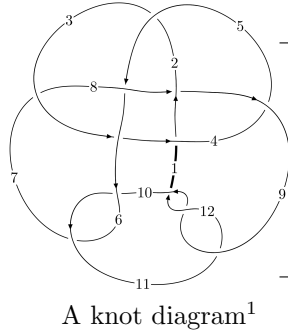
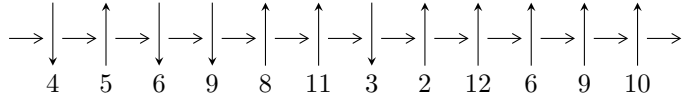


12n<sub>0665</sub> (K12n<sub>0665</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$9,12 \xrightarrow{c_9} 10 \xrightarrow{c_{12}} 1,5 \xrightarrow{c_4} 4 \xrightarrow{c_1} 2 \xrightarrow{c_8} 8 \xrightarrow{c_5} 6 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \Rightarrow c_2, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1.16371 \times 10^{21} u^{21} - 5.81881 \times 10^{21} u^{20} + \dots + 1.46625 \times 10^{23} b - 4.63210 \times 10^{22}, \\ 2.23290 \times 10^{22} u^{21} - 1.79700 \times 10^{23} u^{20} + \dots + 1.17300 \times 10^{24} a - 8.46516 \times 10^{23}, u^{22} - 7u^{21} + \dots - u - 16 \rangle$$

$$I_2^u = \langle -12a^3 + 35a^2 + 361b + 258a + 225, 4a^4 + 7a^3 + 20a^2 + 5a + 11, u + 1 \rangle$$

$$I_3^u = \langle -u^8 + 4u^7 - 6u^6 + 2u^5 + 5u^4 - 6u^3 + 4u^2 + b - 3u, u^8 - 3u^7 + 2u^6 + 4u^5 - 7u^4 + u^3 + u^2 + a + u + 2, \\ u^{11} - 4u^{10} + 5u^9 + 2u^8 - 11u^7 + 8u^6 - u^4 + 4u^3 - 5u^2 + u - 1 \rangle$$

$$I_4^u = \langle -1309u^{10}a + 39316u^{10} + \dots - 49959a - 27286, -16711u^{10}a + 2773u^{10} + \dots - 53855a - 50795, \\ u^{11} - 5u^{10} + 12u^9 - 14u^8 + 4u^7 + 11u^6 - 16u^5 + 14u^4 - 8u^3 - 13u^2 + 7u - 1 \rangle$$

$$I_5^u = \langle -2a^5 - 176a^4 - 669a^3 + 284a^2 + 13805b + 9351a + 7409, a^6 + 6a^5 + 21a^4 + 39a^3 + 66a^2 + 49a + 59, \\ u + 1 \rangle$$

