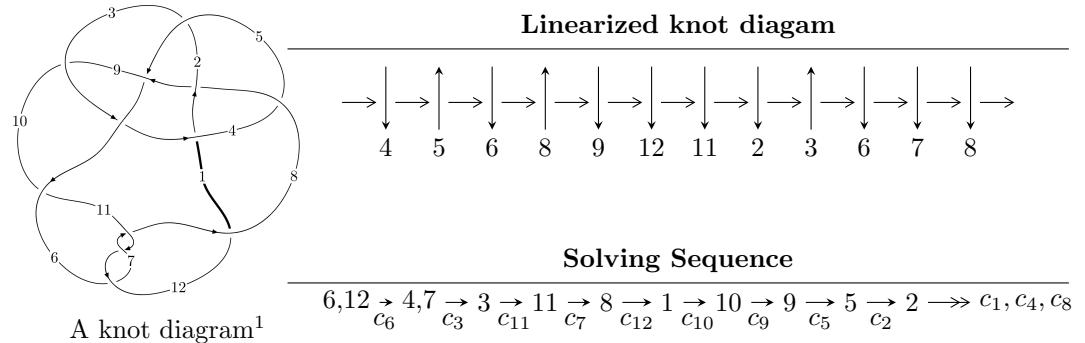


$12n_{0667}$  ( $K12n_{0667}$ )



## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
I_1^u &= \langle -3u^{20} - 26u^{19} + \dots + 7b + 97, -83u^{20} - 325u^{19} + \dots + 63a + 558, u^{21} + 5u^{20} + \dots - 72u - 9 \rangle \\
I_2^u &= \langle -3u^{14}a + 5u^{14} + \dots + a + 24, -u^{14}a + 2u^{13}a + \dots + 3a + 4, u^{15} - 2u^{14} + \dots - 4u + 1 \rangle \\
I_3^u &= \langle -u^6 - 2u^5 - 5u^4 - 6u^3 - 6u^2 + b - 4u - 1, u^8 + 2u^7 + 7u^6 + 10u^5 + 15u^4 + 14u^3 + 9u^2 + a + 5u - 1, \\
&\quad u^9 + 2u^8 + 7u^7 + 10u^6 + 16u^5 + 16u^4 + 13u^3 + 9u^2 + 2u + 1 \rangle \\
I_4^u &= \langle b + 1, 2u^2a + a^2 - 2au + 3a + u - 1, u^3 - u^2 + 2u - 1 \rangle
\end{aligned}$$

$$I_1^v = \langle a, b+1, v+1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 67 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILS/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3u^{20} - 26u^{19} + \cdots + 7b + 97, -83u^{20} - 325u^{19} + \cdots + 63a + 558, u^{21} + 5u^{20} + \cdots - 72u - 9 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \left( \frac{83}{63}u^{20} + \frac{325}{63}u^{19} + \cdots - 66u - \frac{62}{7} \right) \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \left( \frac{110}{63}u^{20} + \frac{559}{63}u^{19} + \cdots - 161u - \frac{159}{7} \right) \\ a_{11} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix} \\ a_9 &= \left( \frac{83}{63}u^{20} + \frac{325}{63}u^{19} + \cdots - 86u - \frac{90}{7} \right) \\ a_5 &= \left( -\frac{97}{63}u^{20} - \frac{458}{63}u^{19} + \cdots + 111u + \frac{111}{7} \right) \\ a_2 &= \left( -\frac{52}{63}u^{20} - \frac{215}{63}u^{19} + \cdots + 39u + \frac{38}{7} \right) \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{4}{7}u^{20} + \frac{51}{7}u^{19} + \cdots - 324u - \frac{456}{7}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{21} + 2u^{20} + \cdots + 8u + 1$
$c_2$	$u^{21} + 15u^{20} + \cdots + 63u + 9$
$c_4, c_9$	$u^{21} - 2u^{20} + \cdots - 11u^2 + 1$
$c_5, c_8$	$u^{21} - u^{20} + \cdots - u - 1$
$c_6, c_7, c_{11}$	$u^{21} + 5u^{20} + \cdots - 72u - 9$
$c_{10}, c_{12}$	$u^{21} - 5u^{20} + \cdots - 2988u - 1413$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{21} + 30y^{20} + \cdots + 6y - 1$
$c_2$	$y^{21} - 13y^{20} + \cdots - 1377y - 81$
$c_4, c_9$	$y^{21} - 22y^{20} + \cdots + 22y - 1$
