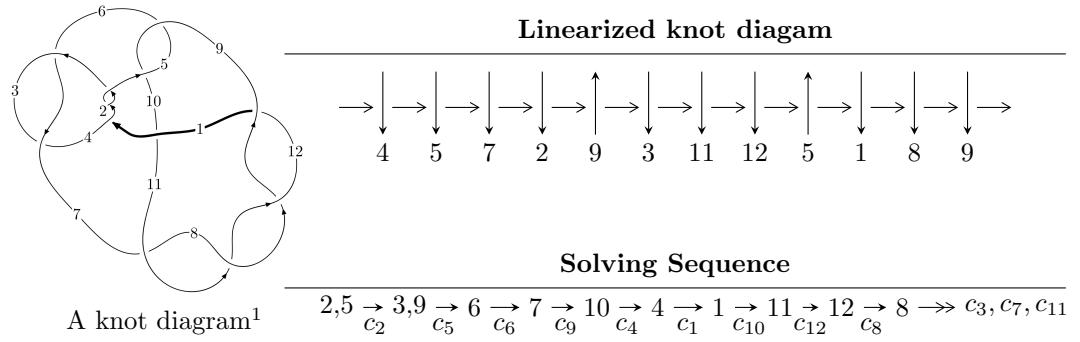


$12n_{0674}$  ( $K12n_{0674}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -8.95545 \times 10^{24} u^{41} - 2.72305 \times 10^{25} u^{40} + \dots + 2.32080 \times 10^{24} b + 1.04846 \times 10^{24}, \\
 &\quad - 2.76332 \times 10^{24} u^{41} - 4.41119 \times 10^{24} u^{40} + \dots + 2.32080 \times 10^{24} a + 2.12642 \times 10^{25}, \\
 &\quad u^{42} + 4u^{41} + \dots + 14u - 1 \rangle \\
 I_2^u &= \langle b + 1, a, u^2 + u - 1 \rangle \\
 I_3^u &= \langle b - u - 2, a, u^2 + u - 1 \rangle \\
 I_4^u &= \langle b, a + 1, u - 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 47 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -8.96 \times 10^{24}u^{41} - 2.72 \times 10^{25}u^{40} + \dots + 2.32 \times 10^{24}b + 1.05 \times 10^{24}, -2.76 \times 10^{24}u^{41} - 4.41 \times 10^{24}u^{40} + \dots + 2.32 \times 10^{24}a + 2.13 \times 10^{25}, u^{42} + 4u^{41} + \dots + 14u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.19067u^{41} + 1.90072u^{40} + \dots + 60.6010u - 9.16243 \\ 3.85878u^{41} + 11.7332u^{40} + \dots + 22.3744u - 0.451767 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.105132u^{41} - 0.0128494u^{40} + \dots - 34.8388u + 4.84834 \\ -0.848783u^{41} - 2.84893u^{40} + \dots - 15.2500u + 0.685419 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.978378u^{41} + 2.65739u^{40} + \dots - 25.4014u + 4.57060 \\ 1.25612u^{41} + 2.68484u^{40} + \dots + 9.12669u - 0.978378 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1.19067u^{41} + 1.90072u^{40} + \dots + 60.6010u - 9.16243 \\ 0.716340u^{41} + 3.10175u^{40} + \dots - 18.8840u + 2.41021 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 2.55115u^{41} + 4.97020u^{40} + \dots + 92.6692u - 12.2894 \\ 5.70141u^{41} + 16.8545u^{40} + \dots + 38.1516u - 1.40486 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.546898u^{41} - 1.27331u^{40} + \dots - 34.6001u + 6.91046 \\ -1.81884u^{41} - 4.93743u^{40} + \dots - 37.5544u + 2.14072 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.0791429u^{41} + 0.265882u^{40} + \dots - 13.4298u - 0.240862 \\ -0.00645021u^{41} - 0.654296u^{40} + \dots + 17.6519u - 1.13841 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{8061029839060072009079083}{55742079073151734903802548}u^{41} + \frac{4209450828705721840877893}{580200482478865422121953}u^{40} + \dots +$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_4$	$u^{42} - 4u^{41} + \cdots - 14u - 1$
$c_3, c_6$	$u^{42} + 3u^{41} + \cdots - 15u^2 + 2$
$c_5, c_9$	$u^{42} - 2u^{41} + \cdots - 32u - 16$
$c_7, c_8, c_{11}$ $c_{12}$	$u^{42} + 4u^{41} + \cdots - 10u + 1$
$c_{10}$	$u^{42} - 8u^{41} + \cdots - 11932u - 167$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$y^{42} - 36y^{41} + \cdots - 78y + 1$
$c_3, c_6$	$y^{42} - 15y^{41} + \cdots - 60y + 4$
