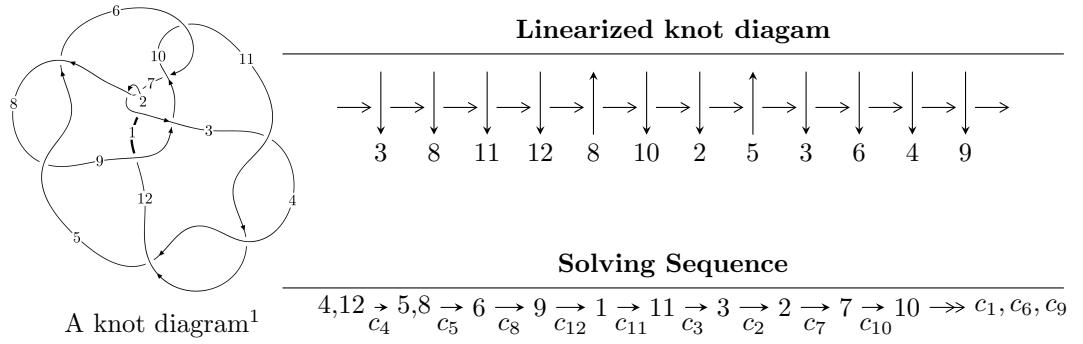


## $12n_{0653}$ ( $K12n_{0653}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 15u^{19} + 52u^{18} + \dots + b - 21, 21u^{19} + 75u^{18} + \dots + 2a - 23, u^{20} + 5u^{19} + \dots + u - 2 \rangle \\
 I_2^u &= \langle 2u^{12} - 2u^{11} - 11u^{10} + 8u^9 + 23u^8 - 5u^7 - 22u^6 - 13u^5 + 4u^4 + 16u^3 + 8u^2 + b - u - 2, \\
 &\quad 2u^{12} - 2u^{11} - 12u^{10} + 9u^9 + 28u^8 - 9u^7 - 31u^6 - 10u^5 + 11u^4 + 20u^3 + 8u^2 + a - 6u - 5, \\
 &\quad u^{13} - 2u^{12} - 5u^{11} + 10u^{10} + 10u^9 - 16u^8 - 13u^7 + 6u^6 + 12u^5 + 8u^4 - 4u^3 - 7u^2 - 2u + 1 \rangle \\
 I_3^u &= \langle u^5 - u^4 - 2u^3 - au + u^2 + b + u + 1, -u^5a - 4u^5 + 4u^3a + u^4 + 11u^3 + a^2 - 3au + u^2 - 2a - 4u - 6, \\
 &\quad u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 15u^{19} + 52u^{18} + \dots + b - 21, 21u^{19} + 75u^{18} + \dots + 2a - 23, u^{20} + 5u^{19} + \dots + u - 2 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -10.5000u^{19} - 37.5000u^{18} + \dots - 17.5000u + 11.5000 \\ -15u^{19} - 52u^{18} + \dots - 22u + 21 \end{pmatrix} \\ a_6 &= \begin{pmatrix} \frac{11}{2}u^{19} + \frac{37}{2}u^{18} + \dots + \frac{11}{2}u - \frac{11}{2} \\ 9u^{19} + 30u^{18} + \dots + 12u - 11 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{5}{2}u^{19} - \frac{19}{2}u^{18} + \dots - \frac{7}{2}u + \frac{5}{2} \\ 4u^{19} + 13u^{18} + \dots + 6u - 3 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{5}{2}u^{19} - \frac{17}{2}u^{18} + \dots - \frac{7}{2}u + \frac{7}{2} \\ -6u^{19} - 20u^{18} + \dots - 7u + 7 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{5}{2}u^{19} + \frac{19}{2}u^{18} + \dots + \frac{9}{2}u - \frac{7}{2} \\ 3u^{19} + 12u^{18} + \dots + 7u - 5 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -23u^{19} - 80u^{18} + \dots - 34u + 27 \\ -32u^{19} - 110u^{18} + \dots - 45u + 42 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -22.5000u^{19} - 78.5000u^{18} + \dots - 33.5000u + 27.5000 \\ -29u^{19} - 100u^{18} + \dots - 41u + 39 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes**

$$\begin{aligned} &= -15u^{19} - 52u^{18} + 51u^{17} + 300u^{16} - 63u^{15} - 689u^{14} + 302u^{13} + 905u^{12} - 1067u^{11} - \\ &777u^{10} + 1394u^9 + 39u^8 - 722u^7 + 587u^6 + 181u^5 + 7u^4 + 174u^3 - 147u^2 - 9u + 12 \end{aligned}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{20} + 31u^{19} + \cdots - 5u + 1$
$c_2, c_7, c_{12}$	$u^{20} + u^{19} + \cdots - 3u - 1$
