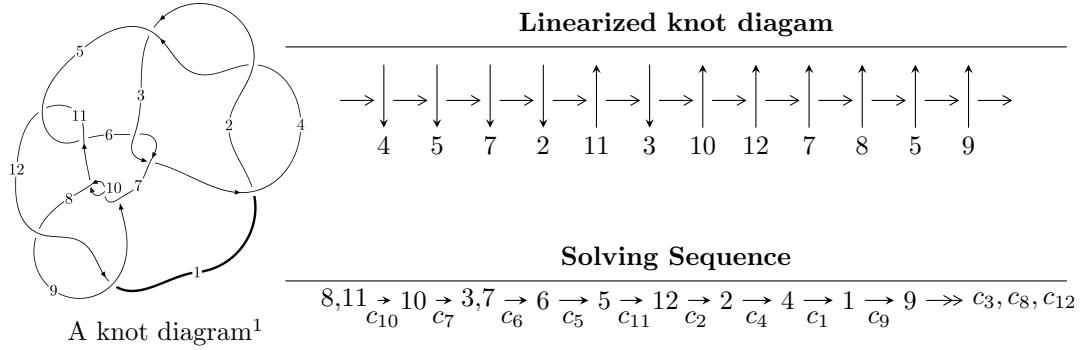


## $12n_{0681}$ ( $K12n_{0681}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -1.29319 \times 10^{25} u^{26} - 8.14562 \times 10^{25} u^{25} + \dots + 2.10275 \times 10^{26} b + 1.50746 \times 10^{26}, \\
 &\quad 9.51680 \times 10^{25} u^{26} + 6.52825 \times 10^{26} u^{25} + \dots + 2.10275 \times 10^{26} a - 7.67512 \times 10^{27}, u^{27} + 7u^{26} + \dots - 65u + \\
 I_2^u &= \langle -u^7 - 2u^6 + 2u^5 + 4u^4 - 2u^3 - u^2 + b + u - 3, 2u^7 + 2u^6 - 5u^5 - 4u^4 + 3u^3 + a + u + 3, \\
 &\quad u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1 \rangle \\
 I_3^u &= \langle 4a^2 + 23b - 33a + 3, a^3 - 8a^2 + 3a - 7, u - 1 \rangle \\
 I_4^u &= \langle b - 2u + 1, a + u + 4, u^2 + u - 1 \rangle \\
 I_5^u &= \langle b + u, a - u - 2, u^2 + u - 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 42 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.29 \times 10^{25}u^{26} - 8.15 \times 10^{25}u^{25} + \dots + 2.10 \times 10^{26}b + 1.51 \times 10^{26}, 9.52 \times 10^{25}u^{26} + 6.53 \times 10^{26}u^{25} + \dots + 2.10 \times 10^{26}a - 7.68 \times 10^{27}, u^{27} + 7u^{26} + \dots - 65u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.452588u^{26} - 3.10462u^{25} + \dots - 55.6935u + 36.5004 \\ 0.0614998u^{26} + 0.387379u^{25} + \dots + 3.33121u - 0.716900 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.486093u^{26} - 3.57968u^{25} + \dots - 55.8612u + 20.4963 \\ 0.0646653u^{26} + 0.428826u^{25} + \dots + 0.403387u - 0.357433 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.550758u^{26} - 4.00850u^{25} + \dots - 56.2646u + 20.8537 \\ 0.0646653u^{26} + 0.428826u^{25} + \dots + 0.403387u - 0.357433 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.0697411u^{26} - 0.446921u^{25} + \dots - 5.57659u + 8.05416 \\ -0.0811376u^{26} - 0.484277u^{25} + \dots + 5.23091u - 0.200858 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.478778u^{26} - 3.47699u^{25} + \dots - 53.7199u + 20.8543 \\ 0.0459720u^{26} + 0.264293u^{25} + \dots - 0.415707u - 0.385704 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.514677u^{26} - 3.50894u^{25} + \dots - 55.7920u + 36.4942 \\ 0.0496659u^{26} + 0.333051u^{25} + \dots + 5.46117u - 0.741054 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.0759051u^{26} + 0.518888u^{25} + \dots + 8.57256u - 7.97571 \\ 0.100287u^{26} + 0.631138u^{25} + \dots - 2.83878u + 0.163326 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{128221912491069143432166825}{210275241869650933749294956}u^{26} - \frac{1069012753234217659630964039}{210275241869650933749294956}u^{25} + \dots - \frac{14132876007342110386546979695}{210275241869650933749294956}u - \frac{1802365230129749281114104905}{210275241869650933749294956}$$

