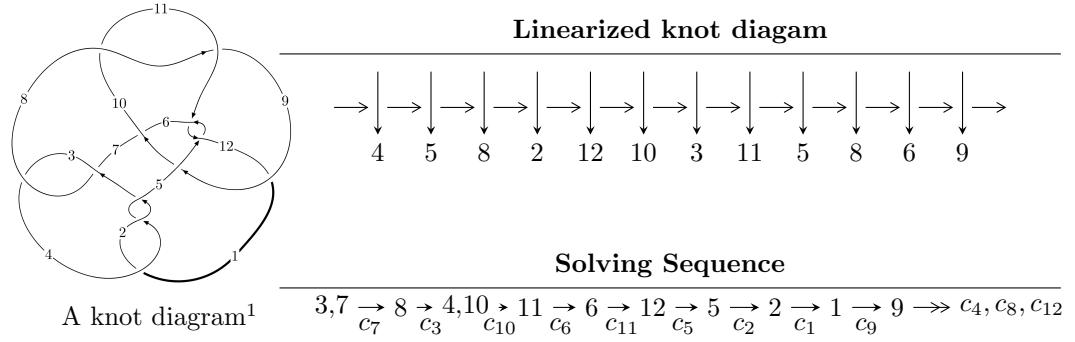


## $12n_{0691}$ ( $K12n_{0691}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 16394625770u^{16} + 7361888468u^{15} + \dots + 176471185595b + 67083506624, \\ - 638545424984u^{16} + 494483967338u^{15} + \dots + 176471185595a + 990730965236, \\ u^{17} - u^{16} + \dots - u + 1 \rangle$$

$$I_2^u = \langle u^7 - 2u^5 + 3u^3 + b - 2u - 1, -2u^7 - 2u^6 + 3u^5 + 4u^4 - 4u^3 - 4u^2 + a + 3u + 4, \\ u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1 \rangle$$

$$I_3^u = \langle 2.09794 \times 10^{14}u^{15} - 1.54864 \times 10^{15}u^{14} + \dots + 1.00649 \times 10^{18}b - 1.27599 \times 10^{18}, \\ 3.01917 \times 10^{14}u^{15} - 2.04767 \times 10^{15}u^{14} + \dots + 2.01298 \times 10^{18}a - 2.50594 \times 10^{18}, \\ u^{16} - u^{15} + \dots + 640u + 256 \rangle$$

$$I_1^v = \langle a, 669v^7 + 1791v^6 + 1344v^5 - 4076v^4 - 11099v^3 + 10779v^2 + 887b + 981v - 54, \\ v^8 + 2v^7 - 8v^5 - 13v^4 + 28v^3 - 7v^2 - 3v + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 49 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**I.**

$$I_1^u = \langle 1.64 \times 10^{10} u^{16} + 7.36 \times 10^9 u^{15} + \dots + 1.76 \times 10^{11} b + 6.71 \times 10^{10}, -6.39 \times 10^{11} u^{16} + 4.94 \times 10^{11} u^{15} + \dots + 1.76 \times 10^{11} a + 9.91 \times 10^{11}, u^{17} - u^{16} + \dots - u + 1 \rangle$$

(i) **Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3.61841u^{16} - 2.80207u^{15} + \dots - 2.45782u - 5.61412 \\ -0.0929026u^{16} - 0.0417172u^{15} + \dots - 1.35646u - 0.380139 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3.73975u^{16} - 3.05444u^{15} + \dots - 3.90343u - 6.05033 \\ 0.0499193u^{16} - 0.188766u^{15} + \dots - 1.60883u - 0.249100 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 3.51660u^{16} - 1.48871u^{15} + \dots + 10.1705u - 1.96079 \\ -0.183505u^{16} - 0.0479152u^{15} + \dots - 0.736610u - 1.19077 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 4.59450u^{16} - 5.53078u^{15} + \dots - 7.72513u - 11.9429 \\ -0.302029u^{16} - 0.353052u^{15} + \dots - 4.64374u + 0.978839 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.436207u^{16} - 0.314873u^{15} + \dots - 2.65787u - 1.88181 \\ -0.318145u^{16} + 0.389552u^{15} + \dots + 0.690292u - 0.0974507 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.249100u^{16} + 0.199181u^{15} + \dots + 1.65271u + 1.85793 \\ -0.0482596u^{16} - 0.0849909u^{15} + \dots + 1.20435u + 0.0738023 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.118062u^{16} - 0.0746790u^{15} + \dots + 1.96758u + 1.97926 \\ -0.175071u^{16} + 0.0850715u^{15} + \dots + 0.615613u + 0.0952905 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3.49708u^{16} - 2.54969u^{15} + \dots - 1.01221u - 5.17792 \\ -0.164310u^{16} + 0.0417260u^{15} + \dots - 0.940864u - 0.698283 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes**

