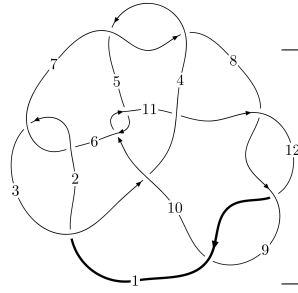
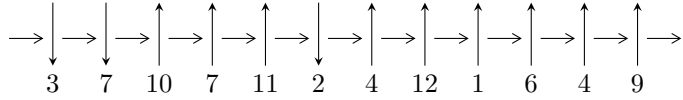


12n<sub>0592</sub> (K12n<sub>0592</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,7 \xrightarrow{c_2} 3,10 \xrightarrow{c_3} 4 \xrightarrow{c_1} 1 \xrightarrow{c_6} 6 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \xrightarrow{c_8} 8 \twoheadrightarrow c_4, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -13u^{16} - 54u^{15} + \dots + 4b - 36, -9u^{16} - 28u^{15} + \dots + 8a + 20, u^{17} + 6u^{16} + \dots + 56u + 8 \rangle$$

$$I_2^u = \langle 3u^{10} - 8u^9 + 3u^8 + 16u^7 - 11u^6 - 21u^5 + 21u^4 + 16u^3 - 17u^2 + b - 6u + 6, \\ 6u^{10} - 15u^9 + 4u^8 + 33u^7 - 20u^6 - 41u^5 + 39u^4 + 33u^3 - 32u^2 + a - 11u + 12, \\ u^{11} - 3u^{10} + 2u^9 + 5u^8 - 6u^7 - 5u^6 + 10u^5 + 2u^4 - 8u^3 + u^2 + 3u - 1 \rangle$$

$$I_3^u = \langle -37a^5u^2 + 123a^4u^2 + \dots - 100a + 168, a^5u^2 - 3a^4u^2 + \dots + 13a + 20, u^3 - u^2 + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 46 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -13u^{16} - 54u^{15} + \dots + 4b - 36, -9u^{16} - 28u^{15} + \dots + 8a + 20, u^{17} + 6u^{16} + \dots + 56u + 8 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{9}{8}u^{16} + \frac{7}{2}u^{15} + \dots - \frac{29}{2}u - \frac{5}{2} \\ \frac{13}{4}u^{16} + \frac{27}{2}u^{15} + \dots + \frac{131}{2}u + 9 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{4}u^{16} + u^{15} + \dots + \frac{3}{2}u + \frac{1}{2} \\ \frac{1}{2}u^{16} + \frac{5}{2}u^{15} + \dots + \frac{29}{2}u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{33}{8}u^{16} + \frac{39}{2}u^{15} + \dots + \frac{245}{2}u + \frac{39}{2} \\ \frac{25}{4}u^{16} + \frac{59}{2}u^{15} + \dots + \frac{405}{2}u + 31 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{4}u^{16} + u^{15} + \dots + \frac{3}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^{15} - 2u^{14} + \dots - \frac{23}{2}u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{9}{8}u^{16} - 4u^{15} + \dots + 12u + \frac{9}{2} \\ -\frac{15}{4}u^{16} - \frac{29}{2}u^{15} + \dots - \frac{29}{2}u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{9}{4}u^{16} + 12u^{15} + \dots + \frac{201}{2}u + \frac{35}{2} \\ 2u^{16} + \frac{25}{2}u^{15} + \dots + \frac{311}{2}u + 26 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{11}{4}u^{16} - \frac{59}{4}u^{15} + \dots - \frac{429}{4}u - 16 \\ -\frac{9}{4}u^{16} - 14u^{15} + \dots - 141u - 22 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -9u^{16} - 52u^{15} - 116u^{14} - 68u^{13} + 190u^{12} + 347u^{11} - 140u^{10} - 1029u^9 - 1025u^8 + 472u^7 + 1947u^6 + 1504u^5 - 415u^4 - 1702u^3 - 1433u^2 - 576u - 82$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{17} + 6u^{16} + \dots + 480u + 64$