$c_5, c_8$	$y^{21} - 11y^{20} + \cdots + 21y - 1$
$c_6, c_7, c_{11}$	$y^{21} + 23y^{20} + \cdots + 324y - 81$
$c_{10}, c_{12}$	$y^{21} + 19y^{20} + \cdots - 3839724y - 1996569$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.834623 + 0.573705I$		
$a = 1.005930 + 0.264258I$	$6.40877 + 10.26430I$	$-4.52348 - 6.93928I$
$b = 0.62121 - 1.82385I$		
$u = -0.834623 - 0.573705I$		
$a = 1.005930 - 0.264258I$	$6.40877 - 10.26430I$	$-4.52348 + 6.93928I$
$b = 0.62121 + 1.82385I$		
$u = -0.847213 + 0.586710I$		
$a = -0.922945 + 0.173773I$	$6.42391 - 4.68256I$	$-3.99466 + 2.17560I$
$b = 0.16137 + 1.79856I$		
$u = -0.847213 - 0.586710I$		
$a = -0.922945 - 0.173773I$	$6.42391 + 4.68256I$	$-3.99466 - 2.17560I$
$b = 0.16137 - 1.79856I$		
$u = 0.825151$		
$a = -0.722716$	-5.68389	-17.0230
$b = -0.926404$		
$u = -0.150569 + 1.281090I$		
$a = 0.434742 - 0.402686I$	$3.22602 + 2.41816I$	$-3.53897 - 1.93549I$
$b = 0.074569 + 0.138439I$		
$u = -0.150569 - 1.281090I$		
$a = 0.434742 + 0.402686I$	$3.22602 - 2.41816I$	$-3.53897 + 1.93549I$
$b = 0.074569 - 0.138439I$		
$u = -0.323088 + 0.617615I$		
$a = 0.358624 - 0.512504I$	$0.52795 + 2.17494I$	$-5.93194 - 4.33334I$
$b = -0.096498 + 0.850760I$		
$u = -0.323088 - 0.617615I$		
$a = 0.358624 + 0.512504I$	$0.52795 - 2.17494I$	$-5.93194 + 4.33334I$
$b = -0.096498 - 0.850760I$		
$u = 0.373837 + 1.314800I$		
$a = 0.363936 + 0.564961I$	$-1.57111 - 4.30895I$	$-11.00324 + 1.55396I$
$b = -0.998750 + 0.204857I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.373837 - 1.314800I$		
$a = 0.363936 - 0.564961I$	$-1.57111 + 4.30895I$	$-11.00324 - 1.55396I$
$b = -0.998750 - 0.204857I$		
$u = -0.027283 + 1.412760I$		
$a = 0.78061 + 1.55576I$	$3.18953 + 0.20531I$	$-5.89178 + 0.57061I$
$b = -1.109230 - 0.677694I$		
$u = -0.027283 - 1.412760I$		
$a = 0.78061 - 1.55576I$	$3.18953 - 0.20531I$	$-5.89178 - 0.57061I$
$b = -1.109230 + 0.677694I$		
$u = -0.437416 + 0.103332I$		
$a = 0.929988 - 0.551312I$	$-0.974855 + 0.275619I$	$-10.86571 - 2.54923I$
$b = -0.189823 + 0.028334I$		
$u = -0.437416 - 0.103332I$		
$a = 0.929988 + 0.551312I$	$-0.974855 - 0.275619I$	$-10.86571 + 2.54923I$
$b = -0.189823 - 0.028334I$		
$u = -0.09149 + 1.57120I$		
$a = -0.26719 - 1.73552I$	$7.94844 + 3.68537I$	$-6.18348 + 2.45338I$
$b = 0.33826 + 1.86261I$		
$u = -0.09149 - 1.57120I$		
$a = -0.26719 + 1.73552I$	$7.94844 - 3.68537I$	$-6.18348 - 2.45338I$
