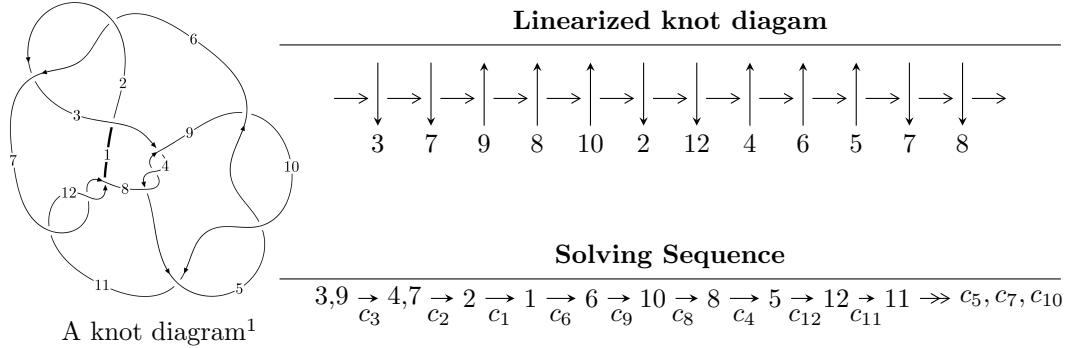


## $12n_{0602}$ ( $K12n_{0602}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -u^9 - 3u^8 - 7u^7 - 10u^6 - 9u^5 + 2u^4 + 5u^3 + 11u^2 + 8b - 6u - 2, \\
 &\quad u^8 + 5u^6 - u^5 + 6u^4 - 2u^3 + u^2 + 4a + 2u - 2, u^{10} + 6u^8 - 3u^7 + 11u^6 - 13u^5 + 9u^4 - 12u^3 + 7u^2 + 2 \rangle \\
 I_2^u &= \langle -937u^{13} - 2472u^{12} + \dots + 1987b - 6836, 12531u^{13} + 27338u^{12} + \dots + 19870a + 85927, \\
 &\quad u^{14} + 3u^{13} + \dots + 22u + 5 \rangle \\
 I_3^u &= \langle -u^4a - u^2a - u^3 - au + b + a - u - 1, \\
 &\quad -2u^5a - 2u^4a + u^5 - 6u^3a + u^4 - 6u^2a + 2u^3 + 2a^2 - 6au + 3u^2 - 6a + u + 3, \\
 &\quad u^6 + 3u^4 + u^3 + 2u^2 + 2u - 1 \rangle \\
 I_4^u &= \langle 2u^9a + 10u^9 + \dots + 7a + 1, -2u^9 + 3u^8 + \dots + a^2 - 4, u^{10} - u^9 + 4u^8 - 4u^7 + 6u^6 - 6u^5 + 3u^4 - 3u^3 + 1 \rangle \\
 I_5^u &= \langle b - 1, 6a - u - 3, u^2 + 3 \rangle \\
 I_6^u &= \langle b - u, 2a + u + 1, u^2 + 1 \rangle
 \end{aligned}$$