$$I_6^u = \langle au + b - a - 2u + 3, a^2 + 4au - 3a - 3u + 6, u^2 - u - 1 \rangle$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 69 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.16 \times 10^{21} u^{21} - 5.82 \times 10^{21} u^{20} + \dots + 1.47 \times 10^{23} b - 4.63 \times 10^{22}, 2.23 \times 10^{22} u^{21} - 1.80 \times 10^{23} u^{20} + \dots + 1.17 \times 10^{24} a - 8.47 \times 10^{23}, u^{22} - 7u^{21} + \dots - u - 16 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0190358u^{21} + 0.153197u^{20} + \dots + 2.30959u + 0.721667 \\ -0.00793664u^{21} + 0.0396850u^{20} + \dots + 0.0736575u + 0.315914 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0269724u^{21} + 0.192882u^{20} + \dots + 2.38324u + 1.03758 \\ -0.00793664u^{21} + 0.0396850u^{20} + \dots + 0.0736575u + 0.315914 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00755456u^{21} + 0.0556100u^{20} + \dots + 2.97731u + 1.14656 \\ 0.0129445u^{21} - 0.0689040u^{20} + \dots + 0.462289u + 0.147994 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0468616u^{21} - 0.281682u^{20} + \dots + 0.728053u + 0.542790 \\ -0.0303212u^{21} + 0.179358u^{20} + \dots - 0.268846u - 0.786470 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0501899u^{21} + 0.326221u^{20} + \dots + 0.776174u - 0.236818 \\ 0.0251088u^{21} - 0.165046u^{20} + \dots + 0.287008u + 0.803039 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.0503171u^{21} + 0.321861u^{20} + \dots + 0.00116367u - 0.311783 \\ 0.0264975u^{21} - 0.160879u^{20} + \dots + 1.44637u + 0.689429 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0529780u^{21} - 0.337734u^{20} + \dots - 0.360484u + 0.467102 \\ -0.0278969u^{21} + 0.176559u^{20} + \dots - 0.702698u - 1.03332 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{1046540992390926455030041}{4692001596758932331121536} u^{21} - \frac{692312832330241174483901}{586500199594866541390192} u^{20} + \dots + \frac{21996001093684558786173143}{4692001596758932331121536} u + \frac{1233054846153246715242967}{293250099797433270695096}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{22} - 22u^{20} + \dots - 78u + 1$
$c_2$	$u^{22} + 17u^{21} + \dots + 72u + 4$
$c_4, c_7$	$u^{22} - 10u^{20} + \dots - 82u + 17$
$c_5, c_8$	$u^{22} + u^{21} + \dots - u + 1$
$c_6, c_{10}$	$u^{22} + 5u^{21} + \dots + 224u - 256$
$c_9, c_{11}, c_{12}$	$u^{22} + 7u^{21} + \dots + u - 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{22} - 44y^{21} + \dots - 6066y + 1$
$c_2$	$y^{22} - y^{21} + \dots - 984y + 16$
$c_4, c_7$	$y^{22} - 20y^{21} + \dots - 4038y + 289$
$c_5, c_8$	$y^{22} + 9y^{21} + \dots + 9y + 1$
$c_6, c_{10}$	$y^{22} + 27y^{21} + \dots - 291840y + 65536$