$$= \frac{2048919230872}{176471185595} u^{16} - \frac{1391303845096}{176471185595} u^{15} + \dots - \frac{3163149744064}{176471185595} u - \frac{6932356318654}{176471185595}$$

**(iv) u-Polynomials at the component**

| Crossings                        | u-Polynomials at each crossing          |
|----------------------------------|---|
| $c_1, c_2, c_4$<br>$c_8, c_{10}$ | $u^{17} - 7u^{16} + \cdots - 5u - 1$    |
| $c_3, c_7, c_9$                  | $u^{17} - u^{16} + \cdots - u + 1$      |
| $c_5, c_{11}$                    | $u^{17} - u^{16} + \cdots + 3u - 1$     |
| $c_6$                            | $u^{17} + u^{16} + \cdots - 699u + 199$ |
| $c_{12}$                         | $u^{17} + 3u^{16} + \cdots - 263u - 83$ |

**(v) Riley Polynomials at the component**

| Crossings                        | Riley Polynomials at each crossing             |
|----------------------------------|--|
| $c_1, c_2, c_4$<br>$c_8, c_{10}$ | $y^{17} - 13y^{16} + \cdots + 21y - 1$         |
| $c_3, c_7, c_9$                  | $y^{17} + 15y^{16} + \cdots + 13y - 1$         |
| $c_5, c_{11}$                    | $y^{17} + 11y^{16} + \cdots + 25y - 1$         |
| $c_6$                            | $y^{17} + 27y^{16} + \cdots + 947097y - 39601$ |
| $c_{12}$                         | $y^{17} + 7y^{16} + \cdots + 91413y - 6889$    |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.764077 + 0.442209I$ |                                       |                       |
| $a = 0.346619 + 0.162821I$  | $-4.55533 + 6.93072I$                 | $-21.1582 - 11.9778I$ |
| $b = -0.958812 + 0.033588I$ |                                       |                       |
| $u = -0.764077 - 0.442209I$ |                                       |                       |
| $a = 0.346619 - 0.162821I$  | $-4.55533 - 6.93072I$                 | $-21.1582 + 11.9778I$ |
| $b = -0.958812 - 0.033588I$ |                                       |                       |
| $u = 0.791671$              |                                       |                       |
| $a = 0.322502$              | $-8.70952$                            | $-30.7710$            |
| $b = -1.02671$              |                                       |                       |
| $u = -0.753921 + 0.115715I$ |                                       |                       |
| $a = 1.18926 - 1.58502I$    | $-0.77832 - 2.01331I$                 | $-15.1488 + 1.3786I$  |
| $b = 1.125680 - 0.771688I$  |                                       |                       |
| $u = -0.753921 - 0.115715I$ |                                       |                       |
| $a = 1.18926 + 1.58502I$    | $-0.77832 + 2.01331I$                 | $-15.1488 - 1.3786I$  |
| $b = 1.125680 + 0.771688I$  |                                       |                       |
| $u = 0.502094 + 0.490826I$  |                                       |                       |
| $a = 1.152440 + 0.058194I$  | $2.49540 - 2.02523I$                  | $-6.20824 + 3.33819I$ |
| $b = -0.008463 + 0.987921I$ |                                       |                       |
| $u = 0.502094 - 0.490826I$  |                                       |                       |
| $a = 1.152440 - 0.058194I$  | $2.49540 + 2.02523I$                  | $-6.20824 - 3.33819I$ |
| $b = -0.008463 - 0.987921I$ |                                       |                       |
| $u = 0.291694 + 0.477697I$  |                                       |                       |
| $a = 7.34853 + 5.73057I$    | $-2.45442 + 0.76114I$                 | $-1.7282 + 15.9915I$  |
| $b = -1.56713 + 1.11619I$   |                                       |                       |
| $u = 0.291694 - 0.477697I$  |                                       |                       |
| $a = 7.34853 - 5.73057I$    | $-2.45442 - 0.76114I$                 | $-1.7282 - 15.9915I$  |
| $b = -1.56713 - 1.11619I$   |                                       |                       |
| $u = -0.439135$             |                                       |                       |
| $a = 0.949461$              | $-0.644803$                           | $-15.2830$            |
| $b = 0.384048$              |                                       |                       |