$$I_1^v = \langle a, b - 1, v + 1 \rangle$$

\* 7 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 61 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^9 - 3u^8 + \dots + 8b - 2, u^8 + 5u^6 - u^5 + 6u^4 - 2u^3 + u^2 + 4a + 2u - 2, u^{10} + 6u^8 + \dots + 7u^2 + 2 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{1}{4}u^8 - \frac{5}{4}u^6 + \dots - \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{8}u^9 + \frac{3}{8}u^8 + \dots + \frac{3}{4}u + \frac{1}{4} \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{4}u^8 - \frac{5}{4}u^6 + \dots - \frac{1}{2}u + \frac{1}{2} \\ -\frac{3}{8}u^9 + \frac{3}{8}u^8 + \dots - \frac{5}{4}u + \frac{1}{4} \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{3}{8}u^9 + \frac{1}{8}u^8 + \dots - \frac{7}{4}u + \frac{3}{4} \\ -\frac{3}{8}u^9 + \frac{3}{8}u^8 + \dots - \frac{5}{4}u + \frac{1}{4} \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ \frac{1}{2}u^9 + \frac{1}{2}u^8 + \dots + u + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ \frac{1}{2}u^9 - \frac{1}{2}u^8 + \dots + 2u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} \frac{1}{4}u^8 + \frac{5}{4}u^6 + \dots - \frac{3}{2}u + \frac{1}{2} \\ -\frac{1}{8}u^9 + \frac{1}{8}u^8 + \dots - \frac{3}{4}u + \frac{3}{4} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^3 - 2u \\ -\frac{1}{2}u^9 + \frac{1}{2}u^8 + \dots - 2u + 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = \frac{3}{2}u^9 - \frac{1}{2}u^8 + \frac{17}{2}u^7 - 8u^6 + \frac{25}{2}u^5 - 25u^4 + \frac{17}{2}u^3 - \frac{27}{2}u^2 + 13u + 1$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{10} + u^9 + 2u^8 - 3u^7 + 12u^6 + 24u^5 + 46u^4 + 37u^3 + 7u^2 - 3u + 4$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$u^{10} - 3u^9 + 4u^8 - u^7 - 4u^6 + 6u^5 - 3u^3 + u^2 + u + 2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$u^{10} + 6u^8 + 3u^7 + 11u^6 + 13u^5 + 9u^4 + 12u^3 + 7u^2 + 2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{10} + 3y^9 + \cdots + 47y + 16$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$y^{10} - y^9 + 2y^8 + 3y^7 + 12y^6 - 24y^5 + 46y^4 - 37y^3 + 7y^2 + 3y + 4$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$y^{10} + 12y^9 + \cdots + 28y + 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.849669 + 0.278925I$		
$a = 0.126908 - 1.402190I$	$2.59736 + 5.48528I$	$0.63906 - 6.67204I$
$b = -0.935978 + 0.707374I$		
$u = 0.849669 - 0.278925I$		
$a = 0.126908 + 1.402190I$	$2.59736 - 5.48528I$	$0.63906 + 6.67204I$
$b = -0.935978 - 0.707374I$		
$u = -0.179655 + 1.191160I$		
$a = 0.250838 - 0.636140I$	$-2.21767 - 1.59735I$	$-7.51312 + 4.64580I$
$b = -0.46356 + 1.36046I$		
$u = -0.179655 - 1.191160I$		
$a = 0.250838 + 0.636140I$	$-2.21767 + 1.59735I$	$-7.51312 - 4.64580I$
$b = -0.46356 - 1.36046I$		
$u = -0.44148 + 1.44610I$		
$a = -0.552527 + 1.275850I$	$-8.2686 - 15.1646I$	$-7.51854 + 8.25672I$
$b = -1.28583 - 0.66001I$		
$u = -0.44148 - 1.44610I$		
$a = -0.552527 - 1.275850I$	$-8.2686 + 15.1646I$	$-7.51854 - 8.25672I$
$b = -1.28583 + 0.66001I$		
$u = -0.171957 + 0.454648I$		
$a = 0.655512 - 0.286314I$	$0.087563 - 1.088810I$	$1.48967 + 6.22992I$
$b = 0.281118 + 0.559566I$		
$u = -0.171957 - 0.454648I$		
$a = 0.655512 + 0.286314I$	$0.087563 + 1.088810I$	$1.48967 - 6.22992I$
$b = 0.281118 - 0.559566I$		
$u = -0.05658 + 1.78531I$		
$a = 0.519269 + 0.055233I$	$-16.0502 + 0.8822I$	$-5.09706 - 8.51458I$
$b = 0.904241 - 0.202548I$		
$u = -0.05658 - 1.78531I$		
$a = 0.519269 - 0.055233I$	$-16.0502 - 0.8822I$	$-5.09706 + 8.51458I$
$b = 0.904241 + 0.202548I$		