$c_9, c_{11}, c_{12}$	$y^{22} - 5y^{21} + \dots - y + 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073320 + 0.196864I$ $a = -0.633075 + 1.048060I$ $b = -0.468525 - 0.581818I$	$0.748660 - 0.578139I$	$4.16300 - 3.21064I$
$u = -1.073320 - 0.196864I$ $a = -0.633075 - 1.048060I$ $b = -0.468525 + 0.581818I$	$0.748660 + 0.578139I$	$4.16300 + 3.21064I$
$u = 1.196940 + 0.138834I$ $a = 0.69651 - 1.48448I$ $b = -0.525572 + 0.904919I$	$4.76890 + 7.93706I$	$14.4936 - 13.4042I$
$u = 1.196940 - 0.138834I$ $a = 0.69651 + 1.48448I$ $b = -0.525572 - 0.904919I$	$4.76890 - 7.93706I$	$14.4936 + 13.4042I$
$u = -1.281740 + 0.445541I$ $a = -1.340360 - 0.152402I$ $b = 1.042560 - 0.544528I$	$0.63415 - 1.82383I$	$3.25206 + 1.96969I$
$u = -1.281740 - 0.445541I$ $a = -1.340360 + 0.152402I$ $b = 1.042560 + 0.544528I$	$0.63415 + 1.82383I$	$3.25206 - 1.96969I$
$u = 1.41326$ $a = 1.00267$ $b = -0.555579$	$7.32600$	$23.7620$
$u = -0.583556$ $a = -0.207344$ $b = -0.336659$	$0.970302$	$10.0070$
$u = -0.37029 + 1.42559I$ $a = 0.958773 + 0.111950I$ $b = -1.88452 + 0.10002I$	$-3.47219 - 4.63898I$	$1.76510 + 3.68966I$
$u = -0.37029 - 1.42559I$ $a = 0.958773 - 0.111950I$ $b = -1.88452 - 0.10002I$	$-3.47219 + 4.63898I$	$1.76510 - 3.68966I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.305160 + 0.425228I$		
$a = 0.75251 + 1.97105I$	$-0.88734 + 1.99220I$	$-1.51650 - 2.98007I$
$b = 0.656252 - 0.746018I$		
$u = 0.305160 - 0.425228I$		
$a = 0.75251 - 1.97105I$	$-0.88734 - 1.99220I$	$-1.51650 + 2.98007I$
$b = 0.656252 + 0.746018I$		
$u = 1.01095 + 1.14167I$		
$a = 0.424540 - 0.460153I$	$-9.81793 + 5.07725I$	$-1.39233 - 9.54863I$
$b = -1.387840 + 0.091887I$		
$u = 1.01095 - 1.14167I$		
$a = 0.424540 + 0.460153I$	$-9.81793 - 5.07725I$	$-1.39233 + 9.54863I$
$b = -1.387840 - 0.091887I$		
$u = 1.16674 + 1.00051I$		
$a = 0.282150 - 1.116250I$	$-9.23521 + 2.88093I$	$1.62002 + 2.72235I$
$b = -1.143540 + 0.418541I$		
$u = 1.16674 - 1.00051I$		
$a = 0.282150 + 1.116250I$	$-9.23521 - 2.88093I$	$1.62002 - 2.72235I$
$b = -1.143540 - 0.418541I$		
$u = -0.238163 + 0.343586I$		
$a = 0.92161 + 1.69413I$	$-1.61974 - 1.37202I$	$-2.26771 + 5.71937I$
$b = 0.423005 + 0.405652I$		
$u = -0.238163 - 0.343586I$		
$a = 0.92161 - 1.69413I$	$-1.61974 + 1.37202I$	$-2.26771 - 5.71937I$
$b = 0.423005 - 0.405652I$		
$u = 1.44040 + 1.00087I$		
$a = -0.54794 + 2.42657I$	$-10.9142 + 15.8777I$	$4.46326 - 7.01203I$
$b = 1.53075 - 1.61655I$		
$u = 1.44040 - 1.00087I$		
$a = -0.54794 - 2.42657I$	$-10.9142 - 15.8777I$	$4.46326 + 7.01203I$
$b = 1.53075 + 1.61655I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.92846 + 1.61543I$	$-13.0092 - 6.5361I$	$2.81617 + 3.19876I$
$a = -1.69364 - 0.69437I$		
$b = 2.20355 + 1.18551I$		
$u = 0.92846 - 1.61543I$	$-13.0092 + 6.5361I$	$2.81617 - 3.19876I$
$a = -1.69364 + 0.69437I$		
$b = 2.20355 - 1.18551I$		