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|----------------------------|---------------------------------------|------------------------|
| $u = 0.432752$             |                                       |                        |
| $a = -6.06938$             | -2.91990                              | -47.5300               |
| $b = -0.248275$            |                                       |                        |
| $u = 0.78485 + 1.87131I$   |                                       |                        |
| $a = 0.345543 - 0.823882I$ | $11.20130 - 3.50827I$                 | $-11.32341 + 1.79574I$ |
| $b = 0.13775 + 2.40985I$   |                                       |                        |
| $u = 0.78485 - 1.87131I$   |                                       |                        |
| $a = 0.345543 + 0.823882I$ | $11.20130 + 3.50827I$                 | $-11.32341 - 1.79574I$ |
| $b = 0.13775 - 2.40985I$   |                                       |                        |
| $u = -0.93651 + 1.91501I$  |                                       |                        |
| $a = 0.272274 + 0.835217I$ | $6.80306 + 8.74093I$                  | $-14.7558 - 4.0661I$   |
| $b = 0.86840 - 2.32205I$   |                                       |                        |
| $u = -0.93651 - 1.91501I$  |                                       |                        |
| $a = 0.272274 - 0.835217I$ | $6.80306 - 8.74093I$                  | $-14.7558 + 4.0661I$   |
| $b = 0.86840 + 2.32205I$   |                                       |                        |
| $u = 0.98322 + 2.02620I$   |                                       |                        |
| $a = 0.244045 - 0.883210I$ | $10.6972 - 14.1953I$                  | $-12.00000 + 6.60789I$ |
| $b = 1.34803 + 2.71046I$   |                                       |                        |
| $u = 0.98322 - 2.02620I$   |                                       |                        |
| $a = 0.244045 + 0.883210I$ | $10.6972 + 14.1953I$                  | $-12.00000 - 6.60789I$ |
| $b = 1.34803 - 2.71046I$   |                                       |                        |

$$\text{II. } I_2^u = \langle u^7 - 2u^5 + 3u^3 + b - 2u - 1, -2u^7 - 2u^6 + \cdots + a + 4, u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned}
a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_4 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} 2u^7 + 2u^6 - 3u^5 - 4u^4 + 4u^3 + 4u^2 - 3u - 4 \\ -u^7 + 2u^5 - 3u^3 + 2u + 1 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} 2u^7 + 2u^6 - 3u^5 - 4u^4 + 4u^3 + 4u^2 - 3u - 5 \\ -u^7 + 2u^5 - 3u^3 - u^2 + 2u + 1 \end{pmatrix} \\
a_6 &= \begin{pmatrix} 2u^7 + 2u^6 - 4u^5 - 4u^4 + 5u^3 + 4u^2 - 4u - 1 \\ -u^7 + u^5 - u^3 + 2u^2 - 1 \end{pmatrix} \\
a_{12} &= \begin{pmatrix} 2u^6 - 4u^4 + 7u^2 - u - 5 \\ -2u^7 - u^6 + 4u^5 + 3u^4 - 5u^3 - 4u^2 + 3u + 2 \end{pmatrix} \\
a_5 &= \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix} \\
a_2 &= \begin{pmatrix} u^6 - u^4 + 2u^2 - 1 \\ -u^7 - u^6 + 2u^5 + u^4 - 2u^3 - 2u^2 + 2u + 1 \end{pmatrix} \\
a_1 &= \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix} \\
a_9 &= \begin{pmatrix} 2u^7 + 2u^6 - 3u^5 - 4u^4 + 4u^3 + 4u^2 - 3u - 4 \\ -u^7 + 2u^5 - 3u^3 + 2u + 1 \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^7 - 4u^6 + 2u^5 + 5u^4 - 3u^3 - 5u^2 + 5u - 10$