$c_2, c_6$	$u^{17} - 6u^{16} + \dots + 56u - 8$
$c_3, c_5, c_{10}$	$u^{17} - u^{15} + \dots + 3u - 1$
$c_4, c_7$	$u^{17} + 4u^{16} + \dots + 8u - 1$
$c_8, c_9, c_{12}$	$u^{17} - 7u^{16} + \dots + 20u - 8$
$c_{11}$	$u^{17} - 2u^{16} + \dots + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{17} + 22y^{16} + \dots + 66048y - 4096$
$c_2, c_6$	$y^{17} - 6y^{16} + \dots + 480y - 64$
$c_3, c_5, c_{10}$	$y^{17} - 2y^{16} + \dots + 3y - 1$
$c_4, c_7$	$y^{17} - 36y^{16} + \dots + 102y - 1$
$c_8, c_9, c_{12}$	$y^{17} - 21y^{16} + \dots + 272y - 64$
$c_{11}$	$y^{17} - 44y^{16} + \dots + 33y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.582631 + 0.962982I$ $a = -0.764828 + 0.649431I$ $b = 0.179778 + 1.114890I$	$6.08323 - 3.07842I$	$10.91849 + 3.36026I$
$u = -0.582631 - 0.962982I$ $a = -0.764828 - 0.649431I$ $b = 0.179778 - 1.114890I$	$6.08323 + 3.07842I$	$10.91849 - 3.36026I$
$u = -0.998116 + 0.574654I$ $a = -1.30029 + 0.75173I$ $b = -0.86585 + 1.49753I$	$-0.04390 + 4.58131I$	$7.64977 - 6.92778I$
$u = -0.998116 - 0.574654I$ $a = -1.30029 - 0.75173I$ $b = -0.86585 - 1.49753I$	$-0.04390 - 4.58131I$	$7.64977 + 6.92778I$
$u = 1.139290 + 0.263587I$ $a = 0.072389 + 0.255610I$ $b = -0.015097 - 0.310294I$	$-2.02646 - 1.69138I$	$0.73300 + 3.24851I$
$u = 1.139290 - 0.263587I$ $a = 0.072389 - 0.255610I$ $b = -0.015097 + 0.310294I$	$-2.02646 + 1.69138I$	$0.73300 - 3.24851I$
$u = -0.612038 + 0.494740I$ $a = 1.36351 - 0.44192I$ $b = 0.615883 - 0.945055I$	$1.133960 - 0.080801I$	$10.62347 + 1.71983I$
$u = -0.612038 - 0.494740I$ $a = 1.36351 + 0.44192I$ $b = 0.615883 + 0.945055I$	$1.133960 + 0.080801I$	$10.62347 - 1.71983I$
$u = -0.710496 + 1.098260I$ $a = 0.517258 - 0.878567I$ $b = -0.597387 - 1.192300I$	$16.3616 - 5.2854I$	$10.20532 + 2.53472I$
$u = -0.710496 - 1.098260I$ $a = 0.517258 + 0.878567I$ $b = -0.597387 + 1.192300I$	$16.3616 + 5.2854I$	$10.20532 - 2.53472I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.105090 + 0.729938I$ $a = 1.30956 - 0.56888I$ $b = 1.03194 - 1.58456I$	$4.45386 + 9.24930I$	$8.34005 - 7.37887I$
$u = -1.105090 - 0.729938I$ $a = 1.30956 + 0.56888I$ $b = 1.03194 + 1.58456I$	$4.45386 - 9.24930I$	$8.34005 + 7.37887I$
$u = -1.126030 + 0.831805I$ $a = -1.43522 + 0.37456I$ $b = -1.30455 + 1.61559I$	$14.9808 + 12.2193I$	$8.76311 - 5.87051I$
$u = -1.126030 - 0.831805I$ $a = -1.43522 - 0.37456I$ $b = -1.30455 - 1.61559I$	$14.9808 - 12.2193I$	$8.76311 + 5.87051I$
$u = 1.22314 + 0.77434I$ $a = -0.144243 - 0.159249I$ $b = 0.053117 + 0.306476I$	$4.66481 - 3.72406I$	$7.31637 - 0.66089I$