**II.**

$$I_2^u = \langle -12a^3 + 35a^2 + 361b + 258a + 225, 4a^4 + 7a^3 + 20a^2 + 5a + 11, u + 1 \rangle$$

**(i) Arc colorings**

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0.0332410a^3 - 0.0969529a^2 - 0.714681a - 0.623269 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0332410a^3 - 0.0969529a^2 + 0.285319a - 0.623269 \\ 0.0332410a^3 - 0.0969529a^2 - 0.714681a - 0.623269 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0332410a^3 + 0.0969529a^2 - 0.285319a - 1.37673 \\ -0.188366a^3 - 0.783934a^2 - 0.950139a - 0.468144 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.443213a^3 + 1.37396a^2 + 1.47091a + 1.68975 \\ -0.221607a^3 - 0.686981a^2 - 0.235457a - 0.844875 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.387812a^3 + 0.202216a^2 + 0.662050a + 0.728532 \\ -0.387812a^3 - 0.202216a^2 - 0.662050a - 0.728532 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.288089a^3 + 0.493075a^2 - 0.193906a - 0.401662 \\ -0.221607a^3 - 0.686981a^2 - 0.235457a - 0.844875 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.387812a^3 + 0.202216a^2 + 0.662050a + 0.728532 \\ -0.387812a^3 - 0.202216a^2 - 0.662050a - 0.728532 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $\frac{640}{361}a^3 + \frac{1623}{361}a^2 + \frac{2846}{361}a + \frac{2079}{361}$**



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$	$u^4 + u^2 - u + 1$
$c_2$	$u^4 - 3u^3 + 4u^2 - 3u + 2$
$c_5$	$u^4 + 2u^3 + 3u^2 + u + 1$
$c_6, c_{10}$	$u^4$
$c_7$	$u^4 + u^2 + u + 1$
$c_8$	$u^4 - 2u^3 + 3u^2 - u + 1$
$c_9$	$(u + 1)^4$
$c_{11}, c_{12}$	$(u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7$	$y^4 + 2y^3 + 3y^2 + y + 1$
$c_2$	$y^4 - y^3 + 2y^2 + 7y + 4$
$c_5, c_8$	$y^4 + 2y^3 + 7y^2 + 5y + 1$
$c_6, c_{10}$	$y^4$
$c_9, c_{11}, c_{12}$	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = -0.017843 + 0.799588I$ $b = -0.547424 - 0.585652I$	$0.66484 - 1.39709I$	$2.80605 + 5.27044I$
$u = -1.00000$ $a = -0.017843 - 0.799588I$ $b = -0.547424 + 0.585652I$	$0.66484 + 1.39709I$	$2.80605 - 5.27044I$
$u = -1.00000$ $a = -0.85716 + 1.88797I$ $b = 0.547424 - 1.120870I$	$4.26996 + 7.64338I$	$1.41270 - 4.22005I$
$u = -1.00000$ $a = -0.85716 - 1.88797I$ $b = 0.547424 + 1.120870I$	$4.26996 - 7.64338I$	$1.41270 + 4.22005I$

III.