**(iv) u-Polynomials at the component**

| Crossings  | u-Polynomials at each crossing                              |
|------------|---|
| $c_1, c_2$ | $u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$                   |
| $c_3$      | $u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$              |
| $c_4$      | $u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$                   |
| $c_5$      | $u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$ |
| $c_6$      | $u^8 - 2u^7 - u^6 + 5u^5 + 4u^4 - 17u^3 + 17u^2 - 7u + 1$   |
| $c_7$      | $u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$              |
| $c_8$      | $(u - 1)^8$   |
| $c_9$      | $u^8$   |
| $c_{10}$   | $(u + 1)^8$   |
| $c_{11}$   | $u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$ |
| $c_{12}$   | $u^8 + 3u^7 + 6u^6 + 7u^5 + 13u^4 + 11u^3 + 4u^2 + 3u + 1$  |

**(v) Riley Polynomials at the component**

| Crossings       | Riley Polynomials at each crossing                              |
|-----------------|---|
| $c_1, c_2, c_4$ | $y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$     |
| $c_3, c_7$      | $y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$     |
| $c_5, c_{11}$   | $y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$    |
| $c_6$           | $y^8 - 6y^7 + 29y^6 - 67y^5 + 126y^4 - 85y^3 + 59y^2 - 15y + 1$ |
| $c_8, c_{10}$   | $(y - 1)^8$   |
| $c_9$           | $y^8$   |
| $c_{12}$        | $y^8 + 3y^7 + 20y^6 + 49y^5 + 47y^4 - 47y^3 - 24y^2 - y + 1$    |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.570868 + 0.730671I$ |                                       |                        |
| $a = 1.72219 - 2.56817I$    | $-2.68559 - 1.13123I$                 | $-18.1377 + 5.3065I$   |
| $b = -1.50065 - 0.90255I$   |                                       |                        |
| $u = -0.570868 - 0.730671I$ |                                       |                        |
| $a = 1.72219 + 2.56817I$    | $-2.68559 + 1.13123I$                 | $-18.1377 - 5.3065I$   |
| $b = -1.50065 + 0.90255I$   |                                       |                        |
| $u = 0.855237 + 0.665892I$  |                                       |                        |
| $a = -0.658590 - 0.551963I$ | $0.51448 - 2.57849I$                  | $-10.11893 + 3.45077I$ |
| $b = 1.43900 - 0.90910I$    |                                       |                        |
| $u = 0.855237 - 0.665892I$  |                                       |                        |
| $a = -0.658590 + 0.551963I$ | $0.51448 + 2.57849I$                  | $-10.11893 - 3.45077I$ |
| $b = 1.43900 + 0.90910I$    |                                       |                        |
| $u = 1.09818$               |                                       |                        |
| $a = -0.421763$             | $-8.14766$                            | $-12.9880$             |
| $b = 0.491355$              |                                       |                        |
| $u = -1.031810 + 0.655470I$ |                                       |                        |
| $a = -0.420504 - 0.057447I$ | $-4.02461 + 6.44354I$                 | $-10.82984 - 2.68172I$ |
| $b = 0.655281 + 0.532312I$  |                                       |                        |
| $u = -1.031810 - 0.655470I$ |                                       |                        |
| $a = -0.420504 + 0.057447I$ | $-4.02461 - 6.44354I$                 | $-10.82984 + 2.68172I$ |
| $b = 0.655281 - 0.532312I$  |                                       |                        |
| $u = -0.603304$             |                                       |                        |
| $a = -1.86442$              | $-2.48997$                            | $-13.8390$             |
| $b = 0.321397$              |                                       |                        |