$u = 1.22314 - 0.77434I$ $a = -0.144243 + 0.159249I$ $b = 0.053117 - 0.306476I$	$4.66481 + 3.72406I$	$7.31637 + 0.66089I$
$u = -0.456042$ $a = 1.76372$ $b = 0.804333$	0.900511	10.9010

**II.**

$$I_2^u = \langle 3u^{10} - 8u^9 + \dots + b + 6, 6u^{10} - 15u^9 + \dots + a + 12, u^{11} - 3u^{10} + \dots + 3u - 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -6u^{10} + 15u^9 + \dots + 11u - 12 \\ -3u^{10} + 8u^9 + \dots + 6u - 6 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -3u^{10} + 8u^9 + \dots + 5u - 9 \\ -u^{10} + 3u^9 - 2u^8 - 5u^7 + 6u^6 + 5u^5 - 10u^4 - 2u^3 + 9u^2 - u - 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -5u^{10} + 13u^9 + \dots + 8u - 10 \\ -2u^{10} + 6u^9 - 4u^8 - 9u^7 + 9u^6 + 12u^5 - 16u^4 - 8u^3 + 12u^2 + 3u - 4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3u^{10} + 8u^9 + \dots + 5u - 9 \\ -u^{10} + 3u^9 - 2u^8 - 5u^7 + 6u^6 + 5u^5 - 10u^4 - 2u^3 + 8u^2 - u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -4u^{10} + 10u^9 + \dots + 7u - 8 \\ -3u^{10} + 8u^9 + \dots + 6u - 6 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 4u^{10} - 10u^9 + \dots - 4u + 11 \\ 3u^{10} - 7u^9 + u^8 + 16u^7 - 8u^6 - 19u^5 + 17u^4 + 14u^3 - 13u^2 - 3u + 6 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 8u^{10} - 21u^9 + \dots - 13u + 19 \\ 3u^{10} - 8u^9 + \dots - 5u + 9 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**

$$= 7u^{10} - 19u^9 + 13u^8 + 28u^7 - 27u^6 - 29u^5 + 51u^4 + 18u^3 - 28u^2 + u + 16$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{11} - 5u^{10} + \dots + 11u - 1$
$c_2$	$u^{11} - 3u^{10} + 2u^9 + 5u^8 - 6u^7 - 5u^6 + 10u^5 + 2u^4 - 8u^3 + u^2 + 3u - 1$
$c_3, c_{10}$	$u^{11} + 4u^9 + u^8 + 4u^7 + 4u^6 - u^5 + 5u^4 - 2u^3 + 3u^2 - u + 1$
$c_4$	$u^{11} + 3u^9 + 6u^8 + u^7 + 20u^6 - 4u^5 + 26u^4 - 6u^3 + 15u^2 - 4u + 3$
$c_5$	$u^{11} + 4u^9 - u^8 + 4u^7 - 4u^6 - u^5 - 5u^4 - 2u^3 - 3u^2 - u - 1$
$c_6$	$u^{11} + 3u^{10} + 2u^9 - 5u^8 - 6u^7 + 5u^6 + 10u^5 - 2u^4 - 8u^3 - u^2 + 3u + 1$
$c_7$	$u^{11} + 3u^9 - 6u^8 + u^7 - 20u^6 - 4u^5 - 26u^4 - 6u^3 - 15u^2 - 4u - 3$
$c_8, c_9$	$u^{11} - 8u^9 - u^8 + 23u^7 + 5u^6 - 28u^5 - 7u^4 + 13u^3 + 2u^2 - 2u - 1$
$c_{11}$	$u^{11} + 7u^9 - 22u^8 + 7u^7 - 56u^6 - 3u^5 - 45u^4 - 6u^3 - 12u^2 - u - 1$
$c_{12}$	$u^{11} - 8u^9 + u^8 + 23u^7 - 5u^6 - 28u^5 + 7u^4 + 13u^3 - 2u^2 - 2u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{11} + 19y^{10} + \dots + 31y - 1$
$c_2, c_6$	$y^{11} - 5y^{10} + \dots + 11y - 1$
$c_3, c_5, c_{10}$	$y^{11} + 8y^{10} + \dots - 5y - 1$
$c_4, c_7$	$y^{11} + 6y^{10} + \dots - 74y - 9$
$c_8, c_9, c_{12}$	$y^{11} - 16y^{10} + \dots + 8y - 1$