$$I_3^u = \langle -u^8 + 4u^7 + \cdots + b - 3u, u^8 - 3u^7 + \cdots + a + 2, u^{11} - 4u^{10} + \cdots + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^8 + 3u^7 - 2u^6 - 4u^5 + 7u^4 - u^3 - u^2 - u - 2 \\ u^8 - 4u^7 + 6u^6 - 2u^5 - 5u^4 + 6u^3 - 4u^2 + 3u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^7 + 4u^6 - 6u^5 + 2u^4 + 5u^3 - 5u^2 + 2u - 2 \\ u^8 - 4u^7 + 6u^6 - 2u^5 - 5u^4 + 6u^3 - 4u^2 + 3u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -2u^{10} + 10u^9 + \cdots - 3u + 2 \\ u^8 - 4u^7 + 6u^6 - 2u^5 - 5u^4 + 5u^3 - 3u^2 + 3u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^{10} + 6u^9 + \cdots - 3u + 3 \\ u^{10} - 5u^9 + 9u^8 - 4u^7 - 8u^6 + 10u^5 - 2u^4 + 3u^3 - 3u^2 - 2u - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^{10} - 4u^9 + 4u^8 + 5u^7 - 14u^6 + 6u^5 + 6u^4 - 4u^3 + 4u^2 - 4u \\ u^9 - 3u^8 + 3u^7 + 2u^6 - 6u^5 + 3u^4 - u^2 + u - 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^7 + 4u^6 - 6u^5 + 2u^4 + 5u^3 - 4u^2 + 2u - 3 \\ u^8 - 4u^7 + 6u^6 - 2u^5 - 5u^4 + 5u^3 - 4u^2 + 4u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{10} - 3u^9 + u^8 + 8u^7 - 13u^6 + 3u^5 + 6u^4 - 6u^3 + 7u^2 - 4u + 1 \\ u^6 - 3u^5 + 3u^4 + 2u^3 - 4u^2 + u - 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -6u^{10} + 27u^9 - 43u^8 + 8u^7 + 58u^6 - 59u^5 + 6u^4 + 4u^3 - 6u^2 + 18u + 1$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{11} - 6u^{10} + \dots + u - 1$
$c_2$	$u^{11} + 5u^{10} + \dots + 66u + 11$
$c_4, c_7$	$u^{11} - 3u^9 - 3u^8 + 3u^7 + 5u^6 + u^5 - 2u^4 + u^3 + 4u^2 + 3u + 1$
$c_5, c_8$	$u^{11} + 3u^{10} + 4u^9 + u^8 - 2u^7 + u^6 + 5u^5 + 3u^4 - 3u^3 - 3u^2 + 1$
$c_6$	$u^{11} + 2u^{10} + 5u^9 + 3u^8 - 6u^7 - 12u^6 - 4u^5 - u^4 - 4u^3 - 5u^2 - u - 1$
$c_9$	$u^{11} - 4u^{10} + 5u^9 + 2u^8 - 11u^7 + 8u^6 - u^4 + 4u^3 - 5u^2 + u - 1$
$c_{10}$	$u^{11} - 2u^{10} + 5u^9 - 3u^8 - 6u^7 + 12u^6 - 4u^5 + u^4 - 4u^3 + 5u^2 - u + 1$
$c_{11}, c_{12}$	$u^{11} + 4u^{10} + 5u^9 - 2u^8 - 11u^7 - 8u^6 + u^4 + 4u^3 + 5u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{11} - 6y^{10} + \dots - 11y - 1$
$c_2$	$y^{11} - 5y^{10} + \dots + 1056y - 121$
$c_4, c_7$	$y^{11} - 6y^{10} + \dots + y - 1$
$c_5, c_8$	$y^{11} - y^{10} + \dots + 6y - 1$
$c_6, c_{10}$	$y^{11} + 6y^{10} + \dots - 9y - 1$
$c_9, c_{11}, c_{12}$	$y^{11} - 6y^{10} + \dots - 9y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.086170 + 0.009391I$ $a = 4.41295 + 0.00742I$ $b = -0.701762 - 0.657333I$	$2.65196 - 3.67431I$	$-5.84307 + 3.56499I$
$u = -1.086170 - 0.009391I$ $a = 4.41295 - 0.00742I$ $b = -0.701762 + 0.657333I$	$2.65196 + 3.67431I$	$-5.84307 - 3.56499I$
$u = -0.107619 + 0.709932I$ $a = 0.895151 + 0.275061I$ $b = 0.954711 - 0.673787I$	$0.30466 + 2.75309I$	$5.01781 - 3.90984I$
$u = -0.107619 - 0.709932I$ $a = 0.895151 - 0.275061I$ $b = 0.954711 + 0.673787I$	$0.30466 - 2.75309I$	$5.01781 + 3.90984I$
$u = 1.298730 + 0.273936I$ $a = -0.597874 + 1.164320I$ $b = 0.400683 - 0.540159I$	$4.37786 + 7.33604I$	$4.82590 - 2.92832I$
$u = 1.298730 - 0.273936I$ $a = -0.597874 - 1.164320I$ $b = 0.400683 + 0.540159I$	$4.37786 - 7.33604I$	$4.82590 + 2.92832I$
$u = 1.47992$ $a = -1.10702$ $b = 0.798074$	$6.99554$	$-1.23750$
$u = 0.031910 + 0.483612I$ $a = -1.42549 - 0.63001I$ $b = 0.551419 + 0.729779I$	$0.36189 - 4.26572I$	$1.88771 + 6.83487I$
$u = 0.031910 - 0.483612I$ $a = -1.42549 + 0.63001I$ $b = 0.551419 - 0.729779I$	$0.36189 + 4.26572I$	$1.88771 - 6.83487I$
$u = 1.12319 + 1.19275I$ $a = 0.768773 - 0.735083I$ $b = -1.60409 + 0.22290I$	$-9.54921 + 4.30931I$	$3.23041 - 0.76635I$

	Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$1.12319 - 1.19275I$		
$a =$	$0.768773 + 0.735083I$	$-9.54921 - 4.30931I$	$3.23041 + 0.76635I$
$b =$	$-1.60409 - 0.22290I$		



$$\text{IV. } I_4^u = \langle -1309u^{10}a + 39316u^{10} + \dots - 49959a - 27286, -16711u^{10}a + 2773u^{10} + \dots - 53855a - 50795, u^{11} - 5u^{10} + \dots + 7u - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0.00589438au^{10} - 0.177038u^{10} + \dots + 0.224964a + 0.122868 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.00589438au^{10} - 0.177038u^{10} + \dots + 1.22496a + 0.122868 \\ 0.00589438au^{10} - 0.177038u^{10} + \dots + 0.224964a + 0.122868 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.773073au^{10} + 0.470695u^{10} + \dots - 3.09852a - 1.05429 \\ 0.224964au^{10} - 0.715602u^{10} + \dots + 0.773073a - 1.44519 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.119743au^{10} - 1.31813u^{10} + \dots + 0.473820a - 2.23776 \\ -0.143618au^{10} + 0.302113u^{10} + \dots - 0.296781a + 0.607909 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.65276u^{10} - 7.83688u^9 + \dots - 24.1541u + 5.81695 \\ -0.426939u^{10} + 2.03454u^9 + \dots + 5.75239u - 1.65276 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.360480au^{10} + 0.470695u^{10} + \dots - 0.370306a - 1.05429 \\ 0.140546au^{10} - 0.617437u^{10} + \dots + 0.591338a - 0.524865 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.71387u^{10} + 8.17163u^9 + \dots + 25.2157u - 6.14373 \\ 0.488045u^{10} - 2.36929u^9 + \dots - 6.81403u + 1.97954 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{1665}{1882}u^{10} + \frac{7853}{1882}u^9 - \frac{15635}{1882}u^8 + \frac{9431}{1882}u^7 + \frac{19187}{1882}u^6 - \frac{21601}{941}u^5 + \frac{38751}{1882}u^4 - \frac{9650}{941}u^3 + \frac{7699}{1882}u^2 + \frac{38133}{1882}u - \frac{2836}{941}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{22} + 4u^{21} + \dots + 3144u - 1751$
$c_2$	$(u^{11} - 2u^{10} + 4u^9 - 4u^8 + 7u^7 - 6u^6 + 8u^5 - 3u^4 + 7u^3 - 5u^2 + 6u + 4)^2$
$c_4, c_7$	$u^{22} - u^{21} + \dots - 1853u - 367$
$c_5, c_8$	$u^{22} + 3u^{21} + \dots + 43u + 17$
$c_6, c_{10}$	$(u^{11} - 2u^{10} + \dots + 20u + 8)^2$
$c_9, c_{11}, c_{12}$	$(u^{11} + 5u^{10} + \dots + 7u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{22} - 34y^{21} + \dots + 14797360y + 3066001$
$c_2$	$(y^{11} + 4y^{10} + \dots + 76y - 16)^2$
$c_4, c_7$	$y^{22} - 21y^{21} + \dots - 11844515y + 134689$
$c_5, c_8$	$y^{22} - 5y^{21} + \dots + 157y + 289$
$c_6, c_{10}$	$(y^{11} + 18y^{10} + \dots - 48y - 64)^2$
$c_9, c_{11}, c_{12}$	$(y^{11} - y^{10} + \dots + 23y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.079725 + 1.068410I$ $a = 0.856962 + 0.168668I$ $b = -2.18146 - 0.23527I$	$-1.62432 + 3.00088I$	$0.33499 - 3.49194I$
$u = -0.079725 + 1.068410I$ $a = 0.439244 + 1.098550I$ $b = 0.798257 - 1.114970I$	$-1.62432 + 3.00088I$	$0.33499 - 3.49194I$
$u = -0.079725 - 1.068410I$ $a = 0.856962 - 0.168668I$ $b = -2.18146 + 0.23527I$	$-1.62432 - 3.00088I$	$0.33499 + 3.49194I$
$u = -0.079725 - 1.068410I$ $a = 0.439244 - 1.098550I$ $b = 0.798257 + 1.114970I$	$-1.62432 - 3.00088I$	$0.33499 + 3.49194I$
$u = -0.884145 + 0.095736I$ $a = -1.16290 - 2.05270I$ $b = -0.559456 + 0.879724I$	$2.07033 + 3.52584I$	$11.0814 - 10.6105I$
$u = -0.884145 + 0.095736I$ $a = -0.69396 - 4.81962I$ $b = 0.969577 - 0.463172I$	$2.07033 + 3.52584I$	$11.0814 - 10.6105I$
$u = -0.884145 - 0.095736I$ $a = -1.16290 + 2.05270I$ $b = -0.559456 - 0.879724I$	$2.07033 - 3.52584I$	$11.0814 + 10.6105I$
$u = -0.884145 - 0.095736I$ $a = -0.69396 + 4.81962I$ $b = 0.969577 + 0.463172I$	$2.07033 - 3.52584I$	$11.0814 + 10.6105I$
$u = 1.53174$ $a = 0.113755$ $b = 0.109337$	$7.41447$	$30.3990$
$u = 1.53174$ $a = 2.58390$ $b = -1.70388$	$7.41447$	$30.3990$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.238296 + 0.095870I$		
$a = 2.84346 - 2.84451I$	$0.52440 - 2.64086I$	$1.94796 + 2.03870I$
$b = -0.419609 + 0.270447I$		
$u = 0.238296 + 0.095870I$		
$a = -2.77344 - 3.23631I$	$0.52440 - 2.64086I$	$1.94796 + 2.03870I$
$b = 0.478533 + 1.099150I$		
$u = 0.238296 - 0.095870I$		
$a = 2.84346 + 2.84451I$	$0.52440 + 2.64086I$	$1.94796 - 2.03870I$
$b = -0.419609 - 0.270447I$		
$u = 0.238296 - 0.095870I$		
$a = -2.77344 + 3.23631I$	$0.52440 + 2.64086I$	$1.94796 - 2.03870I$
$b = 0.478533 - 1.099150I$		
$u = 1.45203 + 1.04949I$		
$a = 0.660877 - 1.207490I$	$-9.67193 + 7.23582I$	$3.59903 - 5.42641I$
$b = -1.32301 + 0.63561I$		
$u = 1.45203 + 1.04949I$		
$a = -0.68206 + 2.97589I$	$-9.67193 + 7.23582I$	$3.59903 - 5.42641I$
$b = 1.68145 - 2.15398I$		
$u = 1.45203 - 1.04949I$		
$a = 0.660877 + 1.207490I$	$-9.67193 - 7.23582I$	$3.59903 + 5.42641I$
$b = -1.32301 - 0.63561I$		
$u = 1.45203 - 1.04949I$		
$a = -0.68206 - 2.97589I$	$-9.67193 - 7.23582I$	$3.59903 + 5.42641I$
$b = 1.68145 + 2.15398I$		
$u = 1.00768 + 1.54288I$		
$a = 0.930928 - 0.584899I$	$-11.45500 + 2.23657I$	$0.837127 - 0.170303I$
$b = -1.71241 + 0.28243I$		
$u = 1.00768 + 1.54288I$		
$a = -2.26794 - 1.18182I$	$-11.45500 + 2.23657I$	$0.837127 - 0.170303I$
$b = 2.56540 + 1.84699I$		