$$\text{III. } I_3^u = \langle 2.10 \times 10^{14} u^{15} - 1.55 \times 10^{15} u^{14} + \dots + 1.01 \times 10^{18} b - 1.28 \times 10^{18}, \ 3.02 \times 10^{14} u^{15} - 2.05 \times 10^{15} u^{14} + \dots + 2.01 \times 10^{18} a - 2.51 \times 10^{18}, \ u^{16} - u^{15} + \dots + 640u + 256 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.000149985u^{15} + 0.00101723u^{14} + \dots + 0.522231u + 1.24489 \\ -0.000208441u^{15} + 0.00153866u^{14} + \dots + 0.527819u + 1.26776 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.000149985u^{15} - 0.00101723u^{14} + \dots - 0.522231u - 0.244888 \\ -0.000391498u^{15} + 0.00253027u^{14} + \dots + 1.56110u + 1.71179 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0000210778u^{15} - 0.00137312u^{14} + \dots - 1.23583u - 0.524902 \\ 0.000823010u^{15} - 0.00190398u^{14} + \dots - 1.08393u - 1.43592 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.000987334u^{15} + 0.000332252u^{14} + \dots - 1.64360u - 0.285638 \\ -0.00263050u^{15} + 0.00407270u^{14} + \dots - 2.52850u + 0.754844 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.000548337u^{15} - 0.000148181u^{14} + \dots - 1.41913u - 0.208839 \\ 0.00209134u^{15} - 0.00192142u^{14} + \dots + 1.92702u + 0.216705 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.000318911u^{15} + 0.000923900u^{14} + \dots + 0.0782544u + 0.170443 \\ 0.0000474371u^{15} + 0.00190210u^{14} + \dots + 1.03533u - 0.116481 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.00154300u^{15} + 0.00206961u^{14} + \dots - 0.507891u - 0.00786525 \\ 0.00175647u^{15} + 0.00275194u^{14} + \dots + 1.98501u + 0.0818943 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.000675440u^{15} + 0.000547485u^{14} + \dots - 1.09374u + 0.615472 \\ 0.00211859u^{15} - 0.000320222u^{14} + \dots + 3.48674u + 2.29159 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{4129940980039711}{1006491371550221696} u^{15} - \frac{3800282985571637}{1006491371550221696} u^{14} + \dots + \frac{45304359399533900}{7863213840236107} u - \frac{73541352487366340}{7863213840236107}$$

**(iv) u-Polynomials at the component**

| Crossings                        | u-Polynomials at each crossing                  |
|----------------------------------|---|
| $c_1, c_2, c_4$<br>$c_8, c_{10}$ | $u^{16} - 3u^{15} + \cdots - 8u + 1$            |
| $c_3, c_7, c_9$                  | $u^{16} - u^{15} + \cdots + 640u + 256$         |
| $c_5, c_{11}$                    | $(u^8 - u^7 + 3u^6 - 2u^5 + 3u^4 - 2u^3 - 1)^2$ |
| $c_6$                            | $u^{16} + 3u^{15} + \cdots + 2169u + 361$       |
| $c_{12}$                         | $u^{16} - 4u^{15} + \cdots - 189u + 297$        |