$c_3, c_4, c_{11}$	$u^{20} + 5u^{19} + \cdots + u - 2$
$c_5, c_8$	$u^{20} - u^{19} + \cdots - 7u + 1$
$c_6, c_{10}$	$u^{20} + 14u^{19} + \cdots + 608u + 64$
$c_9$	$u^{20} - 26u^{18} + \cdots - 494u - 599$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{20} - 103y^{19} + \cdots - 159y + 1$
$c_2, c_7, c_{12}$	$y^{20} - 31y^{19} + \cdots + 5y + 1$
$c_3, c_4, c_{11}$	$y^{20} - 21y^{19} + \cdots - 61y + 4$
$c_5, c_8$	$y^{20} + 29y^{19} + \cdots - 55y + 1$
$c_6, c_{10}$	$y^{20} + 6y^{19} + \cdots - 33792y + 4096$
$c_9$	$y^{20} - 52y^{19} + \cdots + 2577254y + 358801$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.537648 + 0.858586I$		
$a = 0.960669 - 0.049342I$	$-14.2098 + 2.1239I$	$-11.72729 + 0.16245I$
$b = -0.558866 - 0.798289I$		
$u = 0.537648 - 0.858586I$		
$a = 0.960669 + 0.049342I$	$-14.2098 - 2.1239I$	$-11.72729 - 0.16245I$
$b = -0.558866 + 0.798289I$		
$u = 0.606622 + 0.819368I$		
$a = -0.914544 - 0.419396I$	$-14.4361 - 7.6779I$	$-11.74067 + 4.57873I$
$b = 0.211143 + 1.003760I$		
$u = 0.606622 - 0.819368I$		
$a = -0.914544 + 0.419396I$	$-14.4361 + 7.6779I$	$-11.74067 - 4.57873I$
$b = 0.211143 - 1.003760I$		
$u = -1.223290 + 0.229738I$		
$a = -0.518734 - 0.448442I$	$-1.41396 + 1.68379I$	$-7.75011 + 2.58763I$
$b = -0.737585 - 0.429401I$		
$u = -1.223290 - 0.229738I$		
$a = -0.518734 + 0.448442I$	$-1.41396 - 1.68379I$	$-7.75011 - 2.58763I$
$b = -0.737585 + 0.429401I$		
$u = -0.087774 + 0.628145I$		
$a = 0.205193 + 0.654515I$	$2.02337 + 1.45900I$	$-2.57228 - 5.20755I$
$b = 0.429141 - 0.071442I$		
$u = -0.087774 - 0.628145I$		
$a = 0.205193 - 0.654515I$	$2.02337 - 1.45900I$	$-2.57228 + 5.20755I$
$b = 0.429141 + 0.071442I$		
$u = 1.382330 + 0.213207I$		
$a = -0.232569 + 0.103641I$	$-2.65671 - 4.43053I$	$-10.17327 + 4.41788I$
$b = 0.343585 - 0.093682I$		
$u = 1.382330 - 0.213207I$		
$a = -0.232569 - 0.103641I$	$-2.65671 + 4.43053I$	$-10.17327 - 4.41788I$
$b = 0.343585 + 0.093682I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.43646$		
$a = 0.235964$	-6.53090	-14.6160
$b = -0.338953$		
$u = -1.51134 + 0.02336I$		
$a = -0.24536 - 2.15134I$	$-7.13768 + 2.65728I$	$-12.42433 - 2.06390I$
$b = -0.42108 - 3.24569I$		
$u = -1.51134 - 0.02336I$		
$a = -0.24536 + 2.15134I$	$-7.13768 - 2.65728I$	$-12.42433 + 2.06390I$
$b = -0.42108 + 3.24569I$		
$u = 0.418033 + 0.095358I$		
$a = -0.16881 + 1.84075I$	$-0.61706 - 2.23609I$	$-3.44792 + 0.63650I$
$b = 0.246100 - 0.753394I$		
$u = 0.418033 - 0.095358I$		