$c_5, c_9$	$y^{42} - 26y^{41} + \cdots - 7296y + 256$
$c_7, c_8, c_{11}$ $c_{12}$	$y^{42} - 48y^{41} + \cdots - 154y + 1$
$c_{10}$	$y^{42} + 12y^{41} + \cdots - 132872662y + 27889$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.238287 + 0.993330I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.256688 - 1.363750I$	$-3.87928 - 8.09823I$	$-11.51544 + 5.48666I$
$b = 0.448503 - 0.389957I$		
$u = 0.238287 - 0.993330I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.256688 + 1.363750I$	$-3.87928 + 8.09823I$	$-11.51544 - 5.48666I$
$b = 0.448503 + 0.389957I$		
$u = 1.060390 + 0.045339I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.258751 + 0.376269I$	$-2.71639 - 0.33816I$	$-4.0081 - 13.7250I$
$b = -0.47464 + 2.91568I$		
$u = 1.060390 - 0.045339I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.258751 - 0.376269I$	$-2.71639 + 0.33816I$	$-4.0081 + 13.7250I$
$b = -0.47464 - 2.91568I$		
$u = 0.106704 + 0.918803I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.26496 + 1.45259I$	$3.36143 - 5.24537I$	$-7.74689 + 6.20199I$
$b = -0.086830 + 0.297294I$		
$u = 0.106704 - 0.918803I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.26496 - 1.45259I$	$3.36143 + 5.24537I$	$-7.74689 - 6.20199I$
$b = -0.086830 - 0.297294I$		
$u = 1.147150 + 0.210471I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.302824 - 0.583834I$	$-10.17350 - 0.96398I$	$-18.1472 - 3.3317I$
$b = -0.04054 - 3.07018I$		
$u = 1.147150 - 0.210471I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.302824 + 0.583834I$	$-10.17350 + 0.96398I$	$-18.1472 + 3.3317I$
$b = -0.04054 + 3.07018I$		
$u = -0.049648 + 0.825086I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.32016 - 1.57337I$	$4.07908 - 1.05002I$	$-5.39403 - 0.20283I$
$b = -0.281826 - 0.254570I$		
$u = -0.049648 - 0.825086I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.32016 + 1.57337I$	$4.07908 + 1.05002I$	$-5.39403 + 0.20283I$
$b = -0.281826 + 0.254570I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.168990 + 0.199735I$		
$a = 1.249760 + 0.642269I$	$-3.90037 + 1.20976I$	$-15.7241 - 4.9251I$
$b = 1.006910 + 0.970924I$		
$u = -1.168990 - 0.199735I$		
$a = 1.249760 - 0.642269I$	$-3.90037 - 1.20976I$	$-15.7241 + 4.9251I$
$b = 1.006910 - 0.970924I$		
$u = -0.314243 + 0.696899I$		
$a = 0.56188 + 1.69109I$	$-1.53621 + 1.78916I$	$-8.56962 - 1.59900I$
$b = 0.733268 + 0.302512I$		
$u = -0.314243 - 0.696899I$		
$a = 0.56188 - 1.69109I$	$-1.53621 - 1.78916I$	$-8.56962 + 1.59900I$
$b = 0.733268 - 0.302512I$		
$u = -1.244640 + 0.090513I$		
$a = 0.277107 - 1.196450I$	$-4.74961 + 2.33690I$	$-17.2595 - 5.0904I$
$b = 0.18513 - 2.18299I$		
$u = -1.244640 - 0.090513I$		
$a = 0.277107 + 1.196450I$	$-4.74961 - 2.33690I$	$-17.2595 + 5.0904I$
$b = 0.18513 + 2.18299I$		
$u = 1.157940 + 0.481959I$		
$a = -0.776705 + 0.303294I$	$0.121226 + 0.269727I$	$-8.00000 - 3.11579I$
$b = -0.979087 + 0.599725I$		