**(v) Riley Polynomials at the component**

| Crossings                        | Riley Polynomials at each crossing                        |
|----------------------------------|---|
| $c_1, c_2, c_4$<br>$c_8, c_{10}$ | $y^{16} + 9y^{15} + \cdots + 4y + 1$                      |
| $c_3, c_7, c_9$                  | $y^{16} + 33y^{15} + \cdots + 606208y + 65536$            |
| $c_5, c_{11}$                    | $(y^8 + 5y^7 + 11y^6 + 10y^5 - y^4 - 10y^3 - 6y^2 + 1)^2$ |
| $c_6$                            | $y^{16} + 31y^{15} + \cdots - 741503y + 130321$           |
| $c_{12}$                         | $y^{16} + 32y^{15} + \cdots + 78327y + 88209$             |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -0.928106 + 0.575657I$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |                        |
| $a = 0.600905 + 0.372711I$  | -0.290648                             | $-13.26997 + 0.I$      |
| $b = 0.918546 + 0.300867I$  |                                       |                        |
| $u = -0.928106 - 0.575657I$ |                                       |                        |
| $a = 0.600905 - 0.372711I$  | -0.290648                             | $-13.26997 + 0.I$      |
| $b = 0.918546 - 0.300867I$  |                                       |                        |
| $u = -0.684023 + 0.882805I$ |                                       |                        |
| $a = 0.433643 - 0.063937I$  | -1.15366 - 1.27532I                   | $-10.53127 + 1.72199I$ |
| $b = -0.344993 - 0.631679I$ |                                       |                        |
| $u = -0.684023 - 0.882805I$ |                                       |                        |
| $a = 0.433643 + 0.063937I$  | -1.15366 + 1.27532I                   | $-10.53127 - 1.72199I$ |
| $b = -0.344993 + 0.631679I$ |                                       |                        |
| $u = 0.577755 + 0.986475I$  |                                       |                        |
| $a = 0.638361 - 0.648733I$  | 2.70026 + 3.63283I                    | $-9.34305 - 4.59352I$  |
| $b = 0.608076 - 0.155053I$  |                                       |                        |
| $u = 0.577755 - 0.986475I$  |                                       |                        |
| $a = 0.638361 + 0.648733I$  | 2.70026 - 3.63283I                    | $-9.34305 + 4.59352I$  |
| $b = 0.608076 + 0.155053I$  |                                       |                        |
| $u = -0.153757 + 0.400659I$ |                                       |                        |
| $a = 1.128490 + 0.166387I$  | -1.15366 - 1.27532I                   | $-10.53127 + 1.72199I$ |
| $b = 1.123000 + 0.170958I$  |                                       |                        |
| $u = -0.153757 - 0.400659I$ |                                       |                        |
| $a = 1.128490 - 0.166387I$  | -1.15366 + 1.27532I                   | $-10.53127 - 1.72199I$ |
| $b = 1.123000 - 0.170958I$  |                                       |                        |
| $u = 1.61868 + 0.98339I$    |                                       |                        |
| $a = 0.385316 - 0.391577I$  | 2.70026 - 3.63283I                    | $-9.34305 + 4.59352I$  |
| $b = 1.65420 - 0.20376I$    |                                       |                        |
| $u = 1.61868 - 0.98339I$    |                                       |                        |
| $a = 0.385316 + 0.391577I$  | 2.70026 + 3.63283I                    | $-9.34305 - 4.59352I$  |
| $b = 1.65420 + 0.20376I$    |                                       |                        |

| Solutions to $I_3^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|----------------------------|---------------------------------------|------------------------|
| $u = 0.05666 + 2.24811I$   |                                       |                        |
| $a = 0.010165 + 0.766423I$ | $12.42750 - 4.93524I$                 | $-10.31351 + 3.19667I$ |
| $b = -1.22626 - 2.33561I$  |                                       |                        |
| $u = 0.05666 - 2.24811I$   |                                       |                        |
| $a = 0.010165 - 0.766423I$ | $12.42750 + 4.93524I$                 | $-10.31351 - 3.19667I$ |
| $b = -1.22626 + 2.33561I$  |                                       |                        |
| $u = 0.14941 + 2.37106I$   |                                       |                        |
| $a = 0.044468 - 0.705707I$ | 8.53095                               | $-13.35437 + 0.I$      |
| $b = -0.66007 + 2.57178I$  |                                       |                        |
| $u = 0.14941 - 2.37106I$   |                                       |                        |
| $a = 0.044468 + 0.705707I$ | 8.53095                               | $-13.35437 + 0.I$      |
| $b = -0.66007 - 2.57178I$  |                                       |                        |
| $u = -0.13661 + 2.63887I$  |                                       |                        |
| $a = 0.008651 + 0.652267I$ | $12.42750 + 4.93524I$                 | $-10.31351 - 3.19667I$ |
| $b = -0.57250 - 3.23168I$  |                                       |                        |
| $u = -0.13661 - 2.63887I$  |                                       |                        |
| $a = 0.008651 - 0.652267I$ | $12.42750 - 4.93524I$                 | $-10.31351 + 3.19667I$ |
| $b = -0.57250 + 3.23168I$  |                                       |                        |