$c_{11}$	$y^{11} + 14y^{10} + \dots - 23y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.856562 + 0.586236I$ $a = -0.588949 + 0.335331I$ $b = 0.307889 - 0.632495I$	$2.23625 + 2.32410I$	$6.78884 - 2.44901I$
$u = -0.856562 - 0.586236I$ $a = -0.588949 - 0.335331I$ $b = 0.307889 + 0.632495I$	$2.23625 - 2.32410I$	$6.78884 + 2.44901I$
$u = -0.855558 + 0.209235I$ $a = 0.357696 - 0.809834I$ $b = -0.136583 + 0.767702I$	$-5.34223 + 0.90366I$	$2.99552 - 7.97302I$
$u = -0.855558 - 0.209235I$ $a = 0.357696 + 0.809834I$ $b = -0.136583 - 0.767702I$	$-5.34223 - 0.90366I$	$2.99552 + 7.97302I$
$u = 0.736045 + 0.353997I$ $a = 1.99508 - 0.41979I$ $b = 1.61707 + 0.39727I$	$0.857139 - 1.116710I$	$8.63274 + 6.10960I$
$u = 0.736045 - 0.353997I$ $a = 1.99508 + 0.41979I$ $b = 1.61707 - 0.39727I$	$0.857139 + 1.116710I$	$8.63274 - 6.10960I$
$u = 1.011880 + 0.753500I$ $a = -0.801625 + 0.134986I$ $b = -0.912860 - 0.467435I$	$-1.90477 - 3.17083I$	$-2.15194 + 8.40607I$
$u = 1.011880 - 0.753500I$ $a = -0.801625 - 0.134986I$ $b = -0.912860 + 0.467435I$	$-1.90477 + 3.17083I$	$-2.15194 - 8.40607I$
$u = 0.419548$ $a = -4.82997$ $b = -2.02640$	$12.4935$	$13.9460$
$u = 1.25442 + 1.05470I$ $a = 0.452785 - 0.066086I$ $b = 0.637684 + 0.394653I$	$4.48658 - 4.37367I$	$3.76171 + 10.00302I$

	Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.25442 - 1.05470I$		
$a =$	$0.452785 + 0.066086I$	$4.48658 + 4.37367I$	$3.76171 - 10.00302I$
$b =$	$0.637684 - 0.394653I$		

$$\text{III. } I_3^u = \langle -37a^5u^2 + 123a^4u^2 + \dots - 100a + 168, a^5u^2 - 3a^4u^2 + \dots + 13a + 20, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0.110778a^5u^2 - 0.368263a^4u^2 + \dots + 0.299401a - 0.502994 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.182635a^5u^2 - 0.323353a^4u^2 + \dots - 0.371257a + 0.143713 \\ 0.365269a^5u^2 - 0.646707a^4u^2 + \dots - 0.742515a + 0.287425 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.434132a^5u^2 + 0.0838323a^4u^2 + \dots - 0.718563a - 0.592814 \\ 0.544910a^5u^2 - 0.284431a^4u^2 + \dots - 1.41916a - 1.09581 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.182635a^5u^2 - 0.323353a^4u^2 + \dots - 0.371257a + 0.143713 \\ 0.703593a^5u^2 - 1.12275a^4u^2 + \dots - 0.733533a + 0.832335 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.799401a^5u^2 - 0.0628743a^4u^2 + \dots - 0.461078a - 0.305389 \\ 0.868263a^5u^2 + 0.167665a^4u^2 + \dots - 1.43713a - 1.18563 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.00898a^5u^2 + 1.55689a^4u^2 + \dots + 0.583832a - 0.580838 \\ -0.853293a^5u^2 + 1.40419a^4u^2 + \dots + 0.964072a - 0.179641 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.407186a^5u^2 + 1.24551a^4u^2 + \dots + 0.467066a - 0.664671 \\ -0.736527a^5u^2 + 1.66467a^4u^2 + \dots + 0.874251a - 0.628743 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^3 + u^2 + 2u + 1)^6$
