$	$3.37208 - 0.07368I$	$2.57677 + 1.78560I$
$u = 0.544682 + 0.641471I$ $a = 0.35849 + 1.75353I$ $b = -0.92958 + 1.18508I$	$-3.74937 + 1.02775I$	$-3.94340 - 0.09185I$
$u = 0.544682 - 0.641471I$ $a = 0.35849 - 1.75353I$ $b = -0.92958 - 1.18508I$	$-3.74937 - 1.02775I$	$-3.94340 + 0.09185I$
$u = 1.047900 + 0.563172I$ $a = -2.02559 + 0.01283I$ $b = -2.12984 - 1.12732I$	$-5.29588 - 5.77472I$	$-4.89114 + 4.98759I$
$u = 1.047900 - 0.563172I$ $a = -2.02559 - 0.01283I$ $b = -2.12984 + 1.12732I$	$-5.29588 + 5.77472I$	$-4.89114 - 4.98759I$
$u = -0.782222 + 0.186398I$ $a = 0.296177 - 0.982955I$ $b = -0.048455 + 0.824096I$	$-5.78836 + 2.01747I$	$0.74667 - 4.58846I$
$u = -0.782222 - 0.186398I$ $a = 0.296177 + 0.982955I$ $b = -0.048455 - 0.824096I$	$-5.78836 - 2.01747I$	$0.74667 + 4.58846I$
$u = -1.226180 + 0.389290I$ $a = -0.269525 + 0.335576I$ $b = 0.199850 - 0.516400I$	$-10.01640 + 3.30562I$	$-9.26157 - 2.61451I$
$u = -1.226180 - 0.389290I$ $a = -0.269525 - 0.335576I$ $b = 0.199850 + 0.516400I$	$-10.01640 - 3.30562I$	$-9.26157 + 2.61451I$

	Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.227930 + 0.530969I$		
$a =$	$1.286540 + 0.437612I$	$-8.99565 - 5.89312I$	$-7.53678 + 2.20155I$
$b =$	$1.34742 + 1.22047I$		
$u =$	$1.227930 - 0.530969I$		
$a =$	$1.286540 - 0.437612I$	$-8.99565 + 5.89312I$	$-7.53678 - 2.20155I$
$b =$	$1.34742 - 1.22047I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^8)(u^{22} - 12u^{21} + \dots - 33u + 4) \cdot (u^{32} + 15u^{31} + \dots + 1152u + 256)$
$c_2$	$((u^6 + u^5 - u^4 - 2u^3 + u + 1)^8)(u^{22} - 6u^{20} + \dots - u + 2) \cdot (u^{32} - 9u^{31} + \dots - 128u + 16)$
$c_3, c_9$	$(u^{22} + 9u^{20} + \dots - u + 1)(u^{32} + 8u^{30} + \dots + 2u + 1) \cdot (u^{48} - u^{47} + \dots + 1188u + 891)$
$c_4$	$(u^{22} + 2u^{20} + \dots - 2u + 1)(u^{32} + 21u^{30} + \dots + u + 1) \cdot (u^{48} - 3u^{47} + \dots + 2288u + 457)$
$c_5$	$(u^{22} + 9u^{20} + \dots + u + 1)(u^{32} + 8u^{30} + \dots + 2u + 1) \cdot (u^{48} - u^{47} + \dots + 1188u + 891)$
$c_6$	$((u^6 + u^5 - u^4 - 2u^3 + u + 1)^8)(u^{22} - 6u^{20} + \dots + u + 2) \cdot (u^{32} - 9u^{31} + \dots - 128u + 16)$
$c_7$	$((u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^8)(u^{22} + 2u^{20} + \dots + u + 2) \cdot (u^{32} - 27u^{31} + \dots - 128512u + 13840)$
$c_8$	$((u^4 - u^3 + u^2 + 1)^{12})(u^{22} + 4u^{21} + \dots + 9u^2 + 1) \cdot (u^{32} + 15u^{31} + \dots + 544u + 64)$
$c_{10}$	$(u^{22} + u^{21} + \dots + 161u + 208)(u^{32} + u^{31} + \dots - 24u + 10) \cdot (u^{48} - u^{47} + \dots - 56112u + 5549)$
$c_{11}$	$((u^4 - u^3 + u^2 + 1)^{12})(u^{22} - 4u^{21} + \dots + 9u^2 + 1) \cdot (u^{32} + 15u^{31} + \dots + 544u + 64)$
$c_{12}$	$(u^{22} + 2u^{20} + \dots + 2u + 1)(u^{32} + 21u^{30} + \dots + u + 1) \cdot (u^{48} - 3u^{47} + \dots + 2288u + 457)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^8)(y^{22} + 4y^{21} + \dots - 17y + 16)$ $\cdot (y^{32} + 5y^{31} + \dots + 843776y + 65536)$
$c_2, c_6$	$((y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^8)(y^{22} - 12y^{21} + \dots - 33y + 4)$ $\cdot (y^{32} - 15y^{31} + \dots - 1152y + 256)$
$c_3, c_5, c_9$	$(y^{22} + 18y^{21} + \dots - 5y + 1)(y^{32} + 16y^{31} + \dots + 4y + 1)$ $\cdot (y^{48} + 27y^{47} + \dots + 36823248y + 793881)$
$c_4, c_{12}$	$(y^{22} + 4y^{21} + \dots - 10y + 1)(y^{32} + 42y^{31} + \dots - 21y + 1)$ $\cdot (y^{48} + 15y^{47} + \dots - 4710308y + 208849)$
$c_7$	$((y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^8)(y^{22} + 4y^{21} + \dots - 33y + 4)$ $\cdot (y^{32} + 5y^{31} + \dots - 1955321984y + 191545600)$
$c_8, c_{11}$	$((y^4 + y^3 + 3y^2 + 2y + 1)^{12})(y^{22} + 14y^{21} + \dots + 18y + 1)$ $\cdot (y^{32} + 15y^{31} + \dots + 23552y + 4096)$
$c_{10}$	$(y^{22} + y^{21} + \dots - 79169y + 43264)(y^{32} - 29y^{31} + \dots - 2956y + 100)$ $\cdot (y^{48} + 3y^{47} + \dots - 1819227006y + 30791401)$