$$\text{II. } I_2^u = \langle -937u^{13} - 2472u^{12} + \cdots + 1987b - 6836, 12531u^{13} + 27338u^{12} + \cdots + 19870a + 85927, u^{14} + 3u^{13} + \cdots + 22u + 5 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.630649u^{13} - 1.37584u^{12} + \cdots - 15.3917u - 4.32446 \\ 0.471565u^{13} + 1.24409u^{12} + \cdots + 9.17765u + 3.44036 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.253296u^{13} + 0.379668u^{12} + \cdots + 0.855511u + 0.00558631 \\ -0.425264u^{13} - 0.827378u^{12} + \cdots - 8.90941u - 2.81228 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.171968u^{13} - 0.447710u^{12} + \cdots - 8.05390u - 2.80669 \\ -0.425264u^{13} - 0.827378u^{12} + \cdots - 8.90941u - 2.81228 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.693105u^{13} - 1.63795u^{12} + \cdots - 20.3068u - 6.28908 \\ 0.351787u^{13} + 1.16608u^{12} + \cdots + 6.24459u + 3.20684 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.241369u^{13} - 0.372320u^{12} + \cdots - 0.359235u + 0.934474 \\ 0.330649u^{13} + 0.975843u^{12} + \cdots + 16.4917u + 5.22446 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.342577u^{13} - 0.983191u^{12} + \cdots - 14.9880u - 5.16452 \\ -0.112733u^{13} - 0.0145949u^{12} + \cdots - 3.34877u - 0.572723 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0892803u^{13} - 0.603523u^{12} + \cdots - 14.1325u - 6.15893 \\ -0.537997u^{13} - 0.841973u^{12} + \cdots - 12.2582u - 3.38500 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $\frac{2058}{1987}u^{13} + \frac{6600}{1987}u^{12} + \cdots + \frac{37538}{1987}u + \frac{12194}{1987}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^7 + 3u^6 + 7u^5 + 8u^4 + 9u^3 + 6u^2 + 5u + 1)^2$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$(u^7 + u^6 - u^5 - 2u^4 + u^3 + 2u^2 + u - 1)^2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$u^{14} - 3u^{13} + \dots - 22u + 5$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^7 + 5y^6 + 19y^5 + 36y^4 + 49y^3 + 38y^2 + 13y - 1)^2$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$(y^7 - 3y^6 + 7y^5 - 8y^4 + 9y^3 - 6y^2 + 5y - 1)^2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$y^{14} + 11y^{13} + \dots - 4y + 25$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.370785 + 0.946704I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.209881 - 0.303567I$	$0.562491 - 0.955395I$	$0.68929 + 2.37083I$
$b = 0.597306 + 0.773845I$		
$u = 0.370785 - 0.946704I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.209881 + 0.303567I$	$0.562491 + 0.955395I$	$0.68929 - 2.37083I$
$b = 0.597306 - 0.773845I$		
$u = -1.022710 + 0.247588I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.520411 - 1.220230I$	$-2.92618 - 9.93065I$	$-4.46028 + 7.33664I$
$b = 1.139460 + 0.630170I$		
$u = -1.022710 - 0.247588I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.520411 + 1.220230I$	$-2.92618 + 9.93065I$	$-4.46028 - 7.33664I$
$b = 1.139460 - 0.630170I$		
$u = 0.306472 + 1.132160I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.482637 - 0.675154I$	$-4.24127$	$-5.93921 + 0.I$
$b = -0.502855$		
$u = 0.306472 - 1.132160I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.482637 + 0.675154I$	$-4.24127$	$-5.93921 + 0.I$
$b = -0.502855$		
$u = -0.736932 + 1.071510I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.318588 - 0.053278I$	$-5.38528 + 3.93070I$	$-6.25941 - 4.87230I$
$b = -0.985336 + 0.506466I$		
$u = -0.736932 - 1.071510I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.318588 + 0.053278I$	$-5.38528 - 3.93070I$	$-6.25941 + 4.87230I$
$b = -0.985336 - 0.506466I$		
$u = -0.538570 + 0.272073I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.71818 - 1.43908I$	$0.562491 - 0.955395I$	$0.68929 + 2.37083I$
$b = 0.597306 + 0.773845I$		
$u = -0.538570 - 0.272073I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.71818 + 1.43908I$	$0.562491 + 0.955395I$	$0.68929 - 2.37083I$
$b = 0.597306 - 0.773845I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.36817 + 1.45006I$		
$a = 0.797752 + 1.077130I$	$-2.92618 + 9.93065I$	$-4.46028 - 7.33664I$
$b = 1.139460 - 0.630170I$		
$u = 0.36817 - 1.45006I$		
$a = 0.797752 - 1.077130I$	$-2.92618 - 9.93065I$	$-4.46028 + 7.33664I$
$b = 1.139460 + 0.630170I$		
$u = -0.24721 + 1.49766I$		
$a = -0.921588 + 0.632363I$	$-5.38528 - 3.93070I$	$-6.25941 + 4.87230I$
$b = -0.985336 - 0.506466I$		
$u = -0.24721 - 1.49766I$		
$a = -0.921588 - 0.632363I$	$-5.38528 + 3.93070I$	$-6.25941 - 4.87230I$
$b = -0.985336 + 0.506466I$		