$a = -0.16881 - 1.84075I$	$-0.61706 + 2.23609I$	$-3.44792 - 0.63650I$
$b = 0.246100 + 0.753394I$		
$u = -1.56523 + 0.31596I$		
$a = 0.97491 - 1.39039I$	$18.4230 + 2.2284I$	$-14.3978 - 0.8992I$
$b = 1.08666 - 2.48431I$		
$u = -1.56523 - 0.31596I$		
$a = 0.97491 + 1.39039I$	$18.4230 - 2.2284I$	$-14.3978 + 0.8992I$
$b = 1.08666 + 2.48431I$		
$u = -1.58137 + 0.27874I$		
$a = -0.51960 + 1.97559I$	$17.8528 + 11.7492I$	$-14.2038 - 4.7569I$
$b = -0.27100 + 3.26896I$		
$u = -1.58137 - 0.27874I$		
$a = -0.51960 - 1.97559I$	$17.8528 - 11.7492I$	$-14.2038 + 4.7569I$
$b = -0.27100 - 3.26896I$		
$u = -0.387724$		
$a = -0.818265$	-0.639359	-15.5090
$b = -0.317261$		

$$I_2^u = \langle 2u^{12} - 2u^{11} + \dots + b - 2, \ 2u^{12} - 2u^{11} + \dots + a - 5, \ u^{13} - 2u^{12} + \dots - 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2u^{12} + 2u^{11} + \dots + 6u + 5 \\ -2u^{12} + 2u^{11} + \dots + u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 3u^{12} - 3u^{11} + \dots - 5u - 5 \\ 3u^{12} - 2u^{11} + \dots + 17u^2 - 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^{12} + 3u^{11} + \dots + 9u + 5 \\ -u^{12} + 2u^{11} + \dots + 3u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{12} - 3u^{11} + \dots - 17u - 7 \\ -u^{11} + u^{10} + 5u^9 - 3u^8 - 10u^7 + 9u^5 + 7u^4 - 6u^2 - 4u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{12} - u^{11} + \dots - 15u - 4 \\ -3u^{12} + u^{11} + \dots - 7u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 5u^{12} - 6u^{11} + \dots - 10u - 9 \\ 5u^{12} - 4u^{11} + \dots + u - 6 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3u^{12} + 3u^{11} + \dots + 5u + 5 \\ -4u^{12} + 4u^{11} + \dots + u + 3 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes**

$$= -4u^{12} + 9u^{11} + 17u^{10} - 41u^9 - 27u^8 + 56u^7 + 32u^6 - 11u^5 - 30u^4 - 29u^3 + 8u^2 + 12u - 8$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{13} - 15u^{12} + \cdots + 9u - 1$
$c_2$	$u^{13} + u^{12} + \cdots + 3u - 1$
$c_3, c_4$	$u^{13} - 2u^{12} + \cdots - 2u + 1$
$c_5$	$u^{13} - u^{12} + \cdots + u - 1$
$c_6$	$u^{13} + u^{12} + \cdots + u + 1$
$c_7, c_{12}$	$u^{13} - u^{12} + \cdots + 3u + 1$
$c_8$	$u^{13} + u^{12} + \cdots + u + 1$
$c_9$	$u^{13} - 6u^{11} - 8u^{10} + 7u^8 + 3u^7 + 16u^6 - 2u^5 + 14u^4 - 3u^3 + 6u^2 + 1$
$c_{10}$	$u^{13} - u^{12} + \cdots + u - 1$
$c_{11}$	$u^{13} + 2u^{12} + \cdots - 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{13} - 31y^{12} + \cdots - 15y - 1$