$$\text{IV. } I_1^v = \langle a, 669v^7 + 1791v^6 + \dots + 887b - 54, v^8 + 2v^7 - 8v^5 - 13v^4 + 28v^3 - 7v^2 - 3v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -0.754228v^7 - 2.01917v^6 + \dots - 1.10598v + 0.0608794 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.754228v^7 + 2.01917v^6 + \dots + 1.10598v - 0.0608794 \\ -0.754228v^7 - 2.01917v^6 + \dots - 1.10598v + 0.0608794 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1.32244v^7 - 3.19504v^6 + \dots - 1.54904v + 1.44307 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.872604v^7 - 1.55581v^6 + \dots - 0.0732807v + 3.76550 \\ 3.44419v^7 + 7.94701v^6 + \dots + 1.00113v - 9.59639 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.510710v^7 - 1.51522v^6 + \dots - 3.20180v + 0.754228 \\ -v^7 - 2v^6 + 8v^4 + 13v^3 - 28v^2 + 7v + 3 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.510710v^7 + 1.51522v^6 + \dots + 4.20180v - 0.754228 \\ v^7 + 2v^6 - 8v^4 - 13v^3 + 28v^2 - 7v - 3 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.510710v^7 + 1.51522v^6 + \dots + 3.20180v - 0.754228 \\ v^7 + 2v^6 - 8v^4 - 13v^3 + 28v^2 - 7v - 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1.32244v^7 - 3.19504v^6 + \dots - 1.54904v + 2.44307 \\ 1.32244v^7 + 3.19504v^6 + \dots + 1.54904v - 1.44307 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes  
 $= \frac{2247}{887}v^7 + \frac{4687}{887}v^6 - \frac{426}{887}v^5 - \frac{21184}{887}v^4 - \frac{35807}{887}v^3 + \frac{61378}{887}v^2 + \frac{5411}{887}v - \frac{17810}{887}$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                              |
|---------------|---|
| $c_1, c_2$    | $(u - 1)^8$   |
| $c_3, c_7$    | $u^8$   |
| $c_4$         | $(u + 1)^8$   |
| $c_5$         | $u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$ |
| $c_6, c_8$    | $u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$                   |
| $c_9, c_{12}$ | $u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$              |
| $c_{10}$      | $u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$                   |
| $c_{11}$      | $u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$ |

**(v) Riley Polynomials at the component**

| Crossings          | Riley Polynomials at each crossing                           |
|--------------------|--|
| $c_1, c_2, c_4$    | $(y - 1)^8$  |
| $c_3, c_7$         | $y^8$  |
| $c_5, c_{11}$      | $y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$ |
| $c_6, c_8, c_{10}$ | $y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$  |
| $c_9, c_{12}$      | $y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $v = 1.230330 + 0.083902I$  |                                       |                        |
| $a = 0$                     | $0.51448 + 2.57849I$                  | $-10.11893 - 3.45077I$ |
| $b = 0.108090 - 0.747508I$  |                                       |                        |
| $v = 1.230330 - 0.083902I$  |                                       |                        |
| $a = 0$                     | $0.51448 - 2.57849I$                  | $-10.11893 + 3.45077I$ |
| $b = 0.108090 + 0.747508I$  |                                       |                        |
| $v = 0.370895 + 0.073482I$  |                                       |                        |
| $a = 0$                     | $-4.02461 - 6.44354I$                 | $-10.82984 + 2.68172I$ |
| $b = -1.334530 - 0.318930I$ |                                       |                        |
| $v = 0.370895 - 0.073482I$  |                                       |                        |
| $a = 0$                     | $-4.02461 + 6.44354I$                 | $-10.82984 - 2.68172I$ |
| $b = -1.334530 + 0.318930I$ |                                       |                        |
| $v = -0.337834$             |                                       |                        |
| $a = 0$                     | $-8.14766$                            | $-12.9880$             |
| $b = -1.37100$              |                                       |                        |
| $v = -1.21928 + 2.03110I$   |                                       |                        |
| $a = 0$                     | $-2.68559 + 1.13123I$                 | $-18.1377 - 5.3065I$   |
| $b = 1.180120 - 0.268597I$  |                                       |                        |
| $v = -1.21928 - 2.03110I$   |                                       |                        |
| $a = 0$                     | $-2.68559 - 1.13123I$                 | $-18.1377 + 5.3065I$   |
| $b = 1.180120 + 0.268597I$  |                                       |                        |
| $v = -2.42604$              |                                       |                        |
| $a = 0$                     | $-2.48997$                            | $-13.8390$             |
| $b = 0.463640$              |                                       |                        |