$$\text{III. } I_3^u = \langle -u^4a - u^2a - u^3 - au + b + a - u - 1, -2u^5a + u^5 + \dots - 6a + 3, u^6 + 3u^4 + u^3 + 2u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} a \\ u^4a + u^2a + u^3 + au - a + u + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} a \\ u^5a + 2u^3a + u^2a - u^3 - u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^5a + 2u^3a + u^2a - u^3 + a - u - 1 \\ u^5a + 2u^3a + u^2a - u^3 - u - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^5 + u^4 + 2u^3 + 2u^2 + u - 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u^5 - u^4 + u^3 - u^2 - 2u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^3a - u^3 + au + a - 2u - 1 \\ -1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^3 - 2u \\ u^4 + u^3 + u^2 + 2u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^5 + 4u^4 + 8u^3 + 12u^2 + 4u + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} + 7u^{11} + \cdots + 438u + 169$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$u^{12} - 3u^{11} + \cdots + 42u - 13$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$(u^6 + 3u^4 - u^3 + 2u^2 - 2u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} - 3y^{11} + \cdots - 59686y + 28561$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$y^{12} - 7y^{11} + \cdots - 438y + 169$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$(y^6 + 6y^5 + 13y^4 + 9y^3 - 6y^2 - 8y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.841864$		
$a = 0.445035 + 1.177780I$	3.23778	2.68180
$b = -0.719261 - 0.742974I$		
$u = -0.841864$		
$a = 0.445035 - 1.177780I$	3.23778	2.68180
$b = -0.719261 + 0.742974I$		
$u = -0.126468 + 1.352400I$		
$a = -0.034921 + 1.148040I$	$-11.65360 - 3.39374I$	$-10.36018 + 3.51762I$
$b = -1.026470 - 0.870245I$		
$u = -0.126468 + 1.352400I$		
$a = 0.383840 + 0.027542I$	$-11.65360 - 3.39374I$	$-10.36018 + 3.51762I$
$b = 1.59190 - 0.18598I$		
$u = -0.126468 - 1.352400I$		
$a = -0.034921 - 1.148040I$	$-11.65360 + 3.39374I$	$-10.36018 - 3.51762I$
$b = -1.026470 + 0.870245I$		
$u = -0.126468 - 1.352400I$		
$a = 0.383840 - 0.027542I$	$-11.65360 + 3.39374I$	$-10.36018 - 3.51762I$
$b = 1.59190 + 0.18598I$		
$u = 0.376468 + 1.319680I$		
$a = -0.443330 - 1.186910I$	$-5.05799 + 8.77346I$	$-5.56216 - 5.90094I$
$b = -1.27617 + 0.73937I$		
$u = 0.376468 + 1.319680I$		
$a = 0.392175 + 0.613857I$	$-5.05799 + 8.77346I$	$-5.56216 - 5.90094I$
$b = -0.260915 - 1.156860I$		
$u = 0.376468 - 1.319680I$		
$a = -0.443330 + 1.186910I$	$-5.05799 - 8.77346I$	$-5.56216 + 5.90094I$
$b = -1.27617 - 0.73937I$		
$u = 0.376468 - 1.319680I$		
$a = 0.392175 - 0.613857I$	$-5.05799 - 8.77346I$	$-5.56216 + 5.90094I$
$b = -0.260915 + 1.156860I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.341865$		
$a = 0.468459$	-2.71328	5.16290
$b = 1.13466$		
$u = 0.341865$		
$a = 4.04594$	-2.71328	5.16290
$b = -0.752839$		