$b = 0.33826 - 1.86261I$		
$u = -0.28888 + 1.56597I$		
$a = 0.45254 + 2.00394I$	$13.4087 + 14.4061I$	$-2.12525 - 6.98840I$
$b = 1.01317 - 2.01561I$		
$u = -0.28888 - 1.56597I$		
$a = 0.45254 - 2.00394I$	$13.4087 - 14.4061I$	$-2.12525 + 6.98840I$
$b = 1.01317 + 2.01561I$		
$u = -0.28585 + 1.59217I$		
$a = -0.77487 - 1.52631I$	$13.60260 - 0.45994I$	$-1.43013 + 1.46856I$
$b = -0.35107 + 2.01142I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.28585 - 1.59217I$		
$a = -0.77487 + 1.52631I$	$13.60260 + 0.45994I$	$-1.43013 - 1.46856I$
$b = -0.35107 - 2.01142I$		

$$\text{II. } I_2^u = \langle -3u^{14}a + 5u^{14} + \cdots + a + 24, -u^{14}a + 2u^{13}a + \cdots + 3a + 4, u^{15} - 2u^{14} + \cdots - 4u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} a \\ \frac{3}{14}u^{14}a - \frac{5}{14}u^{14} + \cdots - \frac{1}{14}a - \frac{12}{7} \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.214286au^{14} - 0.357143u^{14} + \cdots + 0.928571a - 1.71429 \\ \frac{3}{14}u^{14}a - \frac{5}{14}u^{14} + \cdots - \frac{1}{14}a - \frac{12}{7} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} \frac{10}{7}u^{14}a + \frac{9}{7}u^{14} + \cdots - \frac{8}{7}a - \frac{10}{7} \\ \frac{5}{14}u^{14}a + \frac{1}{14}u^{14} + \cdots - \frac{25}{14}a - \frac{6}{7} \end{pmatrix} \\ a_5 &= \begin{pmatrix} -\frac{1}{14}u^{14}a - \frac{5}{7}u^{14} + \cdots + \frac{6}{7}a + \frac{1}{14} \\ -0.142857au^{14} - 0.928571u^{14} + \cdots + 0.214286a - 0.357143 \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{5}{14}u^{14}a - \frac{3}{7}u^{14} + \cdots + \frac{12}{7}a + \frac{9}{14} \\ 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

$$(iii) \text{ Cusp Shapes} = 11u^{14} - 16u^{13} + 97u^{12} - 120u^{11} + 326u^{10} - 337u^9 + 511u^8 - 400u^7 + 342u^6 - 95u^5 + 10u^4 + 150u^3 - 84u^2 + 55u - 19$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{30} - 7u^{29} + \cdots - 676u - 329$
$c_2$	$(u^{15} - 7u^{14} + \cdots + 28u - 8)^2$
$c_4, c_9$	$u^{30} - 14u^{28} + \cdots - 641u + 151$
$c_5, c_8$	$u^{30} + 9u^{26} + \cdots - u - 1$
$c_6, c_7, c_{11}$	$(u^{15} - 2u^{14} + \cdots - 4u + 1)^2$
$c_{10}, c_{12}$	$(u^{15} + 2u^{14} + \cdots - 16u + 5)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{30} + 33y^{29} + \cdots + 1028130y + 108241$
$c_2$	$(y^{15} - 7y^{14} + \cdots + 528y - 64)^2$