$u = 1.157940 - 0.481959I$		
$a = -0.776705 - 0.303294I$	$0.121226 - 0.269727I$	$-8.00000 + 3.11579I$
$b = -0.979087 - 0.599725I$		
$u = 1.057900 + 0.692054I$		
$a = 0.907159 - 0.280920I$	$-6.34245 + 2.32209I$	$-13.28779 + 0.I$
$b = 0.898757 + 0.137083I$		
$u = 1.057900 - 0.692054I$		
$a = 0.907159 + 0.280920I$	$-6.34245 - 2.32209I$	$-13.28779 + 0.I$
$b = 0.898757 - 0.137083I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.722474$		
$a = -0.399724$	-1.09552	-8.48520
$b = 0.258120$		
$u = -1.245000 + 0.375694I$		
$a = -0.928202 - 0.816670I$	$0.37946 + 5.36737I$	0
$b = -1.17456 - 1.47199I$		
$u = -1.245000 - 0.375694I$		
$a = -0.928202 + 0.816670I$	$0.37946 - 5.36737I$	0
$b = -1.17456 + 1.47199I$		
$u = -1.31935$		
$a = -1.01441$	-14.8036	-18.1030
$b = -0.0413566$		
$u = -1.308760 + 0.256721I$		
$a = -0.597154 + 0.929246I$	$-11.72140 + 5.51488I$	0
$b = -0.45147 + 2.20887I$		
$u = -1.308760 - 0.256721I$		
$a = -0.597154 - 0.929246I$	$-11.72140 - 5.51488I$	0
$b = -0.45147 - 2.20887I$		
$u = 0.126480 + 0.653902I$		
$a = 1.60072 - 0.06394I$	$-7.23822 - 2.23215I$	$-12.66894 + 2.87063I$
$b = -0.579441 - 0.327004I$		
$u = 0.126480 - 0.653902I$		
$a = 1.60072 + 0.06394I$	$-7.23822 + 2.23215I$	$-12.66894 - 2.87063I$
$b = -0.579441 + 0.327004I$		
$u = 1.329240 + 0.371704I$		
$a = 0.714985 - 0.404132I$	-0.24891 - 3.25176I	0
$b = 1.36849 - 1.26529I$		
$u = 1.329240 - 0.371704I$		
$a = 0.714985 + 0.404132I$	-0.24891 + 3.25176I	0
$b = 1.36849 + 1.26529I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.35150 + 0.42227I$		
$a = 0.777238 + 0.800492I$	$-1.20516 + 10.04620I$	0
$b = 1.23840 + 1.87181I$		
$u = -1.35150 - 0.42227I$		
$a = 0.777238 - 0.800492I$	$-1.20516 - 10.04620I$	0
$b = 1.23840 - 1.87181I$		
$u = 1.46265 + 0.31490I$		
$a = -0.703570 + 0.478725I$	$-7.27437 - 5.59691I$	0
$b = -1.75849 + 1.73373I$		
$u = 1.46265 - 0.31490I$		
$a = -0.703570 - 0.478725I$	$-7.27437 + 5.59691I$	0
$b = -1.75849 - 1.73373I$		
$u = -1.43580 + 0.43130I$		
$a = -0.682703 - 0.780467I$	$-9.1607 + 13.1986I$	0
$b = -1.24611 - 2.24244I$		
$u = -1.43580 - 0.43130I$		
$a = -0.682703 + 0.780467I$	$-9.1607 - 13.1986I$	0
$b = -1.24611 + 2.24244I$		
$u = 0.403841$		
$a = 1.04866$	$-9.66299$	4.31750
$b = -2.15536$		
$u = -1.64023$		
$a = 0.220147$	$-9.70143$	0
$b = 0.661174$		
$u = 0.152045 + 0.289588I$		
$a = -1.95648 - 0.86091I$	$-0.703904 - 0.992275I$	$-8.59202 + 6.89400I$
$b = 0.166595 + 0.401559I$		
$u = 0.152045 - 0.289588I$		
$a = -1.95648 + 0.86091I$	$-0.703904 + 0.992275I$	$-8.59202 - 6.89400I$
$b = 0.166595 - 0.401559I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.71883$		
$a = -0.450881$	-16.8863	0
$b = -1.47918$		
$u = 0.111686$		
$a = -4.57994$	-1.32929	-5.96870
$b = 0.810470$		