$c_2, c_6$	$(u^3 + u^2 - 1)^6$
$c_3, c_5, c_{10}$	$u^{18} + u^{17} + \dots + 4u - 8$
$c_4, c_7$	$u^{18} + u^{17} + \dots - 684u - 216$
$c_8, c_9, c_{12}$	$(u^3 + u^2 - 2u - 1)^6$
$c_{11}$	$u^{18} - u^{17} + \dots - 196u - 392$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^3 + 3y^2 + 2y - 1)^6$
$c_2, c_6$	$(y^3 - y^2 + 2y - 1)^6$
$c_3, c_5, c_{10}$	$y^{18} + 3y^{17} + \dots - 80y + 64$
$c_4, c_7$	$y^{18} - 21y^{17} + \dots + 55728y + 46656$
$c_8, c_9, c_{12}$	$(y^3 - 5y^2 + 6y - 1)^6$
$c_{11}$	$y^{18} - 33y^{17} + \dots - 16464y + 153664$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$ $a = 0.961970 - 0.199906I$ $b = 0.842708 + 0.290892I$	$-1.20570 - 2.82812I$	$9.50976 + 2.97945I$
$u = 0.877439 + 0.744862I$ $a = -0.641730 - 0.729183I$ $b = -0.62835 - 2.13101I$	$15.7136 - 2.8281I$	$9.50976 + 2.97945I$
$u = 0.877439 + 0.744862I$ $a = -0.721738 + 0.281163I$ $b = -0.992973 - 0.541129I$	$-1.20570 - 2.82812I$	$9.50976 + 2.97945I$
$u = 0.877439 + 0.744862I$ $a = -1.189520 - 0.508099I$ $b = -0.244232 - 0.630700I$	$4.43407 - 2.82812I$	$9.50976 + 2.97945I$
$u = 0.877439 + 0.744862I$ $a = 0.516399 + 0.280423I$ $b = 0.66526 + 1.33185I$	$4.43407 - 2.82812I$	$9.50976 + 2.97945I$
$u = 0.877439 + 0.744862I$ $a = 1.61441 + 1.05819I$ $b = 0.019938 + 1.117810I$	$15.7136 - 2.8281I$	$9.50976 + 2.97945I$
$u = 0.877439 - 0.744862I$ $a = 0.961970 + 0.199906I$ $b = 0.842708 - 0.290892I$	$-1.20570 + 2.82812I$	$9.50976 - 2.97945I$
$u = 0.877439 - 0.744862I$ $a = -0.641730 + 0.729183I$ $b = -0.62835 + 2.13101I$	$15.7136 + 2.8281I$	$9.50976 - 2.97945I$
$u = 0.877439 - 0.744862I$ $a = -0.721738 - 0.281163I$ $b = -0.992973 + 0.541129I$	$-1.20570 + 2.82812I$	$9.50976 - 2.97945I$
$u = 0.877439 - 0.744862I$ $a = -1.189520 + 0.508099I$ $b = -0.244232 + 0.630700I$	$4.43407 + 2.82812I$	$9.50976 - 2.97945I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 - 0.744862I$ $a = 0.516399 - 0.280423I$ $b = 0.66526 - 1.33185I$	$4.43407 + 2.82812I$	$9.50976 - 2.97945I$
$u = 0.877439 - 0.744862I$ $a = 1.61441 - 1.05819I$ $b = 0.019938 - 1.117810I$	$15.7136 + 2.8281I$	$9.50976 - 2.97945I$
$u = -0.754878$ $a = -0.685274 + 1.096670I$ $b = -0.517298 - 0.827854I$	$-5.34329$	$2.98050$
$u = -0.754878$ $a = -0.685274 - 1.096670I$ $b = -0.517298 + 0.827854I$	$-5.34329$	$2.98050$
$u = -0.754878$ $a = -1.95258$ $b = -2.71504$	$11.5760$	$2.98050$
$u = -0.754878$ $a = 1.92010 + 0.60556I$ $b = 1.44944 - 0.45713I$	$0.296489$	$2.98050$