$c_4, c_9$	$y^{30} - 28y^{29} + \cdots + 125773y + 22801$
$c_5, c_8$	$y^{30} + 18y^{28} + \cdots - 35y + 1$
$c_6, c_7, c_{11}$	$(y^{15} + 16y^{14} + \cdots - 4y - 1)^2$
$c_{10}, c_{12}$	$(y^{15} + 16y^{14} + \cdots - 344y - 25)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.783022 + 0.548748I$		
$a = -0.815000 - 0.070479I$	$7.57107 - 2.60312I$	$-2.84235 + 2.92184I$
$b = 0.23196 - 1.72434I$		
$u = 0.783022 + 0.548748I$		
$a = 1.150630 - 0.405666I$	$7.57107 - 2.60312I$	$-2.84235 + 2.92184I$
$b = 0.61243 + 1.61879I$		
$u = 0.783022 - 0.548748I$		
$a = -0.815000 + 0.070479I$	$7.57107 + 2.60312I$	$-2.84235 - 2.92184I$
$b = 0.23196 + 1.72434I$		
$u = 0.783022 - 0.548748I$		
$a = 1.150630 + 0.405666I$	$7.57107 + 2.60312I$	$-2.84235 - 2.92184I$
$b = 0.61243 - 1.61879I$		
$u = -0.216855 + 1.221530I$		
$a = 0.741221 - 0.405618I$	$1.58567 + 3.38986I$	$-3.26125 - 8.75376I$
$b = -0.661072 + 0.460812I$		
$u = -0.216855 + 1.221530I$		
$a = 0.660981 + 1.010040I$	$1.58567 + 3.38986I$	$-3.26125 - 8.75376I$
$b = 0.913612 + 0.021844I$		
$u = -0.216855 - 1.221530I$		
$a = 0.741221 + 0.405618I$	$1.58567 - 3.38986I$	$-3.26125 + 8.75376I$
$b = -0.661072 - 0.460812I$		
$u = -0.216855 - 1.221530I$		
$a = 0.660981 - 1.010040I$	$1.58567 - 3.38986I$	$-3.26125 + 8.75376I$
$b = 0.913612 - 0.021844I$		
$u = -0.699136$		
$a = 0.498930$	$-2.08475$	$-3.31340$
$b = -0.445090$		
$u = -0.699136$		
$a = 1.87307$	$-2.08475$	$-3.31340$
$b = 0.972659$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.061637 + 0.608365I$		
$a = 0.934694 + 0.293027I$	$1.61379 + 2.57496I$	$-1.10179 - 1.01110I$
$b = 0.986562 + 0.556921I$		
$u = 0.061637 + 0.608365I$		
$a = 0.94855 - 1.35297I$	$1.61379 + 2.57496I$	$-1.10179 - 1.01110I$
$b = -0.329324 + 1.042070I$		
$u = 0.061637 - 0.608365I$		
$a = 0.934694 - 0.293027I$	$1.61379 - 2.57496I$	$-1.10179 + 1.01110I$
$b = 0.986562 - 0.556921I$		
$u = 0.061637 - 0.608365I$		
$a = 0.94855 + 1.35297I$	$1.61379 - 2.57496I$	$-1.10179 + 1.01110I$
$b = -0.329324 - 1.042070I$		
$u = 0.09920 + 1.46553I$		
$a = -0.395823 - 0.646191I$	$6.22877 - 5.97807I$	$-2.99155 + 7.20850I$
$b = -0.609648 + 0.043969I$		
$u = 0.09920 + 1.46553I$		
$a = -0.26994 + 2.77190I$	$6.22877 - 5.97807I$	$-2.99155 + 7.20850I$
$b = -0.31360 - 2.40695I$		
$u = 0.09920 - 1.46553I$		
$a = -0.395823 + 0.646191I$	$6.22877 + 5.97807I$	$-2.99155 - 7.20850I$
$b = -0.609648 - 0.043969I$		