**IV.**

$$I_4^u = \langle 2u^9a + 10u^9 + \dots + 7a + 1, -2u^9 + 3u^8 + \dots + a^2 - 4, u^{10} - u^9 + \dots - 3u^3 + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ -0.117647au^9 - 0.588235u^9 + \dots - 0.411765a - 0.0588235 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.588235au^9 + 0.0588235u^9 + \dots - 0.0588235a + 2.70588 \\ 0.176471au^9 - 0.117647u^9 + \dots + 0.117647a - 1.41176 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.411765au^9 - 0.0588235u^9 + \dots + 0.0588235a + 1.29412 \\ 0.176471au^9 - 0.117647u^9 + \dots + 0.117647a - 1.41176 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^9 - 4u^7 - 5u^5 + 3u \\ u^9 + 3u^7 + 3u^5 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^9 - u^8 + 8u^7 - 5u^6 + 12u^5 - 9u^4 + 6u^3 - 6u^2 - u - 1 \\ -2u^9 + u^8 - 8u^7 + 4u^6 - 12u^5 + 6u^4 - 5u^3 + 4u^2 + 3u + 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.588235au^9 + 0.0588235u^9 + \dots - 0.0588235a + 0.705882 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^6 + 3u^4 + 2u^2 - 1 \\ -u^6 - 2u^4 - u^2 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^9 - 12u^7 - 12u^5 + 4u^3 + 8u - 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{10} + 5u^9 + \dots + 4u + 1)^2$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$(u^{10} + u^9 - 2u^8 - 4u^7 + 4u^5 + 3u^4 - u^3 - 2u^2 + 1)^2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$(u^{10} + u^9 + 4u^8 + 4u^7 + 6u^6 + 6u^5 + 3u^4 + 3u^3 + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{10} - y^9 - 6y^7 + 22y^6 + 6y^5 + 45y^4 + 15y^3 + 22y^2 + 4y + 1)^2$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$(y^{10} - 5y^9 + \dots - 4y + 1)^2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$(y^{10} + 7y^9 + 20y^8 + 26y^7 + 6y^6 - 22y^5 - 19y^4 + 3y^3 + 6y^2 + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.839548 + 0.070481I$	$-0.70717 + 4.40083I$	$-1.25569 - 3.49859I$
$a = -0.900079 + 0.957609I$		
$b = 1.018500 - 0.644891I$		
$u = 0.839548 + 0.070481I$	$-0.70717 + 4.40083I$	$-1.25569 - 3.49859I$
$a = 0.01855 - 1.45994I$		
$b = 0.400287 + 0.864056I$		
$u = 0.839548 - 0.070481I$	$-0.70717 - 4.40083I$	$-1.25569 + 3.49859I$
$a = -0.900079 - 0.957609I$		
$b = 1.018500 + 0.644891I$		
$u = 0.839548 - 0.070481I$	$-0.70717 - 4.40083I$	$-1.25569 + 3.49859I$
$a = 0.01855 + 1.45994I$		
$b = 0.400287 - 0.864056I$		
$u = 0.090539 + 1.215350I$	$-6.25064 + 1.53058I$	$-5.48489 - 4.43065I$
$a = -1.57349 + 0.24896I$		
$b = -1.236040 - 0.156723I$		
$u = 0.090539 + 1.215350I$	$-6.25064 + 1.53058I$	$-5.48489 - 4.43065I$
$a = 0.23726 + 1.84586I$		
$b = 0.926127 - 0.393188I$		
$u = 0.090539 - 1.215350I$	$-6.25064 - 1.53058I$	$-5.48489 + 4.43065I$
$a = -1.57349 - 0.24896I$		
$b = -1.236040 + 0.156723I$		
$u = 0.090539 - 1.215350I$	$-6.25064 - 1.53058I$	$-5.48489 + 4.43065I$
$a = 0.23726 - 1.84586I$		
$b = 0.926127 + 0.393188I$		
$u = 0.383413 + 1.200420I$	$-4.17865$	$-4.51886 + 0.I$
$a = -0.734177 - 0.829669I$		
$b = -0.608868 + 0.334904I$		
$u = 0.383413 + 1.200420I$	$-4.17865$	$-4.51886 + 0.I$
$a = -0.073892 - 0.370754I$		
$b = -0.608868 - 0.334904I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.383413 - 1.200420I$		
$a = -0.734177 + 0.829669I$	-4.17865	$-4.51886 + 0.I$
$b = -0.608868 - 0.334904I$		
$u = 0.383413 - 1.200420I$		
$a = -0.073892 + 0.370754I$	-4.17865	$-4.51886 + 0.I$
$b = -0.608868 + 0.334904I$		
$u = -0.383851 + 1.270630I$		
$a = 0.614423 - 1.130320I$	-0.70717 - 4.40083I	$-1.25569 + 3.49859I$
$b = 1.018500 + 0.644891I$		
$u = -0.383851 + 1.270630I$		
$a = -0.272551 + 0.291529I$	-0.70717 - 4.40083I	$-1.25569 + 3.49859I$
$b = 0.400287 - 0.864056I$		
$u = -0.383851 - 1.270630I$		
$a = 0.614423 + 1.130320I$	-0.70717 + 4.40083I	$-1.25569 - 3.49859I$
$b = 1.018500 - 0.644891I$		
$u = -0.383851 - 1.270630I$		
$a = -0.272551 - 0.291529I$	-0.70717 + 4.40083I	$-1.25569 - 3.49859I$
$b = 0.400287 + 0.864056I$		
$u = -0.429649 + 0.392970I$		
$a = 1.58670 - 1.31909I$	-6.25064 - 1.53058I	$-5.48489 + 4.43065I$
$b = -1.236040 + 0.156723I$		
$u = -0.429649 + 0.392970I$		
$a = -2.40274 - 2.38405I$	-6.25064 - 1.53058I	$-5.48489 + 4.43065I$
$b = 0.926127 + 0.393188I$		
$u = -0.429649 - 0.392970I$		
$a = 1.58670 + 1.31909I$	-6.25064 + 1.53058I	$-5.48489 - 4.43065I$
$b = -1.236040 - 0.156723I$		
$u = -0.429649 - 0.392970I$		
$a = -2.40274 + 2.38405I$	-6.25064 + 1.53058I	$-5.48489 - 4.43065I$
$b = 0.926127 - 0.393188I$		