**(iv) u-Polynomials at the component**

| Crossings          | u-Polynomials at each crossing           |
|--------------------|--|
| $c_1, c_2, c_4$    | $u^{27} - 12u^{26} + \cdots - 82u - 1$   |
| $c_3, c_6$         | $u^{27} + 4u^{26} + \cdots + 640u - 256$ |
| $c_5, c_{11}$      | $u^{27} + 3u^{26} + \cdots - 112u + 16$  |
| $c_7, c_9, c_{10}$ | $u^{27} + 7u^{26} + \cdots - 65u + 1$    |
| $c_8, c_{12}$      | $u^{27} - 4u^{26} + \cdots - 36u + 8$    |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing              |
|--------------------|---|
| $c_1, c_2, c_4$    | $y^{27} - 46y^{26} + \cdots + 6314y - 1$        |
| $c_3, c_6$         | $y^{27} - 54y^{26} + \cdots + 5095424y - 65536$ |
| $c_5, c_{11}$      | $y^{27} + 25y^{26} + \cdots + 12928y - 256$     |
| $c_7, c_9, c_{10}$ | $y^{27} - 15y^{26} + \cdots + 4023y - 1$        |
| $c_8, c_{12}$      | $y^{27} + 12y^{26} + \cdots + 7696y - 64$       |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 0.989617$              |                                       |                        |
| $a = 9.38049$               | 0.561362                              | 203.500                |
| $b = 0.408460$              |                                       |                        |
| $u = -1.035410 + 0.203452I$ |                                       |                        |
| $a = -0.415320 + 0.863420I$ | $4.69512 + 2.40532I$                  | $3.41247 + 6.32084I$   |
| $b = -0.33969 + 1.38997I$   |                                       |                        |
| $u = -1.035410 - 0.203452I$ |                                       |                        |
| $a = -0.415320 - 0.863420I$ | $4.69512 - 2.40532I$                  | $3.41247 - 6.32084I$   |
| $b = -0.33969 - 1.38997I$   |                                       |                        |
| $u = 1.035950 + 0.225932I$  |                                       |                        |
| $a = -0.376658 + 0.725229I$ | $1.156740 + 0.801856I$                | $6.71973 + 0.16728I$   |
| $b = -0.061105 - 0.490914I$ |                                       |                        |
| $u = 1.035950 - 0.225932I$  |                                       |                        |
| $a = -0.376658 - 0.725229I$ | $1.156740 - 0.801856I$                | $6.71973 - 0.16728I$   |
| $b = -0.061105 + 0.490914I$ |                                       |                        |
| $u = -0.231476 + 0.812947I$ |                                       |                        |
| $a = -1.010650 - 0.337430I$ | $-2.46734 + 1.28188I$                 | $0.019660 - 0.966602I$ |
| $b = 0.147510 + 0.585443I$  |                                       |                        |
| $u = -0.231476 - 0.812947I$ |                                       |                        |
| $a = -1.010650 + 0.337430I$ | $-2.46734 - 1.28188I$                 | $0.019660 + 0.966602I$ |
| $b = 0.147510 - 0.585443I$  |                                       |                        |
| $u = 0.707396$              |                                       |                        |
| $a = -4.75513$              | -7.81649                              | 57.8300                |
| $b = 0.0513464$             |                                       |                        |
| $u = -1.305580 + 0.386979I$ |                                       |                        |
| $a = -0.110314 - 0.122910I$ | $1.16826 - 5.86191I$                  | $6.68570 + 1.60407I$   |
| $b = 0.073018 - 0.478334I$  |                                       |                        |
| $u = -1.305580 - 0.386979I$ |                                       |                        |
| $a = -0.110314 + 0.122910I$ | $1.16826 + 5.86191I$                  | $6.68570 - 1.60407I$   |
| $b = 0.073018 + 0.478334I$  |                                       |                        |