$c_2, c_7, c_{12}$	$y^{13} - 15y^{12} + \cdots + 9y - 1$
$c_3, c_4, c_{11}$	$y^{13} - 14y^{12} + \cdots + 18y - 1$
$c_5, c_8$	$y^{13} + 5y^{12} + \cdots - 7y - 1$
$c_6, c_{10}$	$y^{13} + 7y^{12} + \cdots - 5y - 1$
$c_9$	$y^{13} - 12y^{12} + \cdots - 12y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.132140 + 0.168986I$		
$a = 0.092976 + 0.325055I$	$-1.75574 + 2.59120I$	$-12.09350 - 3.87877I$
$b = -0.160192 - 0.352296I$		
$u = -1.132140 - 0.168986I$		
$a = 0.092976 - 0.325055I$	$-1.75574 - 2.59120I$	$-12.09350 + 3.87877I$
$b = -0.160192 + 0.352296I$		
$u = -0.189605 + 0.771385I$		
$a = 0.646314 + 0.286377I$	$0.707606 + 0.983665I$	$-10.21762 - 1.58969I$
$b = -0.343451 + 0.444258I$		
$u = -0.189605 - 0.771385I$		
$a = 0.646314 - 0.286377I$	$0.707606 - 0.983665I$	$-10.21762 + 1.58969I$
$b = -0.343451 - 0.444258I$		
$u = 1.27456$		
$a = -2.12141$	$-10.1403$	$-16.1260$
$b = -2.70385$		
$u = -0.596279 + 0.393194I$		
$a = -0.433017 + 0.867082I$	$-1.18520 + 2.76688I$	$-11.52015 - 6.83060I$
$b = -0.082733 - 0.687283I$		
$u = -0.596279 - 0.393194I$		
$a = -0.433017 - 0.867082I$	$-1.18520 - 2.76688I$	$-11.52015 + 6.83060I$
$b = -0.082733 + 0.687283I$		
$u = 1.369650 + 0.339979I$		
$a = 0.746659 + 0.696939I$	$-4.20868 - 5.03112I$	$-13.5740 + 4.7480I$
$b = 0.78571 + 1.20841I$		
$u = 1.369650 - 0.339979I$		
$a = 0.746659 - 0.696939I$	$-4.20868 + 5.03112I$	$-13.5740 - 4.7480I$
$b = 0.78571 - 1.20841I$		
$u = -1.51524$		
$a = -0.421908$	$-12.9834$	$-12.2240$
$b = 0.639294$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.53980 + 0.14093I$		
$a = -0.10346 - 1.87763I$	$-8.24712 - 4.85635I$	$-12.41808 + 4.09970I$
$b = 0.10530 - 2.90577I$		
$u = 1.53980 - 0.14093I$		
$a = -0.10346 + 1.87763I$	$-8.24712 + 4.85635I$	$-12.41808 - 4.09970I$
$b = 0.10530 + 2.90577I$		
$u = 0.257830$		
$a = 5.64437$	$-6.71567$	$-5.00350$
$b = 1.45529$		

$$\text{III. } I_3^u = \langle u^5 - u^4 - 2u^3 - au + u^2 + b + u + 1, -u^5a - 4u^5 + \dots - 2a - 6, u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ -u^5 + u^4 + 2u^3 + au - u^2 - u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^4a + u^5 - u^3a - u^4 - u^2a - u^3 + a - u \\ u^4a - u^3a - u^2a + 2u^3 - 2u^2 + a - 3u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 + u^4 - u^2a + 2u^3 + au - u^2 + a - u - 1 \\ -u^4a - 2u^5 + u^3a + 2u^4 + 3u^3 + au - u^2 - 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3u^5 + 2u^4 + 8u^3 + au - 2u^2 - a - 5u - 4 \\ -2u^5 + 2u^4 + 4u^3 + au - 2u^2 - 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4a - 3u^5 + u^3a + u^4 + u^2a + 7u^3 - a - 4u - 2 \\ -u^4a - 4u^5 + u^3a + 2u^4 + 8u^3 + au - u^2 - 3u - 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -2u^4a - 2u^5 + 2u^3a + 2u^4 + 2u^2a + 2u^3 - 2a + u \\ -2u^4a + 2u^3a + 2u^2a - 4u^3 + 4u^2 - 2a + 5u + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^4a + u^5 - u^3a - u^4 - u^2a - u^3 + a \\ u^4a - u^3a - u^2a + 2u^3 - 2u^2 + a - 2u - 1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $4u^3 - 8u - 18$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} + 21u^{11} + \cdots + 44976u + 9409$
$c_2, c_7, c_{12}$	$u^{12} - u^{11} + \cdots + 68u + 97$
$c_3, c_4, c_{11}$	$(u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^2$
$c_5, c_8$	$u^{12} + 7u^{11} + \cdots - 48u - 23$
$c_6, c_{10}$	$(u - 1)^{12}$
$c_9$	$u^{12} - u^{11} + \cdots - 320u + 239$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} - 37y^{11} + \cdots - 144089092y + 88529281$
$c_2, c_7, c_{12}$	$y^{12} - 21y^{11} + \cdots - 44976y + 9409$
$c_3, c_4, c_{11}$	$(y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1)^2$
$c_5, c_8$	$y^{12} + 7y^{11} + \cdots - 7180y + 529$
$c_6, c_{10}$	$(y - 1)^{12}$
$c_9$	$y^{12} - 33y^{11} + \cdots - 136816y + 57121$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.493180 + 0.575288I$		
$a = 0.597504 - 0.159655I$	$-3.61949 + 1.97241I$	$-12.57572 - 3.68478I$
$b = -0.294522 + 1.202870I$		
$u = -0.493180 + 0.575288I$		
$a = -1.45815 + 0.73808I$	$-3.61949 + 1.97241I$	$-12.57572 - 3.68478I$
$b = 0.202829 - 0.422475I$		
$u = -0.493180 - 0.575288I$		
$a = 0.597504 + 0.159655I$	$-3.61949 - 1.97241I$	$-12.57572 + 3.68478I$
$b = -0.294522 - 1.202870I$		
$u = -0.493180 - 0.575288I$		
$a = -1.45815 - 0.73808I$	$-3.61949 - 1.97241I$	$-12.57572 + 3.68478I$
$b = 0.202829 + 0.422475I$		
$u = 0.483672$		
$a = -1.45315$	$-7.31859$	$-21.4170$
$b = -2.16590$		
$u = 0.483672$		
$a = 4.47804$	$-7.31859$	$-21.4170$
$b = 0.702848$		
$u = 1.52087 + 0.16310I$		
$a = -0.53855 - 1.90937I$	$-10.27530 - 4.59213I$	$-16.5811 + 3.2048I$
$b = -0.74685 - 3.39023I$		
$u = 1.52087 + 0.16310I$		
$a = 0.72182 + 2.15174I$	$-10.27530 - 4.59213I$	$-16.5811 + 3.2048I$
$b = 0.50765 + 2.99173I$		
$u = 1.52087 - 0.16310I$		
$a = -0.53855 + 1.90937I$	$-10.27530 + 4.59213I$	$-16.5811 - 3.2048I$
$b = -0.74685 + 3.39023I$		
$u = 1.52087 - 0.16310I$		
$a = 0.72182 - 2.15174I$	$-10.27530 + 4.59213I$	$-16.5811 - 3.2048I$