$$\mathbf{V} \cdot I_5^u = \langle b - 1, \ 6a - u - 3, \ u^2 + 3 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 3 \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{6}u + \frac{1}{2} \\ 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{6}u + \frac{1}{2} \\ -1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{1}{6}u - \frac{1}{2} \\ -1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ -2u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2 \\ -3 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -\frac{7}{6}u - \frac{1}{2} \\ -2u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ -2u \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = 1

(iii) **Cusp Shapes** = -12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$	$(u - 1)^2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$u^2 + 3$
$c_6, c_{11}, c_{12}$	$(u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{11}, c_{12}$	$(y - 1)^2$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$(y + 3)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.73205I$		
$a = 0.500000 + 0.288675I$	-16.4493	-12.0000
$b = 1.00000$		
$u = -1.73205I$		
$a = 0.500000 - 0.288675I$	-16.4493	-12.0000
$b = 1.00000$		

$$\text{VI. } I_6^u = \langle b - u, 2a + u + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{1}{2}u - \frac{1}{2} \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{1}{2}u + \frac{1}{2} \\ 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{1}{2}u + \frac{3}{2} \\ 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -1 \\ 2u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u + 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} \frac{1}{2}u + \frac{1}{2} \\ 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -4

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u + 1)^2$
$c_2, c_3, c_4$	
$c_5, c_6, c_7$	
$c_8, c_9, c_{10}$	$u^2 + 1$
$c_{11}, c_{12}$	

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^2$
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$(y + 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$		
$a = -0.500000 - 0.500000I$	-1.64493	-4.00000
$b = 1.000000I$		
$u = -1.000000I$		
$a = -0.500000 + 0.500000I$	-1.64493	-4.00000
$b = -1.000000I$		

$$\text{VII. } I_1^v = \langle a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$	$u - 1$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$u$
$c_6, c_{11}, c_{12}$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_7, c_{11}, c_{12}$	$y - 1$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	-3.28987	-12.0000
$b = 1.00000$		