$u = 0.09920 - 1.46553I$		
$a = -0.26994 - 2.77190I$	$6.22877 + 5.97807I$	$-2.99155 - 7.20850I$
$b = -0.31360 + 2.40695I$		
$u = -0.01760 + 1.52899I$		
$a = -1.250130 - 0.500701I$	$8.69622 + 2.65996I$	$1.50438 - 2.01476I$
$b = 2.00715 + 0.63605I$		
$u = -0.01760 + 1.52899I$		
$a = 0.23286 - 2.06811I$	$8.69622 + 2.65996I$	$1.50438 - 2.01476I$
$b = -0.18397 + 1.61289I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.01760 - 1.52899I$		
$a = -1.250130 + 0.500701I$	$8.69622 - 2.65996I$	$1.50438 + 2.01476I$
$b = 2.00715 - 0.63605I$		
$u = -0.01760 - 1.52899I$		
$a = 0.23286 + 2.06811I$	$8.69622 - 2.65996I$	$1.50438 + 2.01476I$
$b = -0.18397 - 1.61289I$		
$u = 0.367791 + 0.287869I$		
$a = -1.078570 + 0.747772I$	$0.39798 - 4.38767I$	$-9.5578 + 11.0682I$
$b = -0.34613 - 1.55473I$		
$u = 0.367791 + 0.287869I$		
$a = -1.52156 - 2.49296I$	$0.39798 - 4.38767I$	$-9.5578 + 11.0682I$
$b = -0.006820 - 0.312135I$		
$u = 0.367791 - 0.287869I$		
$a = -1.078570 - 0.747772I$	$0.39798 + 4.38767I$	$-9.5578 - 11.0682I$
$b = -0.34613 + 1.55473I$		
$u = 0.367791 - 0.287869I$		
$a = -1.52156 + 2.49296I$	$0.39798 + 4.38767I$	$-9.5578 - 11.0682I$
$b = -0.006820 + 0.312135I$		
$u = 0.27238 + 1.54795I$		
$a = -0.97464 + 1.65279I$	$14.4273 - 6.4879I$	$-0.59296 + 3.62205I$
$b = -0.05742 - 2.01595I$		
$u = 0.27238 + 1.54795I$		
$a = 0.45074 - 1.92343I$	$14.4273 - 6.4879I$	$-0.59296 + 3.62205I$
$b = 0.99248 + 1.70658I$		
$u = 0.27238 - 1.54795I$		
$a = -0.97464 - 1.65279I$	$14.4273 + 6.4879I$	$-0.59296 - 3.62205I$
$b = -0.05742 + 2.01595I$		
$u = 0.27238 - 1.54795I$		
$a = 0.45074 + 1.92343I$	$14.4273 + 6.4879I$	$-0.59296 - 3.62205I$
$b = 0.99248 - 1.70658I$		

$$\text{III. } I_3^u = \langle -u^6 - 2u^5 - 5u^4 - 6u^3 - 6u^2 + b - 4u - 1, u^8 + 2u^7 + \dots + a - 1, u^9 + 2u^8 + \dots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^8 - 2u^7 - 7u^6 - 10u^5 - 15u^4 - 14u^3 - 9u^2 - 5u + 1 \\ u^6 + 2u^5 + 5u^4 + 6u^3 + 6u^2 + 4u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^8 - 2u^7 - 6u^6 - 8u^5 - 10u^4 - 8u^3 - 3u^2 - u + 2 \\ u^6 + 2u^5 + 5u^4 + 6u^3 + 6u^2 + 4u + 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^5 - 2u^3 - u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^7 - 2u^6 - 6u^5 - 8u^4 - 10u^3 - 9u^2 - 4u - 3 \\ -u^8 - 2u^7 - 6u^6 - 8u^5 - 11u^4 - 9u^3 - 6u^2 - 3u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^8 - 2u^7 - 7u^6 - 9u^5 - 14u^4 - 11u^3 - 7u^2 - 3u + 2 \\ u^7 + 2u^6 + 6u^5 + 8u^4 + 10u^3 + 8u^2 + 4u + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^8 - 2u^7 - 6u^6 - 10u^5 - 13u^4 - 16u^3 - 11u^2 - 9u - 3 \\ -u^7 - u^6 - 4u^5 - 3u^4 - 4u^3 - 2u^2 + 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $u^8 - 4u^6 - 13u^5 - 32u^4 - 38u^3 - 40u^2 - 24u - 8$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^9 + 3u^8 + 9u^7 + 14u^6 + 18u^5 + 18u^4 + 13u^3 + 8u^2 + 4u + 1$
$c_2$	$u^9 + 12u^8 + \dots + 401u + 89$
$c_4, c_9$	$u^9 - u^8 - u^7 + 2u^6 + 2u^5 - 2u^4 - u^3 + 2u^2 - 1$
$c_5, c_8$	$u^9 - 2u^7 - u^6 + 2u^5 + 2u^4 - 2u^3 - u^2 + u + 1$
$c_6, c_7$	$u^9 + 2u^8 + 7u^7 + 10u^6 + 16u^5 + 16u^4 + 13u^3 + 9u^2 + 2u + 1$
$c_{10}, c_{12}$	$u^9 + 2u^8 + 3u^7 + u^6 - 18u^5 - 20u^4 - 4u^3 - 11u^2 - 1$
$c_{11}$	$u^9 - 2u^8 + 7u^7 - 10u^6 + 16u^5 - 16u^4 + 13u^3 - 9u^2 + 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^9 + 9y^8 + 33y^7 + 46y^6 + 14y^5 - 14y^4 - 3y^3 + 4y^2 - 1$
$c_2$	$y^9 - 6y^8 + \dots + 8789y - 7921$
$c_4, c_9$	$y^9 - 3y^8 + 9y^7 - 14y^6 + 18y^5 - 18y^4 + 13y^3 - 8y^2 + 4y - 1$
$c_5, c_8$	$y^9 - 4y^8 + 8y^7 - 13y^6 + 18y^5 - 18y^4 + 14y^3 - 9y^2 + 3y - 1$
$c_6, c_7, c_{11}$	$y^9 + 10y^8 + 41y^7 + 86y^6 + 86y^5 + 4y^4 - 75y^3 - 61y^2 - 14y - 1$
$c_{10}, c_{12}$	$y^9 + 2y^8 - 31y^7 - 37y^6 + 384y^5 - 230y^4 - 422y^3 - 161y^2 - 22y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.942156$		
$a = 0.835924$	-4.78668	-6.85480
$b = 0.693833$		
$u = 0.025437 + 1.219490I$		
$a = -0.848257 + 0.499627I$	$3.87432 - 3.77454I$	$-1.17699 + 5.61151I$
$b = -0.174357 - 0.757557I$		
$u = 0.025437 - 1.219490I$		
$a = -0.848257 - 0.499627I$	$3.87432 + 3.77454I$	$-1.17699 - 5.61151I$
$b = -0.174357 + 0.757557I$		
$u = -0.465053 + 1.257920I$		
$a = 0.128314 + 0.500319I$	-0.89563 + 5.00672I	-5.11040 - 6.89072I
$b = 0.628101 + 0.278164I$		
$u = -0.465053 - 1.257920I$		
$a = 0.128314 - 0.500319I$	-0.89563 - 5.00672I	-5.11040 + 6.89072I
$b = 0.628101 - 0.278164I$		
$u = -0.05596 + 1.56008I$		
$a = -0.27494 - 1.81410I$	$8.14041 + 4.21823I$	$-1.16365 - 10.14642I$
$b = 0.58625 + 1.89814I$		
$u = -0.05596 - 1.56008I$		
$a = -0.27494 + 1.81410I$	$8.14041 - 4.21823I$	$-1.16365 + 10.14642I$
$b = 0.58625 - 1.89814I$		
$u = -0.033345 + 0.402052I$		
$a = 2.07693 - 1.08799I$	$1.14384 + 3.68908I$	$-2.12153 - 6.55211I$