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00768 - 1.54288I$	$-11.45500 - 2.23657I$	$0.837127 + 0.170303I$
$a = 0.930928 + 0.584899I$		
$b = -1.71241 - 0.28243I$		
$u = 1.00768 - 1.54288I$	$-11.45500 - 2.23657I$	$0.837127 + 0.170303I$
$a = -2.26794 + 1.18182I$		
$b = 2.56540 - 1.84699I$		

$$\mathbf{V. } I_5^u = \langle -2a^5 + 13805b + \dots + 9351a + 7409, a^6 + 6a^5 + 21a^4 + 39a^3 + 66a^2 + 49a + 59, u + 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0.000144875a^5 + 0.0127490a^4 + \dots - 0.677363a - 0.536690 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.000144875a^5 + 0.0127490a^4 + \dots + 0.322637a - 0.536690 \\ 0.000144875a^5 + 0.0127490a^4 + \dots - 0.677363a - 0.536690 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.000144875a^5 - 0.0127490a^4 + \dots - 0.322637a - 1.46331 \\ 0.0117349a^5 + 0.0326693a^4 + \dots - 0.866425a - 0.471858 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0231800a^5 - 0.0398406a^4 + \dots + 1.37812a + 1.87034 \\ 0.0594712a^5 + 0.233466a^4 + \dots - 0.557624a - 1.81108 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0488953a^5 - 0.302789a^4 + \dots - 0.889895a - 1.36726 \\ 0.0488953a^5 + 0.302789a^4 + \dots + 0.889895a + 1.36726 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.0591815a^5 - 0.207968a^4 + \dots + 0.202898a + 0.737704 \\ 0.0594712a^5 + 0.233466a^4 + \dots - 0.557624a - 1.81108 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0488953a^5 - 0.302789a^4 + \dots - 0.889895a - 1.36726 \\ 0.0488953a^5 + 0.302789a^4 + \dots + 0.889895a + 1.36726 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{32}{2761}a^5 - \frac{5}{251}a^4 + \frac{340}{2761}a^3 + \frac{1783}{2761}a^2 + \frac{3283}{2761}a + \frac{24670}{2761}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$	$u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_5$	$u^6 + 3u^5 + 4u^4 + 2u^3 + 1$
$c_6, c_{10}$	$u^6$
$c_7$	$u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$
$c_8$	$u^6 - 3u^5 + 4u^4 - 2u^3 + 1$
$c_9$	$(u + 1)^6$
$c_{11}, c_{12}$	$(u - 1)^6$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7$	$y^6 + 3y^5 + 4y^4 + 2y^3 + 1$
$c_2$	$(y^3 - y^2 + 2y - 1)^2$
$c_5, c_8$	$y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$
$c_6, c_{10}$	$y^6$
$c_9, c_{11}, c_{12}$	$(y - 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 0.037526 + 1.309480I$ $b = -0.498832 - 1.001300I$	$1.91067 - 2.82812I$	$7.78492 + 1.30714I$
$u = -1.00000$ $a = 0.037526 - 1.309480I$ $b = -0.498832 + 1.001300I$	$1.91067 + 2.82812I$	$7.78492 - 1.30714I$
$u = -1.00000$ $a = -0.69240 + 1.75059I$ $b = 0.284920 - 1.115140I$	$6.04826$	$7.43016 + 0.I$
$u = -1.00000$ $a = -0.69240 - 1.75059I$ $b = 0.284920 + 1.115140I$	$6.04826$	$7.43016 + 0.I$
$u = -1.00000$ $a = -2.34512 + 2.04966I$ $b = 0.713912 - 0.305839I$	$1.91067 - 2.82812I$	$7.78492 + 1.30714I$
$u = -1.00000$ $a = -2.34512 - 2.04966I$ $b = 0.713912 + 0.305839I$	$1.91067 + 2.82812I$	$7.78492 - 1.30714I$

$$\text{VI. } I_6^u = \langle au + b - a - 2u + 3, a^2 + 4au - 3a - 3u + 6, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -au + a + 2u - 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -au + 2a + 2u - 3 \\ -au + a + 2u - 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -au + 2a + 3u - 3 \\ -au + a + u - 4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2au + 2a + 3u - 8 \\ au + 2u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -au + 2a + 3u - 3 \\ -au + a + u - 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-9u - 1$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u - 1)^4$
$c_2$	$u^4$
$c_4, c_5, c_7$ $c_8$	$u^4 + 3u^3 + 3u^2 + 3u + 1$
$c_6, c_9$	$(u^2 - u - 1)^2$
$c_{10}, c_{11}, c_{12}$	$(u^2 + u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$(y - 1)^4$
$c_2$	$y^4$
$c_4, c_5, c_7$ $c_8$	$y^4 - 3y^3 - 7y^2 - 3y + 1$
$c_6, c_9, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = 2.73607 + 0.60666I$ $b = 0.190983 + 0.981593I$	-0.657974	4.56230
$u = -0.618034$ $a = 2.73607 - 0.60666I$ $b = 0.190983 - 0.981593I$	-0.657974	4.56230
$u = 1.61803$ $a = -0.369308$ $b = 0.464313$	7.23771	-15.5620
$u = 1.61803$ $a = -3.10283$ $b = 2.15372$	7.23771	-15.5620