### VIII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^3(u + 1)^2(u^7 + 3u^6 + 7u^5 + 8u^4 + 9u^3 + 6u^2 + 5u + 1)^2$ $\cdot (u^{10} + u^9 + 2u^8 - 3u^7 + 12u^6 + 24u^5 + 46u^4 + 37u^3 + 7u^2 - 3u + 4)$ $\cdot ((u^{10} + 5u^9 + \dots + 4u + 1)^2)(u^{12} + 7u^{11} + \dots + 438u + 169)$
$c_2, c_7$	$(u - 1)^3(u^2 + 1)(u^7 + u^6 - u^5 - 2u^4 + u^3 + 2u^2 + u - 1)^2$ $\cdot (u^{10} - 3u^9 + 4u^8 - u^7 - 4u^6 + 6u^5 - 3u^3 + u^2 + u + 2)$ $\cdot (u^{10} + u^9 - 2u^8 - 4u^7 + 4u^5 + 3u^4 - u^3 - 2u^2 + 1)^2$ $\cdot (u^{12} - 3u^{11} + \dots + 42u - 13)$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$u(u^2 + 1)(u^2 + 3)(u^6 + 3u^4 - u^3 + 2u^2 - 2u - 1)^2$ $\cdot (u^{10} + 6u^8 + 3u^7 + 11u^6 + 13u^5 + 9u^4 + 12u^3 + 7u^2 + 2)$ $\cdot (u^{10} + u^9 + 4u^8 + 4u^7 + 6u^6 + 6u^5 + 3u^4 + 3u^3 + 1)^2$ $\cdot (u^{14} - 3u^{13} + \dots - 22u + 5)$
$c_6, c_{11}, c_{12}$	$(u + 1)^3(u^2 + 1)(u^7 + u^6 - u^5 - 2u^4 + u^3 + 2u^2 + u - 1)^2$ $\cdot (u^{10} - 3u^9 + 4u^8 - u^7 - 4u^6 + 6u^5 - 3u^3 + u^2 + u + 2)$ $\cdot (u^{10} + u^9 - 2u^8 - 4u^7 + 4u^5 + 3u^4 - u^3 - 2u^2 + 1)^2$ $\cdot (u^{12} - 3u^{11} + \dots + 42u - 13)$

## IX. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)^5(y^7 + 5y^6 + 19y^5 + 36y^4 + 49y^3 + 38y^2 + 13y - 1)^2$ $\cdot (y^{10} - y^9 - 6y^7 + 22y^6 + 6y^5 + 45y^4 + 15y^3 + 22y^2 + 4y + 1)^2$ $\cdot (y^{10} + 3y^9 + \dots + 47y + 16)(y^{12} - 3y^{11} + \dots - 59686y + 28561)$
$c_2, c_6, c_7$ $c_{11}, c_{12}$	$(y - 1)^3(y + 1)^2(y^7 - 3y^6 + 7y^5 - 8y^4 + 9y^3 - 6y^2 + 5y - 1)^2$ $\cdot (y^{10} - 5y^9 + \dots - 4y + 1)^2$ $\cdot (y^{10} - y^9 + 2y^8 + 3y^7 + 12y^6 - 24y^5 + 46y^4 - 37y^3 + 7y^2 + 3y + 4)$ $\cdot (y^{12} - 7y^{11} + \dots - 438y + 169)$
$c_3, c_4, c_5$ $c_8, c_9, c_{10}$	$y(y + 1)^2(y + 3)^2(y^6 + 6y^5 + 13y^4 + 9y^3 - 6y^2 - 8y + 1)^2$ $\cdot (y^{10} + 7y^9 + 20y^8 + 26y^7 + 6y^6 - 22y^5 - 19y^4 + 3y^3 + 6y^2 + 1)^2$ $\cdot (y^{10} + 12y^9 + \dots + 28y + 4)(y^{14} + 11y^{13} + \dots - 4y + 25)$