| Solutions to $I_1^u$          | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-------------------------------|---------------------------------------|-----------------------|
| $u = -0.836004 + 1.095460I$   |                                       |                       |
| $a = -0.0688478 + 0.0584922I$ | $-7.44159 - 1.29405I$                 | $-1.37770 + 1.27497I$ |
| $b = -0.25035 + 1.73182I$     |                                       |                       |
| $u = -0.836004 - 1.095460I$   |                                       |                       |
| $a = -0.0688478 - 0.0584922I$ | $-7.44159 + 1.29405I$                 | $-1.37770 - 1.27497I$ |
| $b = -0.25035 - 1.73182I$     |                                       |                       |
| $u = 0.558394 + 0.255485I$    |                                       |                       |
| $a = 0.39540 + 1.82247I$      | $-0.834252 + 0.150815I$               | $17.5464 - 6.6365I$   |
| $b = -0.99845 - 1.93414I$     |                                       |                       |
| $u = 0.558394 - 0.255485I$    |                                       |                       |
| $a = 0.39540 - 1.82247I$      | $-0.834252 - 0.150815I$               | $17.5464 + 6.6365I$   |
| $b = -0.99845 + 1.93414I$     |                                       |                       |
| $u = -1.016510 + 0.945163I$   |                                       |                       |
| $a = 1.046130 - 0.262688I$    | $-13.16990 - 3.53439I$                | $-0.41212 + 2.09406I$ |
| $b = -0.340400 - 0.098336I$   |                                       |                       |
| $u = -1.016510 - 0.945163I$   |                                       |                       |
| $a = 1.046130 + 0.262688I$    | $-13.16990 + 3.53439I$                | $-0.41212 - 2.09406I$ |
| $b = -0.340400 + 0.098336I$   |                                       |                       |
| $u = -1.16800 + 0.91505I$     |                                       |                       |
| $a = 1.271790 - 0.556686I$    | $-6.34499 - 6.08931I$                 | $-0.21731 + 3.73020I$ |
| $b = -0.35535 - 1.77081I$     |                                       |                       |
| $u = -1.16800 - 0.91505I$     |                                       |                       |
| $a = 1.271790 + 0.556686I$    | $-6.34499 + 6.08931I$                 | $-0.21731 - 3.73020I$ |
| $b = -0.35535 + 1.77081I$     |                                       |                       |
| $u = 0.491518$                |                                       |                       |
| $a = -0.797650$               | 0.859867                              | 11.9670               |
| $b = 0.376982$                |                                       |                       |
| $u = 0.06761 + 1.51979I$      |                                       |                       |
| $a = -0.239446 + 0.151266I$   | $18.5782 + 5.9421I$                   | $-1.31050 - 2.20591I$ |
| $b = 0.28102 - 2.41058I$      |                                       |                       |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.06761 - 1.51979I$    |                                       |                       |
| $a = -0.239446 - 0.151266I$ | $18.5782 - 5.9421I$                   | $-1.31050 + 2.20591I$ |
| $b = 0.28102 + 2.41058I$    |                                       |                       |
| $u = -1.60127$              |                                       |                       |
| $a = 2.03965$               | 7.98804                               | 43.0640               |
| $b = 3.57318$               |                                       |                       |
| $u = -1.55855 + 0.65683I$   |                                       |                       |
| $a = -1.03603 + 1.21486I$   | $-15.7574 - 13.5083I$                 | $0.77209 + 5.37939I$  |
| $b = 0.57720 + 2.23959I$    |                                       |                       |
| $u = -1.55855 - 0.65683I$   |                                       |                       |
| $a = -1.03603 - 1.21486I$   | $-15.7574 + 13.5083I$                 | $0.77209 - 5.37939I$  |
| $b = 0.57720 - 2.23959I$    |                                       |                       |
| $u = 1.68805 + 0.77291I$    |                                       |                       |
| $a = 0.823135 + 0.943566I$  | $-16.0044 + 2.3695I$                  | 0                     |
| $b = -0.10758 + 2.58327I$   |                                       |                       |
| $u = 1.68805 - 0.77291I$    |                                       |                       |
| $a = 0.823135 - 0.943566I$  | $-16.0044 - 2.3695I$                  | 0                     |
| $b = -0.10758 - 2.58327I$   |                                       |                       |
| $u = 0.0157914$             |                                       |                       |
| $a = 35.5742$               | -1.12664                              | -9.59770              |
| $b = -0.661597$             |                                       |                       |

$$\text{II. } I_2^u = \langle -u^7 - 2u^6 + 2u^5 + 4u^4 - 2u^3 - u^2 + b + u - 3, 2u^7 + 2u^6 - 5u^5 - 4u^4 + 3u^3 + a + u + 3, u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1 \rangle$$