$b = 0.50765 - 2.99173I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.53904$		
$a = 1.22065$	-14.2398	-20.2690
$b = 3.24620$		
$u = -1.53904$		
$a = 2.10923$	-14.2398	-20.2690
$b = 1.87863$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{12} + 21u^{11} + \dots + 44976u + 9409)(u^{13} - 15u^{12} + \dots + 9u - 1)$ $\cdot (u^{20} + 31u^{19} + \dots - 5u + 1)$
$c_2$	$(u^{12} - u^{11} + \dots + 68u + 97)(u^{13} + u^{12} + \dots + 3u - 1)$ $\cdot (u^{20} + u^{19} + \dots - 3u - 1)$
$c_3, c_4$	$((u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^2)(u^{13} - 2u^{12} + \dots - 2u + 1)$ $\cdot (u^{20} + 5u^{19} + \dots + u - 2)$
$c_5$	$(u^{12} + 7u^{11} + \dots - 48u - 23)(u^{13} - u^{12} + \dots + u - 1)$ $\cdot (u^{20} - u^{19} + \dots - 7u + 1)$
$c_6$	$((u - 1)^{12})(u^{13} + u^{12} + \dots + u + 1)(u^{20} + 14u^{19} + \dots + 608u + 64)$
$c_7, c_{12}$	$(u^{12} - u^{11} + \dots + 68u + 97)(u^{13} - u^{12} + \dots + 3u + 1)$ $\cdot (u^{20} + u^{19} + \dots - 3u - 1)$
$c_8$	$(u^{12} + 7u^{11} + \dots - 48u - 23)(u^{13} + u^{12} + \dots + u + 1)$ $\cdot (u^{20} - u^{19} + \dots - 7u + 1)$
$c_9$	$(u^{12} - u^{11} + \dots - 320u + 239)$ $\cdot (u^{13} - 6u^{11} - 8u^{10} + 7u^8 + 3u^7 + 16u^6 - 2u^5 + 14u^4 - 3u^3 + 6u^2 + 1)$ $\cdot (u^{20} - 26u^{18} + \dots - 494u - 599)$
$c_{10}$	$((u - 1)^{12})(u^{13} - u^{12} + \dots + u - 1)(u^{20} + 14u^{19} + \dots + 608u + 64)$
$c_{11}$	$((u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1)^2)(u^{13} + 2u^{12} + \dots - 2u - 1)$ $\cdot (u^{20} + 5u^{19} + \dots + u - 2)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{12} - 37y^{11} + \dots - 144089092y + 88529281)$ $\cdot (y^{13} - 31y^{12} + \dots - 15y - 1)(y^{20} - 103y^{19} + \dots - 159y + 1)$
$c_2, c_7, c_{12}$	$(y^{12} - 21y^{11} + \dots - 44976y + 9409)(y^{13} - 15y^{12} + \dots + 9y - 1)$ $\cdot (y^{20} - 31y^{19} + \dots + 5y + 1)$
$c_3, c_4, c_{11}$	$(y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1)^2$ $\cdot (y^{13} - 14y^{12} + \dots + 18y - 1)(y^{20} - 21y^{19} + \dots - 61y + 4)$
$c_5, c_8$	$(y^{12} + 7y^{11} + \dots - 7180y + 529)(y^{13} + 5y^{12} + \dots - 7y - 1)$ $\cdot (y^{20} + 29y^{19} + \dots - 55y + 1)$
$c_6, c_{10}$	$((y - 1)^{12})(y^{13} + 7y^{12} + \dots - 5y - 1)$ $\cdot (y^{20} + 6y^{19} + \dots - 33792y + 4096)$
$c_9$	$(y^{12} - 33y^{11} + \dots - 136816y + 57121)(y^{13} - 12y^{12} + \dots - 12y - 1)$ $\cdot (y^{20} - 52y^{19} + \dots + 2577254y + 358801)$