$u = -0.754878$ $a = 1.92010 - 0.60556I$ $b = 1.44944 + 0.45713I$	$0.296489$	$2.98050$
$u = -0.754878$ $a = -3.59666$ $b = -1.47396$	$11.5760$	$2.98050$



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^3 + u^2 + 2u + 1)^6)(u^{11} - 5u^{10} + \dots + 11u - 1)$ $\cdot (u^{17} + 6u^{16} + \dots + 480u + 64)$
$c_2$	$(u^3 + u^2 - 1)^6$ $\cdot (u^{11} - 3u^{10} + 2u^9 + 5u^8 - 6u^7 - 5u^6 + 10u^5 + 2u^4 - 8u^3 + u^2 + 3u - 1)$ $\cdot (u^{17} - 6u^{16} + \dots + 56u - 8)$
$c_3, c_{10}$	$(u^{11} + 4u^9 + u^8 + 4u^7 + 4u^6 - u^5 + 5u^4 - 2u^3 + 3u^2 - u + 1)$ $\cdot (u^{17} - u^{15} + \dots + 3u - 1)(u^{18} + u^{17} + \dots + 4u - 8)$
$c_4$	$(u^{11} + 3u^9 + 6u^8 + u^7 + 20u^6 - 4u^5 + 26u^4 - 6u^3 + 15u^2 - 4u + 3)$ $\cdot (u^{17} + 4u^{16} + \dots + 8u - 1)(u^{18} + u^{17} + \dots - 684u - 216)$
$c_5$	$(u^{11} + 4u^9 - u^8 + 4u^7 - 4u^6 - u^5 - 5u^4 - 2u^3 - 3u^2 - u - 1)$ $\cdot (u^{17} - u^{15} + \dots + 3u - 1)(u^{18} + u^{17} + \dots + 4u - 8)$
$c_6$	$(u^3 + u^2 - 1)^6$ $\cdot (u^{11} + 3u^{10} + 2u^9 - 5u^8 - 6u^7 + 5u^6 + 10u^5 - 2u^4 - 8u^3 - u^2 + 3u + 1)$ $\cdot (u^{17} - 6u^{16} + \dots + 56u - 8)$
$c_7$	$(u^{11} + 3u^9 - 6u^8 + u^7 - 20u^6 - 4u^5 - 26u^4 - 6u^3 - 15u^2 - 4u - 3)$ $\cdot (u^{17} + 4u^{16} + \dots + 8u - 1)(u^{18} + u^{17} + \dots - 684u - 216)$
$c_8, c_9$	$(u^3 + u^2 - 2u - 1)^6$ $\cdot (u^{11} - 8u^9 - u^8 + 23u^7 + 5u^6 - 28u^5 - 7u^4 + 13u^3 + 2u^2 - 2u - 1)$ $\cdot (u^{17} - 7u^{16} + \dots + 20u - 8)$
$c_{11}$	$(u^{11} + 7u^9 - 22u^8 + 7u^7 - 56u^6 - 3u^5 - 45u^4 - 6u^3 - 12u^2 - u - 1)$ $\cdot (u^{17} - 2u^{16} + \dots + u - 1)(u^{18} - u^{17} + \dots - 196u - 392)$
$c_{12}$	$(u^3 + u^2 - 2u - 1)^6$ $\cdot (u^{11} - 8u^9 + u^8 + 23u^7 - 5u^6 - 28u^5 + 7u^4 + 13u^3 - 2u^2 - 2u + 1)$ $\cdot (u^{17} - 7u^{16} + \dots + 20u - 8)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^3 + 3y^2 + 2y - 1)^6)(y^{11} + 19y^{10} + \dots + 31y - 1)$ $\cdot (y^{17} + 22y^{16} + \dots + 66048y - 4096)$
$c_2, c_6$	$((y^3 - y^2 + 2y - 1)^6)(y^{11} - 5y^{10} + \dots + 11y - 1)$ $\cdot (y^{17} - 6y^{16} + \dots + 480y - 64)$
$c_3, c_5, c_{10}$	$(y^{11} + 8y^{10} + \dots - 5y - 1)(y^{17} - 2y^{16} + \dots + 3y - 1)$ $\cdot (y^{18} + 3y^{17} + \dots - 80y + 64)$
$c_4, c_7$	$(y^{11} + 6y^{10} + \dots - 74y - 9)(y^{17} - 36y^{16} + \dots + 102y - 1)$ $\cdot (y^{18} - 21y^{17} + \dots + 55728y + 46656)$
$c_8, c_9, c_{12}$	$((y^3 - 5y^2 + 6y - 1)^6)(y^{11} - 16y^{10} + \dots + 8y - 1)$ $\cdot (y^{17} - 21y^{16} + \dots + 272y - 64)$
$c_{11}$	$(y^{11} + 14y^{10} + \dots - 23y - 1)(y^{17} - 44y^{16} + \dots + 33y - 1)$ $\cdot (y^{18} - 33y^{17} + \dots - 16464y + 153664)$