(i) **Arc colorings**

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^7 - 2u^6 + 5u^5 + 4u^4 - 3u^3 - u - 3 \\ u^7 + 2u^6 - 2u^5 - 4u^4 + 2u^3 + u^2 - u + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ -u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^7 - 2u^6 + 5u^5 + 4u^4 - 4u^3 + u - 3 \\ u^7 + 2u^6 - 2u^5 - 4u^4 + 3u^3 + u^2 - 2u + 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u^7 - 2u^6 + 5u^5 + 4u^4 - 3u^3 - u - 3 \\ u^7 + 2u^6 - 2u^5 - 4u^4 + 2u^3 + u^2 - u + 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 + 2u \\ u^3 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $21u^7 + 38u^6 - 48u^5 - 85u^4 + 39u^3 + 27u^2 - 5u + 58$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                              |
|---------------|---|
| $c_1, c_2$    | $(u - 1)^8$   |
| $c_3, c_6$    | $u^8$   |
| $c_4$         | $(u + 1)^8$   |
| $c_5$         | $u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$ |
| $c_7$         | $u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$                   |
| $c_8$         | $u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$              |
| $c_9, c_{10}$ | $u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$                   |
| $c_{11}$      | $u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$ |
| $c_{12}$      | $u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$              |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing                           |
|--------------------|--|
| $c_1, c_2, c_4$    | $(y - 1)^8$  |
| $c_3, c_6$         | $y^8$  |
| $c_5, c_{11}$      | $y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$ |
| $c_7, c_9, c_{10}$ | $y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$  |
| $c_8, c_{12}$      | $y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 1.180120 + 0.268597I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = 1.23903 + 1.07030I$    | $-0.604279 + 1.131230I$               | $0.744211 + 0.553382I$ |
| $b = -0.281371 + 1.128550I$ |                                       |                        |
| $u = 1.180120 - 0.268597I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = 1.23903 - 1.07030I$    | $-0.604279 - 1.131230I$               | $0.744211 - 0.553382I$ |
| $b = -0.281371 - 1.128550I$ |                                       |                        |
| $u = 0.108090 + 0.747508I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = -0.188536 + 0.513699I$ | $-3.80435 + 2.57849I$                 | $-2.39106 - 4.72239I$  |
| $b = 0.208670 - 0.825203I$  |                                       |                        |
| $u = 0.108090 - 0.747508I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = -0.188536 - 0.513699I$ | $-3.80435 - 2.57849I$                 | $-2.39106 + 4.72239I$  |
| $b = 0.208670 + 0.825203I$  |                                       |                        |
| $u = -1.37100$              | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = 0.942639$              | 4.85780                               | 8.45210                |
| $b = 0.829189$              |                                       |                        |
| $u = -1.334530 + 0.318930I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = -0.271933 + 0.551071I$ | $0.73474 - 6.44354I$                  | $0.47538 + 9.99765I$   |
| $b = 0.284386 + 0.605794I$  |                                       |                        |
| $u = -1.334530 - 0.318930I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = -0.271933 - 0.551071I$ | $0.73474 + 6.44354I$                  | $0.47538 - 9.99765I$   |
| $b = 0.284386 - 0.605794I$  |                                       |                        |
| $u = 0.463640$              | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = -3.49976$              | -0.799899                             | 60.8910                |
| $b = 2.74744$               |                                       |                        |