$b = 0.113094 + 1.126000I$		
$u = -0.033345 - 0.402052I$		
$a = 2.07693 + 1.08799I$	$1.14384 - 3.68908I$	$-2.12153 + 6.55211I$
$b = 0.113094 - 1.126000I$		

$$\text{IV. } I_4^u = \langle b + 1, 2u^2a + a^2 - 2au + 3a + u - 1, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a - 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^2a - au + 2a + u + 1 \\ u^2a - au + u^2 + a + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + u - 2 \\ -au - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a - 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u^2 - 16$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u - 1)^6$
$c_2$	$u^6$
$c_4, c_5, c_8$ $c_9$	$u^6 + u^5 - 3u^4 - 3u^3 + 3u^2 + u - 1$
$c_6, c_7$	$(u^3 - u^2 + 2u - 1)^2$
$c_{10}, c_{12}$	$(u^3 - u^2 + 1)^2$
$c_{11}$	$(u^3 + u^2 + 2u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$(y - 1)^6$
$c_2$	$y^6$
$c_4, c_5, c_8$ $c_9$	$y^6 - 7y^5 + 21y^4 - 31y^3 + 21y^2 - 7y + 1$
$c_6, c_7, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_{10}, c_{12}$	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.215080 + 1.307140I$		
$a = 1.153780 + 0.265134I$	$1.37919 - 2.82812I$	$-7.68821 - 2.81140I$
$b = -1.00000$		
$u = 0.215080 + 1.307140I$		
$a = -0.398899 + 1.224590I$	$1.37919 - 2.82812I$	$-7.68821 - 2.81140I$
$b = -1.00000$		
$u = 0.215080 - 1.307140I$		
$a = 1.153780 - 0.265134I$	$1.37919 + 2.82812I$	$-7.68821 + 2.81140I$
$b = -1.00000$		
$u = 0.215080 - 1.307140I$		
$a = -0.398899 - 1.224590I$	$1.37919 + 2.82812I$	$-7.68821 + 2.81140I$
$b = -1.00000$		
$u = 0.569840$		
$a = 0.161059$	$-2.75839$	$-17.6240$
$b = -1.00000$		
$u = 0.569840$		
$a = -2.67081$	$-2.75839$	$-17.6240$
$b = -1.00000$		

$$\mathbf{V} \cdot I_1^v = \langle a, b+1, v+1 \rangle$$

(i) **Arc colorings**

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = -6

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_8, c_9$	$u + 1$
$c_2, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$u$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_8, c_9$	$y - 1$
$c_2, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	-1.64493	-6.00000
$b = -1.00000$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u - 1)^6(u + 1)$ $\cdot (u^9 + 3u^8 + 9u^7 + 14u^6 + 18u^5 + 18u^4 + 13u^3 + 8u^2 + 4u + 1)$ $\cdot (u^{21} + 2u^{20} + \dots + 8u + 1)(u^{30} - 7u^{29} + \dots - 676u - 329)$