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u-1)^4(u^4+u^2-u+1)(u^6+u^5+2u^4+2u^3+2u^2+2u+1)$ $\cdot (u^{11}-6u^{10}+\dots+u-1)(u^{22}-22u^{20}+\dots-78u+1)$ $\cdot (u^{22}+4u^{21}+\dots+3144u-1751)$
$c_2$	$u^4(u^3+u^2-1)^2(u^4-3u^3+4u^2-3u+2)$ $\cdot (u^{11}-2u^{10}+4u^9-4u^8+7u^7-6u^6+8u^5-3u^4+7u^3-5u^2+6u+4)^2$ $\cdot (u^{11}+5u^{10}+\dots+66u+11)(u^{22}+17u^{21}+\dots+72u+4)$
$c_4$	$(u^4+u^2-u+1)(u^4+3u^3+3u^2+3u+1)$ $\cdot (u^6+u^5+2u^4+2u^3+2u^2+2u+1)$ $\cdot (u^{11}-3u^9-3u^8+3u^7+5u^6+u^5-2u^4+u^3+4u^2+3u+1)$ $\cdot (u^{22}-10u^{20}+\dots-82u+17)(u^{22}-u^{21}+\dots-1853u-367)$
$c_5$	$(u^4+2u^3+3u^2+u+1)(u^4+3u^3+3u^2+3u+1)$ $\cdot (u^6+3u^5+4u^4+2u^3+1)$ $\cdot (u^{11}+3u^{10}+4u^9+u^8-2u^7+u^6+5u^5+3u^4-3u^3-3u^2+1)$ $\cdot (u^{22}+u^{21}+\dots-u+1)(u^{22}+3u^{21}+\dots+43u+17)$
$c_6$	$u^{10}(u^2-u-1)^2(u^{11}-2u^{10}+\dots+20u+8)^2$ $\cdot (u^{11}+2u^{10}+5u^9+3u^8-6u^7-12u^6-4u^5-u^4-4u^3-5u^2-u-1)$ $\cdot (u^{22}+5u^{21}+\dots+224u-256)$
$c_7$	$(u^4+u^2+u+1)(u^4+3u^3+3u^2+3u+1)$ $\cdot (u^6-u^5+2u^4-2u^3+2u^2-2u+1)$ $\cdot (u^{11}-3u^9-3u^8+3u^7+5u^6+u^5-2u^4+u^3+4u^2+3u+1)$ $\cdot (u^{22}-10u^{20}+\dots-82u+17)(u^{22}-u^{21}+\dots-1853u-367)$
$c_8$	$(u^4-2u^3+3u^2-u+1)(u^4+3u^3+3u^2+3u+1)$ $\cdot (u^6-3u^5+4u^4-2u^3+1)$ $\cdot (u^{11}+3u^{10}+4u^9+u^8-2u^7+u^6+5u^5+3u^4-3u^3-3u^2+1)$ $\cdot (u^{22}+u^{21}+\dots-u+1)(u^{22}+3u^{21}+\dots+43u+17)$
$c_9$	$(u+1)^{10}(u^2-u-1)^2$ $\cdot (u^{11}-4u^{10}+5u^9+2u^8-11u^7+8u^6-u^4+4u^3-5u^2+u-1)$ $\cdot ((u^{11}+5u^{10}+\dots+7u+1)^2)(u^{22}+7u^{21}+\dots+u-16)$
$c_{10}$	$u^{10}(u^2+u-1)^2$ $\cdot (u^{11}-2u^{10}+5u^9-3u^8-6u^7+12u^6-4u^5+u^4-4u^3+5u^2-u+1)$ $\cdot ((u^{11}-2u^{10}+\dots+20u+8)^2)(u^{22}+5u^{21}+\dots+224u-256)$
$c_{11}, c_{12}$	$(u-1)^{10}(u^2+u-1)^2$ $\cdot (u^{11}+4u^{10}+5u^9-2u^8-11u^7-8u^6+u^4+4u^3+5u^2+u+1)$ $\cdot ((u^{11}+5u^{10}+\dots+7u+1)^2)(u^{22}+7u^{21}+\dots+u-16)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$(y-1)^4(y^4+2y^3+3y^2+y+1)(y^6+3y^5+4y^4+2y^3+1)$ $\cdot (y^{11}-6y^{10}+\dots-11y-1)(y^{22}-44y^{21}+\dots-6066y+1)$ $\cdot (y^{22}-34y^{21}+\dots+14797360y+3066001)$
$c_2$	$y^4(y^3-y^2+2y-1)^2(y^4-y^3+2y^2+7y+4)$ $\cdot (y^{11}-5y^{10}+\dots+1056y-121)(y^{11}+4y^{10}+\dots+76y-16)^2$ $\cdot (y^{22}-y^{21}+\dots-984y+16)$
$c_4, c_7$	$(y^4-3y^3-7y^2-3y+1)(y^4+2y^3+3y^2+y+1)$ $\cdot (y^6+3y^5+4y^4+2y^3+1)(y^{11}-6y^{10}+\dots+y-1)$ $\cdot (y^{22}-21y^{21}+\dots-11844515y+134689)$ $\cdot (y^{22}-20y^{21}+\dots-4038y+289)$
$c_5, c_8$	$(y^4-3y^3-7y^2-3y+1)(y^4+2y^3+7y^2+5y+1)$ $\cdot (y^6-y^5+4y^4-2y^3+8y^2+1)(y^{11}-y^{10}+\dots+6y-1)$ $\cdot (y^{22}-5y^{21}+\dots+157y+289)(y^{22}+9y^{21}+\dots+9y+1)$
$c_6, c_{10}$	$y^{10}(y^2-3y+1)^2(y^{11}+6y^{10}+\dots-9y-1)$ $\cdot (y^{11}+18y^{10}+\dots-48y-64)^2$ $\cdot (y^{22}+27y^{21}+\dots-291840y+65536)$
$c_9, c_{11}, c_{12}$	$((y-1)^{10})(y^2-3y+1)^2(y^{11}-6y^{10}+\dots-9y-1)$ $\cdot ((y^{11}-y^{10}+\dots+23y-1)^2)(y^{22}-5y^{21}+\dots-y+256)$