$$\text{II. } I_2^u = \langle b+1, a, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u+1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u+1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u-1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u+1 \\ -2u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u-1 \\ u-1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -21

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_8, c_{10}$	$u^2 + u - 1$
$c_4, c_6, c_{11}$ $c_{12}$	$u^2 - u - 1$
$c_5, c_9$	$u^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$	
$c_4, c_6, c_7$	$y^2 - 3y + 1$
$c_8, c_{10}, c_{11}$	
$c_{12}$	
$c_5, c_9$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$		
$a = 0$	-1.97392	-21.0000
$b = -1.00000$		
$u = -1.61803$		
$a = 0$	-17.7653	-21.0000
$b = -1.00000$		

$$\text{III. } I_3^u = \langle b - u - 2, a, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 2u + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u - 4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -3u - 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -36

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_7, c_8, c_{10}$	$u^2 + u - 1$
$c_4, c_6, c_{11}$ $c_{12}$	$u^2 - u - 1$
$c_5, c_9$	$u^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$	
$c_4, c_6, c_7$	$y^2 - 3y + 1$
$c_8, c_{10}, c_{11}$	
$c_{12}$	
$c_5, c_9$	$y^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$		
$a = 0$	-9.86960	-36.0000
$b = 2.61803$		
$u = -1.61803$		
$a = 0$	-9.86960	-36.0000
$b = 0.381966$		

$$\text{IV. } I_4^u = \langle b, a+1, u-1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$ $c_7, c_8, c_{10}$	$u - 1$
$c_3, c_6$	$u$
$c_4, c_9, c_{11}$ $c_{12}$	$u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	
$c_5, c_7, c_8$	$y - 1$
$c_9, c_{10}, c_{11}$	
$c_{12}$	
$c_3, c_6$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -1.00000$	-3.28987	-12.0000
$b = 0$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)(u^2 + u - 1)^2(u^{42} - 4u^{41} + \dots - 14u - 1)$
$c_3$	$u(u^2 + u - 1)^2(u^{42} + 3u^{41} + \dots - 15u^2 + 2)$
$c_4$	$(u + 1)(u^2 - u - 1)^2(u^{42} - 4u^{41} + \dots - 14u - 1)$
$c_5$	$u^4(u - 1)(u^{42} - 2u^{41} + \dots - 32u - 16)$
$c_6$	$u(u^2 - u - 1)^2(u^{42} + 3u^{41} + \dots - 15u^2 + 2)$
$c_7, c_8$	$(u - 1)(u^2 + u - 1)^2(u^{42} + 4u^{41} + \dots - 10u + 1)$
$c_9$	$u^4(u + 1)(u^{42} - 2u^{41} + \dots - 32u - 16)$
$c_{10}$	$(u - 1)(u^2 + u - 1)^2(u^{42} - 8u^{41} + \dots - 11932u - 167)$
$c_{11}, c_{12}$	$(u + 1)(u^2 - u - 1)^2(u^{42} + 4u^{41} + \dots - 10u + 1)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)(y^2 - 3y + 1)^2(y^{42} - 36y^{41} + \cdots - 78y + 1)$
$c_3, c_6$	$y(y^2 - 3y + 1)^2(y^{42} - 15y^{41} + \cdots - 60y + 4)$
$c_5, c_9$	$y^4(y - 1)(y^{42} - 26y^{41} + \cdots - 7296y + 256)$
$c_7, c_8, c_{11}$ $c_{12}$	$(y - 1)(y^2 - 3y + 1)^2(y^{42} - 48y^{41} + \cdots - 154y + 1)$
$c_{10}$	$(y - 1)(y^2 - 3y + 1)^2(y^{42} + 12y^{41} + \cdots - 1.32873 \times 10^8y + 27889)$