## V. u-Polynomials

| Crossings       | u-Polynomials at each crossing  |
|-----------------|---|
| $c_1, c_2, c_8$ | $((u - 1)^8)(u^8 + u^7 + \dots + 2u - 1)(u^{16} - 3u^{15} + \dots - 8u + 1)$<br>$\cdot (u^{17} - 7u^{16} + \dots - 5u - 1)$   |
| $c_3$           | $u^8(u^8 - u^7 + \dots + 2u - 1)(u^{16} - u^{15} + \dots + 640u + 256)$<br>$\cdot (u^{17} - u^{16} + \dots - u + 1)$  |
| $c_4, c_{10}$   | $((u + 1)^8)(u^8 - u^7 + \dots - 2u - 1)(u^{16} - 3u^{15} + \dots - 8u + 1)$<br>$\cdot (u^{17} - 7u^{16} + \dots - 5u - 1)$   |
| $c_5, c_{11}$   | $(u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1)$<br>$\cdot (u^8 - u^7 + 3u^6 - 2u^5 + 3u^4 - 2u^3 - 1)^2$<br>$\cdot (u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1)$<br>$\cdot (u^{17} - u^{16} + \dots + 3u - 1)$ |
| $c_6$           | $(u^8 - 2u^7 - u^6 + 5u^5 + 4u^4 - 17u^3 + 17u^2 - 7u + 1)$<br>$\cdot (u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{16} + 3u^{15} + \dots + 2169u + 361)$<br>$\cdot (u^{17} + u^{16} + \dots - 699u + 199)$                                  |
| $c_7, c_9$      | $u^8(u^8 + u^7 + \dots - 2u - 1)(u^{16} - u^{15} + \dots + 640u + 256)$<br>$\cdot (u^{17} - u^{16} + \dots - u + 1)$  |
| $c_{12}$        | $(u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1)$<br>$\cdot (u^8 + 3u^7 + 6u^6 + 7u^5 + 13u^4 + 11u^3 + 4u^2 + 3u + 1)$<br>$\cdot (u^{16} - 4u^{15} + \dots - 189u + 297)(u^{17} + 3u^{16} + \dots - 263u - 83)$                             |

## VI. Riley Polynomials

| Crossings                        | Riley Polynomials at each crossing   |
|----------------------------------|--|
| $c_1, c_2, c_4$<br>$c_8, c_{10}$ | $(y - 1)^8(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^{16} + 9y^{15} + \dots + 4y + 1)(y^{17} - 13y^{16} + \dots + 21y - 1)$  |
| $c_3, c_7, c_9$                  | $y^8(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{16} + 33y^{15} + \dots + 606208y + 65536)(y^{17} + 15y^{16} + \dots + 13y - 1)$  |
| $c_5, c_{11}$                    | $(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)^2$ $\cdot (y^8 + 5y^7 + 11y^6 + 10y^5 - y^4 - 10y^3 - 6y^2 + 1)^2$ $\cdot (y^{17} + 11y^{16} + \dots + 25y - 1)$   |
| $c_6$                            | $(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^8 - 6y^7 + 29y^6 - 67y^5 + 126y^4 - 85y^3 + 59y^2 - 15y + 1)$ $\cdot (y^{16} + 31y^{15} + \dots - 741503y + 130321)$ $\cdot (y^{17} + 27y^{16} + \dots + 947097y - 39601)$ |
| $c_{12}$                         | $(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^8 + 3y^7 + 20y^6 + 49y^5 + 47y^4 - 47y^3 - 24y^2 - y + 1)$ $\cdot (y^{16} + 32y^{15} + \dots + 78327y + 88209)$ $\cdot (y^{17} + 7y^{16} + \dots + 91413y - 6889)$         |