$$\text{III. } I_3^u = \langle 4a^2 + 23b - 33a + 3, a^3 - 8a^2 + 3a - 7, u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -\frac{4}{23}a^2 + \frac{33}{23}a - \frac{3}{23} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{23}a^2 + \frac{9}{23}a - \frac{51}{23} \\ -\frac{1}{23}a^2 + \frac{14}{23}a - \frac{41}{23} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{2}{23}a^2 - \frac{5}{23}a - \frac{10}{23} \\ -\frac{1}{23}a^2 + \frac{14}{23}a - \frac{41}{23} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -\frac{5}{23}a^2 + \frac{47}{23}a - \frac{67}{23} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{23}a^2 + \frac{9}{23}a - \frac{5}{23} \\ -\frac{1}{23}a^2 + \frac{14}{23}a - \frac{41}{23} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{4}{23}a^2 - \frac{10}{23}a + \frac{3}{23} \\ -\frac{4}{23}a^2 + \frac{33}{23}a - \frac{3}{23} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -\frac{5}{23}a^2 + \frac{47}{23}a - \frac{67}{23} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-\frac{75}{23}a^2 + \frac{314}{23}a - \frac{39}{23}$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing |
|---------------|--------------------------------|
| $c_1, c_2$    | $u^3 + u^2 - 1$                |
| $c_3$         | $u^3 - u^2 + 2u - 1$           |
| $c_4$         | $u^3 - u^2 + 1$                |
| $c_5$         | $u^3 - 3u^2 + 2u + 1$          |
| $c_6$         | $u^3 + u^2 + 2u + 1$           |
| $c_7$         | $(u + 1)^3$                    |
| $c_8, c_{12}$ | $u^3$                          |
| $c_9, c_{10}$ | $(u - 1)^3$                    |
| $c_{11}$      | $u^3 + 3u^2 + 2u - 1$          |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing |
|--------------------|------------------------------------|
| $c_1, c_2, c_4$    | $y^3 - y^2 + 2y - 1$               |
| $c_3, c_6$         | $y^3 + 3y^2 + 2y - 1$              |
| $c_5, c_{11}$      | $y^3 - 5y^2 + 10y - 1$             |
| $c_7, c_9, c_{10}$ | $(y - 1)^3$                        |
| $c_8, c_{12}$      | $y^3$                              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_3^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|----------------------------|---------------------------------------|-----------------------|
| $u = 1.00000$              |                                       |                       |
| $a = 0.135484 + 0.941977I$ | $4.66906 - 2.82812I$                  | $2.98758 + 12.02771I$ |
| $b = 0.215080 + 1.307140I$ |                                       |                       |
| $u = 1.00000$              |                                       |                       |
| $a = 0.135484 - 0.941977I$ | $4.66906 + 2.82812I$                  | $2.98758 - 12.02771I$ |
| $b = 0.215080 - 1.307140I$ |                                       |                       |
| $u = 1.00000$              |                                       |                       |
| $a = 7.72903$              | 0.531480                              | -90.9750              |
| $b = 0.569840$             |                                       |                       |

$$\text{IV. } I_4^u = \langle b - 2u + 1, a + u + 4, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u - 4 \\ 2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 3u + 5 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 3u + 5 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4u + 4 \\ 2u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u - 3 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -45

**(iv) u-Polynomials at the component**

| Crossings                                | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_2, c_3$<br>$c_9, c_{10}, c_{12}$ | $u^2 + u - 1$                  |
| $c_4, c_6, c_7$<br>$c_8$                 | $u^2 - u - 1$                  |
| $c_5, c_{11}$                            | $u^2$                          |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing |
|--------------------|------------------------------------|
| $c_1, c_2, c_3$    |                                    |
| $c_4, c_6, c_7$    | $y^2 - 3y + 1$                     |
| $c_8, c_9, c_{10}$ |                                    |
| $c_{12}$           |                                    |
| $c_5, c_{11}$      | $y^2$                              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_4^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 0.618034$       |                                       |            |
| $a = -4.61803$       | -7.89568                              | -45.0000   |
| $b = 0.236068$       |                                       |            |
| $u = -1.61803$       |                                       |            |
| $a = -2.38197$       | 7.89568                               | -45.0000   |
| $b = -4.23607$       |                                       |            |

$$\mathbf{V. } I_5^u = \langle b + u, a - u - 2, u^2 + u - 1 \rangle$$

(i) **Arc colorings**

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u + 2 \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2u + 1 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = 0**