$c_2$	$u^7(u^9 + 12u^8 + \dots + 401u + 89)(u^{15} - 7u^{14} + \dots + 28u - 8)^2$ $\cdot (u^{21} + 15u^{20} + \dots + 63u + 9)$
$c_4, c_9$	$(u + 1)(u^6 + u^5 - 3u^4 - 3u^3 + 3u^2 + u - 1)$ $\cdot (u^9 - u^8 - u^7 + 2u^6 + 2u^5 - 2u^4 - u^3 + 2u^2 - 1)$ $\cdot (u^{21} - 2u^{20} + \dots - 11u^2 + 1)(u^{30} - 14u^{28} + \dots - 641u + 151)$
$c_5, c_8$	$(u + 1)(u^6 + u^5 - 3u^4 - 3u^3 + 3u^2 + u - 1)$ $\cdot (u^9 - 2u^7 + \dots + u + 1)(u^{21} - u^{20} + \dots - u - 1)$ $\cdot (u^{30} + 9u^{26} + \dots - u - 1)$
$c_6, c_7$	$u(u^3 - u^2 + 2u - 1)^2$ $\cdot (u^9 + 2u^8 + 7u^7 + 10u^6 + 16u^5 + 16u^4 + 13u^3 + 9u^2 + 2u + 1)$ $\cdot ((u^{15} - 2u^{14} + \dots - 4u + 1)^2)(u^{21} + 5u^{20} + \dots - 72u - 9)$
$c_{10}, c_{12}$	$u(u^3 - u^2 + 1)^2(u^9 + 2u^8 + 3u^7 + u^6 - 18u^5 - 20u^4 - 4u^3 - 11u^2 - 1)$ $\cdot ((u^{15} + 2u^{14} + \dots - 16u + 5)^2)(u^{21} - 5u^{20} + \dots - 2988u - 1413)$
$c_{11}$	$u(u^3 + u^2 + 2u + 1)^2$ $\cdot (u^9 - 2u^8 + 7u^7 - 10u^6 + 16u^5 - 16u^4 + 13u^3 - 9u^2 + 2u - 1)$ $\cdot ((u^{15} - 2u^{14} + \dots - 4u + 1)^2)(u^{21} + 5u^{20} + \dots - 72u - 9)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$(y - 1)^7(y^9 + 9y^8 + 33y^7 + 46y^6 + 14y^5 - 14y^4 - 3y^3 + 4y^2 - 1) \cdot (y^{21} + 30y^{20} + \dots + 6y - 1)(y^{30} + 33y^{29} + \dots + 1028130y + 108241)$
$c_2$	$y^7(y^9 - 6y^8 + \dots + 8789y - 7921)(y^{15} - 7y^{14} + \dots + 528y - 64)^2 \cdot (y^{21} - 13y^{20} + \dots - 1377y - 81)$
$c_4, c_9$	$(y - 1)(y^6 - 7y^5 + 21y^4 - 31y^3 + 21y^2 - 7y + 1) \cdot (y^9 - 3y^8 + 9y^7 - 14y^6 + 18y^5 - 18y^4 + 13y^3 - 8y^2 + 4y - 1) \cdot (y^{21} - 22y^{20} + \dots + 22y - 1)(y^{30} - 28y^{29} + \dots + 125773y + 22801)$
$c_5, c_8$	$(y - 1)(y^6 - 7y^5 + 21y^4 - 31y^3 + 21y^2 - 7y + 1) \cdot (y^9 - 4y^8 + 8y^7 - 13y^6 + 18y^5 - 18y^4 + 14y^3 - 9y^2 + 3y - 1) \cdot (y^{21} - 11y^{20} + \dots + 21y - 1)(y^{30} + 18y^{28} + \dots - 35y + 1)$
$c_6, c_7, c_{11}$	$y(y^3 + 3y^2 + 2y - 1)^2 \cdot (y^9 + 10y^8 + 41y^7 + 86y^6 + 86y^5 + 4y^4 - 75y^3 - 61y^2 - 14y - 1) \cdot ((y^{15} + 16y^{14} + \dots - 4y - 1)^2)(y^{21} + 23y^{20} + \dots + 324y - 81)$
$c_{10}, c_{12}$	$y(y^3 - y^2 + 2y - 1)^2 \cdot (y^9 + 2y^8 - 31y^7 - 37y^6 + 384y^5 - 230y^4 - 422y^3 - 161y^2 - 22y - 1) \cdot (y^{15} + 16y^{14} + \dots - 344y - 25)^2 \cdot (y^{21} + 19y^{20} + \dots - 3839724y - 1996569)$