**(iv) u-Polynomials at the component**

| Crossings                                | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_2, c_3$<br>$c_9, c_{10}, c_{12}$ | $u^2 + u - 1$                  |
| $c_4, c_6, c_7$<br>$c_8$                 | $u^2 - u - 1$                  |
| $c_5, c_{11}$                            | $u^2$                          |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing |
|--------------------|------------------------------------|
| $c_1, c_2, c_3$    |                                    |
| $c_4, c_6, c_7$    | $y^2 - 3y + 1$                     |
| $c_8, c_9, c_{10}$ |                                    |
| $c_{12}$           |                                    |
| $c_5, c_{11}$      | $y^2$                              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_3^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 0.618034$       |                                       |            |
| $a = 2.61803$        | 0                                     | 0          |
| $b = -0.618034$      |                                       |            |
| $u = -1.61803$       |                                       |            |
| $a = 0.381966$       | 0                                     | 0          |
| $b = 1.61803$        |                                       |            |

## VI. u-Polynomials

| Crossings     | u-Polynomials at each crossing  |
|---------------|---|
| $c_1, c_2$    | $((u - 1)^8)(u^2 + u - 1)^2(u^3 + u^2 - 1)(u^{27} - 12u^{26} + \dots - 82u - 1)$  |
| $c_3$         | $u^8(u^2 + u - 1)^2(u^3 - u^2 + 2u - 1)(u^{27} + 4u^{26} + \dots + 640u - 256)$   |
| $c_4$         | $((u + 1)^8)(u^2 - u - 1)^2(u^3 - u^2 + 1)(u^{27} - 12u^{26} + \dots - 82u - 1)$  |
| $c_5$         | $u^4(u^3 - 3u^2 + 2u + 1)$<br>$\cdot (u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1)$<br>$\cdot (u^{27} + 3u^{26} + \dots - 112u + 16)$ |
| $c_6$         | $u^8(u^2 - u - 1)^2(u^3 + u^2 + 2u + 1)(u^{27} + 4u^{26} + \dots + 640u - 256)$   |
| $c_7$         | $(u + 1)^3(u^2 - u - 1)^2(u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1)$<br>$\cdot (u^{27} + 7u^{26} + \dots - 65u + 1)$                                 |
| $c_8$         | $u^3(u^2 - u - 1)^2(u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1)$<br>$\cdot (u^{27} - 4u^{26} + \dots - 36u + 8)$                                  |
| $c_9, c_{10}$ | $(u - 1)^3(u^2 + u - 1)^2(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)$<br>$\cdot (u^{27} + 7u^{26} + \dots - 65u + 1)$                                 |
| $c_{11}$      | $u^4(u^3 + 3u^2 + 2u - 1)$<br>$\cdot (u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1)$<br>$\cdot (u^{27} + 3u^{26} + \dots - 112u + 16)$ |
| $c_{12}$      | $u^3(u^2 + u - 1)^2(u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1)$<br>$\cdot (u^{27} - 4u^{26} + \dots - 36u + 8)$                                  |

## VII. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing  |
|--------------------|---|
| $c_1, c_2, c_4$    | $(y - 1)^8(y^2 - 3y + 1)^2(y^3 - y^2 + 2y - 1) \\ \cdot (y^{27} - 46y^{26} + \dots + 6314y - 1)$  |
| $c_3, c_6$         | $y^8(y^2 - 3y + 1)^2(y^3 + 3y^2 + 2y - 1) \\ \cdot (y^{27} - 54y^{26} + \dots + 5095424y - 65536)$  |
| $c_5, c_{11}$      | $y^4(y^3 - 5y^2 + 10y - 1) \\ \cdot (y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1) \\ \cdot (y^{27} + 25y^{26} + \dots + 12928y - 256)$ |
| $c_7, c_9, c_{10}$ | $(y - 1)^3(y^2 - 3y + 1)^2 \\ \cdot (y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1) \\ \cdot (y^{27} - 15y^{26} + \dots + 4023y - 1)$     |
| $c_8, c_{12}$      | $y^3(y^2 - 3y + 1)^2(y^8 - 3y^7 + \dots - 4y + 1) \\ \cdot (y^{27} + 12y^{26} + \dots + 7696y - 64)$  |